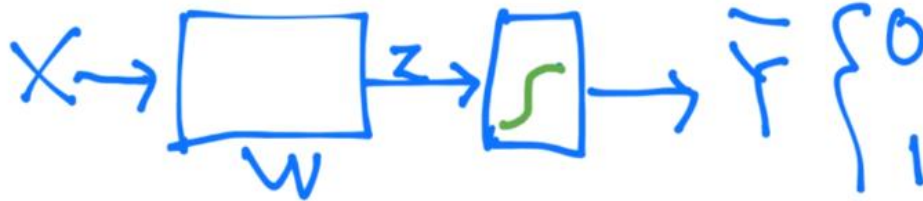


ML lec 06-1

✓ Sigmoid(Logistic Classification)의 요약

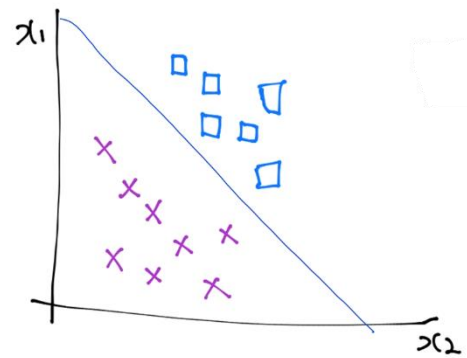


• 보통 y : 실제값, \hat{y} : 예측값으로 많이 씀

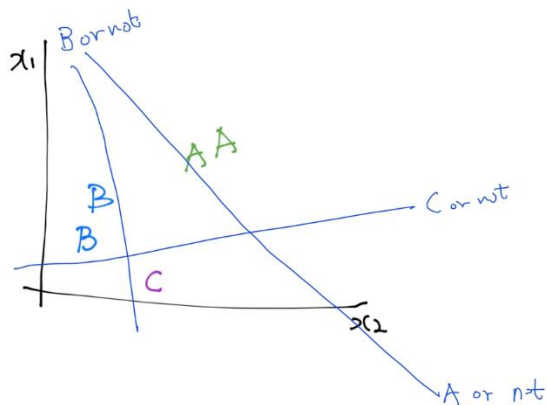
• 위 그림의 직관적 의미는

어떤 두 가지를 구분하는 선을

찾아낸다는 것



✓ Multinomial Classification



Multinomial은 Binary로 표현가능 ·

• Binary를 Matrix로 모으면 아래 그림처럼 간단히 표현가능하다

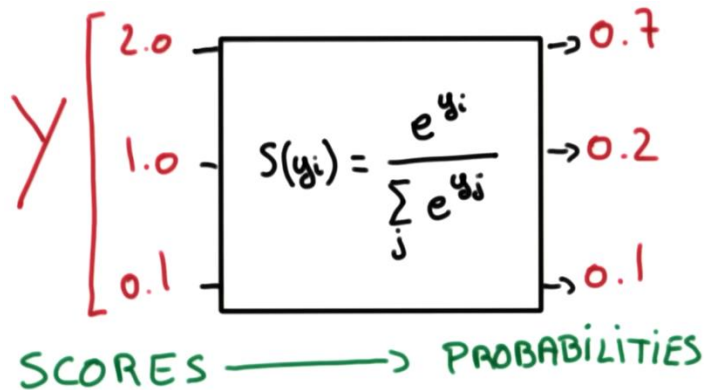
$$\begin{bmatrix} w_{A1} & w_{A2} & w_{A3} \\ w_{B1} & w_{B2} & w_{B3} \\ w_{C1} & w_{C2} & w_{C3} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} w_{A1}x_1 + w_{A2}x_2 + w_{A3}x_3 \\ w_{B1}x_1 + w_{B2}x_2 + w_{B3}x_3 \\ w_{C1}x_1 + w_{C2}x_2 + w_{C3}x_3 \end{bmatrix} = \begin{bmatrix} \bar{y}_A \\ \bar{y}_B \\ \bar{y}_C \end{bmatrix} \begin{bmatrix} 2.0 \\ 1.0 \\ 0.1 \end{bmatrix}$$

ML lec 06-2

✓ 원하던 결과는 0~1의 값이다

- 결과값을 모두 합했을 때 1이 되게 할 순 없을까?

✓ Softmax(hypothesis)으로 가능하다



one-hot encoding으로

우세한 값을 1로 표현가능

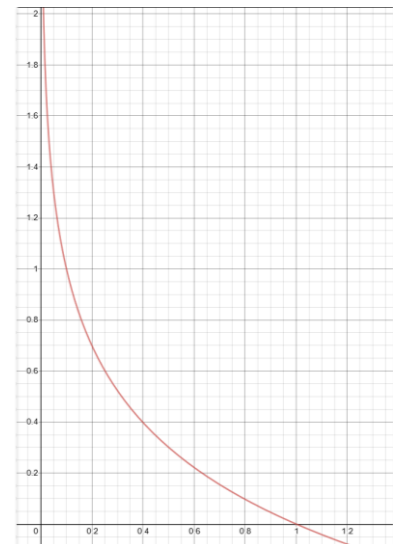
- 이제 필요한 것은 Cost Function

✓ Cross Entropy가 Softmax의 Cost Function에 적합

- Cross Entropy : $D(S, L) = -\sum_i L_i \log S_i$ ($S = \hat{Y}, L = Y$)
- $-\log x$ 그래프의 특성을 이용
- 여러 개의 Training Set도 고려하면

$$\text{Cost Function: } \mathbf{L} = \frac{1}{N} \sum_i D(S(wx_i + b), L_i)$$

(\mathbf{L} = Loss Function, i = Training Set)



ML lab 06-1

✓ Softmax의 구현법

```
1 hypothesis = tf.nn.softmax(tf.matmul(X, W)+b)
2 cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
3
4 optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
```

✓ arg_max를 사용하여 one-hot encoding하기

```
1 a = sess.run(hypothesis, feed_dict={X: [[1, 11, 7, 9] ... ]})
2 print(a, sess.run(tf.argmax(a, 1)))
>>> [[ 1...e-03   9...e-01   9...e-06]] [1]
```

- 끝의 [1]은 one-hot이 적용된 자리를 의미

ML lab 06-2

✓ logits(WX+b) = scores

✓ Cross entropy를 조금 더 간단하게

```
1 logits = tf.matmul(X, W) + b
2 hypothesis = tf.nn.softmax(logits)
3
4 cost_i = tf.nn.softmax_cross_entropy_with_logits(logits=logits,
5                                                    labels=Y_one_hot)
6 cost = tf.reduce_mean(cost_i)
```

✓ 이것을 이용한 Animal Classification

- 총 101R × 17C, 마지막 Q열은 y data
- 그런데 tf.one_hot을 사용하게 되면, **차원이 한 차원 더 높아지게 된다.**

✓ 그래서 필요한 것이 tf.reshape

```

1 Y = tf.placeholder(tf.int32, [None, 1])
2 Y_one_hot = tf.one_hot(Y, nb_classes)
3 Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes])

```

- tf.reshape을 사용하면 차원을 조절할 수 있다
- 다음은 위의 내용을 종합한 Animal Classification의 구현

```

1  xy = np.loadtxt('data-04-zoo.csv', delimiter=',', dtype=np.float32)
2  x_data = xy[:, 0:-1] # 전체 행에서 Q열을 제외
3  y_data = xy[:, [-1]] # 전체 행에서 Q열만 포함
4
5  nb_classes = 7 # 다리는 0~6개라서
6
7  X = tf.placeholder(tf.float32, [None, 16])
8  Y = tf.placeholder(tf.int32, [None, 1])
9  Y_one_hot = tf.one_hot(Y, nb_classes)
10 Y_one_hot = tf.reshape(Y_one_hot, [-1, nb_classes])
11
12 W = tf.Variable(tf.random_normal([16, nb_classes]), name='weight')
13 b = tf.Variable(tf.random_normal([nb_classes]), name='bias')
14
15 logits = tf.matmul(X, W) + b
16 hypothesis = tf.nn.softmax(logits)
17
18 cost_i = tf.nn.softmax_cross_entropy_with_logits(logits=logits,
19                                                    labels=Y_one_hot)
20 cost = tf.reduce_mean(cost_i)
21 optimizer = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
22
23 prediction = tf.argmax(hypothesis, 1)
24 correct_prediction = tf.equal(prediction, tf.argmax(Y_one_hot, 1))
25 accuracy = tf.reduce_mean(tf.cast(correct_prediction, tf.float32))
26
27 with tf.Session() as sess:
28     sess.run(tf.global_variable_initializer())
29
30     for step in range(2000):
31         sess.run(optimizer, feed_dict={X: x_data, Y: y_data})
32         if step % 100 == 0:
33             loss, acc = sess.run([cost, accuracy], feed_dict={
34                 X: x_data, Y: y_data})
35             print("Step: {:>5}|tLoss: {:.3f}|tAcc: {:.2%}".format(
36                 step, loss, acc))
37
38 pred = sess.run(prediction, feed_dict={X: x_data})
39 for p, y in zip(pred, y_data.flatten()): # flatten: [[1], [0]] -> [1, 0]
40     print("[{}] Prediction: {} True Y: {}".
41         format(p == int(y), p, int(y)))

```

✓ 결과 : 제대로 작동한다

```
IPython console
Console 1/A
In [1]: runfile('D:/Documents/ML/동물 분석/Animal Learning.py', wdir='D:/Documents/ML/동물
분석')
WARNING:tensorflow:From D:/Documents/ML/동물 분석/Animal Learning.py:25:
softmax_cross_entropy_with_logits (from tensorflow.python.ops.nn_ops) is deprecated and
will be removed in a future version.
Instructions for updating:

Future major versions of TensorFlow will allow gradients to flow
into the labels input on backprop by default.

See tf.nn.softmax_cross_entropy_with_logits_v2.

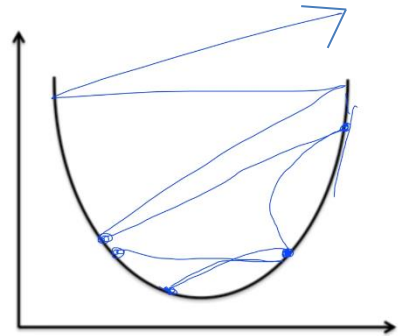
Step:      0      Loss: 3.387      Acc: 18.81%
Step:    100      Loss: 0.576      Acc: 85.15%
Step:    200      Loss: 0.370      Acc: 90.10%
Step:    300      Loss: 0.284      Acc: 94.06%
Step:    400      Loss: 0.233      Acc: 95.05%
Step:    500      Loss: 0.197      Acc: 96.04%
Step:    600      Loss: 0.170      Acc: 97.03%
Step:    700      Loss: 0.148      Acc: 97.03%
Step:    800      Loss: 0.131      Acc: 98.02%
Step:    900      Loss: 0.117      Acc: 100.00%
Step:   1000      Loss: 0.106      Acc: 100.00%
Step:   1100      Loss: 0.096      Acc: 100.00%
Step:   1200      Loss: 0.088      Acc: 100.00%
Step:   1300      Loss: 0.081      Acc: 100.00%
Step:   1400      Loss: 0.076      Acc: 100.00%
Step:   1500      Loss: 0.071      Acc: 100.00%
Step:   1600      Loss: 0.066      Acc: 100.00%
Step:   1700      Loss: 0.063      Acc: 100.00%
Step:   1800      Loss: 0.059      Acc: 100.00%
Step:   1900      Loss: 0.056      Acc: 100.00%
[True] Prediction: 0 True Y: 0
[True] Prediction: 0 True Y: 0
[True] Prediction: 3 True Y: 3
[True] Prediction: 0 True Y: 0
[True] Prediction: 0 True Y: 0
[True] Prediction: 0 True Y: 0
[True] Prediction: 0 True Y: 0
[True] Prediction: 3 True Y: 3
[True] Prediction: 3 True Y: 3
[True] Prediction: 0 True Y: 0
[True] Prediction: 0 True Y: 0
[True] Prediction: 1 True Y: 1
[True] Prediction: 3 True Y: 3
[True] Prediction: 6 True Y: 6
[True] Prediction: 6 True Y: 6
[True] Prediction: 6 True Y: 6
[True] Prediction: 1 True Y: 1
[True] Prediction: 0 True Y: 0
[True] Prediction: 3 True Y: 3

IPython console | History log | Python console
Permissions: RW | End-of-lines: CRLF | Encoding: UTF-8-GUESSED | Line: 1 | Column: 1 | Memory: 81%
```

