

When you speak, your voice is picked up by an analog sensor in the cell phone's microphone.

An analog-to-digital converter chip converts your voice, which is an analog signal, into digital signals, represented by 1s and 0s.

The DSP compresses the digital signals and removes any background noise.

In the listener's cell phone, a digital-to-analog converter chip changes the digital signals back to an analog voice signal.

Your voice exits the phone through the speaker.

# EHM 310

## SAYISAL İŞARET İŞLEME

### MATLAB UYGULAMALAR (1)

$$x(n) = \{2, 1, -1, 0, 1, 4, 3, 7\}$$

↑

```
>> n=[-3,-2,-1,0,1,2,3,4];  x=[2,1,-1,0,1,4,3,7];
```

$\delta[n]$

```
n=-10:10;
```

```
x=n.*0;
```

```
    for i=1:length(n)
```

```
        if(n(i))==x(i)=1;
```

```
    end
```

```
end
```

```
stem(x, x 'filled')
```

$$x[n]=0.9^n$$

```
n=-10:10;
```

```
x=0.9.^n;
```

```
stem(n, x, 'filled')
```

$$x[n]=0.9\sin(2\pi n/10)$$

```
n=-20:20;
```

```
x1=0.9.^n;
```

```
x=x1.*sin(2*pi*n/10);
```

```
stem(n,x, 'filled')
```

$$x_1(n) = e^{j(\pi/6)n}$$

```
n=[0:20*pi];x1=exp(j*pi/6.*n);% zaman vektörü n ve x1 oluşturu  
subplot(2,1,1); stem(n,real(x1));  
title('x1 işaretinin gerçel bölümü');xlabel('n')  
subplot(2,1,2); stem(n,imag(x1));  
title('x1 işaretinin sanal bölümü');xlabel('n')
```

# Konvolüsyon

```
n=-10:10;  
x=[0 0 0 0 1 2 0 -1 0 0 0];  
h=[0 0 0 0 3 2 1 0 0 0],  
y=conv(x,h);  
stem(n,y, 'filled')
```

$$x(n) = e^{(-0.1+j0.3)n}, \quad -10 \leq n \leq 10$$

```
>> n = [-10:1:10]; alpha = -0.1+0.3j;  
>> x = exp(alpha*n);  
>> subplot(2,2,1); stem(n,real(x));title('real part');xlabel('n')  
>> subplot(2,2,2); stem(n,imag(x));title('imaginary part');xlabel('n')  
>> subplot(2,2,3); stem(n,abs(x));title('magnitude part');xlabel('n')  
>> subplot(2,2,4); stem(n,(180/pi)*angle(x));title('phase part');xlabel('n')
```

