

03-Aug-2025

Agenda :-

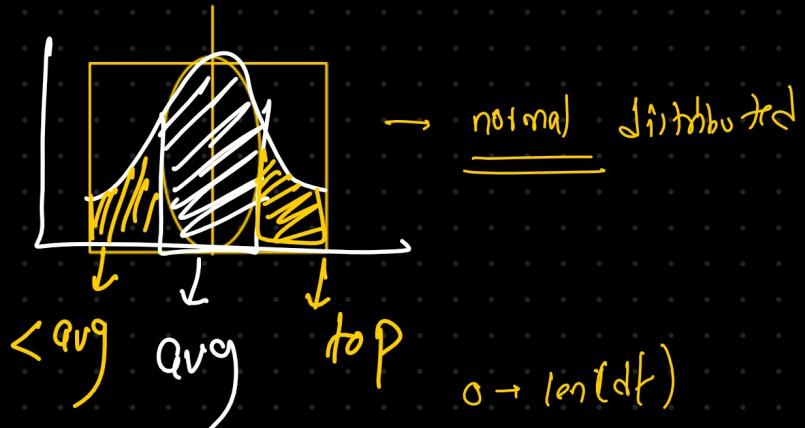
Distribution

Correlation & Covariance

Skewness

Skewness

measures the asymmetry of a distribution.



$$\text{Skewness} = \frac{\sum (x_i - \bar{x})^3 / n}{(\sigma)^3}$$

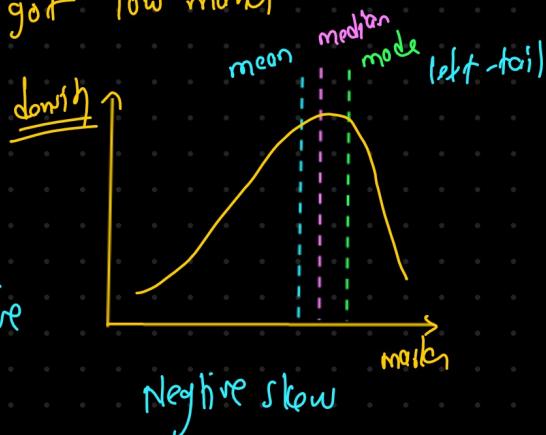
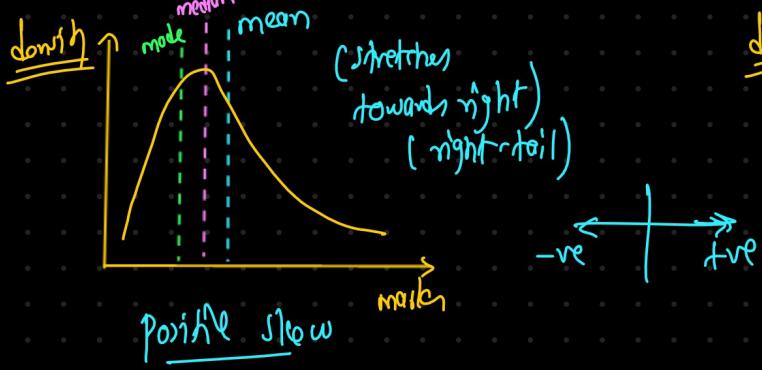
$\sigma \rightarrow SD$

$\bar{x} \rightarrow \text{mean}$

$x_i \rightarrow \text{data point}$

$n \rightarrow \text{total size / no. of obser}$

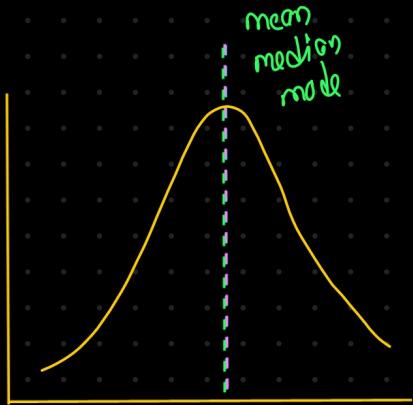
Q. If most of the students scored low Q. If most scored high but few but few got high marks got low marks



Note:

positive: Mean > Median > Mode

negative: Mean < Median < Mode  
skew



- \* understand distributions
- ↓
- test
- ML (Regression model)
- \* Hypothesis testing

$$D \rightarrow \textcircled{6} \rightarrow \left( \frac{1}{6} \right) \rightarrow \text{final} \rightarrow \underline{\text{huge number}}$$

$$\cancel{\textcircled{6}} \rightarrow \hat{6}$$

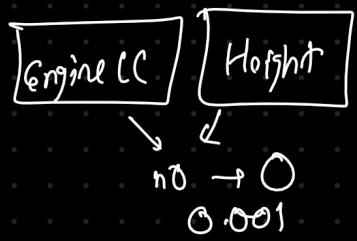
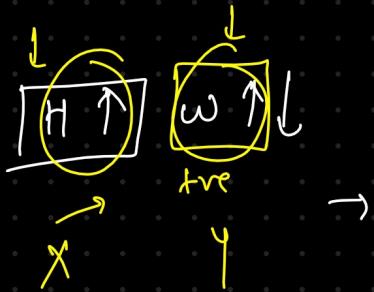
Correlation & covariance