ML lec 07-1

✓ learning_rate이 크다면?

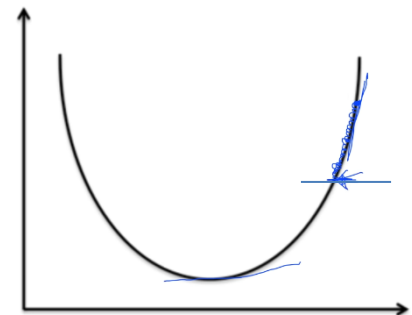
- Overshooting이 일어남



✓ learning_rate이 작다면?

- 오래걸리고, local minimum이 생김

그러므로 조금씩 변경하며 찾아야 함



✓ **Gradient Descent**를 preprocessing(선처리)하는 방법

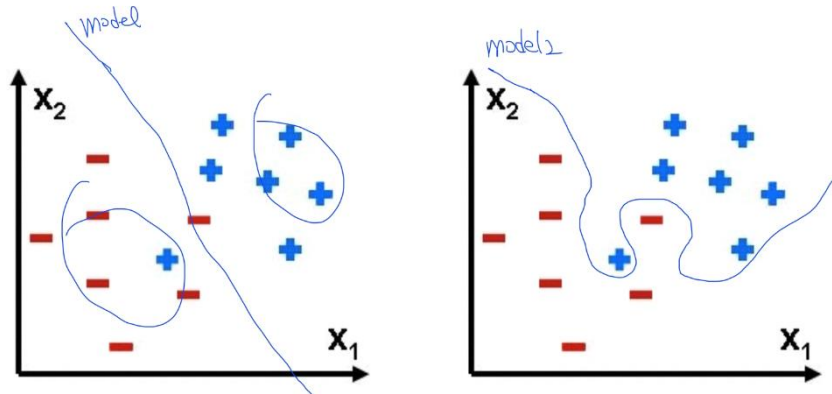
Standardization

$$\mathbf{x}'_j = \frac{\mathbf{x}_j - \mu_j}{\sigma_j}$$

```
x_std[:,0] = (X[:,0] - X[:,0].mean()) / X[:,0].std()
```

✓ Overfitting?

- 어떤 모델에 지나치게 최적화되었을 경우 생김(e.g. model2)



- 해결방법
 - Training Data 늘리기
 - 중복된 features 줄이기
 - **Regularization**

✓ Regularization(일반화)?

- 구부리지 말고, 좀 펴자
- 구부린다는 것은 weight이 큰 값을 가진다는 의미
- Cost Function 뒤에 $\lambda \sum w^2$ 를 추가하면 된다

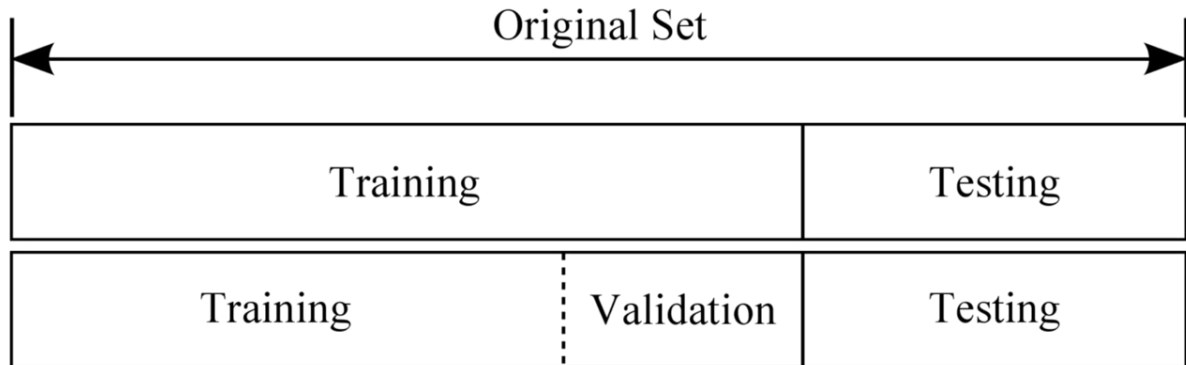
$$L = \frac{1}{N} \sum_i D(S(wx_i + b), L_i) + \lambda \sum w^2$$

