

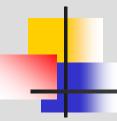
Arithmetic ve Logical Operations

- > ALU (Arithmetic Logical Unit): CPU nun Aritmetik ve logic islemlerinin yapildigi kismina denir.
 - > Temel iki operation
 - > Addition (Toplama)
 - Negation (NOT islemi)
- Islemler sayilarin temsil edilme sekline gore degisiklik gosterirler.
- Hangi sayi temsil sekli islemleri daha cok kolaylastiriyorsa o bilgisyar tasariminda kullanilmaktadir.



Overflow

- Bilgisayar mimarisi sabit uzunluktaki veriler uzerinde islem yaparlar.
 - > 32-bit / 64-bit islemci
- > Overflow
 - Eger islemin sonucu o islem icin ayrılan alana sigmazsa buna overflow denir
 - > Overflow detection (tesbiti) onemli
 - > Aksi halde yanlis sonuclar kullanilarak islemler yapilir.

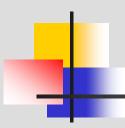


Boolean Operations

- Bir boolean variable iki degerden birini alabilir.
 - > False (0)
 - > True (1)

input	zero	one	invert	same
0	0	1	1	0
1	0	1	0	1

Unary Boolean Operations



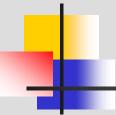
Boolean Operations

- > Binary boolean operations
 - > Iki variable uzerinde islem yapilir

а				nand			
0	0	0	0	1	1	0	1
0	1	0	1	1 1 1	0	1	0
1	0	0	1	1	0	1	0
1	1	1	1	0	0	0	1



SAL daki Logical Operations



Maskeleme İşlemi

- ➤ Boolean islemlerinde birden fazla değişken aynı bellek gozune yazıldığında kullanılırlar.
- Değişkenlerin bellek gozunden cikarilmasi islemine masking denir.

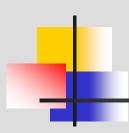
 cell:
 .word
 0x43686172

 mask1:
 .word
 0xff000000

 mask2:
 .word
 0x000ff0000

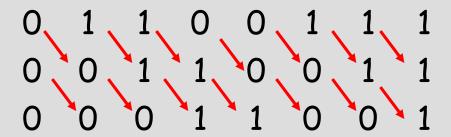
 mask4:
 .word
 0x000000ff

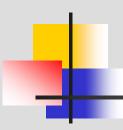
and result, cell, mask1



Shift Operations (Oteleme Islemleri)

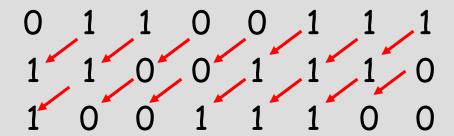
- > Logical Shift
 - > Logical right shift:
 - > Bitler 1 pozisyon saga otelenir
 - En sagdaki bit (LSB) atilir
 - > En soldaki (MSB) bite 0 atanir.

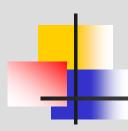




Shift Operations

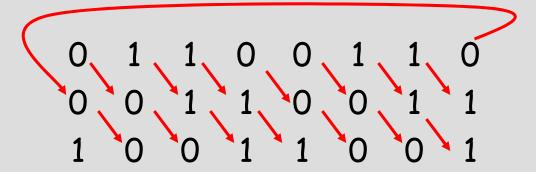
- > Logical Left Shift
 - > Bitler bir pozisyon sola otelenirler
 - > En soldaki bit (MSB) atilir
 - > En sagdaki bit (LSB) O olur

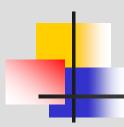




Rotate

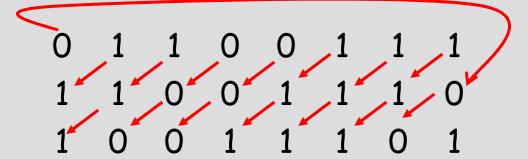
- > Rotate Right
 - > Bitler saga dogru bir pozisyon kaydirilir
 - > LSB, MSB olur

