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Teoria da Computação Lista 2

1. Mostre que:

- a) cada linguagem abaixo não é regular,
- b) cada linguagem abaixo é livre de contexto,
- c) Apresente um autômato de pilha não determinístico que as reconheça, por estado final e por pilha vazia ao mesmo tempo.

$$\begin{array}{lll} \text{L1} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i = j, \ i \geq 1, \ j \geq 1 \} & \text{L2} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ j = 2i, \ i \geq 1, \ j \geq 1 \} \\ \text{L3} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i \leq j, \ i \geq 1, \ j \geq 1 \} & \text{L4} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i \geq j, \ i \geq 1, \ j \geq 1 \} \\ \text{L5} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i = j, \ i \geq 0, \ j \geq 0 \} & \text{L6} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i \geq j, \ i \geq 0, \ j \geq 0 \} \\ \text{L7} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i \leq j, \ i \geq 0, \ j \geq 0 \} & \text{L8} = \{ \ a^{\dot{i}} \ b^{\dot{j}} \ \big| \ i \geq j, \ i \geq 0, \ j \geq 0 \} \end{array}$$

$$L_Q = \{ a^i b^j c^k \mid i = j, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{10} = \{ a^i b^j c^k \mid i = k, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{11} = \{ a^{i} b^{j} c^{k} \mid j = k, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{12} = \{ a^i b^j c^k \mid i \le j, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{13} = \{ \ a^i \ b^j \ c^k \ \big| \ i \leq k, \, i \geq 1, \, j \geq 1, \, k \geq 1 \ \}$$

$$L_{14} = \{ a^{j} b^{j} c^{k} \mid j \leq k, i \geq 1, j \geq 1, k \geq 1 \}$$

$$L_{15} = \{ a^{i} b^{j} c^{k} \mid i \ge j, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{16} = \{ a^{i} b^{j} c^{k} \mid i \geq k, i \geq 1, j \geq 1, k \geq 1 \}$$

$$L_{17} = \{ a^{i} b^{j} c^{k} \mid j \ge k, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{18} = \{ a^{i} b^{j} c^{k} \mid i = j + k, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{10} = \{ a^i b^j c^k \mid k = i + j, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{20} = \{ a^{i} b^{j} c^{k} \mid i = j, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{2,1} = \{ a^i b^j c^k \mid i = k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{22} = \{ a^{j} b^{j} c^{k} \mid j = k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{23} = \{ a^{j} b^{j} c^{k} \mid i \leq j, i \geq 0, j \geq 0, k \geq 0 \}$$

$$L_{24} = \{ a^i b^j c^k \mid i \le k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{25} = \{ a^{j} b^{j} c^{k} \mid j \leq k, i \geq 0, j \geq 0, k \geq 0 \}$$

$$L_{26} = \{ a^{j} b^{j} c^{k} \mid i \ge j, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{27} = \{ a^{i} b^{j} c^{k} \mid i \ge k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{28} = \{ a^{i} b^{j} c^{k} \mid j \ge k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{29} = \{ a^{i} b^{j} c^{k} \mid i = j + k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{30} = \{ a^{i} b^{j} c^{k} \mid k = i + j, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{31} = \{ a^{i} b^{j} c^{m} d^{n} | i = n, j = m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L_{32} = \{ a^{i} b^{j} c^{m} d^{n} | i = n, j = m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{33} = \{ a^{i} b^{j} c^{m} d^{n} | i \le n, j = m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L_{34} = \{ a^{i} b^{j} c^{m} d^{n} | i \le n, j = m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{35} = \{ a^{j} b^{j} c^{m} d^{n} | i = n, j \le m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L_{36} = \{ a^{i} b^{j} c^{m} d^{n} | i = n, j \le m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{37} = \{ a^{i} b^{j} c^{m} d^{n} | i \le n, j \le m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L37 - \{a \text{ osc } u \mid 1 \leq 1, j \leq 11, 1 \geq 1, 11 \geq 1, 11 \geq 1\}$$

$$L_{38} = \{ a^{i} b^{j} c^{m} d^{n} | i \le n, j \le m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{3Q} = \{ a^{j} b^{j} c^{m} d^{n} | i \ge n, j = m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L_{40} = \{ a^{i} b^{j} c^{m} d^{n} | i \ge n, j = m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{41} = \{ a^{i} b^{j} c^{m} d^{n} | i = n, j \ge m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L_{42} = \{ a^{i} b^{j} c^{m} d^{n} | i = n, j \ge m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{43} = \{ a^{i} b^{j} c^{m} d^{n} | i \ge n, j \ge m, i \ge 1, j \ge 1, m \ge 1, n \ge 1 \}$$

