

# Mesh Representation 1

<http://www.mushware.com/>

File generated 2005-04-26 11:15

**DRAFT: This document has not been reviewed and may contain errors.**

## Introduction

This document describes the representation of a four dimensional object using a mesh of connected vertices.

## Problem

The 4D form of objects is to be represented through linked groups of vectors, known here as the mesh. The organisation should support the required operations to be performed, which are:

- Subdivision. Subdivision generates a new mesh at higher resolution than the original. Must support variable level of detail.
- Rendering. Purpose is to generate the triangle list for the renderer. Minimal alteration is useful – a method to calculate new positions without regenerating the list. Calculation should be pushed into the graphics driver where possible.
- Animation. Hierarchical objects connected by rotating joints, or some other method.
- Collision checking. Division into reasonable-sized chunks for collision checking, each with a bounding region.
- Order-dependent transparency. Rough facet order should be obtainable.
- Support chunk-wise occlusion test for rendering speed.
- Support ‘directional’ information, for determination of whether sides of a face are inside or outside of an object.

## Analysis

We should find the simplest representation of the mesh. From this, other representations, such as the facet list for the renderer, can be generated.

Element	Description
Vertices	The position of a point on the mesh as a 4-vector
Faces	A hyperface, with extent in three dimensions whilst being flat in the other <sup>1</sup> .
Facet	A 2D facet of the 3D face. Analogous to an edge in 3D; drawing only facets is similar to drawing 3D in wireframe, i.e. not realistic.
Edge	A line bounding a facet.
Normal	Relevant to a face only. In 4D three independent vectors are required to generate the normal vector. A pair of vectors have a plane which is orthogonal to them. The normal may be implied by predefined vertex ordering.
Texture coordinates	Dependent on the rendering technique. If facets are rendered as polygons, each facet needs at least two texture coordinates at each point. If faces are rendered directly, at least three texture

---

<sup>1</sup> There's no strict requirement that a face be flat, in the same way that a square face in 3D need not have all of its vertices in the same plane. However non-flat faces may complicate the renderer.

	coordinates are required.
<b>Material properties</b>	Material properties stored on a per-face or per-object basis. Smaller scale details must be stored within the textures. Material properties specify which textures should be used and how.
<b>Inside/outside</b>	Records which direction along the normal vector is inside and which outside of the object. This information can be implied by vertex ordering.
<b>Edge smoothness</b>	To what degree an interface between two faces should be smoothed when subdividing.

**Table 1: Basic mesh elements**

<b>Derived element</b>	<b>Description</b>
<b>Subdivided mesh</b>	A mesh generated by subdividing the original mesh.
<b>Render list</b>	The list of coordinates and state changes to be passed to the renderer.
<b>Collision hull</b>	A simplified mesh used for computing whether objects intersect.
<b>Occlusion render list</b>	A simplified mesh used to test whether an object is visible using OpenGL's occlusion test method.
<b>Chunking</b>	Grouping of faces into a hierarchy of adjacent sets, to aid collision and occlusion tests.
<b>Ordering</b>	Order information for depth sorting.
<b>Bounding regions</b>	Each chunk has a bounding region to be used for culling.

**Table 2: Elements derived from the mesh**

## Subdivision

Subdivision generates new vertices with new connectivity. It presents the following difficulties:

- Subdivision generates an entirely new set of vertices and normals.
- Level of detail (LOD) algorithms require that one part of the mesh may be more finely subdivided than an adjacent part. If large objects are present, i.e. with sections both near to and far from the observer, chunks with differing levels of subdivision may need to be patched together.
- Vertices beyond the current face are required to subdivide smoothly.
- The polygon and vertex count grows geometrically; four fold for each cycle of subdivision.

## Collision tests

Collision tests have different requirements to rendering.

- In a multiplayer game only the server need perform collision checking.
- Collision tests do not require access to the renderer.
- The results of some tests may be required before rendering, so that objects are not drawn falling through the floor, etc. This leads to two type of test. Results of projectile-hits-object type tests may not be required before rendering.
- The collision volume may not be the same as the visual volume. It may be simplified, or made larger to make the game easier.