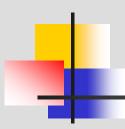




Rotate

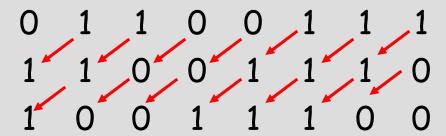
- > Rotate Left
 - > Bitler bir pozisyon sola otelenir
 - > MSB, LSB olur

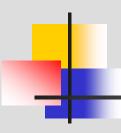




Arithmetic Shift

- > Arithmetic left shift
- > Logical left shift le ayni
 - > Bitler bir pozisyon sola otelenirler
 - > En soldaki bit (MSB) atilir
 - En sagdaki bit (LSB) 0 olur

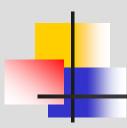




Arithmetic Left Shift

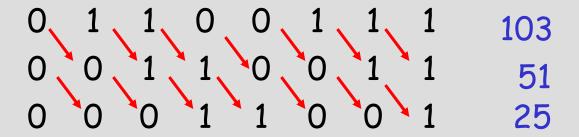
Sayinin arithmetic 1 bit otelenmesi o sayinin 2 ile carpimi anlamina gelir.

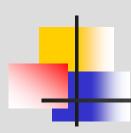
```
1 0 0 1 1 1 0 1 -99
0 0 1 1 1 0 1 0 58
0 1 1 1 0 1 0 0 116
```



Arithmetic Right Shift

- Logical right shift gibi. Tek farki sign bit extended (MSF sayinin sign bitiyle ayni)
- Bir sayinin 1 bit arithmetic saga otelenmesi o sayinin 2 ile bolunmesi anlamina gelir.



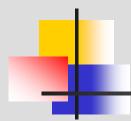


Addition (Toplama) / Subtraction (Cikarma)

Unsigned Integers:

1 010010 (18₁₀) 101000 (24₁₀) 101010 (42₁₀)

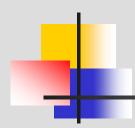
Ci	Xi	y i	Zi	C _{i+1}
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1



Unsigned integers

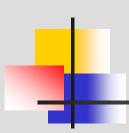
a	b	a-b
		•
O	0	0
0	1	borrow
1	0	1
1	1	0
10	1	1

$$\begin{array}{c} 01000 \\ -00110 \\ \hline 00010 \end{array}$$



Sign magnitude

0 00110
+ 1 10010
$$\longrightarrow$$
 1 01100



Two's Complement Addition/Subtraction

- ➤ Isaret bitlerine bakilmaksizin addition icin ayni algoritma uygulanir.
- Substraction additive inverse alinip addition algoritmasi kullanılmak suretiyle gerceklestirilir.
- Unsigned number larin toplami icin kullanilan ayni devre two's complementi icin toplama ve cikarmada kullanilabilir



	0010 0010	34 ₁₀
+	1001 1000	-104 ₁₀
	1011 1010	-70



Overflow

```
\begin{array}{c} \frac{1}{1} \frac{1}{111111000} \\ + 111111000 \\ \hline 111110000 \\ -8_{10} \\ \hline \\ 111110000 \\ -16_{10} \\ \end{array}
```

no overflow

```
    0 1 1110 126<sub>10</sub>
    + 0110 0000 96<sub>10</sub>
    1101 1110 -34<sub>10</sub>
    yanlis sonuc overflow
```

Multiplication

```
multiplicand \longrightarrow 1 1 0 1 = -3<sub>10</sub>
 multiplier \longrightarrow 0 1 1 0 = 6_{10}
                               1\ 1\ 1\ 1\ 1\ 1\ 0\ 1 = -3_{10}
                               \times 00000110 = 6_{10}
                                 0000000
                               1111101
                              1111101
                            0000000
                          0000000
                        0000000
                      0000000
                  + 0000000
                                  1 1 1 0 1 1 1 0 = -18
```



```
\begin{array}{r}
111111000 = -8_{10} \\
 \times 111111000 = -8_{10} \\
\hline
000000000 \\
00000000 \\
00000000 \\
111111000 \\
111111000 \\
+11111000
\end{array}
```

