

CIS4301 Notes

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1 Relational Algebra

See <http://cise.ufl.edu/class/cis4301sp14/slides/ra.ppt> for class slides on this. These notes are mostly a condensed version of the slides, the slides contain some nice table images to help you visualize the operations.

1.1 What is Relational Algebra?

Operators most common actions you execute on relations

Operands relations or variables that represent relations

1.2 Core Relational Algebra

Union, Intersection, Difference most common actions you execute on relations

Selection picking certain rows

Projection picking certain columns

Products/Joins compositions of relations

Renaming of relations and attributes

1.2.1 Selection

$R1 := \sigma_c(R2)$

C is a condition that refers to attributes of R2

R1 is all tuples of R2 that satisfy C

Relation Sells:			$JoeMenu := \sigma_{bar="Joe's"}(Sells) :$		
bar	beer	price	bar	beer	price
Joe's	Bud	2.50	Joe's	Bud	2.50
Joe's	Miller	2.75	Joe's	Miller	2.75
Sue's	Bud	2.50	Sue's	Bud	2.50
Sue's	Miller	3.00	Sue's	Miller	3.00

1.2.2 Projection

$R1 := \pi_L(R2)$

L is a list of attributes from R2's schema

R1 contains only the attributes of R2 listed in L (in the order they are listed)

Set operation: removes duplicate tuples

1.2.3 Extended Projection

$R1 := \pi_L(R2)$

Like projection, but L can contain arbitrary expressions involving attributes. Example: $\pi_{A+B \rightarrow C, A, A}(R)$ will create a new table where the first column, C, is the sum of A and B, and the next two columns A1 and A2 are copies of the original A.

1.2.4 Product

$R3 := R1 \times R2$

- pair each tuple t1 of R1 with each tuple t2 of R2
- Concatenation $t_1 t_2$ is a tuple of R_3
- Schema of R3 is the attributes of R1 and then R2, in order
- Beware attribute A of same name in R1 and R2: use R1.A and R2.A

Example: $R3 := R1 \times R2$

Duplicate column B, so use R1.B and R2.B to differentiate.

1.2.5 Theta Join

$R3 := R1 \bowtie_C R2$ Equivalent to taking the product $R1 \times R2$ and applying σ_C to the result.

$R \bowtie_\theta S \equiv \sigma_\theta(R \times S)$

C can be any boolean-values condition.

1.2.6 Natural Join

Remove duplicate columns, only return columns that naturally combine. $R3 := R1 \bowtie R2$

1.2.7 Renaming

Gives a new schema to a relation.

$R1 := \rho_{R1(A_1, \dots, A_n)}(R2)$ or $R1(A_1, \dots, A_n) := R2$ (simplified notation)

R1 is a relation with the same tuples as R2 but the attributes A_1, \dots, A_n .

1.3 Building Complex Expressions

Combine operators with parentheses and precedence rules.

Three notations:

1. Sequences of assignment statements
2. Expressions with several operators
3. Expression trees

1.3.1 Operator Precedence

1. $[\sigma, \pi, \rho]$ (highest)
2. $[X, \bowtie]$
3. \cap
4. \cup

1.3.2 Expression Trees

Leaves are operands (variables or constant relations).

Interior nodes are operators applied to children.

Example:

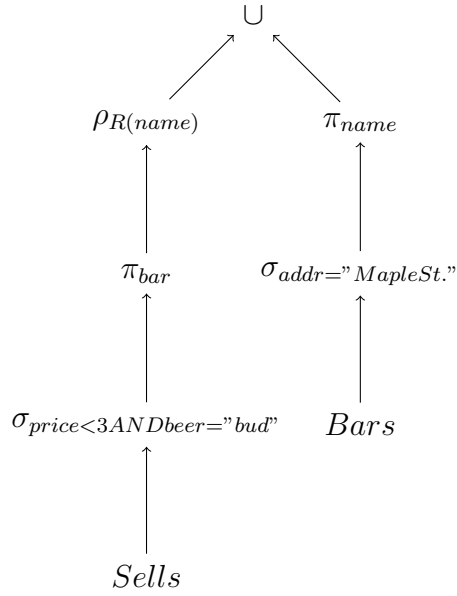


Figure 1: Find the names of all bars that are either on maple street or sell Bud for less than \$3

1.4 Relational Algebra on Bags

A bag is like a set, but duplicate elements are allowed. SQL is a bag language. Operations like projection are more efficient on bags than on sets.

1.4.1 Bag Union

Just add elements together, including duplicates.

$$\{1, 2, 1\} \cup \{1, 1, 2, 3, 1\} = \{1, 1, 1, 1, 1, 2, 2, 3\}$$

1.4.2 Bag Intersection

Minimum number of duplicates in resulting set.

$$\{1, 2, 1, 1\} \cap \{1, 2, 1, 3\} = \{1, 1, 2\}$$

1.4.3 Bag Difference

Result contains all tuples in first relation that aren't in the second.

$$\{1, 2, 1, 1\} - \{1, 2, 3\} = 1, 1$$

1.4.4 Bag Laws != Set Laws

Set union is **idempotent**, (result does not change if applied multiple times.)

For a bag union, if x appears n times in S, then it appears 2n times in union.

2 Why SQL?

SELECT desired attributes

FROM one or more tables

WHERE some condition holds