Recursion in Prolog. Compound terms

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Compound terms

Definition

Compound terms are composed of an atom called *functor* and a sequence of one or more terms called *arguments*.

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The functor acts as the name of the compound term.

Note: The arguments can be themselves compound terms.

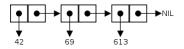
Examples of compound terms

Example of a structure defining a person and of the predicates to extract the information.

```
\% A compound term defining a person with a name and
% a location
person('Alex', location(craiova, romania)).
% Name extractor
name(person(Name, _), Name).
% Location extractor
location(person(_, Location), Location).
% City extractor
city(person(_, location(City, _)), City).
```

Examples of compound terms (cont'd)

Compound terms can be used to define complex data structures such as linked lists.

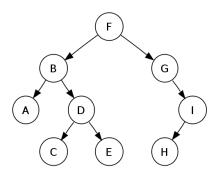


Example

cons(42, cons(69, cons(613, nil))).

Examples of compound terms (cont'd)

Compound terms can be used to define complex data structures such as trees.



Examples of compound terms (cont'd)

```
node(f,
    node(b,
        node(a, leaf, leaf),
        node(d,
            node(c, leaf, leaf),
            node(e, leaf, leaf))),
    node(g,
        leaf,
        node(i,
            node(h, leaf, leaf),
            leaf)))
```

Recursion scheme
(accursion scheme (cont'd)
Recursion example
Recursion example (cont'd)
Recursion example (cont'd)
Tail recursion
Tail calls
Tail calls (cont'd)

Recursion

While defining some rules it is sometimes necessary to refer to the rule we are defining.

Recursion scheme
Recursion scheme (cont'd)
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Recursion example (cont'd)
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Recursion

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Such rules are called *recursive* predicates.

Recursion scheme
Recursion scheme (cont'd)
Recursion example
Recursion example (cont'd)
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Tail recursion
Tail calls
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Recursion

While defining some rules it is sometimes necessary to refer to the rule we are defining.

Such rules are called *recursive* predicates.

Where you would use a loop (e.g. for, while) in an imperative language, in Prolog you use a recursive predicate.

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls

Recursion scheme

A recursive predicate usually has:

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Recursion scheme

A recursive predicate usually has:

base case acts as a termination condition

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Recursion scheme

A recursive predicate usually has:

base case acts as a termination condition recursive case the main part of the predicate

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls

Recursion scheme

A recursive predicate usually has:

base case acts as a termination condition recursive case the main part of the predicate

Note: in some cases the base case is not mandatory since the termination condition can be checked in other ways.

Recursion scheme

The basic shape of a recursive predicate in Prolog:

```
predicate(t_1, \ldots, t_n).
predicate(t_1, \ldots, t_n):-
g_1, \ldots, g_n.
```

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls Tail calls (cont'd)

Recursion example

Assuming we have a knowledge base with the appropriate predicates and we wanted to find the ancestor of a person X we could (naively) go about it like this:

Recursion example

Assuming we have a knowledge base with the appropriate predicates and we wanted to find the ancestor of a person X we could (naively) go about it like this:

```
ancestor(X, Y) :- parent(X, Y).
ancestor(X, Y) :-
   parent(X, A1), parent(A1, Y).
ancestor(X, Y) :-
   parent(X, A1), parent(A1, A2), parent(A2, Y).
...
ancestor(X, Y) :-
   parent(X, A1), ..., parent(AN, Y).
```

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls Tail calls (cont'd)

Recursion example (cont'd)

We could define the ancestor relation as:

Recursion scheme
Recursion scheme (cont'd)
Recursion example
Recursion example (cont'd)
Recursion example (cont'd)
Tail recursion
Tail calls
Tail calls (cont'd)

Recursion example (cont'd)

We could define the ancestor relation as:

Definition

X is the ancestor of Y if X is a direct parent of Y

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls Tail calls (cont'd)

Recursion example (cont'd)

We could define the ancestor relation as:

Definition

- X is the ancestor of Y if X is a direct parent of Y
- X is the ancestor of Y if X is a direct parent of Z and Z is the ancestor of Y

Recursion scheme
Recursion scheme (cont'd)
Recursion example
Recursion example (cont'd)
Recursion example (cont'd)
Tail recursion
Tail calls
Tail calls (cont'd)

Recursion example (cont'd)

```
ancestor(X, Y) :- parent(X, Y).
ancestor(X, Y) :-
parent(X, Z), ancestor(Z, Y).
```

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls Tail calls (cont'd)

Tail recursion

Often recursive implementations are not as efficient as iterative ones.

Recursion scheme
Recursion scheme (cont'd)
Recursion example
Recursion example (cont'd)
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Tail recursion

Often recursive implementations are not as efficient as iterative ones.

This happens because recursion wastes stack space.

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls Tail calls (cont'd)

Tail recursion

Often recursive implementations are not as efficient as iterative ones.

This happens because recursion wastes stack space.

The solution is to use *tail recursion* implemented by *tail calls*.

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls Tail calls (cont'd)

Tail calls

Definition

A tail call is a call in the tail position of the recursive rule.

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls

Tail calls

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A tail call is a call in the tail position of the recursive rule.

Tail calls allow for efficient implementations of recursive predicates.

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Tail calls

Definition

A tail call is a call in the tail position of the recursive rule.

Tail calls allow for efficient implementations of recursive predicates.

Note: the ancestor predicate we defined earlier is tail recursive.

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls

Tail calls

Definition

A tail call is a call in the tail position of the recursive rule.

Tail calls allow for efficient implementations of recursive predicates.

Note: the *ancestor* predicate we defined earlier is tail recursive.

Note: sometimes in order to make a predicate tail recursive we can use accumulators.

Recursion scheme Recursion scheme (cont'd) Recursion example Recursion example (cont'd) Recursion example (cont'd) Tail recursion Tail calls

Tail calls

The basic shape of a tail recursive predicate in Prolog: