

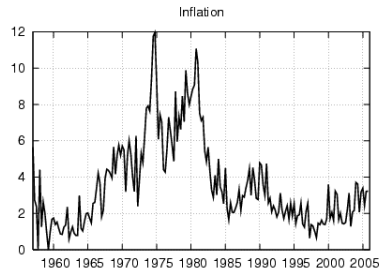
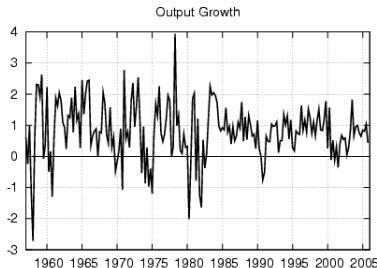
# Regime Switching, Learning, and the Great Moderation

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Dahl School of Business  
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January 23, 2009

# Time Varying Volatility

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# Purpose

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- How much does “bad luck” explain changing volatility when adaptive expectations react to suspicions of structural changes.
- **Great Moderation:** seemingly permanent reduction in macroeconomic volatility since approximately 1982.
- **Bad Luck:** volatile periods were hit with bad shocks.
- **Adaptive Expectations:**
  - Least squares learning - agents run least-squares regressions
  - Predict output and inflation using lagged output, inflation, and interest rates as explanatory variables.

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# Great Moderation Explanations

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- Good vs. bad policy.
  - Lubik and Schorfheide (2004): find monetary policy was destabilizing pre-Volker.
  - Milani (2005): accounting for learning, little evidence of a change in monetary policy.
- Bad luck
  - Sims and Zha (2006): evidence points in favor of bad shocks.
  - Bullard and Singh (2007): bad luck + Bayesian learning.
- Learning
  - It is possible for learning *alone* to generate time-varying volatility.
  - Primiceri (2005), Orphanides and Williams (2005): Monetary authority was optimizing, but mis-informed.

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# Learning Gain

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- Learning gain: how much weight is given to the last (most recent) observation.
- Decreasing learning gain
  - Ordinary least squares - learning gain  $= 1/n$ .
  - As time progresses, sample size increases, learning gain decreases.
  - Implies agents do not suspect structural change.
  - Learning dynamics disappear over time.
- Constant learning gain
  - Gives more weight to most recent observations - weight declines geometrically with time.
  - Agents have constant suspicion of structural change.
  - Learning dynamics persist in the long run.

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# Dynamic Learning Gain

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- Dynamic Gain Learning: agents endogenously switch between decreasing and constant learning gain.
  - Agents use decreasing gain unless forecast errors exceed a threshold.
  - Threshold = historical average absolute value forecast error.
  - Agents only suspect structural change when forecast errors are exceptionally high.
- Milani (2007): generates ARCH time-varying volatility
- Marcet and Nicolini (2003): recurrent hyperinflations.

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# Approach

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- Use a standard, commonly estimated monetary model: New Keynesian Model.
  - Three equation model with optimizing consumers, sticky prices, monetary policy.
  - Stochastic shocks: demand shock, cost-push shock, monetary policy shock.
- Augment the model with dynamic gain learning.
- Also estimate model under RE and constant gain learning.
- Augment the model with Markov switching process for volatility.
  - Volatile regime: shocks have high variances.
  - Less volatile regime: shocks have relatively lower variances.
  - Economy switches between these two regimes by luck.

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# Questions

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- Does the dynamic gain model predict a lower likelihood economy was in volatile regime?
  - Spoiler: No.
- When is the economy in the volatile regime?
  - Spoiler: All models predict dates surrounding NBER recessions of 1970s.
- Does the dynamic gain model predict lower variances for volatile regime shocks?
  - Spoiler: Yes.
- When are agents using larger learning gain?
  - Spoiler: During most of the 1970s.
- What expectations mechanism fits the data best?
  - Spoiler: Rational expectations, constant gain learning, decreasing learning have nearly identical fit.

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## New Keynesian Model: Optimal Consumer Behavior 8/ 22

- Consumers maximize net present value of lifetime utility, subject to their budget constraint.
- As the real interest rate increases, consumers decide to save more, consume less.
- The size of this effect depends on the **intertemporal elasticity of substitution**, estimated in paper.
- As the expected inflation rate rises, expected real interest rate falls.
- Habit formation: current consumption (current utility) depends on past consumption.
- **Degree of habit formation** is between 0 and 1, estimated in paper.
- Consumption subject to a *demand shock*.

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- **Degree of habit formation** is between 0 and 1, estimated in paper.
- Consumption subject to a *demand shock*.

