

Problem Set 3 - Cosets, Normal Subgroups, the Symmetric Group

Problem 1 Write the following product as a product of disjoint cycles

a) $(1\ 2\ 3\ 4)(2\ 3\ 4\ 5)(2\ 4\ 3)(1\ 2)(1\ 4)$

b) $(1\ 2)(1\ 3)(1\ 4)(1\ 5)$

c) $(1\ 2)(1\ 3)(1\ 2)$

d) $(1\ 2)(1\ 2\ 3)(1\ 2)$

e) $(1\ 2)(1\ 2\ 3\ 4)(1\ 2)$

Problem 2 What are the powers of $(1\ 2\ 3\ 4\ 5\ 6)$?

Problem 3 Find the order of

a) $(1\ 2)(3\ 4)(5\ 6)$

b) $(1\ 2)(3\ 4\ 5\ 6)$

c) $(1\ 2)(3\ 4\ 5)$

Problem 3 Let $G = S_3$. Let $H = \{(), (1\ 2)\}$.

a) Show that $H < G$.

b) What groups are conjugate to H in G ?

c) What are the cosets of H in G ?

d) Is $H \triangleleft G$?

Problem 4 a) What do the conjugacy classes of elements in S_5 look like?

b) How many conjugacy classes are there in S_5 ?

c) How many elements are in each conjugacy class in S_5 ?