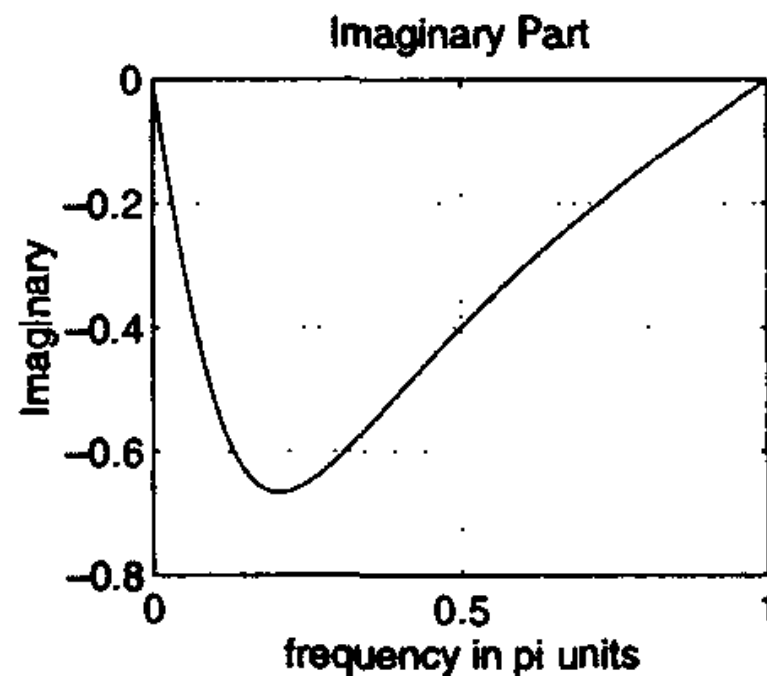
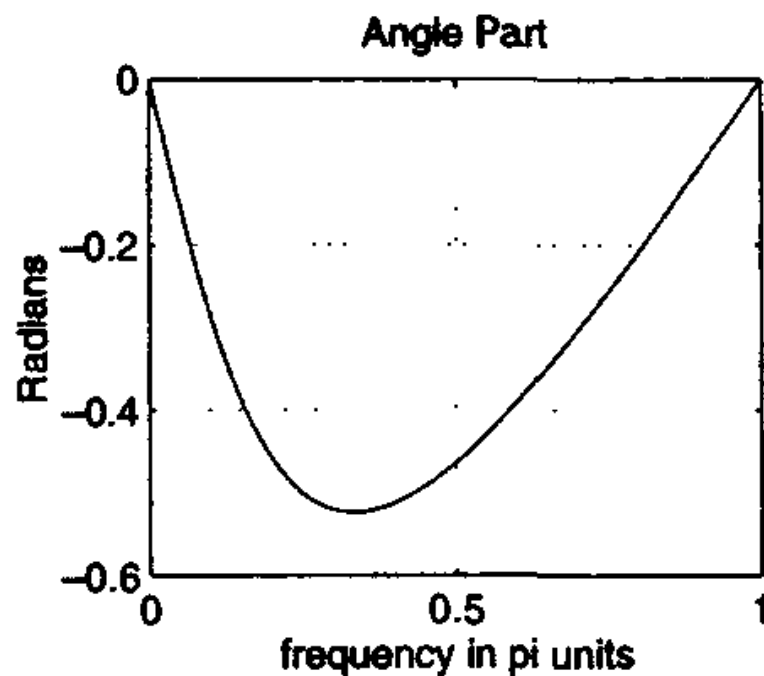
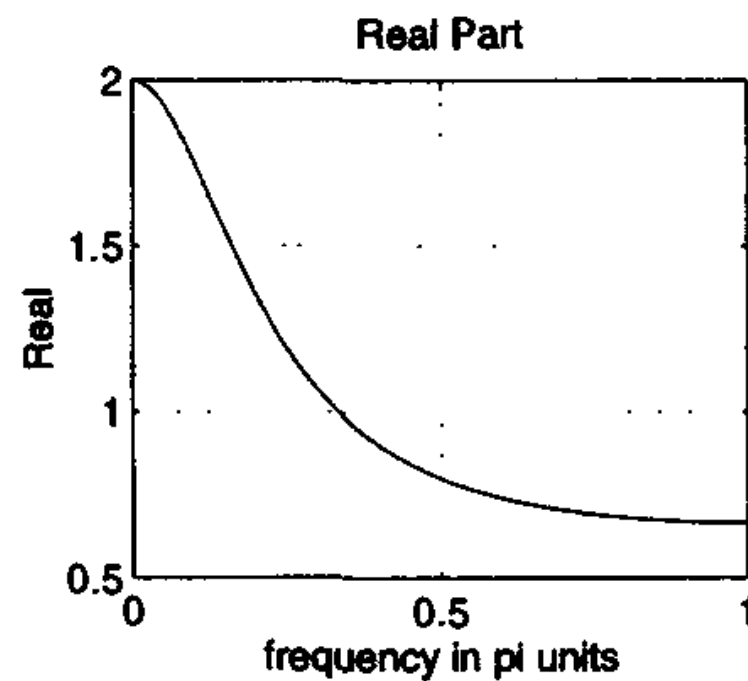
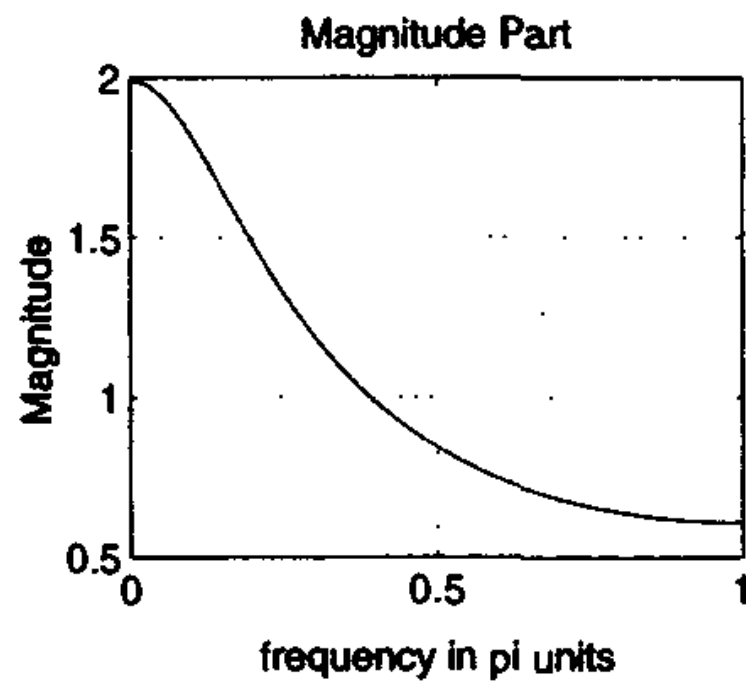