## New Keynesian Model: Optimal Consumer Behavior 8/ 22

- Consumers maximize net present value of lifetime utility, subject to their budget constraint.
- As the real interest rate increases, consumers decide to save more, consume less.
- The size of this effect depends on the **intertemporal elasticity of substitution**, estimated in paper.
- As the expected inflation rate rises, expected real interest rate falls.
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# New Keynesian Model: Optimal Producer Behavior 9/ 22

- Monopolistically competitive firms.
- Exogenously sticky prices: it takes firms an uncertain amount time to appropriately adjust prices to maximize profits.
- Sticky prices enable monetary policy to have real effects on short-run output.
- Price indexation: when firms cannot re-optimize prices, they raise their prices by the past period's rate of inflation.
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# New Keynesian Model: Monetary Policy

10/ 22

- Fed adjusts Federal Funds Rate according to Taylor (1993) rule.
- Federal funds rate in response to:
  - output gap
  - inflation rate
  - past federal funds rate (Fed makes smooth adjustments)
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# Estimation Procedure

11 / 22

- **Maximum Likelihood**
  - Use Kim and Nelson (1999) method.
- Quarterly data from 1960:Q1 through 2008:Q1
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- Pre-sample period to initialize expectations: 1954:Q3 - 1959:Q4.
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# Parameter Estimates

12/ 22

|                | Parameter        | Rational Expectations | Dynamic Gain    | Constant Gain   |
|----------------|------------------|-----------------------|-----------------|-----------------|
| $\sigma_{n,L}$ | Nat. Rate (Low)  | 0.1768 (0.3720)       | 0.0454 (0.0217) | 0.0931 (0.0572) |
| $\sigma_{u,L}$ | Cost Push (Low)  | 0.0023 (0.0001)       | 0.0045 (0.0004) | 0.0042 (0.0001) |
| $\sigma_{r,L}$ | MP Shock (Low)   | 0.0013 (0.0001)       | 0.0012 (0.0000) | 0.0012 (0.0000) |
| $\sigma_{n,H}$ | Nat. Rate (High) | 0.4295 (0.9056)       | 0.0966 (0.0485) | 0.1794 (0.1144) |
| $\sigma_{u,H}$ | Cost Push (High) | 0.0044 (0.0004)       | 0.0092 (0.0010) | 0.0085 (0.0005) |
| $\sigma_{r,H}$ | MP Shock (High)  | 0.0070 (0.0005)       | 0.0064 (0.0003) | 0.0056 (0.0002) |
| $p_L$          | P(Remain Low)    | 0.9609 (0.0224)       | 0.9724 (0.0097) | 0.9780 (0.0109) |
| $p_H$          | P(Remain High)   | 0.8099 (0.0578)       | 0.8924 (0.0264) | 0.9412 (0.0159) |
| $g$            | Learning Gain    | –                     | 0.0045 (0.0007) | 0.0000 (0.0018) |

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Expectations are not adaptive.

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Regimes are highly persistent.

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Learning predicts smaller variances of the natural rate shock.

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Variances of cost push and monetary shock are similar.

# Parameter Estimates

12/ 22

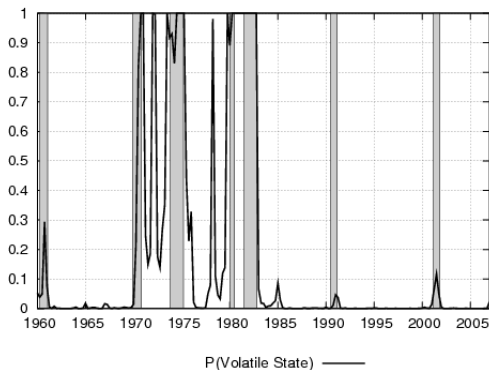
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# Regime-Switching Volatility