## ***Proposed solution***

Firstly the pipeline must be established.

<b>Stage</b>	<b>Description</b>
<b>Gather data</b>	A complete set of objects and views is assembled. The following stages take place for each view. Some views may need to be rendered before others, e.g. for environment and shadow mapping.
<b>Pre-collision transform</b>	The renderer can reuse these transforms, and also the sort lists generated for collision checking.
<b>Pre-cull transform</b>	Perform the necessary transforms required for the geometric cull; usually a transform to eye coordinates in 3D.
<b>Geometric cull</b>	Remove objects and chunks from the scene where it is efficient to do so, using geometric tests on bounding boxes and distance.
<b>Occlusion render and cull</b>	Draw large, near objects and perform occlusion tests on distant ones. May not always be necessary. If used to cull texture jobs, no further tests will be required once a particular texture is known to be needed.
<b>Renderer select</b>	The presence of the following actions depends on what type of output detail is required, e.g. environment map, render to texture, final render, etc.
<b>Level of detail</b>	Each chunk is tagged with the level of detail required.
<b>Reuse</b>	Previous jobs where output is close enough are passed for rendering directly.
<b>Chunking</b>	Work chunks are generated for the worker thread(s). Each thread must have a complete set of data to work with, and ideally results should not be calculated more than once. Render jobs should not be processed in the wrong order, and texture jobs should be despatched first.
<b>Subdivision</b>	The mesh is subdivided as necessary for the level of detail required. It is important to reuse previous work where possible.
<b>Subdivision culling</b>	Some primitives may be discarded during subdivision.
<b>Render job generation</b>	Generate a job definition for the renderer and despatch the job.
<b>Completion</b>	When all chunks are complete, signal the renderer.

**Table 3: Rendering pipeline**

<b>Stage</b>	<b>Description</b>
<b>Pre-collision transform</b>	Perform the necessary transforms required for collision checking; usually a transform to world space in 4D. Sort lists, if the renderer uses them, are generated now, before collision checking proceeds on its own.
<b>Sort</b>	Update sort lists as required.
<b>Candidate sweep and cull</b>	Choose object pairs using the sort list and their extents. Where pairs have known results, use them.
<b>Bounding box cull</b>	If bounding boxes exclude objects, cull the pair.
<b>Mesh cull</b>	Test for intersection using a detailed mesh test.
<b>Report collisions</b>	Return a collision list for further processing.

**Table 4: Collision pipeline**

To support this pipeline we introduce a new type of mesh data; cached results that persist from frame to frame to make overall calculation more efficient. These are:

Persistent element	Description
<b>Collision test results</b>	Results of collision tests between two objects. If a distance between the two can be calculated, this will be still valid if the objects have not moved further than that.
<b>Sort orders</b>	Object orders maintained for collision tests.
<b>World coordinates</b>	Useful for static objects.
<b>Geometrically culled objects</b>	Objects which are still excluded from the view because, e.g. their angular displacement was too great for them to be visible this time.
<b>Renderer jobs</b>	Entire sets of rendering information for non-animated objects.
<b>Subdivided meshes</b>	Complete meshes which can be completely or partially (e.g. just texture coordinates) reused.

**Table 5: Persistent data**

### Minimal mesh representation

The minimal representation contains just the information needed to define the mesh and no other.

Element	Description
<b>Vertices</b>	A single entry for each vertex.
<b>Material reference</b>	Reference to the global material for the mesh.
<b>Texture coordinates</b>	Any number of entries, as required for the faces.
<b>For each face:</b>	
<b>Face type</b>	At least cubic. Prism and tetrahedron also useful.
<b>Vertex list</b>	The three pairs 0→1, 0→2, 0→4 are used in that order to calculate the face normal. These are index values referring to the vertex entries.
<b>Texture coordinate list</b>	A texture coordinate index value for each vertex in the vertex list for this face.
<b>Material reference</b>	Reference to an overriding material for this face, if any.
<b>Edge smoothness</b>	The smoothness of each edge. In this case an edge is the polygon (a quadrilateral in our case) where two faces meet.