## Fourier Dönüşümü

$$x(n) = (0.5)^n u(n).$$

$$\begin{aligned} X(e^{j\omega}) &= \sum_{-\infty}^{\infty} x(n) e^{-j\omega n} = \sum_0^{\infty} (0.5)^n e^{-j\omega n} \\ &= \sum_0^{\infty} (0.5 e^{-j\omega})^n = \frac{1}{1 - 0.5 e^{-j\omega}} = \frac{e^{j\omega}}{e^{j\omega} - 0.5} \end{aligned}$$

```
>> w = [0:1:500]*pi/500; % [0, pi] axis divided into 501 points.
>> X = exp(j*w) ./ (exp(j*w) - 0.5*ones(1,501));
>> magX = abs(X); angX = angle(X);
>> realX = real(X); imagX = imag(X);
>> subplot(2,2,1); plot(w/pi,magX); grid
>> xlabel('frequency in pi units'); title('Magnitude Part'); ylabel('Magnitude')
>> subplot(2,2,3); plot(w/pi,angX); grid
>> xlabel('frequency in pi units'); title('Angle Part'); ylabel('Radians')
>> subplot(2,2,2); plot(w/pi,realX); grid
>> xlabel('frequency in pi units'); title('Real Part'); ylabel('Real')
>> subplot(2,2,4); plot(w/pi,imagX); grid
>> xlabel('frequency in pi units'); title('Imaginary Part'); ylabel('Imaginary')
```

