

LAB 4

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1:  $A \sim \text{Exp}(\frac{1}{80})$   
 $B \sim \text{Exp}(\frac{1}{80})$   
 $C \sim \text{Exp}(\frac{1}{80})$

first, the CDF

$$Y = \max(A, B, C)$$

$$F(y) = P(Y \leq y)$$

$$= P(A \leq y \text{ \& } B \leq y \text{ \& } C \leq y)$$

$$(\text{independent}) = P(A \leq y) \cdot P(B \leq y) \cdot P(C \leq y)$$

$$= (1 - e^{-y/80}) \cdot (1 - e^{-y/80}) \cdot (1 - e^{-y/80})$$

$$= (1 - e^{-y/80})^3$$

CDF of Y  $\rightarrow F(y) = 3e^{-\frac{y}{40}} - 3e^{-\frac{y}{80}} - e^{-\frac{3y}{80}} + 1$

$$\text{PDF} = \frac{d}{dx} \text{CDF}$$

$$= \frac{d}{dx} \left( 3e^{-y/40} - 3e^{-y/80} - e^{-3y/80} + 1 \right)$$

$$f(y) = \frac{-3}{40} e^{-\frac{y}{40}} + \frac{3}{80} e^{-\frac{y}{80}} + \frac{3}{80} e^{-\frac{3y}{80}} \quad (\text{PDF of } Y)$$