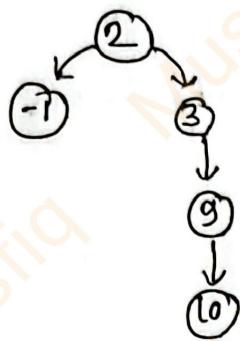


"Data Structure and Algorithms"

2-1
27-05-23

Sorting Algorithm →



Sorting Algorithm →



- * जो एक एवं दूसरे से छोटा हो तो उसे अगले स्थान पर बदला दिया जाता है।
- * यह एक विशेष रूप से एक अवधारणा है।

Types of Sort :

- Insertion sort
- Merge sort
- counting sort
- Quick sort
- bubble sort
- Selection sort

"Insertion Sort"

Process ↴

- ① अपने दूसरे तक 2nd element को बदला दिया।
- ② Starting will be run n times.
- ③ Ascending → 1, 2, 3, 4, 5, 6.
- ④ Descending → 6, 5, 4, 3, 2, 1

21.07.23

Insertion Sort

50

key \rightarrow यह वाला अंकों का संग्रह है {5, 2, 4, 6, 1, 3}

Insertion Sort (A, n)	cost	Times
1, for (i = 2 to n) {	c_1	n
2, key = A[i]	c_2	$n-1$
3, j = i - 1	c_3	$n-1$
4, while (j > 0 && A[j] > key) {	c_4	$j = t_2 + t_3 + t_4 + t_5 + t_6$ 2 2 1 5 4 = 14
5, A[j+1] = A[j]	c_5	$g - (n-1)$
6, j = j - 1 ;	c_6	$g - (n-1)$
7, A[j+1] = key	c_7	n-1

$$T(n) = c_1 n + c_2 (n-1) + c_3 (n-1) + c_4 g + c_5 (g - (n-1)) + c_6 (g - (n-1)) + c_7 (n-1)$$

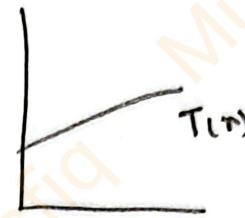
$$= c_8 T + c_9 n + c_{10}$$

Best case \rightarrow array already sorted [1, 2, 3]
 $(O(n))$

Worst case \rightarrow array n n in descending Order [3, 2, 1]
 $(O(n^2))$

Sonated \rightarrow

$$\begin{aligned}
 T(n) &= C_8(n-1) + C_9n + C_{10} \\
 &= C_8n - C_8 + C_9n + C_{10} \\
 &\approx n(C_8 + C_9) + C_{10} - C_8 \\
 &= an + b \\
 &= O(n)
 \end{aligned}$$



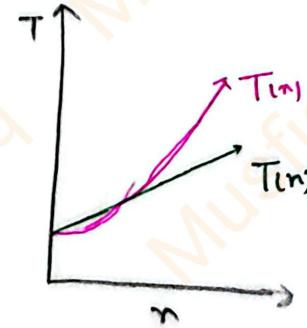
unsonated \rightarrow

$$\begin{aligned}
 T &= 2+3+4+\dots+n \\
 &\approx 2+3+4+\dots+n \\
 &\approx 1+2+3+\dots+n-1 \\
 &= \frac{n(n+1)}{2} - 1
 \end{aligned}$$

$$1+2+3+\dots$$

Worst case

$$\begin{aligned}
 T(n) &= C_8 \left[\frac{n(n+1)}{2} - 1 \right] + C_9n + C_{10} \\
 &= C_8 \left[\frac{n^2}{2} + \frac{n}{2} - 1 \right] + C_9n + C_{10} \\
 &= C_8 \frac{n^2}{2} + C_8 \frac{n}{2} - C_8 + C_9n + C_{10} \\
 &= \frac{C_8}{2} n^2 + n \left(\frac{C_8}{2} + C_9 \right) + (C_{10} - C_8) \\
 &\approx an^2 + bn + c \\
 &= O(n^2)
 \end{aligned}$$



Upper bound Notation

$$f(n) = O(g(n)) \rightarrow \exists c, n_0$$

$$T(n) = O(n^2)$$

$$an^2 + bn + c = O(n^2)$$

$$0 \leq f(n) \leq c \cdot g(n)$$

for some c and n_0
where, $n \geq n_0$

Qn: Show that $f(n) = 10n^2 + 7n + 4 = O(n^2)$

$$g(n)$$

$$0 \leq f(n) \leq c \cdot g(n)$$

$$\text{Let } c = 15$$

$$n=1, f(1) = 10+7+4 = 21, c \cdot g(n) = 15^{15} \cdot n^2 = 15$$

$$n=2, f(2) = 10 \times 4 + 14 + 4 = 58, c \cdot g(n) = 60$$

$$n=3, f(3) = 90 + 21 + 4 = 115, c \cdot g(n) = 135$$

$$\boxed{c=15, n_0=2} \rightarrow \text{satisfied.}$$

* Show that $f(n) = 10n^2 + 4n = O(n^3)$

$$= O(n^3) + (10n^2 + 4n) = O(n^3)$$

$$c=5$$

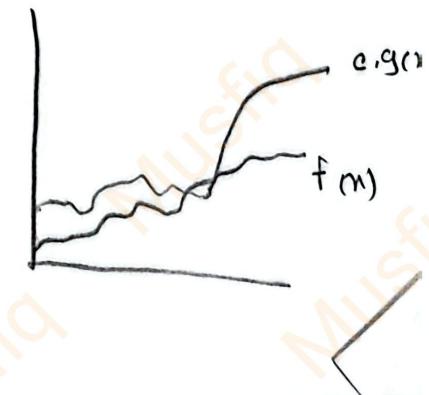
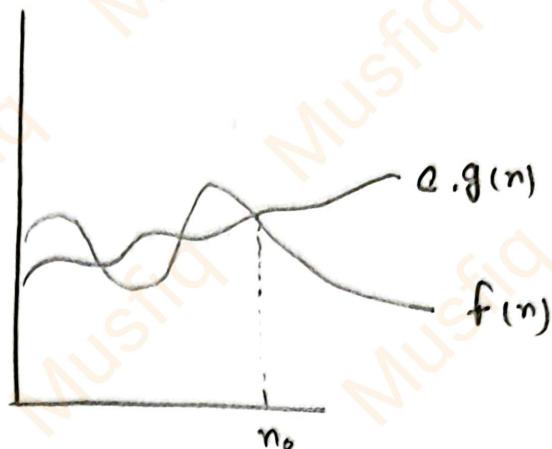
$$n=1, f(1) = 14 ; c \cdot g(n) = 5$$

$$n=2, f(2) = 48 ; c \cdot g(n) = 40$$

$$n=3, f(3) = 102 ; c \cdot g(n) = 135$$

$$\boxed{c=5, n_0=3}$$

$\exists \rightarrow \text{there exist}$
 $\forall \rightarrow \text{For all}$



$$\begin{aligned}
 & \# O(n^2) + O(n^3) + O(n) \\
 & = O(n^3) + O(n^3) + O(n^3) \\
 & = O(n^3)
 \end{aligned}$$