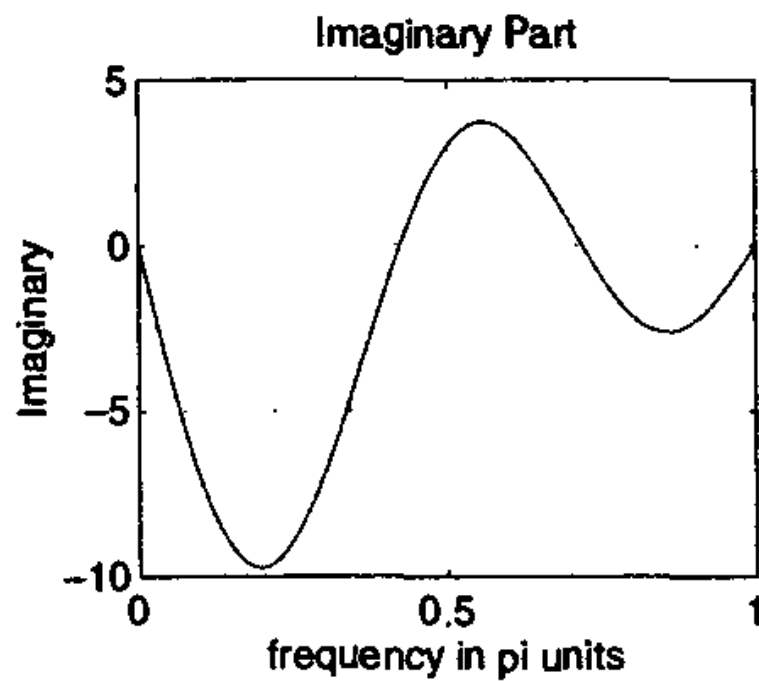
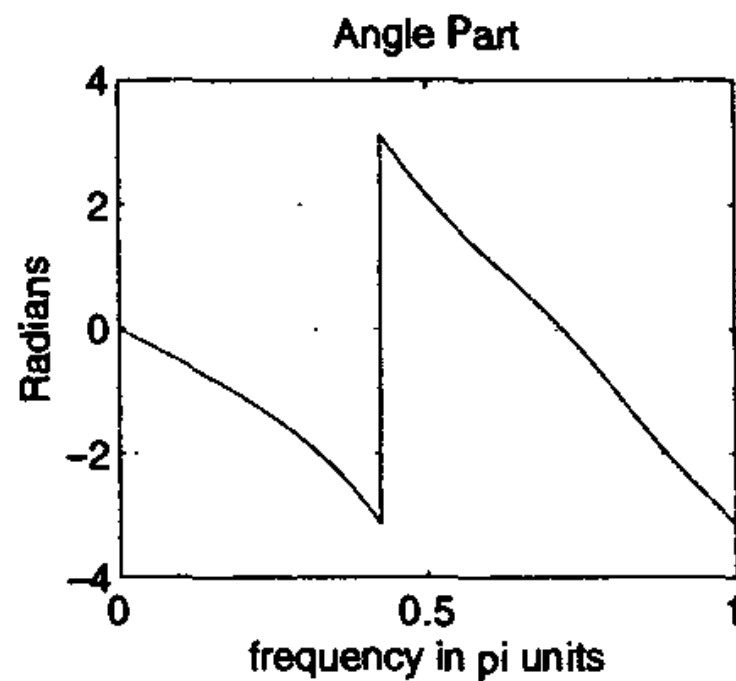
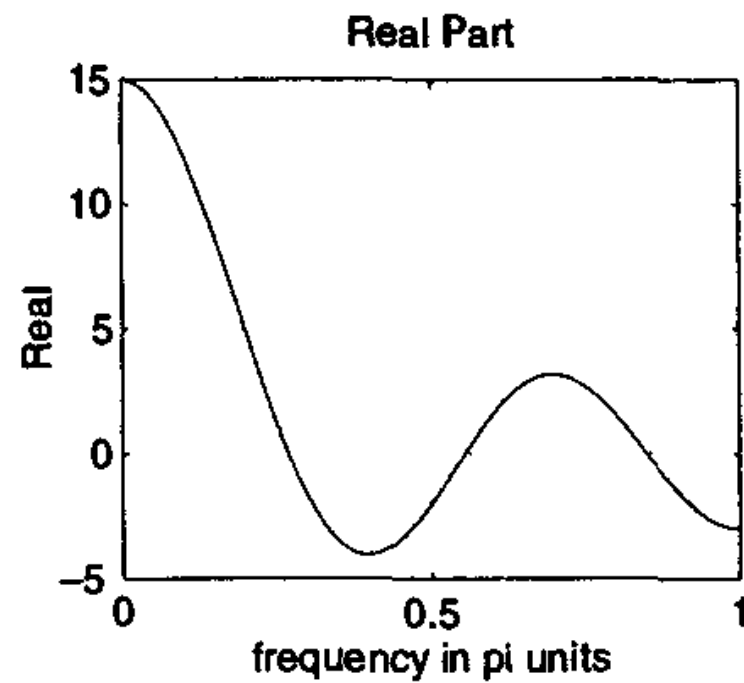
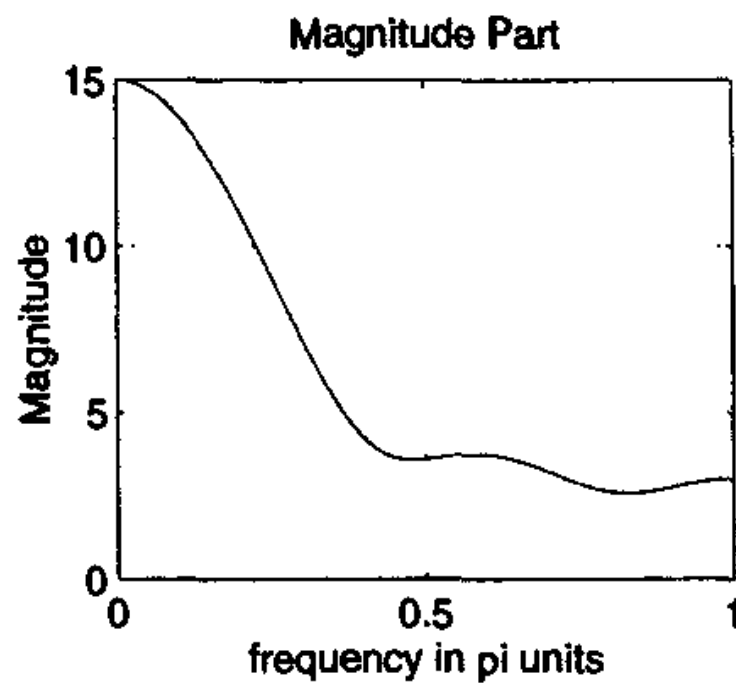