✓ 구현하는 법

- `l2reg = 0.001 * tf.reduce_sum(tf.square(W))`
- # λ 로 강도 결정가능. 0: 신경안씀, 1: 엄청중요, 0.001: 적당히

ML lec 07-2

- ✓ 정확한 평가를 위해 시험평가 같은 Test set이 필요



- ✓ 대표적인 예로 **MNIST Dataset**이 있음

ML lab 07-1

- ✓ Training and Test datasets으로 나누기

```
1 x_data = [[1, 2, 1], [1, 3, 2], [1, 3, 4], ..., [1, 7, 7]]
2 y_data = [[0, 0, 1], [0, 0, 1], [0, 0, 1], ..., [1, 0, 0]]
3
4 x_test = [[2, 1, 1], [3, 1, 2], [3, 3, 4]]
5 y_test = [[0, 0, 1], [0, 0, 1], [0, 0, 1]]
```

- ✓ test 결과 확인하는 법

```
1 is_correct = tf.equal(prediction, tf.argmax(Y, 1))
2 accuracy = tf.reduce_mean(tf.cast(is_correct, tf.float32))
3 ...
4 print("Accuracy: ", sess.run(accuracy, feed_dict={X: x_test, Y: y_test}))
```

✓ learning_rate을 크게 할 경우

```
1 ...
2 optimizer = tf.train.GradientDescentOptimizer(learning_rate=10.0)
3                                     .minimize(cost)
4 ...
>>> 0 68.1359 [[ ... ... ...]
      [ ... ... ...]
      [ ... ... ...]]
      1 inf [[ nan nan nan]
             [ nan nan nan]
             [ nan nan nan]]
      ...
      Prediction: [0 0 0]
      Accuracy: 0.0
```

- 임의의 횟수부터 계산을 포기하게 된다

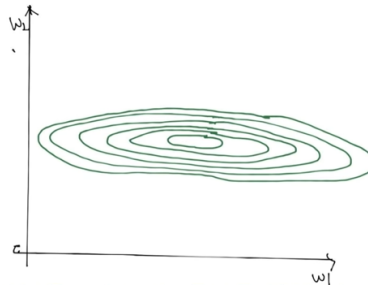
✓ learning_rate을 작게 할 경우

```
1 ...
2 optimizer = tf.train.GradientDescentOptimizer(learning_rate=1e-10)
3                                     .minimize(cost)
4 ...
>>> 0 6.94284 [[ ... ... ...]
      [ ... ... ...]
      [ ... ... ...]]
      1 6.94284 [[ ... ... ...]
                 [ ... ... ...]
                 [ ... ... ...]]
      ...
      200 6.94284 [[ ... ... ...]
                   [ ... ... ...]
                   [ ... ... ...]]
      Prediction: [0 0 0]
      Accuracy: 0.0
```

- 진도가 안나간다

✓ 또는 data값이 불규칙할 경우

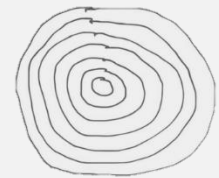
```
xy = np.array([[828.659973, 833.450012, 908100, 828.349976, 831.659973],  
               [823.02002, 828.070007, 1828100, 821.655029, 828.070007],  
               [819.929993, 824.400024, 1438100, 818.97998, 824.159973],  
               [816, 820.958984, 1008100, 815.48999, 819.23999],  
               [819.359985, 823, 1188100, 818.469971, 818.97998],  
               [819, 823, 1198100, 816, 820.450012],  
               [811.700012, 815.25, 1098100, 809.780029, 813.669983],  
               [809.51001, 816.659973, 1398100, 804.539978, 809.559998]])
```