X ve Y nin carpim programi

.data

X: .word ms_sum: .word (

Y: .word bitsum: .word

ls_sum .word 0 mask: .word 0x1

test: word

.text

__start:and test, X, mask # strip off appropriate multiplier bit begz test, shift # skip addition if multiplier is zero

add ms_sum, ms_sum, Y # add partial sum

and bitsum, ms_sum, 1 # determine lsb of ms_sum

r ls_sum, ls_sum, bitsum # place lsb of ms_sum in lsb of ls_sum

shift Is_sum, moving new bit into msb

shift ms_sum, maintaining sign

update index

branch if not last iteration

shift:

ls_sum, ls_sum, bitsum ls_sum, ls_sum, 1 ms_sum, ms_sum, 1

sll mask, mask, 1

bnez mask, __start done



Floating Point (FP) Arithmetic

- Bilgisayar designinda floating point sayilarinmin gosterimi onemli bir yer tutar.
- Duyarliligi yuksek olmasi istenilen islemlerde floating point islemlerinin hizli olmasi istenir
- > Floating Point Operations Per Second (FLOPS)
 - Scientific bilgisayarların performans karsılastırımlarında kullanılır.
- > Floating Point Operations Integer Operationlarindan daha yavastir



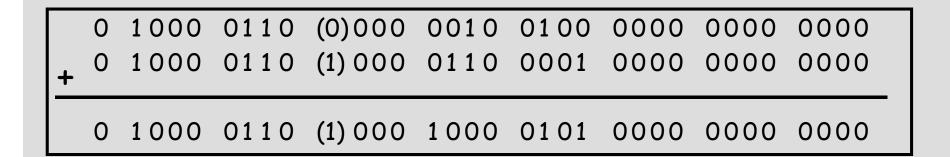
Hardware versus Software Calculatiuons

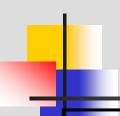
- > Hesaplamalar nasil yapilmali
 - Hardware Implementation: Devreler (circuits)
 FP islemlerini yapar.
 - > Hizli
 - > Pahali
 - > Software
 - > Ucuz (devre acisindan)
 - > Yavas (10 un bir kac kuvveti kadar yavas)



2.25 + 134.0625

0	1000	0000	(1) 001	0000	0000	0000	0000	0000
0	1000	0110	(1) 000	0110	0001	0000	0000	0000





255.0625 + 134.0625

```
      0
      1000
      0110
      (1)111
      1111
      0001
      0000
      0000
      0000

      0
      1000
      0110
      (1)000
      0110
      0001
      0000
      0000
      0000
```

```
      -
      0
      1000
      0110
      (1)111
      1111
      0001
      0000
      0000
      0000

      -
      0
      1000
      0110
      (1)000
      0110
      0010
      0000
      0000
      0000

      0
      1000
      0110
      (1)
      0000
      0101
      0010
      0000
      0000
      0000
```



2.25 + -134.0625

0000 0000 0000 0010 0100 0000 1100 0011

(1) 000 0011 1101 0000 0000 0000

	FloatX: FloatY Float_X_plus_Y: X:	.data .float .float .float .word	134.0625 2.25
	- y:	.word	
_	X_F:	.word	
	X_E:	.word	
	Y_F:	.word	

Y_E: .word
X_time_Y: .word
X_plus_Y: .word

X_plus_Y_F: .word
X_plus_Y_E: .word
X_plus_Y_S: .word
small_F: .word

diff: .word

F_mask: .word 0x007fffff
E_mask: .word 0x7f800000
S_MASK: .word 0x80000000
Hidden_one: .word 0x00800000

