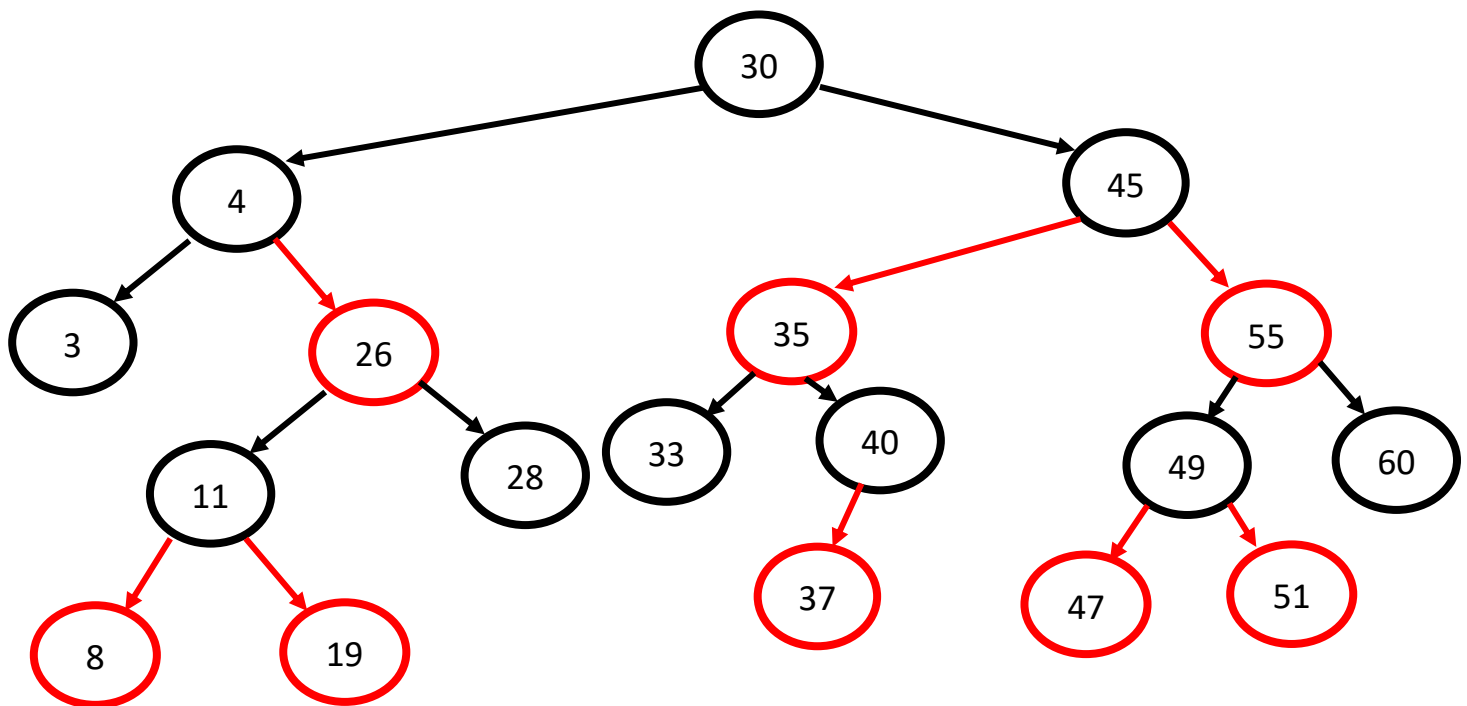
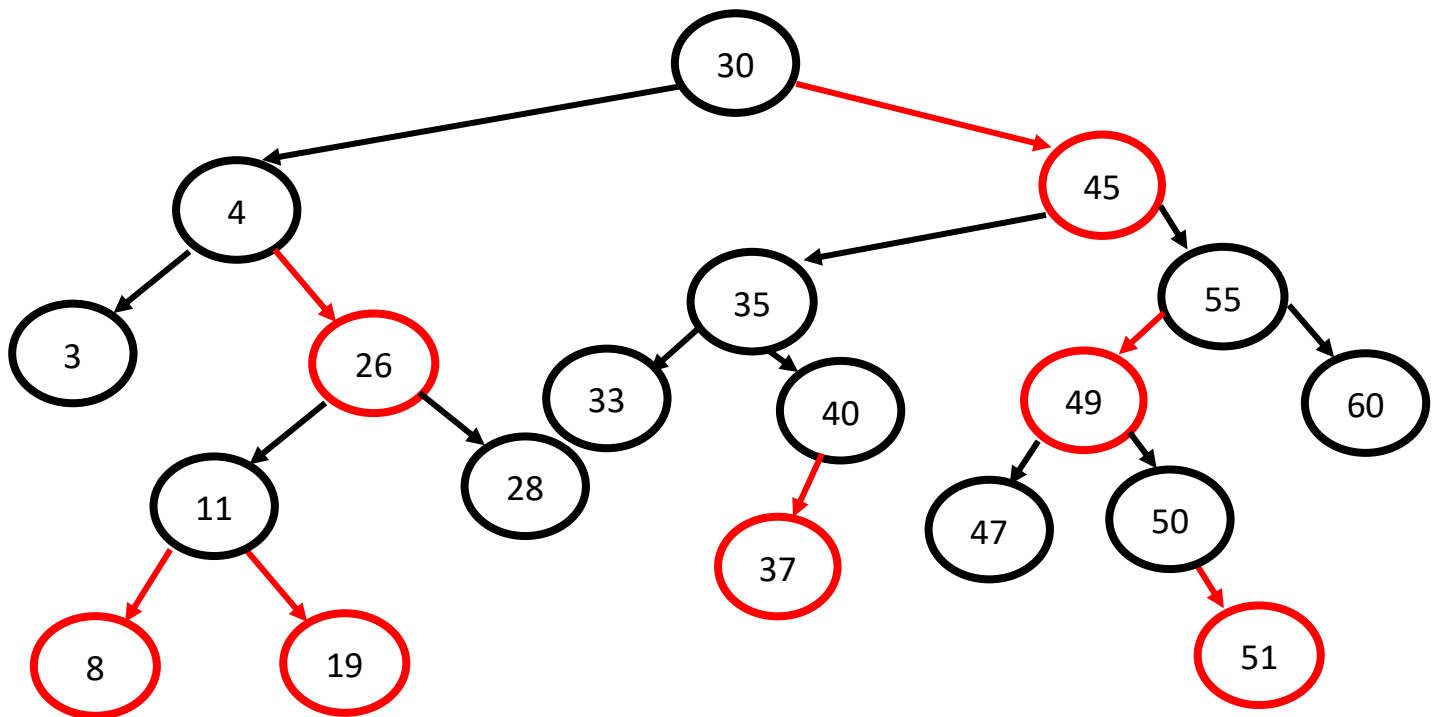