$$x(n) = \{1, 2, 3, 4, 5\}$$

↑

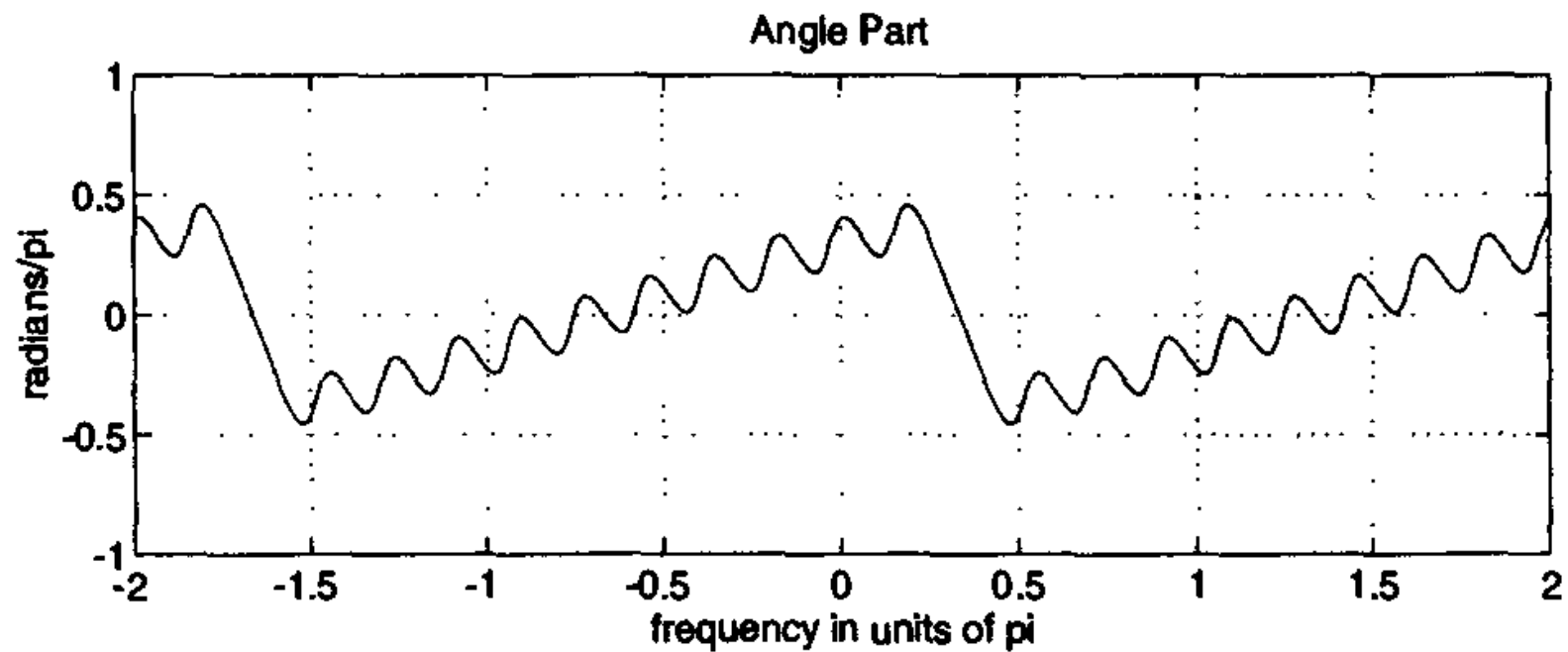
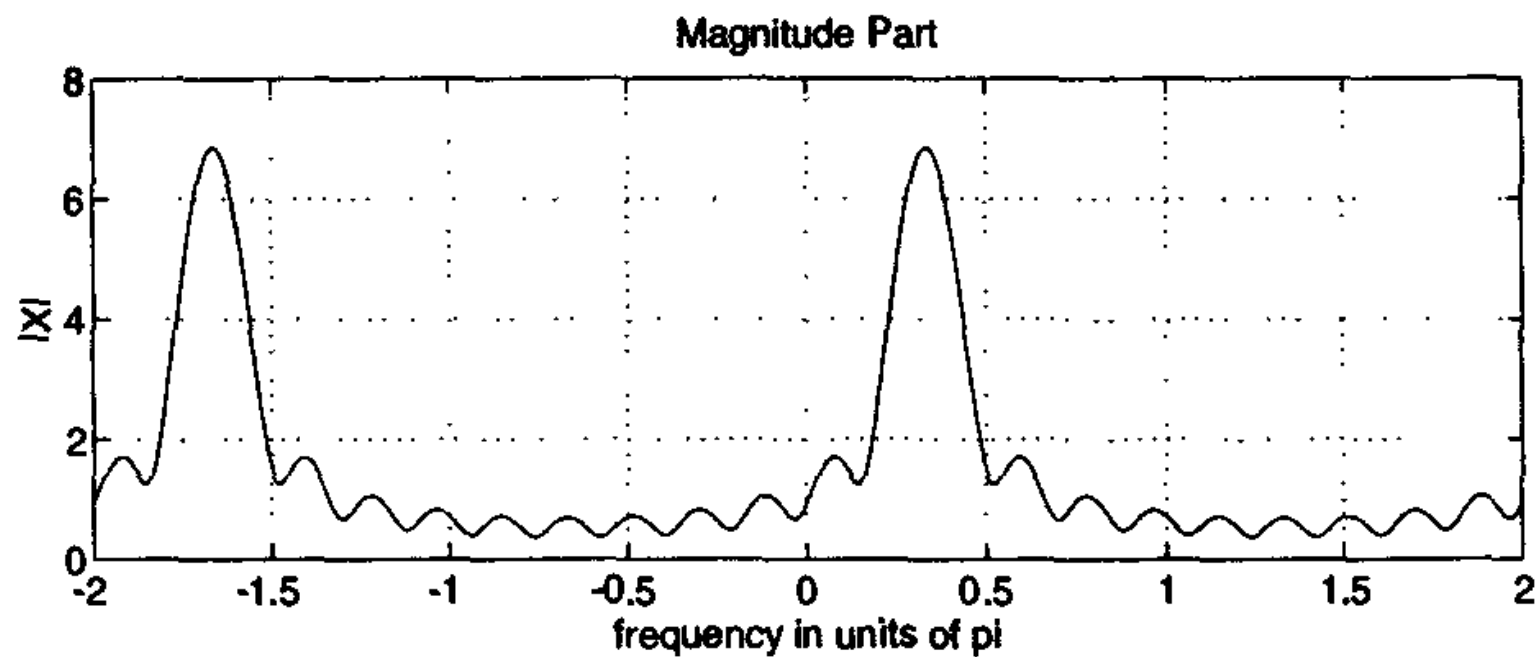
$$X(e^{j\omega}) = \sum_{-\infty}^{\infty} x(n)e^{-j\omega n} = e^{j\omega} + 2 + 3e^{-j\omega} + 4e^{-j2\omega} + 5e^{-j3\omega}$$

```
>> n = -1:3; x = 1:5;
>> k = 0:500; w = (pi/500)*k;
>> X = x * (exp(-j*pi/500)) .^ (n'*k);
>> magX = abs(X); angX = angle(X);
>> realX = real(X); imagX = imag(X);
>> subplot(2,2,1); plot(k/500,magX);grid
>> xlabel('frequency in pi units'); title('Magnitude Part')
>> subplot(2,2,3); plot(k/500,angX/pi);grid
>> xlabel('frequency in pi units'); title('Angle Part')
>> subplot(2,2,2); plot(k/500,realX);grid
>> xlabel('frequency in pi units'); title('Real Part')
>> subplot(2,2,4); plot(k/500,imagX);grid
>> xlabel('frequency in pi units'); title('Imaginary Part')
```