**Table 6: Data required for the minimal representation**

### Additional representation

The additional representation contains hints and precalculation that cannot easily be derived:

Element	Description
<b>Chunking</b>	A chunk hierarchy, dividing the object into groups of faces.
<b>Convex hull</b>	A convex hull for each chunk.

**Table 7: Data supplied in the additional representation**

### Derived representation

The derived representation contains:

Element	Description
<b>Normals</b>	Normal vectors for each face.
<b>Connectivity</b>	A list for each vertex, recording all of its neighbours.
<b>Chunk connectivity</b>	A list for each chunk, recording all of its face-wise neighbours.
<b>Bounding regions</b>	The object and each of its chunks and faces have a bounding region.

Table 8: Data generated in the derived representation

### ***Example: Multi-tentacled beast***

#### **Description**

A particular creature has eight tentacles, two opposed on each axis meeting at a central blob. One is adapted as an eyestalk and the opposite one is stubby and has a sucker. The tentacles can bend in three axes and twist in another three. To animate, each tentacle is algorithmically drawn towards an attractor point.

The creature has a simple control mesh. To simplify, three tentacles are shown in 3D only.

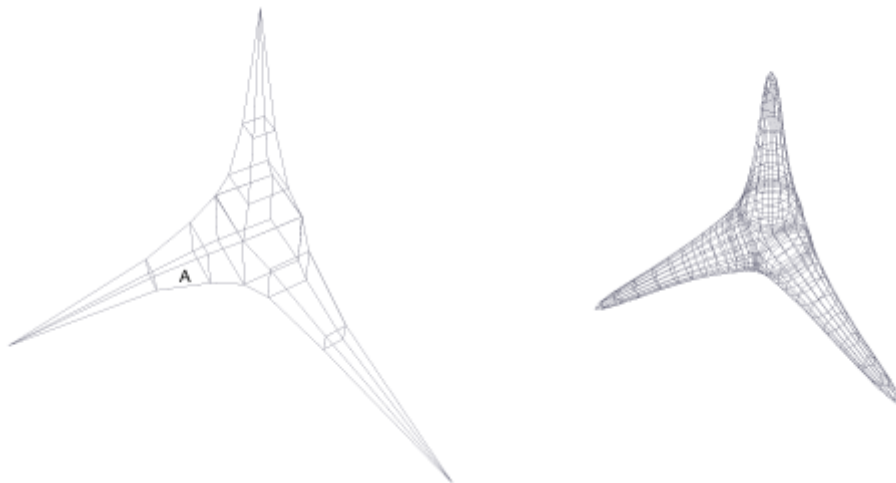


Figure 1: Control and subdivided meshes

In 4D, a cube replaces each square face. The section marked A has four faces, as two are missing where the section joins neighbouring sections. In 4D, this section would be a tesseract with two of its faces missing, leaving six. The shrinkage is a characteristic of the type of subdivision used.

When all tentacles are present the central cube will have no renderable sides, so is not truly a face of the object. If a tentacle is then removed, another face must be introduced to fill the hole.

#### **Generation**

This creature can be generated algorithmically. In 3D, the tentacle is defined by its square cross section at four places, which vanishes to a point at the tip. In 4D the cross section will be a cube, similar to a single face of a tesseract. When moving from cross section to cross section, in 3D there are two angular (bending) degrees of freedom, because there are two axes perpendicular to the direction of the tentacle. The tentacle pointing out of the screen can bend up/down and left/right. It can also

rotate about its axis. The changes in orientation between neighbouring cross sections must be slight to avoid distortion, but more cross sections can be introduced as required. The tentacle can also change length to some extent, ideally becoming fatter as it shortens.

In 4D, the cross section is a cubic face. There are three angular degrees of freedom, because there are three axes perpendicular to the direction of the tentacle. There are three rotational degrees of freedom. If the tentacle is heading in the  $x$  direction, rotation can take place in the  $yz$ ,  $zw$  and  $yw$  planes.