· 이때도 마찬가지로 NaN이 나타나게 된다

✓ 이 경우엔 MinMaxScaler()로 해결 가능

```
1 xy = np.array([[828.659973, 908100, ...],  
2               ...  
3               [809.51001, ...]])  
4  
5 xy = MinMaxScaler(xy)
```



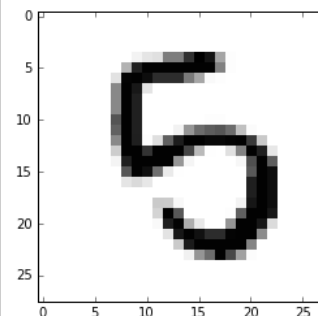
ML lab 07-2

✓ Meet MNIST Dataset

```
Editor - U:\Documents\ML\MNIST\Number Recognition.py
Number Recognition.py x

1 # ML Lab 07-2
2 import tensorflow as tf
3 import matplotlib.pyplot as plt
4 import random
5
6 tf.set_random_seed(777) # for reproducibility
7
8 from tensorflow.examples.tutorials.mnist import input_data
9
10 # Check out https://www.tensorflow.org/get_started/mnist/beginners for
11 # more information about the mnist dataset
12 mnist = input_data.read_data_sets("MNIST_data/", one_hot=True)
13
14 nb_classes = 10
15
16 # MNIST data image of shape 28 * 28 = 784
17 X = tf.placeholder(tf.float32, [None, 784])
18 # 0 - 9 digits recognition = 10 classes
19 Y = tf.placeholder(tf.float32, [None, nb_classes])
20
21 W = tf.Variable(tf.random_normal([784, nb_classes]))
22 b = tf.Variable(tf.random_normal([nb_classes]))
23
24 # Hypothesis (using softmax)
25 hypothesis = tf.nn.softmax(tf.matmul(X, W) + b)
26
27 cost = tf.reduce_mean(-tf.reduce_sum(Y * tf.log(hypothesis), axis=1))
28 train = tf.train.GradientDescentOptimizer(learning_rate=0.1).minimize(cost)
29
30 # Test model
31 is_correct = tf.equal(tf.argmax(hypothesis, 1), tf.argmax(Y, 1))
32 # Calculate accuracy
33 accuracy = tf.reduce_mean(tf.cast(is_correct, tf.float32))
34
35 # parameters
36 num_epochs = 15
37 batch_size = 100
38 num_iterations = int(mnist.train.num_examples / batch_size)
39
40 with tf.Session() as sess:
41     # Initialize TensorFlow variables
42     sess.run(tf.global_variables_initializer())
43     # Training cycle
44     for epoch in range(num_epochs):
45         avg_cost = 0
46
47         for i in range(num_iterations):
48             batch_xs, batch_ys = mnist.train.next_batch(batch_size)
49             _, cost_val = sess.run([train, cost], feed_dict={X: batch_xs, Y: batch_ys})
50             avg_cost += cost_val / num_iterations
51
52         print("Epoch: {:04d}, Cost: {:.9f}".format(epoch + 1, avg_cost))
53
54     print("Learning finished")
55
56     # Test the model using test sets
57     print(
58         "Accuracy: ",
59         accuracy.eval(
60             session=sess, feed_dict={X: mnist.test.images, Y: mnist.test.labels}
61         ),
62     )
63
64     # Get one and predict
65     r = random.randint(0, mnist.test.num_examples - 1)
66     print("Label: ", sess.run(tf.argmax(mnist.test.labels[r : r + 1], 1)))
67     print(
68         "Prediction: ",
69         sess.run(tf.argmax(hypothesis, 1), feed_dict={X: mnist.test.images[r : r + 1]}),
70     )
71
72     plt.imshow(
73         mnist.test.images[r : r + 1].reshape(28, 28),
74         cmap="Greys",
75         interpolation="nearest",
76     )
77     plt.show()
```

```
In [1]: runfile('D:/Documents/ML/MNIST/Number Recognition.py',
wdir='D:/Documents/ML/MNIST')
Extracting MNIST_data/train-images-idx3-ubyte.gz
Extracting MNIST_data/train-labels-idx1-ubyte.gz
Extracting MNIST_data/t10k-images-idx3-ubyte.gz
Extracting MNIST_data/t10k-labels-idx1-ubyte.gz
Epoch: 0001, Cost: 2.826302660
Epoch: 0002, Cost: 1.061668948
Epoch: 0003, Cost: 0.838061307
Epoch: 0004, Cost: 0.733232732
Epoch: 0005, Cost: 0.669279880
Epoch: 0006, Cost: 0.624611828
Epoch: 0007, Cost: 0.591160339
Epoch: 0008, Cost: 0.563868978
Epoch: 0009, Cost: 0.541745167
Epoch: 0010, Cost: 0.522673571
Epoch: 0011, Cost: 0.506782322
Epoch: 0012, Cost: 0.492447640
Epoch: 0013, Cost: 0.479955830
Epoch: 0014, Cost: 0.468893666
Epoch: 0015, Cost: 0.458703479
Learning finished
Accuracy: 0.8951
Label: [5]
Prediction: [6]
```