$$x(n) = (0.9 \exp(j\pi/3))^n, \quad 0 \leq n \leq 10$$

```
>> n = 0:10; x = (0.9*exp(j*pi/3)).^n;
>> k = -200:200; w = (pi/100)*k;
>> X = x * (exp(-j*pi/100)).^(n'*k);
>> magX = abs(X); angX =angle(X);
>> subplot(2,1,1); plot(w/pi,magX);grid
>> xlabel('frequency in units of pi'); ylabel('|X|')
>> title('Magnitude Part')
>> subplot(2,1,2); plot(w/pi,angX/pi);grid
>> xlabel('frequency in units of pi'); ylabel('radians/pi')
>> title('Angle Part')
```



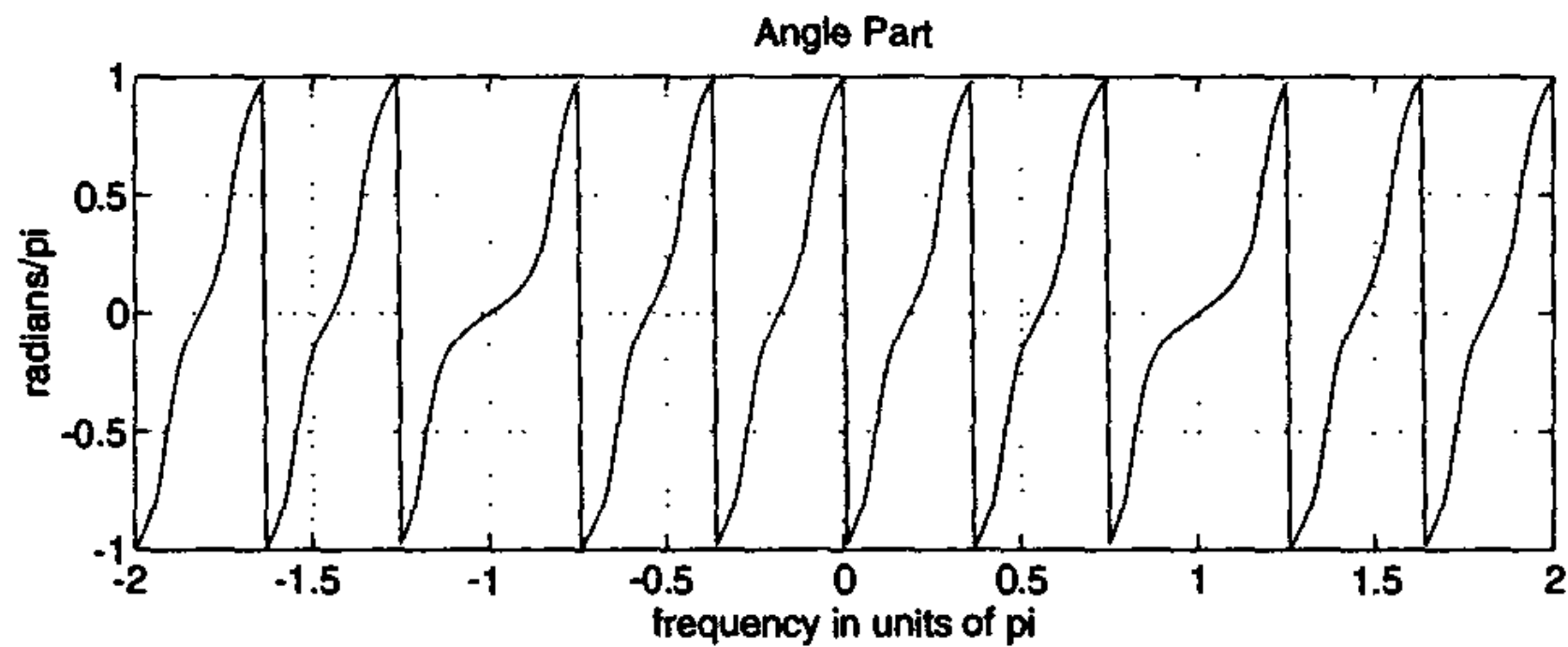