$O(n^3) \rightarrow O_n$
faster growth

Lower Bound Notation

$$\# 5n^2 + 6n + 4 = O(n^2)$$

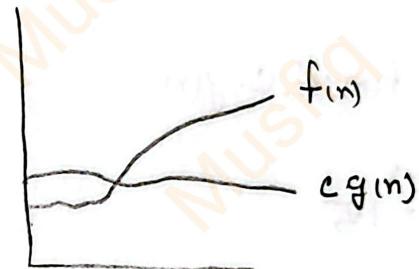
$$\begin{aligned}
 0 \leq f(n) \leq c \cdot g(n) & \rightarrow \text{Upper} \\
 0 \leq c \cdot g(n) \leq f(n) & \rightarrow \text{Lower}
 \end{aligned}$$

$$c=2$$

$$n=1, f(1) = 5+6+4=15, c \cdot g(n) = 2$$

$$n=2, f(2) = 20+12+4=36, c \cdot g(n) = 8$$

$$c=2, n=1$$



Asymptotic Tight Bound (Θ):

$$f(n) = 5n^2 + 6n + 3$$

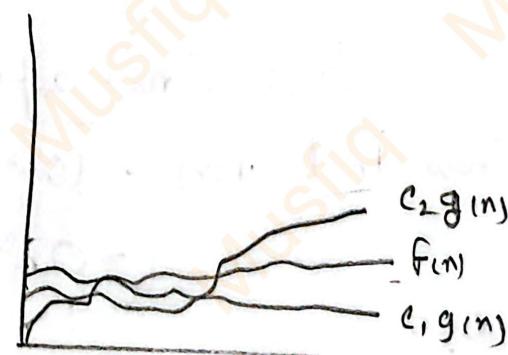
$$\text{condition} \rightarrow c_2 g(n) \leq f(n) \leq c_1 g(n)$$

$$f(n) = 5n^2 + 6n + 3 = O(n^2)$$

$$c=5, n=3$$

$$f(n) = 5n^2 + 6n + 3 = \Omega(n^2)$$

$$c=2, n=2$$



Counting (contd)

(i) External array $\text{Ans}[0 \dots 24]$ (ii) Maximum number Assumed Assumption $\text{Ans}[24] = 25$ (iii) Negative value $\text{Ans}[0 \dots -1]$ Simulation \rightarrow

$$A = \frac{2}{5} \quad \frac{3}{5} \quad \frac{0}{5} \quad \frac{2}{5} \quad \frac{3}{5} \quad \frac{0}{5} \quad \frac{3}{5}$$

 $k=5$

$$C = \frac{2}{0} \quad \frac{0}{1} \quad \frac{2}{2} \quad \frac{3}{3} \quad \frac{0}{4} \quad \frac{1}{5}$$

Adding

$$C : \frac{2}{0} \quad \frac{2}{1} \quad \frac{4}{2} \quad \frac{7}{3} \quad \frac{7}{4} \quad \frac{8}{5}$$

Adding B :

$$A : \frac{2}{1}, \frac{5}{2}, \frac{3}{3}, \frac{0}{4}, \frac{2}{5}, \frac{3}{6}, \frac{0}{7}, \frac{3}{8}$$

$$B : \frac{0}{1}, \frac{0}{2}, \frac{2}{3}, \frac{2}{4}, \frac{3}{5}, \frac{3}{6}, \frac{3}{7}, \frac{8}{8}$$

$$\frac{0}{1}, \frac{0}{2}, \frac{2}{3}, \frac{1}{4}, \frac{3}{5}, \frac{2}{6}, \frac{1}{7}, \frac{3}{8}$$

$$C : \frac{2}{0}, \frac{2}{1}, \frac{4}{2}, \frac{7}{3}, \frac{7}{4}, \frac{8}{5}, \frac{8}{6}, \frac{2}{7}, \frac{4}{8}$$

$$\frac{0}{0}, \frac{2}{1}, \frac{4}{2}, \frac{7}{3}, \frac{7}{4}, \frac{8}{5}, \frac{8}{6}, \frac{2}{7}$$

$$\text{Final } C : \frac{0}{0}, \frac{2}{1}, \frac{2}{2}, \frac{4}{3}, \frac{7}{4}, \frac{7}{5}$$

$$\begin{aligned} \text{Show that } f(n) &\approx 5n^2 + 6n + 3 = \Theta(n^2) \\ &= O(n^2) \\ &\approx n^2 \end{aligned}$$

Condition \downarrow
 $c_2 g(n) \leq f(n) \leq c_1 g(n)$

A
L

Array Mapping :

L_1 = first index.