$$L_{AA} = \{ a^i b^j c^m d^n | i \ge n, j \le m, i \ge 0, j \ge 0, m \ge 0, n \ge 0 \}$$

$$L_{45} = \{ a^i b^{2j} c^{3k} \mid i = j, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{46} = \{ a^i b^2 j c^3 k \mid i = j, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{47} = \{ a^i b^{3j} c^k \mid i = k, i \ge 1, j \ge 1, k \ge 1 \}$$

$$L_{AB} = \{ a^i b^{3j} c^k \mid i = k, i \ge 0, j \ge 0, k \ge 0 \}$$

$$L_{AQ} = \{ a^{3i} b^{j} c^{k} \mid j=k, i \ge 1, j \ge 1, k \ge 1 \}$$

$$\mathbf{L_{50}} = \{ \ \mathbf{a^{3i}} \ \mathbf{b^{\ j}} \ \mathbf{c^{\ k}} \ \big| \ \mathbf{j} = \mathbf{k}, \, \mathbf{i} \geq \mathbf{0}, \, \mathbf{j} \geq \mathbf{0}, \, \mathbf{k} \geq \mathbf{0} \ \}$$

$$L_{51} = \{ \ a^i \ b^{\ 3j} \ c^{\ 2k} \ \big| \ i = k, \, i \geq 1, \, j \geq 1, \, k \geq 1 \ \}$$

$$L_{52} = \{ a^i b^{3j} c^{2k} \mid i = k, i \ge 0, j \ge 0, k \ge 0 \}$$

3. Mostre que são ou não regulares, ou que são ou não livres de contexto as seguintes linguagens, com o auxílio dos lemas do bombeamento:

$$\begin{array}{lll} L_{_{3a}} = \{ \ a^i b^j \ | \ i,j \geq 0 \ \} & L_{_{3b}} = \{ a^i b^i \ | \ i \geq 0 \ \} \\ L_{_{3c}} = \{ \ a^i b^j \ | \ i \geq j \geq 0 \ \} & L_{_{3d}} = \{ \ a^i b^j \ | \ i \geq 1, j \geq 1 \ \} \\ L_{_{3e}} = \{ \ a^i b^j \ | \ 0 \leq i \leq j \} & L_{_{3f}} = \{ \ a^i b^i c^i \ | \ i \geq 1 \} \\ L_{_{3g}} = \{ w.w \ | \ w \in \{a,b\}^* \ \} & L_{_{3b}} = \{ w.w^R \ | \ w \in \{a,b\}^* \ \} \end{array}$$

4. Utilizando a mT M_4 , $M_4 = (K, \Sigma, \Gamma, \delta, i, F)$, em que $K = \{q_0, q_1, q_2, \dots, q_n\}$ $g_2 g_4$ $\Sigma = \{a, b\}$ $\Gamma = \{a, b, X, Y, \Box\}$ $i = g_0$ $F = \{g_4\}$ e

q_3, q_4 , $\mathcal{L} = \{a, b\}, 1 = \{a, b, A, 1, b\}, 1 = q_0, F = \{q_4\} e$					
δ	a	b	X	Y	
q_0	q_1XR			q_3YR	q_4XR
q_1	q ₁ aR	q_2YL		q_1YR	
q_2	q ₂ aL		q_0XR	q_2YL	
q_3				q ₃ YR	q ₄ XR
q_4					

Verifique se as cadeias <u>aab</u> e <u>abbaa</u> são aceitas por esta mT M₄, mostrando a sequência de configurações assumidas por M₆ ao tentar reconhecer cada cadeia.

5.^a) Construa uma mT M₅ que reconheça as cadeias da linguagem L₅ = $\{ab^{n-2n} | n \ge 1\}.$

6. Tente definir a gramática G_6 , para a linguagem $L_6 = \{abc^i \mid i < j < i\}$ k, $i \ge 1$ }, com base na gramática sensível ao contexto $G_6 = \langle \{S,B,C\}, \}$ $\{a,b,c\}$, P, S >, que gera a linguagem $L_6 = \{a^n b^n c^n \mid n \ge 1\}$, cujas regras encontram-se, a seguir:

S→aSBC $CB \rightarrow BC$ aB→ab bB→bb bC→bc $cC \rightarrow cc$

7.a) Encontre uma gramática para as linguagens:

 $L1=\{a^i: i=k^2, k \text{ um inteiro positivo}\}.$

 $L2=\{xx: x \in \{a,b\}^*\}.$