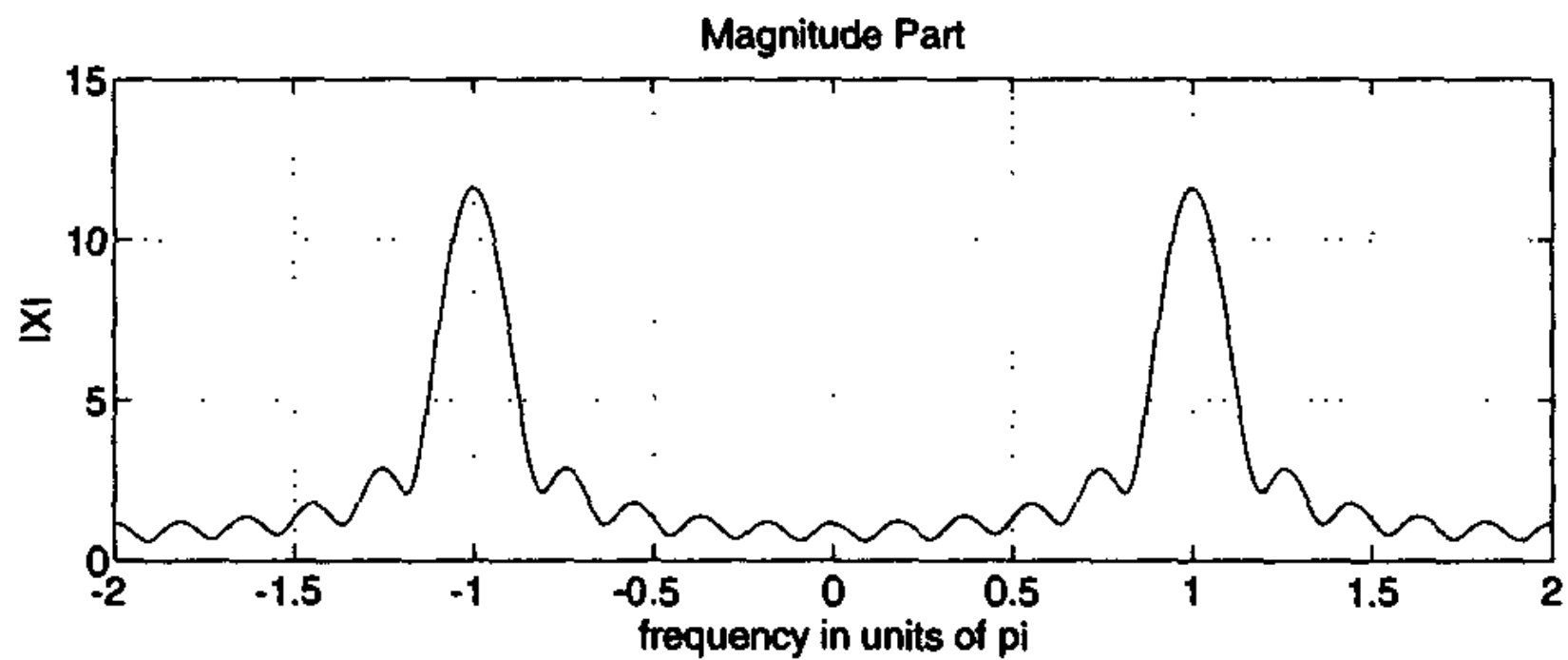
$$x(n) = 2^n, \quad -10 \leq n \leq 10.$$

```

subplot(1,1,1)
n = -5:5; x = (-0.9).^n;
k = -200:200; w = (pi/100)*k;
X = x * (exp(-j*pi/100)).^(n'*k);
magX = abs(X); angX =angle(X);
subplot(2,1,1); plot(w/pi,magX);grid
axis([-2,2,0,15])
xlabel('frequency in units of pi'); ylabel('|X|')
title('Magnitude Part')
subplot(2,1,2); plot(w/pi,angX)/pi;grid
axis([-2,2,-1,1])
xlabel('frequency in units of pi'); ylabel('radians/pi')
title('Angle Part')