Covariance:

- Measures how two variable vary together.
- It tells the direction (positive / negative relationship)
- It does not tell you strength.

formula: —

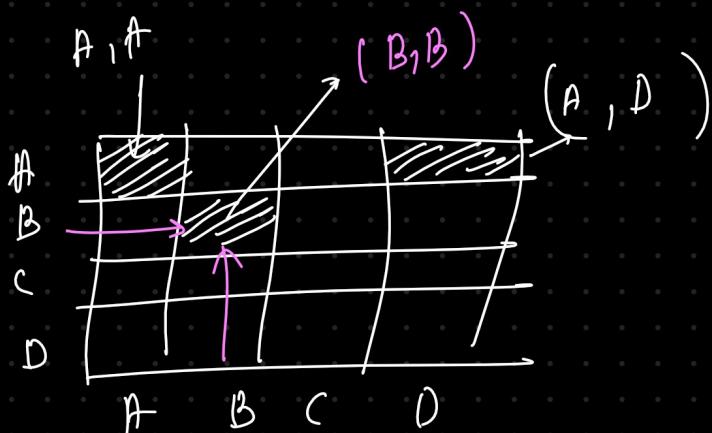
$$\text{cov}(x, y) = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$



### Correlation:

- A scaled version of covariance that also tells you the strength & direction of the relationship between variables.
- The value lies between  $-1 \leq +1$

$$\text{correlation formula } (X, Y) = \frac{\text{cov}(X, Y)}{\sigma_X \cdot \sigma_Y}$$



A w.r.t A  $\rightarrow 1$

positive  $(A, B)$   $\rightarrow$   $+ve \rightarrow \uparrow \text{study}, \uparrow \text{marks}$   
 $\downarrow$   
 study hours  
 higher marks

negative  $(A, B)$   $\rightarrow -ve \rightarrow \uparrow \text{time, } \downarrow \text{decreasing}$   
 $\downarrow$   
 more time on social media  
 lower marks

1, 2, 3

$(\text{Survived}, P(\text{class})) \rightarrow -ve \rightarrow \underline{\text{Survived}} \uparrow, \boxed{P(\text{class})} \downarrow$   
 $\downarrow$   
 A  
 $\downarrow$   
 B

$(\text{higher class of the person})$

Finding : —

Survived & pclass  $\rightarrow -0.34$  (High class (1st class) passenger were likely to survive.)

SibSp & Parch  $\rightarrow 0.41$  (People with more family aboard (sibling, parent, etc) often had both types of relative together)  
 (No. of sibling or spouse aboard with the passenger)  
 (No. of parent or children aboard with the passenger)

Survived & Fare  $\rightarrow 0.26$  (Passenger who paid more had "better chance" of survival.  
 (probably in 1st class))

$[-\infty \rightarrow 187 \text{ } 198 \infty]$

$[-1 \boxed{1} \boxed{-1}]$

$\text{cov} \rightarrow \frac{1}{n}$

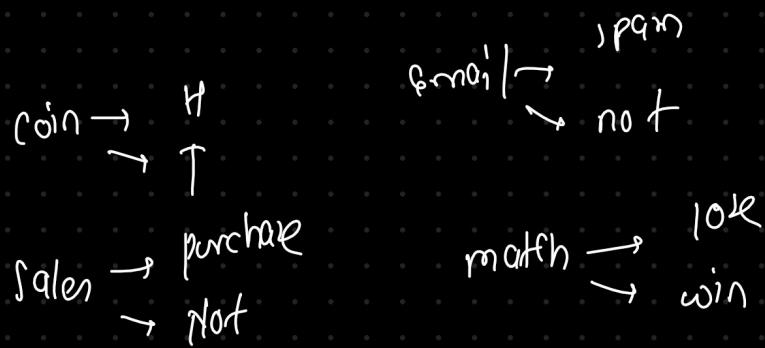
$\rightarrow \frac{\text{covariance}}{10 \quad -160 \quad -1000}$   
 $160$   
 $200$

$\rightarrow \text{correlation} \rightarrow \boxed{-1 \text{ to } 1}$

	Covariance	Correlation
Measure	Direction of linear relationship	Direction & strength
Scale	Raw unit	Standardized (-1 to +1)
Interpret	Positive / Negative / Zero	+1 (strong pos), 0 (none), -1 (strong neg)
Use	Step in calculation correlation	Use for feature relationship.