**Question 1:**

**Part a; Equivalent Red-Black Tree:**



Part b; After inserting 50 Red-Black Tree:



**Question 2:**

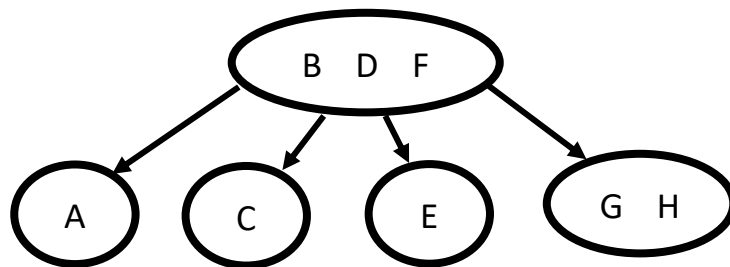
**Part a)**

$$3^h - 1$$

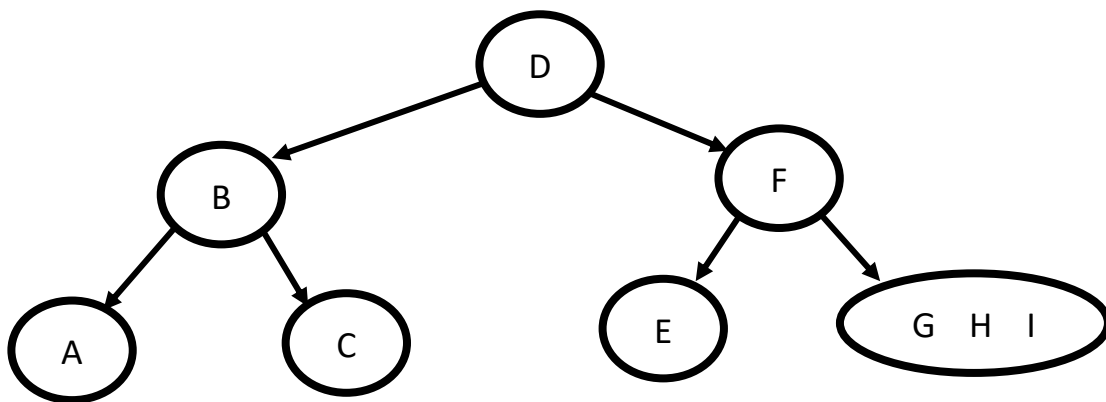
**Part b)**

Letter "i" makes the 2-3-4 tree to grow to height 3 for the first time.

Before inserting "i":



After inserting "i":



### Part c)

**O (N).** Since red-black trees are built in a sorted manner, by simply applying an in-order traversal we can obtain a sorted list.

### Part d)

**No.** A red-black trees must start with a black root, yet, the root of a subtree of a red-black tree can be red, which is not allowed.

### Question 3:

#### Part a)

In this problem, we will need to create a hash table by using the **keys** of the elements in the array (if first element of the array is 5 for example, in the hash table, 5<sup>th</sup> element will contain the location of 5, which is 0 in this case). Algorithm will perform this for every element and it will be spending  $O(N)$  time.

After the initialization of the hash table, again for every element in the array, the algorithm will **assume as the first element is correct** and it will look up for the **second element**, if it finds, it will return these two numbers. It will do this by first **subtracting the current element from the target value**. The remaining number is the second correct element. If, in the hash table, that element exists, then it will get the content of the remaining element and **this will be the second key index**.

The main purpose of using hash tables in this example is to reduce the time for the search time. By using hash tables, this time reduces from  $O(N)$  to  **$O(1)$** .

**Part b)**

**When collisions solved by linear probing:**

Slot	0	1	2	3	4	5	6
Content	30	15	22	11	14	11	

**When collisions solved by quadratic probing:**

Slot	0	1	2	3	4	5	6
Content	30	15	22	11	14		11