A [0.....6] →

0	1	2	3	4	5	6

formula →

$$\text{addr}_R(A[i]) = b + (i - l_1) \times L$$

→ base address
 → array first index
 → variable type size

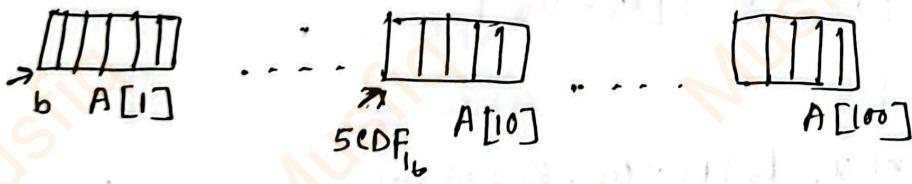
(1D)

$$\begin{aligned}
 \text{add}(A[3]) &= b + (i - l_1) \times L \\
 &\geq 10 + (3 - 0) \times \\
 &\geq 10 + 12 \\
 &= 22.
 \end{aligned}$$

2D

double [1...100]
↓
i
↓
ui

Given, $\text{addr}(A[10]) = 5C0F_{16}$. Find the address of $A[60]_z$,



$$\text{add}(A[10]) = b \cdot (i-l_1) \times L$$

$$b = \text{addr}[A[10]] - (i-1, s)$$

$$\approx 5 \text{DF}_{16} - (10-1) \times 8$$

$$= 5 \text{CDF}_{\text{H}} - 72$$

= 23775-70

$\approx 50\%$

NOW,

$$\text{addr}_2(A[607]) = b + (i - l_1) \times$$

$$= 5093 - (60-1) \times ④$$

$$= 5097 + 472$$

$$= 23703 + 472$$

= 23231

= .24175

$$= (5R6F)_{16}$$

Row Major:

(2D)

$$A[0 \dots 2] [0 \dots 3]$$

l_1

u_1

l_2

u_2

C-2
06-06

$$\text{addr}(a[i][j]) = b + (i-l_1) \times (u_2 - l_2 + 1) \times L + (j - l_2) \times L$$

$$\begin{aligned} \text{addr}(a[1][2]) &= 10 + (1-0) \times (3-0+1) \times 4 + (2-0) \times 4 \\ &= 34. \end{aligned}$$

Column Major:

$$\text{addr}(A[i][j]) = b + (j - l_2) \times (u_1 - l_1 + 1) \times L + (i - l_1) \times L$$

$$A[1 \dots 3][1 \dots 4]$$

$$\begin{aligned} \text{addr}(A[1][2]) &= 10 + (2-1) \times (3-1+1) \times 4 + (1-1) \times 4 \\ &= 10 + 1 \times 3 \times 4 + 0 \\ &= 10 + 12 \\ &= 22. \end{aligned}$$

(3D) \rightarrow

$$a[l_1 \dots u_1] [l_2 \dots u_2] [l_3 \dots u_3]$$

$$a[i][j][k]$$

$$\begin{aligned} &= b + (i-l_1) \times (u_2 - l_2 + 1) \cdot \frac{(u_3 - l_3 + 1)}{3} \times L + (j - l_2) \times \frac{(u_3 - l_3 + 1)}{3} \times L \\ &\quad + \frac{(k - l_3)}{3} L \end{aligned}$$

(4D) \rightarrow

$$a[l_1 \dots u_1] [l_2 \dots u_2] [l_3 \dots u_3] [l_4 \dots u_4]$$

$$a[i][j][k][l]$$

$$\begin{aligned} &= b + (i-l_1) \times (u_2 - l_2 + 1) \cdot (u_3 - l_3 + 1) \cdot (u_4 - l_4 + 1) \times L + (j - l_2) \\ &\quad \times (u_3 - l_3 + 1) \cdot (u_4 - l_4 + 1) \times L + (k - l_3) \times (u_4 - l_4 + 1) \times L + (x - l_4) L \end{aligned}$$

linear search

```

int LinearSearch( int b[], int skey) {
    int i;
    for( i=0; i<size; i++ ) — n+1
        if ·b[i] == skey — 3
            return i — 1/0
    return -1 — 1/0

```

Time Complexity

$$\begin{aligned}
T(n) &= C_1(n+1) + C_2n + C_31 \\
&= O(n) \\
&= \Omega(n) \\
&= \Theta(n)
\end{aligned}$$

Best case : T_{best} : $C_1 + C_2 + C_3 = O(1)$

$$\begin{aligned}
&= O(1) \\
&= \Omega(1) \\
&= \Theta(1)
\end{aligned}$$

Average Case :

$$\text{Avg. time} = \frac{\text{Time required for all possible case}}{\text{Total number of case}}$$

$$\begin{aligned}
&= \frac{(1+2+3+\dots+n)C}{n} \\
&= \frac{\frac{n(n+1)}{2} \times C}{n} \\
&\approx \frac{n+1}{2} \times C \\
&= O(n)
\end{aligned}$$

Binary Search:

Binary Search (A, n, key)

```
1, i = 1 , j = n  
2, while (i <= j)  
3,   mid =  $\lfloor \frac{i+j}{2} \rfloor$   
4,   if (array [mid] == key)  
5,     return mid  
6,   else if (A[mid] < key)  
7,     i = mid + 1  
8,   else if (A[mid] > key)  
9,     j = mid - 1  
10,  return -1
```

R Bin Search (A, l, h, key)

```
if (l > h)  
  return -1  
else:  
  mid =  $\lfloor \frac{l+h}{2} \rfloor$   
  if key == A[mid]  
    return mid  
  if A[mid] < key  
    return RBinSearch (A, mid+1, j, key)  
  if A[mid] > key  
    return RBinSearch (A, i, mid-1, key)
```

x, y, z, p, n, t / $\text{high} = n-1$
 $\text{key} = y$ $\text{low} = 0$

$x = 34, y = 37, z = 71, p = 108, n = 179, t = 287$

$\text{key} = 37$

$\text{while}(l \leq h)$

0	1	2	3	4	5
34	37	71	108	179	287
↑		↑ m		↑	

$$\text{mid} = \left\lfloor \frac{o+5}{2} \right\rfloor = \left\lfloor 2.5 \right\rfloor$$