Initial generation would proceed as follows:

Stage	Description
<b>Position</b>	The position of the tentacles must be known. This implies that the position and orientation of each cross section can be calculated.
<b>Initial cross section</b>	The section where the tentacle joins the body is calculated. This could be fixed, or calculated from a mean of adjacent tentacles.
<b>Next cross section</b>	Generate the next cross section along the tentacle, using the position parameters. This could be done by interpolation, or using known bend/rotate values for each segment.
<b>Vertices</b>	Write the new vertices to the definition.
<b>Create the first chunk</b>	In this example each segment of the tentacle's control mesh will be a single chunk.
<b>Generate faces</b>	Add face definitions for the six faces, using the vertices already added. Add texture coordinates as necessary. Mark the edges as smooth.
<b>Repeat</b>	Generate further tentacle chunks as required, for all tentacles. Generate a chunk of each new segment. The end is capped 6 or 7-sided chunk.
<b>Vertex connectivity</b>	Generate the vertex connectivity information for the whole object.
<b>Normal generation</b>	Using the connectivity information, average the normals for each vertex. This is the average value of the normals of each face of which the vertex is a part. Normals of opposite sign can be detected here. Obey edge smoothness values to weight each vertex. For smooth objects, normals can be shared between adjacent faces.
<b>Chunk connectivity</b>	Record the chunk connectivity in the object. This object isn't suitable for a convex hull, but each chunk of the control mesh is suitable for collision tests.
<b>Bounding regions</b>	Calculate centres and bounding radii for each chunk, and for the object as a whole.

**Table 9: Stages of initial creature mesh generation**

Subsequent updates to the mesh would require:

Stage	Description
<b>Position</b>	The position of the tentacles must be known. This implies that the position and orientation of each cross section can be calculated.
<b>Initial cross section</b>	The section where the tentacle joins the body is calculated. This could be fixed, or calculated from a mean of adjacent tentacles.
<b>Next cross section</b>	Generate the next cross section along the tentacle, using the position parameters. This could be done by interpolation, or using known

	bend/rotate values for each segment.
<b>Vertices</b>	Update the vertex definitions.
<b>Normal calculation</b>	Update the normal definitions. This uses the vertex connectivity information previously calculated.
<b>Bounding regions</b>	Recalculate centres and bounding radii for each chunk, and for the object as a whole. This may not be necessary for every movement, but should be an optimised step. Possibly, a recalculation should only be triggered when the bounding volume is required.

**Table 10: Stages of subsequent creature mesh generation**

## **Movement**

Moving this creature is not trivial. A number of collision checks are required to make sure that a tentacle does not pass through another object, or another part of this object. A simple scheme could be devised:

- When not in contact, the tentacle moved randomly using a consistent-ish bend along its length and minimal rotation.
- When a tentacle touches an object, it recognises it as friendly or nasty.
- For a friendly object, the tentacle moves so as to stay in contact with the objects.
- For nasty objects, the tentacle retracts and reverses its direction of motion.

In this scheme the body of the creature does not move. A walking, slithering, swimming or clambering scheme is also required.

- Zero or one tentacle is the anchor tentacle.
- If zero, the creature swims or walks towards a nearby target, or in large circles.
- If one, the creature waves its tentacles. If a tentacle grabs an object that it hasn't just released, that tentacle becomes the new anchor.
- The anchor tentacle should attempt to coil around what it has just touched.

## **Version History**

1. 2005-04-25: Created with filename mesh-representation1-2005-04-25
2. 2005-04-26: Draft released

Author: Andy Southgate. First published in the UK in 2005.

The author and his employer (Mushware Limited) irrevocably waive all of their copyright rights vested in this particular version of this document to the furthest extent permitted. The author and Mushware Limited also irrevocably waive any and all of their intellectual property rights arising from said document and its creation that would otherwise restrict the rights of any party to use, and/or distribute the use of, the techniques and methods described herein. A written waiver can be obtained via <http://www.mushware.com/>. If required please cite as Document Title, Author's Name, Mushware, Full Date, e.g. Mesh Representation 1, Andy Southgate, Mushware, 2005-04-26.