```





$$x(n) = \cos(\pi n/2), \quad 0 \leq n \leq 100 \quad \text{and} \quad y(n) = e^{j\pi n/4} x(n)$$

```
>> n = 0:100; x = cos(pi*n/2);
>> k = -100:100; w = (pi/100)*k;          % frequency between -pi and +pi
>> X = x * (exp(-j*pi/100)).^(n'*k);      % DTFT of x
%
>> y = exp(j*pi*n/4).*x;                  % signal multiplied by exp(j*pi*n/4)
>> Y = y * (exp(-j*pi/100)).^(n'*k);      % DTFT of y
% Graphical verification
>> subplot(1,1,1)
>> subplot(2,2,1); plot(w/pi,abs(X)); grid; axis([-1,1,0,60])
>> xlabel('frequency in pi units'); ylabel('|X|')
>> title('Magnitude of X')
>> subplot(2,2,2); plot(w/pi,angle(X)/pi); grid; axis([-1,1,-1,1])
>> xlabel('frequency in pi units'); ylabel('radiands/pi')
>> title('Angle of X')
>> subplot(2,2,3); plot(w/pi,abs(Y)); grid; axis([-1,1,0,60])
>> xlabel('frequency in pi units'); ylabel('|Y|')
>> title('Magnitude of Y')
>> subplot(2,2,4); plot(w/pi,angle(Y)/pi); grid; axis([-1,1,-1,1])
>> xlabel('frequency in pi units'); ylabel('radians/pi')
>> title('Angle of Y')
```