$$= 2$$

$$A(m) > k$$

$$n = m - 1$$

$$A(m) \cdot$$

$$b = \text{mid} + 1$$

$$m = \frac{o+1}{2} = \left\lfloor 0.5 \right\rfloor = 0$$

34	37	71	108	179	287
↑	↑ m	↑			
↑ m					

now, found in index $\underline{1}$

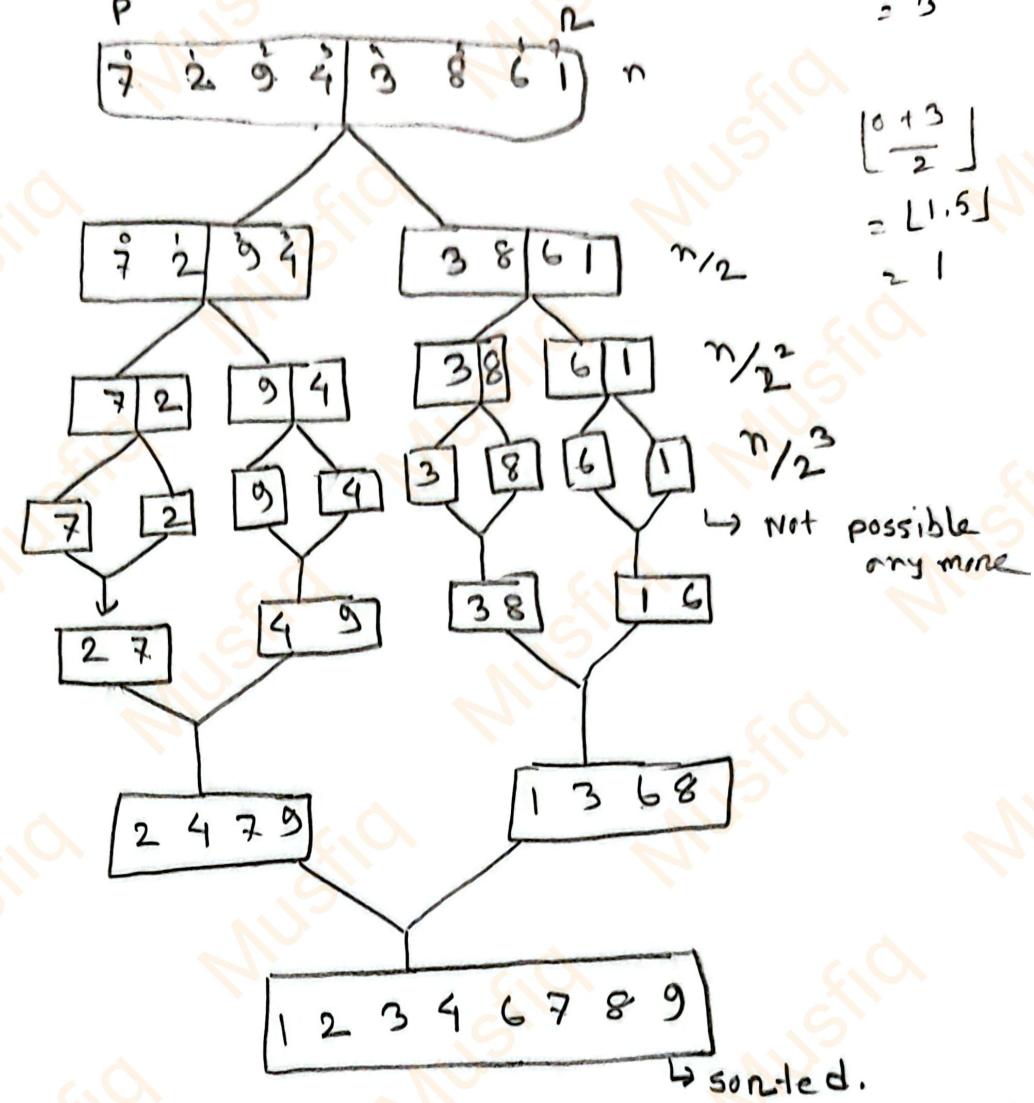
$$1 \leq 1$$

$$m = \left\lfloor \frac{1+1}{2} \right\rfloor = \left\lfloor 1 \right\rfloor = 1$$

$$A[m] = \underline{\underline{k}}$$

Merge Sort · Simulations

7 2 9 4 3 8 6 1
P



pick sort Partition

Partition Function

F L
20 10 5 6 7 3 4
3 4 5 6 7 10 20 — sorted.

① 'i' keep track of the elements smallest than the Pivot (backward)

② 'j' keeps track of the elements that are yet to be explored (forward)

• 'j' keep track of the element that are greater than the the Pivot (backward)

मान्यता
① i वृक्ष अंक 0/-1 तथा, j वृक्ष 2(ज), first index अंक
if index →
if index → 0

② j compare 2(ज) Pivot value एवं मान्यता, ③ Pivot अंक 2(ज) j++
and value of j swap with value of i.

Pivot Position = random (P, R)

x = A[Pivot Position]

i = P-1

for (j=1 to R)

 if (j == Pivot Position)

 continue

 if (A[j] < x)

 i = i + 1

 swap A[i] with A[j]

 swap A[i] with A[Pivot Position]

return i.

④ j का अंकीय Pivot position (रास्ता, जहां Pivot लाई थी) Index 2(ज) अंकल जे close होते, i++
अंक Pivot value एवं मान्यता exchange/swap होती है।

⑤ Pivot mid index 2(ज)
Q position j skip करता है।

$\theta \rightarrow \leftarrow L$

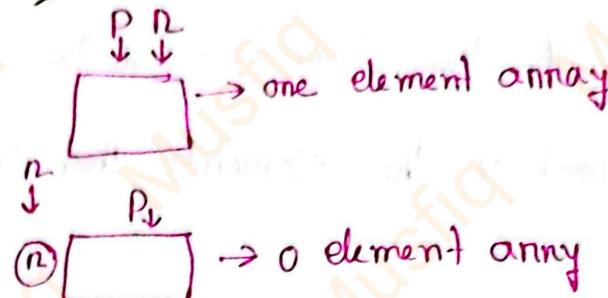
Quick sort (A, P, R)

if ($P < R$)

$q = \text{Partition } (A, P, R)$

Quick Sort ($A, P, q-1$)

Quick Sort ($A, q+1, R$)



Time complexity :

- ① Best case $\rightarrow O(n \log n)$
- ② Worst case $\rightarrow O(n^2)$
- ③ Average case $\rightarrow O(n \log n)$

Qn - Given Array. 2 8 7 1 3 5 6 4, start with 1 index

$$P \\ i=0, j=1 \rightarrow \frac{2}{1} \quad \frac{8}{2} \quad \frac{7}{3} \quad \frac{1}{4} \quad \frac{3}{5} \quad \frac{5}{6} \quad \frac{6}{7} \quad \frac{4}{8}$$

$$i=1, j=1 \rightarrow 2 \quad 8 \quad 7 \quad 1 \quad 3 \quad 5 \quad 6 \quad 4$$

