

Question5

Solution :

Because $\langle 1, 1, -1 \rangle$ can determine a 2 degree polynomial and $\langle 1, 0, -1, 2, -1 \rangle$ can determine a 4 degree polynomial so x can determine a 2 degree polynomial.

We can assume $x = \langle a, b, c \rangle$, we can get:

$$\begin{cases} a = 1 \\ a + b = 0 \\ -a + b + c = -1 \\ -b + c = 2 \\ -c = -1 \end{cases}$$

Solving the equation, we can get: $a = 1, b = -1, c = 1$.

So, $x = \langle 1, -1, 1 \rangle$