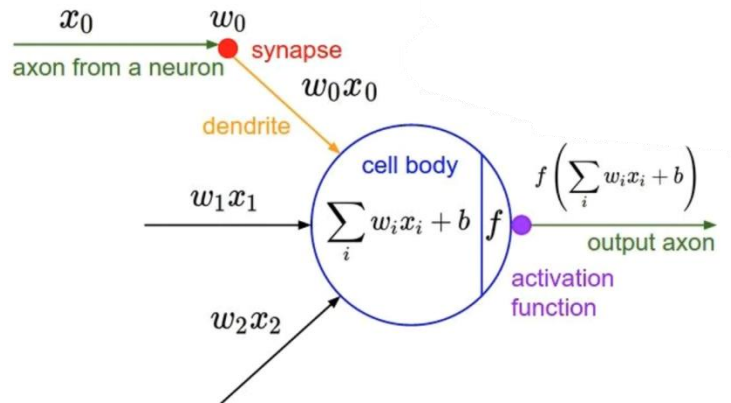


- 아직은 분발이 필요해보인다

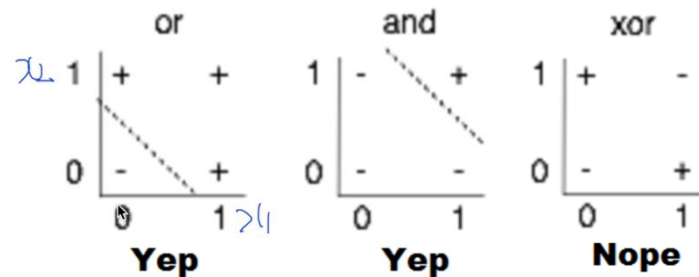
ML lec 08-1, 2

✓ 시초 : thinking machine을 향한 갈망

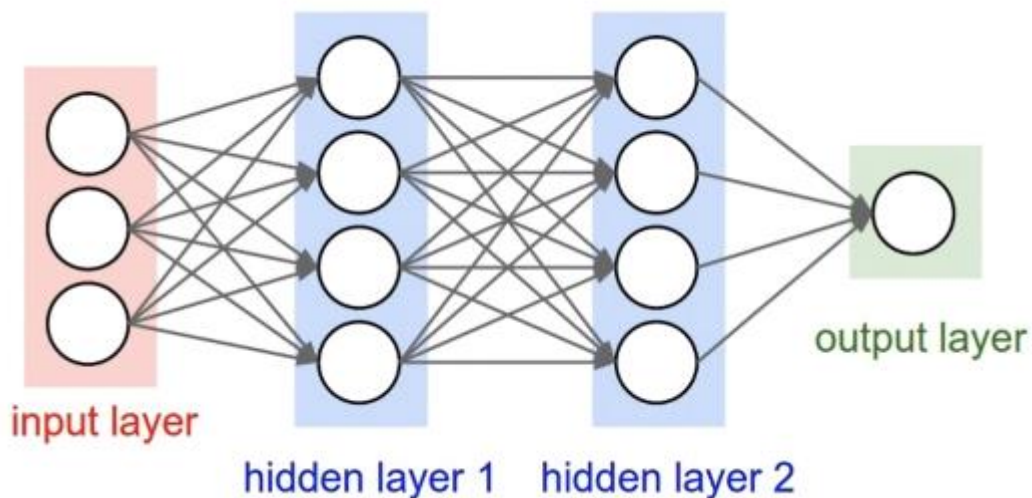
- 뇌의 Neuron을 연구하여 기반을 잡음



✓ 하지만 or, and와는 달리 xor은 구현이 안됨



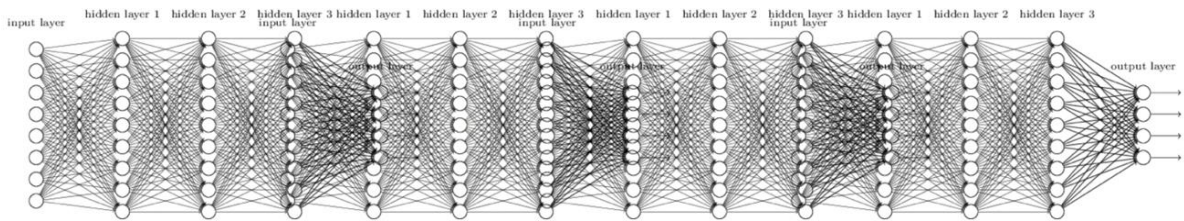
- 불가능하다는 현실직시



✓ **Backpropagation**의 탄생

✓ **Neural Networks**의 탄생

- 하지만 너무 복잡해서 다시 침체기에 들어감



✓ 연구가 진행되며 Deep Learning이란 개념으로 탈바꿈

✓ 활발하게 연구가 이루어져 오차율을 급격하게 낮추게 됨

✓ Facebook, Google, Netflix 등 이미 많이 사용되고 있음

✓ 왜 배워야 하는가?

- 범용성이 넓고, 정확하며 정보가 많아 배우기 간편하기 때문

ML lab 08

✓ 기초 이론 수업

- `a.ndim` : `a`의 rank를 반환
- `rank` : 바깥 대괄호의 개수로 판별 가능
- `shpe` :
 - `(a, b, ..., n)`일 때 `n`은 가장 안쪽 대괄호에 있는 수의 개수
 - `n-1`은 그 다음 대괄호쌍의 개수
 - 반복
- `axis` : 가장 바깥 ~ 가장 안쪽 : $0 \sim n$
- Matmul VS Multiply
 - 일반적인 차원끼리의 곱셈은 `matmul`
 - `Multiply`를 할 경우 Broadcasting이 일어남
 - Broadcasting을 이용하여 rank가 달라도 곱셈 가능
- `reduce_mean(float, axis)`
- `argmax(a, axis)`
- `reshape(a, shape=[-1, n])`
 - `squeeze([[0], [1], [2]]) -> [0, 1, 2]`
 - `expand_dims([0, 1], 1) -> [[0],`

`[1]]` # 차원 추가

- `one_hot(..., depth)` 이후에 `reshape`해야함
- `cast(..., format)`
- `stack([a, b, c], axis)` : 쌓기 -> `[[a],`
`[b],`
`[c]]`

- ones and zeros like

- `ones_like(a)` : 모두 1로 바꿈
- `zeros_like(a)` : 모두 0으로 바꿈

- `for x, y in zip([1, 2, 3], [4, 5, 6]) :`
`print(x, y)`

for 루프를 통해 복수 개의 텐서를 한 방에 출력

-> 1 4

2 5

3 6