Pivot $x = 4$

$$\frac{2}{1} \quad \frac{8}{\cancel{j}} \quad \frac{7}{j} \quad 1 \quad 3 \quad 5 \quad 6 \quad 4$$

$$\frac{2}{\cancel{i}} \quad 8 \quad \frac{7}{\cancel{j}} \quad 1 \quad 3 \quad 5 \quad 6 \quad 4$$

$$\frac{2}{\cancel{i}} \quad 8 \quad 7 \quad \frac{1}{\cancel{j}} \quad 3 \quad 5 \quad 6 \quad 4$$

$$2 \quad \frac{8}{\cancel{i}} \quad 7 \quad \frac{1}{\cancel{j}} \quad 3 \quad 5 \quad 6 \quad 4$$

$$2 \quad \frac{1}{\cancel{i}} \quad 7 \quad \frac{8}{\cancel{j}} \quad 3 \quad 5 \quad 6 \quad 4$$

$$2 \quad \frac{1}{\cancel{i}} \quad 7 \quad 8 \quad \frac{3}{\cancel{j}} \quad 5 \quad 6 \quad 4$$

$$2 \quad 1 \quad \frac{7}{\cancel{i}} \quad 8 \quad \frac{3}{\cancel{j}} \quad 5 \quad 6 \quad 4$$

$$2 \quad 1 \quad \frac{3}{\cancel{i}} \quad 8 \quad \frac{7}{\cancel{j}} \quad 5 \quad 6 \quad 4$$

$$2 \quad 1 \quad \frac{3}{\cancel{i}} \quad 8 \quad 7 \quad \frac{5}{\cancel{j}} \quad 6 \quad 4$$

$$2 \quad 1 \quad \frac{3}{\cancel{i}} \quad 8 \quad 7 \quad 5 \quad \frac{6}{\cancel{j}} \quad 4$$

$$2 \quad 1 \quad 3 \quad \frac{8}{\cancel{i}} \quad 7 \quad 5 \quad \frac{6}{\cancel{j}} \quad 4$$

$$2 \quad 1 \quad 3 \quad \frac{8}{\cancel{i}} \quad 7 \quad 5 \quad \frac{6}{\cancel{j}} \quad 4 \rightarrow i++ \rightarrow j \text{ continue}$$

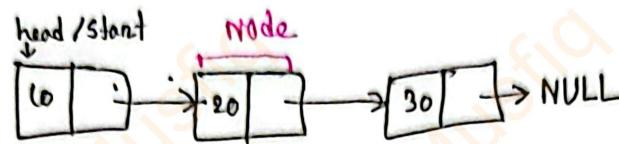
$$2 \quad 1 \quad 3 \quad \frac{8}{\cancel{i}} \quad 7 \quad 5 \quad \frac{6}{\cancel{j}} \quad \frac{8}{\cancel{8}} \rightarrow i \text{ swap with } A[\text{Pivot}]$$

return i;

linked List"

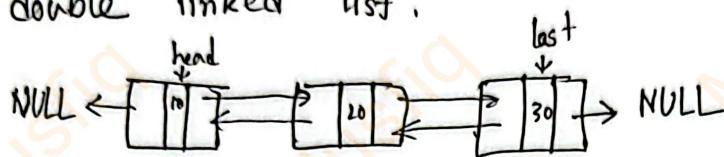
- ① Single Linked list
- ② double "
- ③ circular linked list

① Linear / Single linked list :



box = node

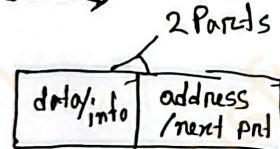
② double linked list :



③ circular linked list :



① Each node,



- * Insert
- * Delete
- * Search
- * Print

street Node {

```
int value;  
struct Node* next;};
```

}

① start = (node*) malloc (sizeof (node));

② temp = (node*) malloc (sizeof (node));

③ temp1 = (node*) malloc (sizeof (node));

④ start -> data = 10;

⑤ temp -> data = 40;

⑥ temp -> data = 30;

⑦ start -> next = temp1

⑧ start -> next -> next = temp

⑨ temp -> next = NULL

⑩ start -> next = temp1 -> next

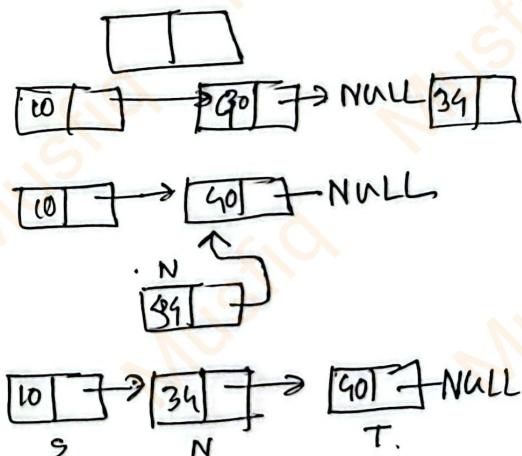
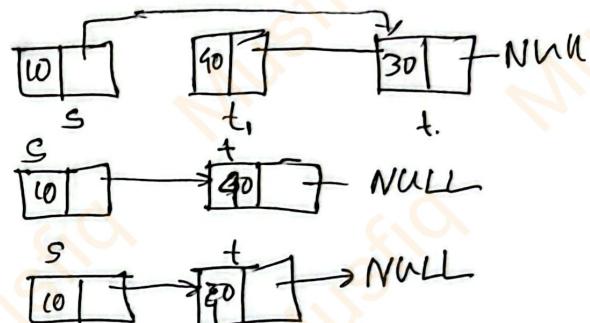
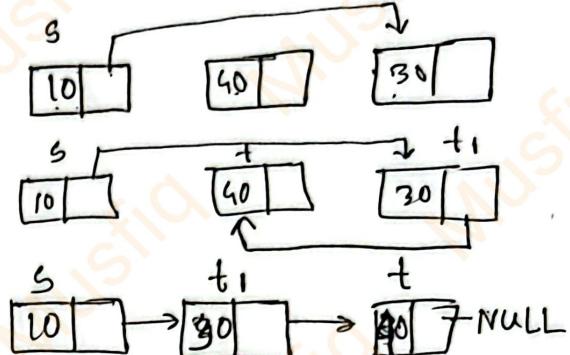
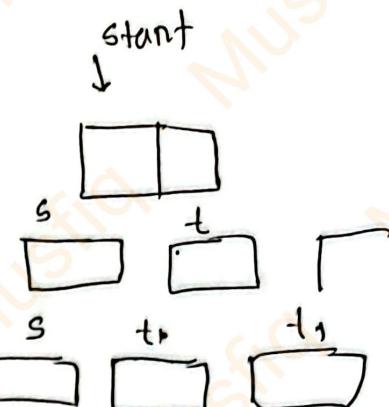
⑪ free (temp1)

