

1) In this part we have to get the position of the robot by using wheel velocities. To do this, we can use the below equation

$$V_{\text{left}} = \omega_{\text{left}} \cdot R$$

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$$\dot{x} = -\frac{R}{2} \cdot \sin(\phi) (\omega_{\text{left}} + \omega_{\text{right}}) \cdot dt$$

$$\dot{y} = \frac{R}{2} \cdot \cos(\phi) (\omega_{\text{left}} + \omega_{\text{right}}) \cdot dt$$

$$\dot{\phi} = (V_{\text{right}} - V_{\text{left}}) \cdot dt / b$$

where,

$R$  = radius of the wheels

$\phi$  = heading of the robot

$dt$  = duration between intervals

$b$  = wheel separation.

This equations can be change based on the chosen coordinate frame.

2) In this part, we have to calculate the necessary velocity values using APF.

$$F_A = G_A \cdot (g - p)$$

$$\gamma = (g - p)^T (g - p)$$

$$F_R = G_R \cdot \gamma \cdot \sum_{i=1}^n (p - o_i) / ((p - o_i)^T (p - o_i) - (r_r + o_r))$$

$$F = F_A + F_R$$

where:

- $G_A$ : Attractive gain
- $p$ : current position of the robot.
- $g$ : goal position

$G_R$ : Repulsive gain

Output  $F$  is the necessary force vector to reach goal.