# Probability Distributions

(1) Bernoulli Distribution:



Models a single experiment with exactly 2 outcomes:

Success (1)

Failure (0)



$$P(H) = 0.5 \quad \begin{matrix} \text{success} \\ \text{of getting Head} \end{matrix}$$

$$P(1-H) = 0.5$$

$\downarrow$   
 success  
 not  
 getting Head

A

$$P(A) = 0.7 \rightarrow \text{success}$$

$$P(1-A) = (1-0.7) = 0.3$$

$0.7$   
 $\downarrow$

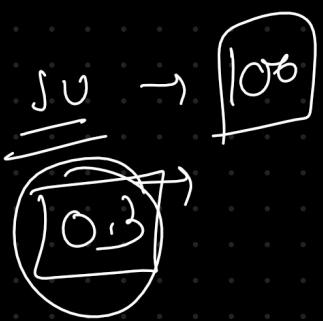
prob. prop

A



$100 \rightarrow$



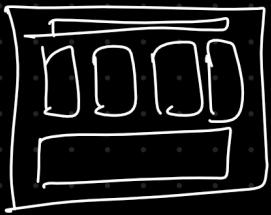


### Hip Testing

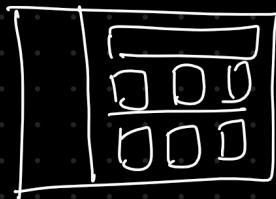


Company A

A → B  
↳ purchase  
full working  
website

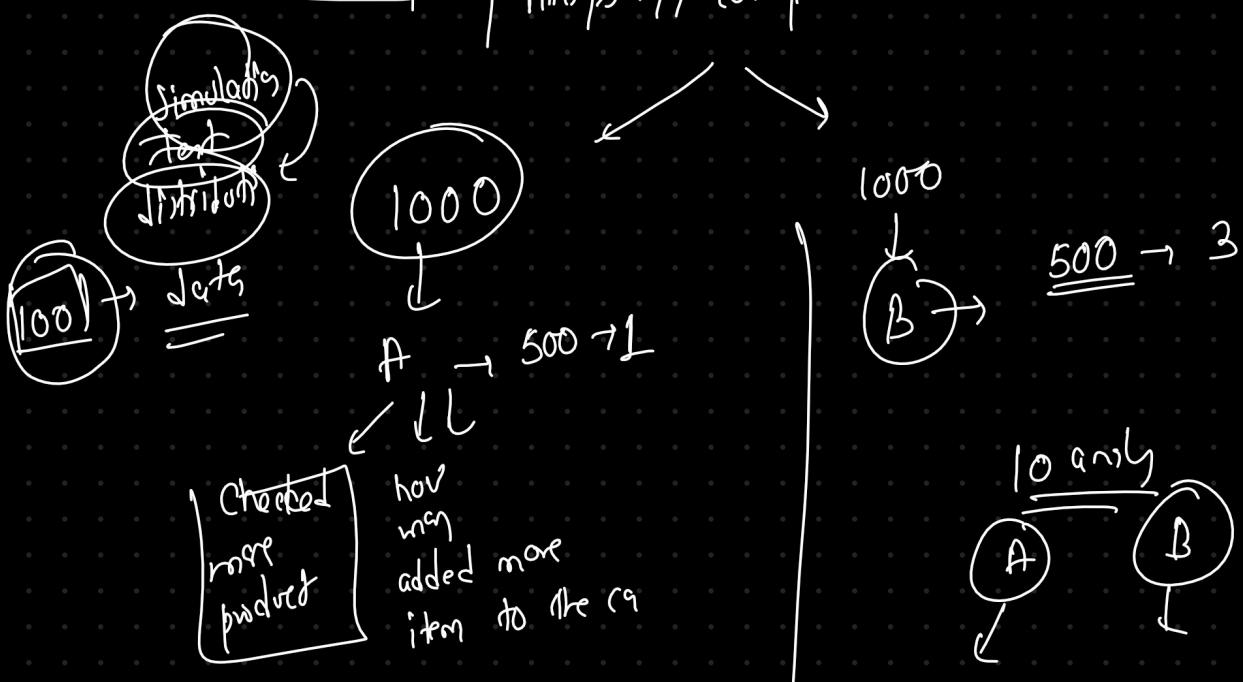


Type A



Type B

different layout



## Binomial distribution

Models the number of success ( $k$ ) in  $n$  independent Bernoulli trials.

$$H \approx 0.6$$

Bern → Coin →  $p = 0.4$ , success rate = 0.6

(Bin) → 10 → success rate

$$P(k) = \binom{n}{k} p^k (1-p)^{n-k}$$

Q: Salesperson has 20% chance of making a sales per call. They make 15 calls.

: what's the prob of exactly 3 sales?

$$P(3) = \binom{15}{3} (0.2)^3 (0.8)^{12} \approx 0.25$$

## Assignment : —

### Task 1 :

Create 1000 student data with numpy ,

Column A → Student id  
Column B → Height  
Column C → weight

) Synthetic →

Task 1,r1 → numpy or pandas , manually write formula for covariance & correlation ,

Task 1,r2 → calculate it .

Task .1,r3 → skewness plot for any one column.  
→ Skewness value .