13/ 22

Rational Expectations  
Probability Economy is in the Volatile Regime

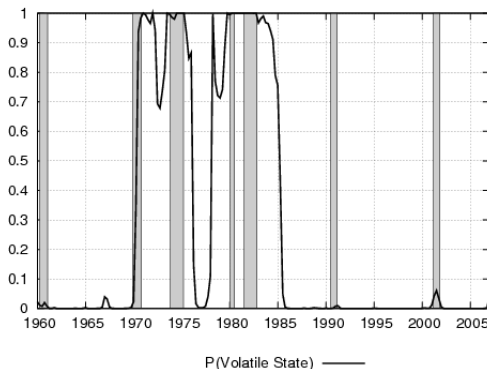


Expected 7.77 volatile years

# Regime-Switching Volatility

14/ 22

Constant Gain Learning  
Probability Economy is in the Volatile Regime



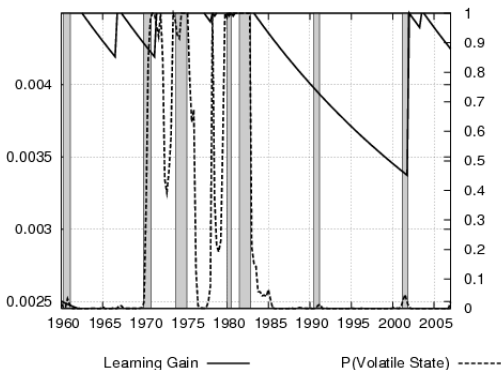
Expected 12.26 volatile years



# Regime-Switching Volatility

15/ 22

Dynamic Gain Learning  
Probability Economy is in the Volatile Regime  
and Evolution of the Learning Gain



Expected 9.17 volatile years

# Forecast Errors Comparison

16/ 22

|                          | Rational Expectations | Dynamic Gain    | Constant Gain   |
|--------------------------|-----------------------|-----------------|-----------------|
| RMSE Output Gap          | 3.12                  | 3.13            | 3.18            |
| RMSE Inflation           | 4.41                  | 4.69            | 4.69            |
| RMSE Federal Funds Rate  | 5.01                  | 5.05            | 5.09            |
| AR(1) Output Variance    | 0.0904 (0.0730)       | 0.1715 (0.0722) | 0.1240 (0.0728) |
| AR(1) Inflation Variance | 0.1760 (0.0716)       | 0.1364 (0.0699) | 0.1073 (0.0653) |
| AR(1) Fed Funds Variance | 0.3851 (0.0670)       | 0.3798 (0.0659) | 0.3798 (0.0636) |

- Rational Expectations actually (very slightly) fits data better than learning models.
- All models show some persistence in volatility of forecast errors.
- Models especially fail to explain changing volatility of the federal funds rate.

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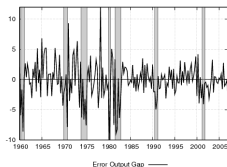
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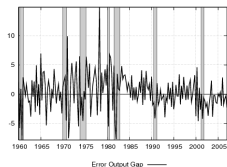
# Forecast Errors: Output Gap

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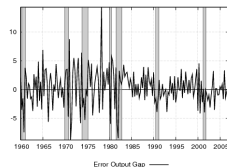
Rational Exp. (1.0)



Constant Gain (0.86)



Dynamic Gain (0.82)

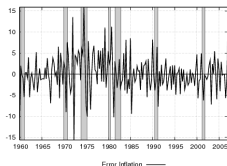


- (Correlation with Rational Expectations)
- All models made similar errors
- Most volatile during recessions in 1970s, early 1980s

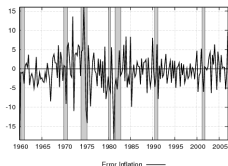
# Forecast Errors: Inflation

18/ 22

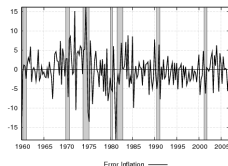
Rational Exp. (1.0)



Constant Gain (0.85)



Dynamic Gain (0.80)

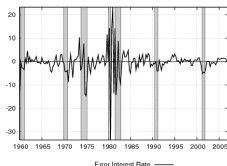


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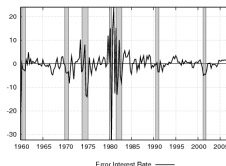
# Forecast Errors: Federal Funds Rate

19/ 22

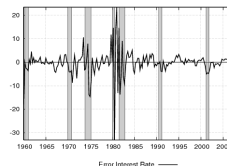
Rational Exp. (1.0)



Constant Gain (0.99)



Dynamic Gain (0.99)



- (Correlation with Rational Expectations)
- Essentially identical errors.
- Do not explain change in policy in early 1980s.

# Conclusions

20 / 22

- When allowing for regime-switching volatility, there is little evidence of adaptive expectations.
- Constant gain learning and dynamic gain learning both produce less volatility for the natural rate shock.
- Learning frameworks actually deliver a higher prediction for the time spent in volatile regime.
- All models make similar forecast errors at similar points in sample.
- Rational expectations model actually yields smallest in-sample MSE.



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# Conclusions

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  - Does living in a dormitory improve student performance?
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