zero: .word 0

max_F: .word 0x01000000



```
.text
             # Extract E (exponent) and F (significand).
       start: move
                    X, FloatX
                    X_F, X, F_Mask
             and
                                          # get X_F
                    X_F, X_F, Hidden_one # add hidden bit
             or
                    X, DoX_E
                                           # skip if positive
             bgtz
                    X_F, zero, X_F
             sub
                                        # convert to 2's comp.
                                       # get X_E
     DoX_E: and X_E, X, E_mask
                    X_E, X_E, 23
                                        # align
             srl
                                         # convert to 2's comp.
                    X E, X E, 127
             sub
             move Y, FloatY
                    Y F. Y. F Mask
                                      # get Y_F
             and
                    Y_F, Y_F, Hidden_one # add hidden bit
             or
             bgtz Y, DoY_E
                                           # skip if positive
             sub Y_F, zero, Y_F
                                           # convert to 2's comp.
     DoY_E: and Y_E, Y, E_mask
                                          # get Y_E
                                           # align
                    Y_E, Y_E, 23
             srl
                    Y_E, Y_E, 127
                                           # convert to 2's comp.
             sub
3/19/2019
                       Bilgisayar Organizasyonu
                                                           3.29
```



Determine which input is smaller

sub diff, Y_E, X_E bltz diff, X_bigger

move X_plus_Y_E, Y_E move X_plus_Y_F, Y_F

move small_F, X_F

b LittleF

X_bigger: move X_plus_Y_E, X_E

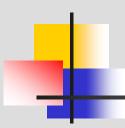
move X_plus_Y_F, X_F

move small_F, Y_F

sub diff, zero, diff

LittleF: sra small_F, small_F, diff # denormalize little F

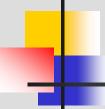
```
X_plus_Y_F, small_F, X_plus_Y_F
                                                       # add Fs
           add
                       X_plus_Y_S, X_plus_Y_F, S_mask
           and
                       X_plus_Y_F, Zero
           begz
                       X_plus_Y_F, L1
           bgez
                                                          # skip if positive
                       X_plus_Y_F, zero, X_plus_Y_F
                                                          # convert to sign/mag
           sub
                       X_plus_Y_E, X_plus_Y_E
           move
                       X_plus_Y_F, max_F, NotTooBig
           blt
                                                          # skip if no overflow
                       X_plus_Y_F, X_plus_Y_F, 1
                                                          # divide F by 2
           srl
                       X_plus_Y_E, X_plus_Y_E, 1
                                                          # adjust E
           add
                       normalized
           b
                       Float_X_plus_Y, 0
Zero:
           move
                       Finished
TooSmall:
           sll
                       X_plus_Y_F, X_plus_Y_F, 1
                                                          # multiply F by 2
                       X_plus_Y_E, X_plus_Y_E, 1
                                                          # adjust E
           sub
NotTooBig: blt
                       X_plus_Y_F, Hidden_one, TooSmall # check if still too big
                       X_plus_Y_F, X_plus_Y_F, Hidden_one # delete hidden one
normalized: sub
                       X_plus_Y_E, X_plus_Y_E, 127 # convert to bias-127
           add
                       X_plus_Y_E, X_plus_Y_E, 23
           sll
                                                          # align properly
                       X_plus_Y, X_plus_Y_E, X_plus_Y_F # merge E, F
           or
                       X_plus_Y, X_plus_Y, X_plus_Y_S # merge S
           or
                       Float_X_plus_Y, X_plus_Y
                                                          # move to floating point
           move
Finished:
           done
```



Multiplication

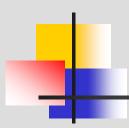
- > Floating Addition dan daha basit
- > 4 adim
 - Mantissa lar uzerinde unsigned multiplication yap
 - > Exponents lere ekle
 - > Sonucu normalize hale getir
 - > Sonucun isaret bitini belirle

18.0 * 9.5



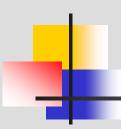
1000 0011 4 + 1000 0010 3 1000 0110 7

 $\times 1001$ 1001 0000 0000 000 +100 1000



Division

- > Multiplication a benzer
- > 4 adim
 - > Mantissalar uzerinde unsigned division yap
 - Divisorun exponentini dividend in exponentinden cikar
 - > Sonucu normalize yap
 - > Sonucun isaret bitini belirle.



Overflow ve Underflow

- > Overflow
 - Normalized sonucun exponenti (biased-127) kendine ayrilan yere sigmadiginda olusur
- > Underflow
 - Sonucun temsil edilemeyecek kadar 0 ya yakin olmasiyle olusur