⑫ newItem = (node*) malloc (sizeof (node));

⑬ newItem -> data = 34

⑭ newItem -> next = start -> next

⑮ start -> next = newItem

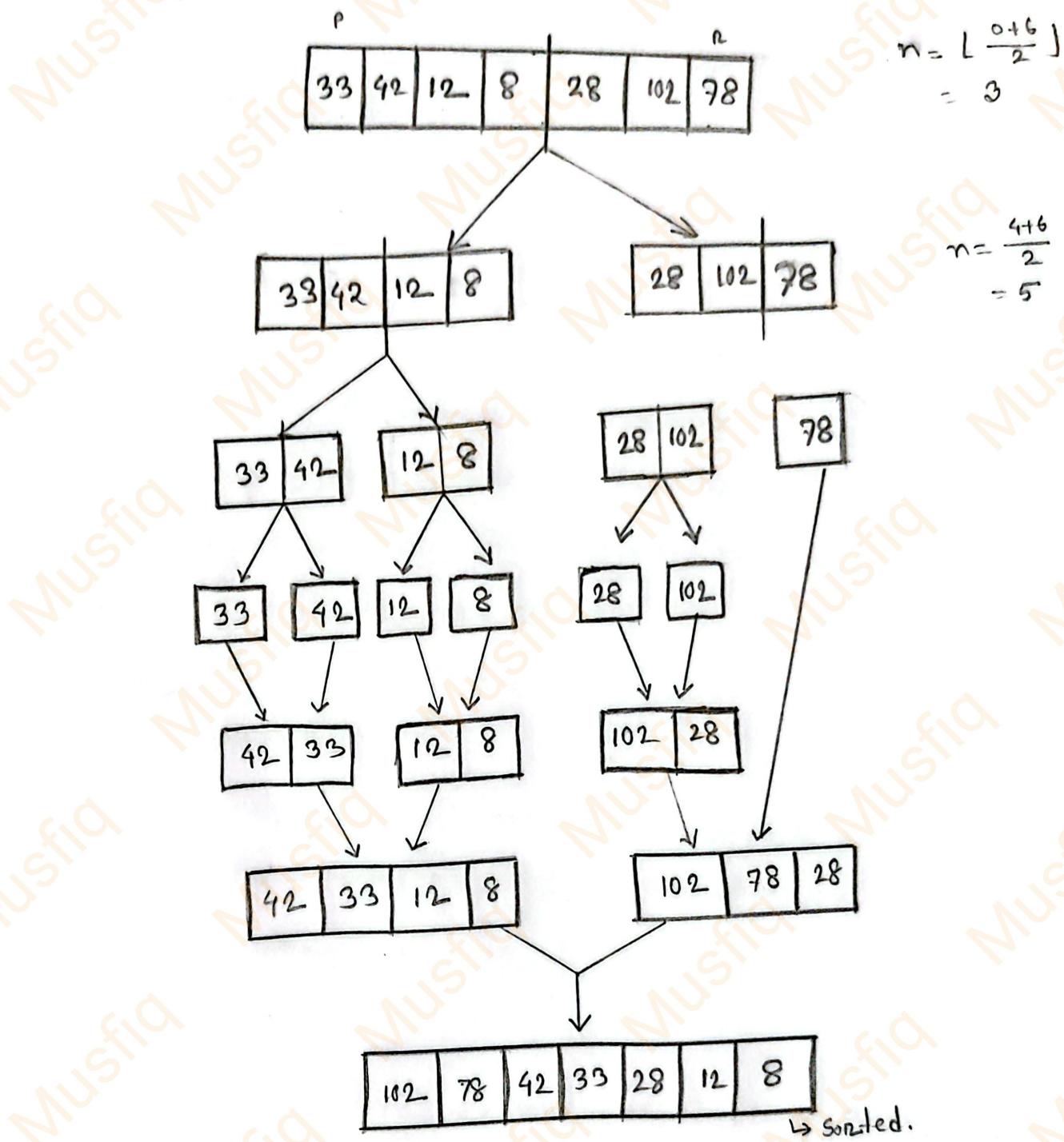


⑤

```
void insertBefore(int elem, int num) {
    struct node * newItem = (struct node*) malloc(sizeof(struct node));
    newItem->value = 25;
    newItem->next = NULL;
    if(head == NULL){
        printf("L.List is empty"); return;
    }
    if(head->value == 30)
    {
        newItem->next = head;
        head = newItem; return;
    }
    struct node * current = head;
    struct node * prev = NULL;
    while(current != NULL && current->value != 30)
    {
        prev = current;
        current = current->next;
    }
    if(current == NULL)
    {
        printf("%d : not exist in List", 30);
        free(NewItem);
        return;
    }
    newItem->next = current;
    prev->next = newItem;
}
```

Ans to the ques no-01

* 33, 42, 12, 8, 28, 102, 78



Descending order merge sort recursive tree.

Ans to the ques no-02

Ticket Reservation Timeout:

Let's consider an online train ticketing system where customer can reserve tickets for their desired train journey. The queue follows a FIFO order.

Queue : A → B → C → D.

For this scenario there is a limited time to complete the transaction.

NOW, let's assume customer C encounters a technical issue during payment process, causing their reservation to time out and expire. For this the system removes customer C from the queue.

The new queue is now,

Queue : A → B → D.

The queue has drifted because customer C is no longer in the queue for time limitation in transaction and D, who came later to C gets served before customer C.

This is the illustrative example of drifting Queue.

Ans the ques no - 03.

code.

$$\text{sum} = 0$$

```
for(i=1; i<=n; i++)
```

```
{ for(j=1; j<=i; j++) {
```

$$\text{sum} = \text{sum} + i + j;$$

}

```
} printf("%d", sum);
```

$$\begin{aligned}
 & 1 + (n+1) + \frac{n(n+1)}{2} + n + \frac{n(n+1)}{2} + 1 \\
 & = n + 1 + \frac{n^2}{2} + \frac{n}{2} + n + \frac{n^2}{2} + \frac{n}{2} + 1 + 1 \\
 & = an^2 + bn + c \\
 & = O(n^2) \text{ Ans.}
 \end{aligned}$$

(4)

④ Last digits \rightarrow 34

Ans to the ques no - 04

$$P = 34 + 5 = 39$$

$$q = P + 3 = 42$$

$$r = P + q = 81$$

$$s = r - 1 = 80$$

$$t = r + s = 161$$

a) head \rightarrow next \rightarrow next \rightarrow value = 81 (r)

b) last \rightarrow prev \rightarrow next \rightarrow value = 161 (t)

c) temp \rightarrow prev \rightarrow prev \rightarrow prev = NULL

d) temp \rightarrow next \rightarrow prev \rightarrow prev \rightarrow value = 42 (q)

e) last \rightarrow prev \rightarrow prev \rightarrow next \rightarrow value = 80 (s)

beg del.

```
struct Node *current;
head = head -> next node;
free(head);
}

Pending:
void deleteAny( int x )
if ( head == NULL )
{ printf( "Sorry " );
}

struct Node *curr;
curr = curr -> prev;

while( curr != NULL && curr->value != x );
{ prev = curr
curr = curr -> nextNode;
}

if( curr == NULL )
{ printf( "Not Found" );
}

if( prev != NULL );
    prev->nextNode = curr -> nextNode;
else
    head = curr -> nextNode;
    free(curr);

}
```

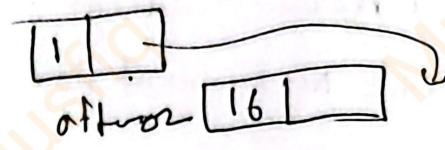
Aftor (Perpendicular)

```
void add_Aftor() {
    if (Head == NULL)
    {
        cout << "Sorry";
        return;
    }

    struct node *NewNode = malloc(sizeof(struct Node));
    NewNode->value = 1;
    NewNode->next = NULL;

    struct Node *traveller;
    traveller = head;

    if (traveller != NULL)
    {
        if (traveller->value == 16)
        {
            NewNode->next = traveller->next;
            traveller->next = NewNode;
            return;
        }
        traveller = traveller->next;
    }
}
```



Stacks

Last in , First out (LIFO) → Item remove in reversed.

First in First out (FIFO)

→ removed in same order.

Push (insert)

Pop (remove/delete) → always delete from top

Top (last element is point)

push(10), push(20), push(40), push(70), pop(), push(100)

10 → top	20 → top	40 → top	70 → top	40 → top	100 → top
10	20	40	70	20	40
10	20	40	70	10	20
10	20	40	70	10	100

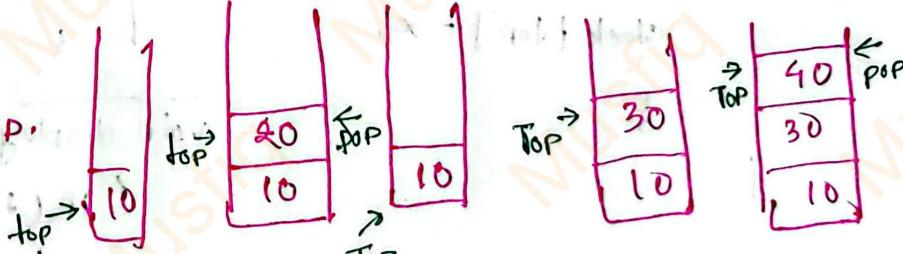
* push(10), push(20), pop(), push(30), push(40), pop(), push()

pop()

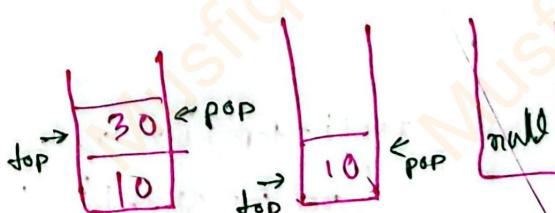
10	20	10	30	40	30	10
10	20	10	30	30	10	10
10	20	10	30	30	10	10
10	20	10	30	30	10	10

Underflow

Insert
Delete → from top.

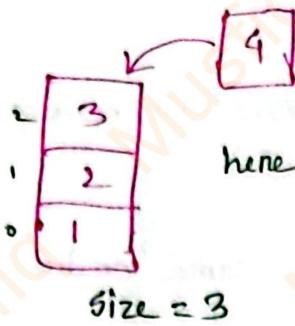


Visual

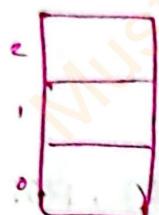
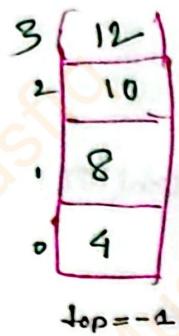


Underflow

Overflow

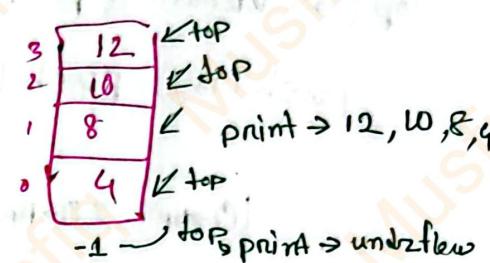


here i want to add 4. that means overflow



called `POP()`, but there is no element here
it's called Underflow..

$\downarrow \text{top} = -1$ \rightarrow global declaration



Push

```
Void Pushl(int x) {
    if (top == maxStack - 1)
    {
        printf("Overflow");
    }
    else
    {
        cin >> x > 4, > 8, > 10, > 12
        top++; >-1+1, 0+1, 1+1, 2+1
        stack [top] = x;
    }
}
```

Pop

```
void Pop() {
    int y;
    if (top <= -1)
    {
        printf("Underflow");
    }
    else
    {
        printf("%d", stack[top]);
        top--; 3-1, 2-1, 1-1, 0-1
    }
}
```

display

```
void display()
{
    if (top <= -1)
        printf("Empty");
    else
        for (i=0, i<=top ; i++)
            cout << stack[i];
    cout << stack[i];
    cout << 9, 8, 10, 12
}
```

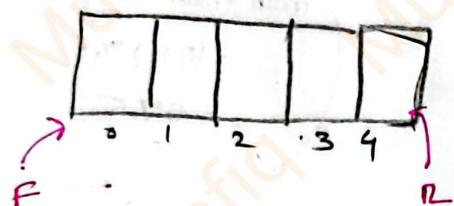
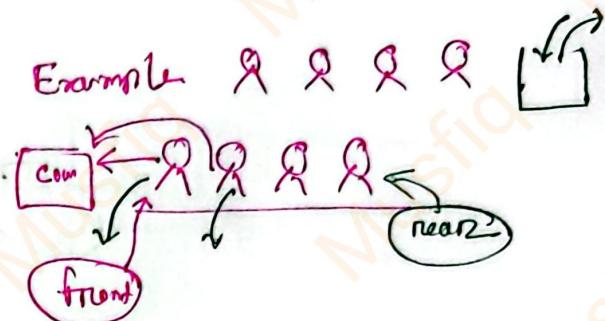
```
for (i=top ; i>=0 ; i--)
{
    cout << stack[i];
}
9, 8, 10, 12
```

Queue

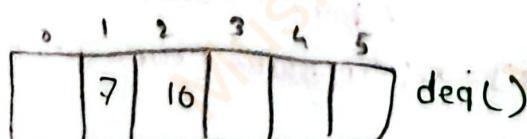
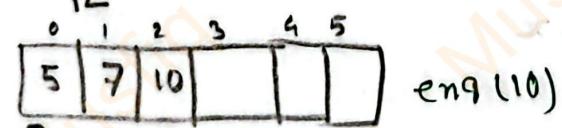
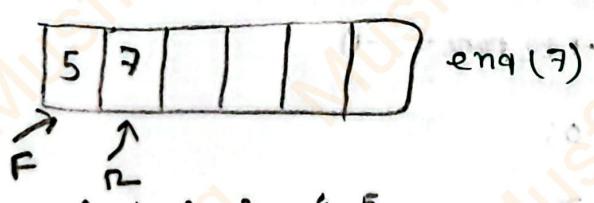
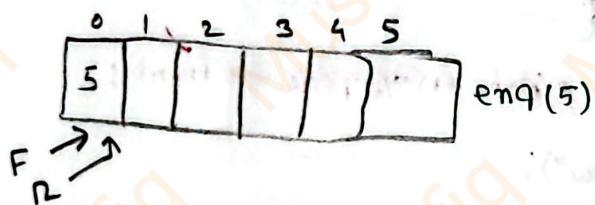
- enqueue (insert)
- dequeue (delete)

special kind of list, where, item one int (inserted) to one end (rear) or delete at the other end (front)

First in, First out (FIFO)



$f = n - 1$ (Queue Empty)



$f = n - 1$



Index to point zero zero zero array to release

enq(5)

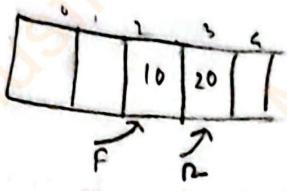
enq(7)

enq(10)

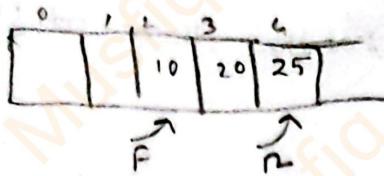
dequeue()

dequeue()

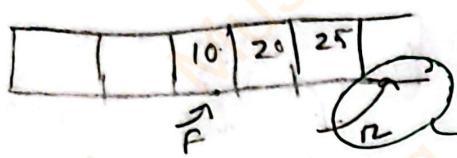
पहला call रखते
तोर Argument
पास पहला भी
तो Always 1st
element delete
पहला पास



enq(20)



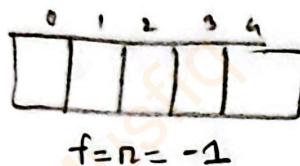
enq(25)



enq(30)

Overflow.

$$n = n - 1 \\ 4 = 4$$



dequeue()

Underflow

case 1: (overflow) \rightarrow enq(20) void enqueue(int x) { $4 = n - 1$ $4 = 4$ overflow. }



if (name == n-1) // (name+1) % q.size == front;

{ printf("Overflow"); }

↓

else if (front == -1 & name == -1)

{ front = name = 0; $q[0] = 5$

queue[name] = x }

↓

else

{ name++; // name = (name+1) % q.size;

queue[name] = x; // queue[name] = x;

}

$$\begin{aligned} \rightarrow q[1] &= 7 \\ \rightarrow q[2] &= 10 \\ \rightarrow q[3] &= 20 \\ \rightarrow q[4] &= 25 \end{aligned}$$

enqueue(5)

enqueue(7)

enqueue(10)

dequeue()

dequeue()

enqueue(10)

enqueue(25)

enqueue(30)

$n = 5$



$f = n = -1$

2x dequeue()

$$\begin{aligned} name &= (name+1) \% q.size \\ &= (4+1) \% 5 \\ &= 5 \% 5 \\ &= 0 \end{aligned}$$

from added size

Dequeue

```
void dequeue() {  
    int y;  
    if (front == -1 && rear == -1)  
        { printf("Empty");  
    }  
    else if (front == rear)  
        { printf("%d", queue[front]);  
        front = rear = -1;  
        }  
    else  
        {  
            front++; // front = (front + 1) % Qsize;  
        }  
}
```

$$\begin{array}{l} q[0] = 5 \\ q[1] = 7 \end{array}$$

```
void display() {  
    int i;  
    if (front == -1 && rear == -1)  
        { printf("Empty");  
    }  
    else {  
        for (i = front; i <= rear; i++)  
            { printf("%d", queue[i]);  
        }  
    }  
}
```