

# Open-Shell Random Phase Approximation : Application to Atomisation Energies and Energy Barrier Heights

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## RSH+RPA formulation

Range separation<sup>[1]</sup> with the range-separation parameter  $\mu$  :

$$E_{\text{exact}} = \min_{\Psi} \left\{ \langle \Psi | \hat{T} + \hat{V}_{ne} + \hat{W}_{ee}^{\text{lr}} | \Psi \rangle + E_{Hxc}^{\text{sr}}[n_{\Psi}] \right\}$$

Single determinant approximation :

$$E_0 = \min_{\Phi} \left\{ \langle \Phi | \hat{T} + \hat{V}_{ne} + \hat{W}_{ee}^{\text{lr}} | \Phi \rangle + E_{Hxc}^{\text{sr}}[n_{\Phi}] \right\}$$

Adding long-range correlation :

$$E_{\text{exact}} = E_0 + E_c^{\text{lr}}$$

There is a wide variety of RPA formulations and variants<sup>[2]</sup>, focus is here brought to : dRPA-I<sup>[2]</sup> and Szabo-Ostlund 2 (SO2)<sup>[3]</sup>.

(dRPA-I includes in no way exchange effects ; SO2 is a variant of RPA that fully includes exchange effects.)

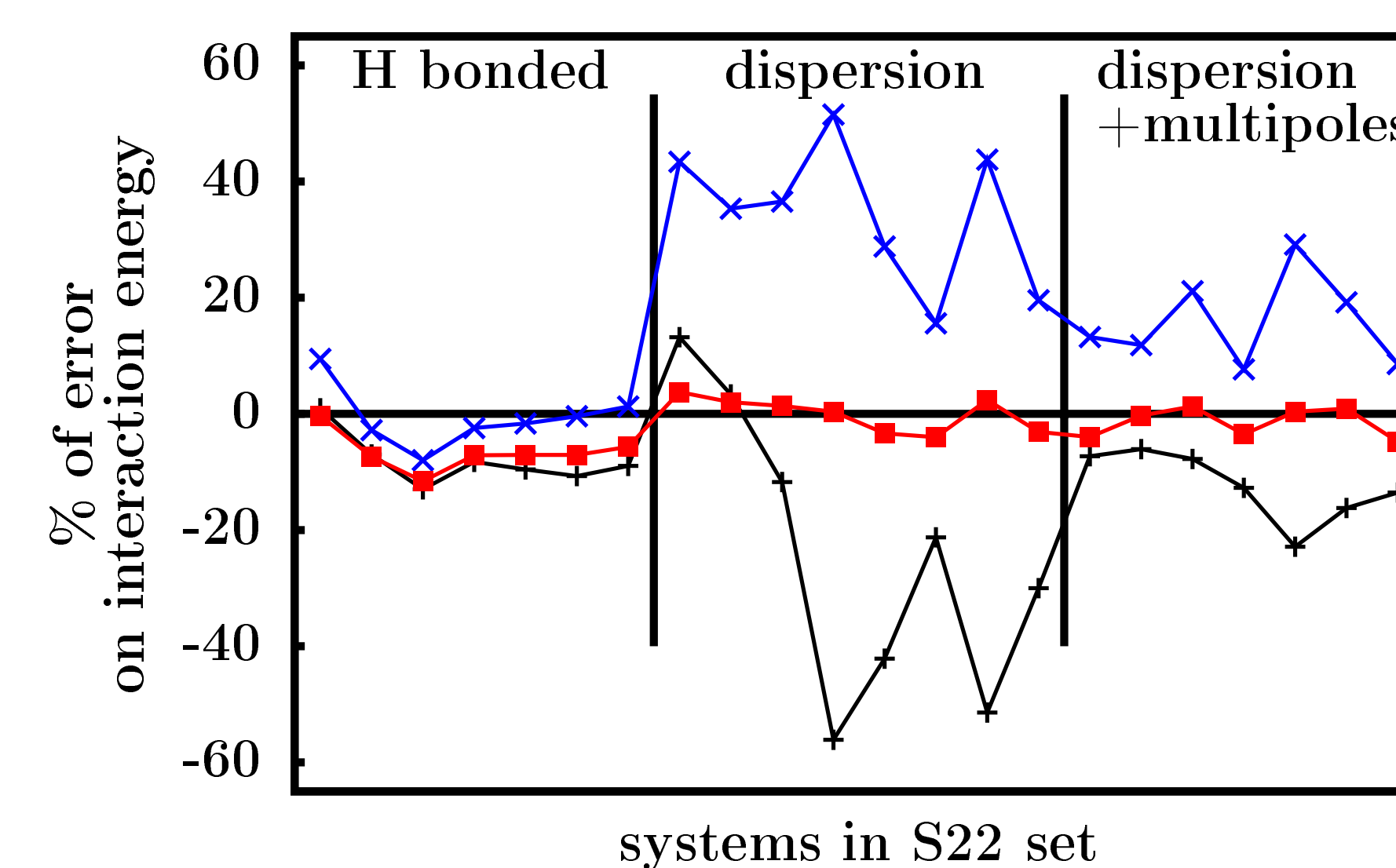
$$\frac{\text{erf}(\mu r_{ij})}{r_{ij}}$$

srLDA, srPBE, ...

lrMP2, lrRPA, ...

## Performance on energies

Study on the S22 set of weakly-interacting molecular systems<sup>[3]</sup> ( $\mu = 0.5 \text{ bohr}^{-1}$ , srPBE functional, aug-cc-pVDZ).

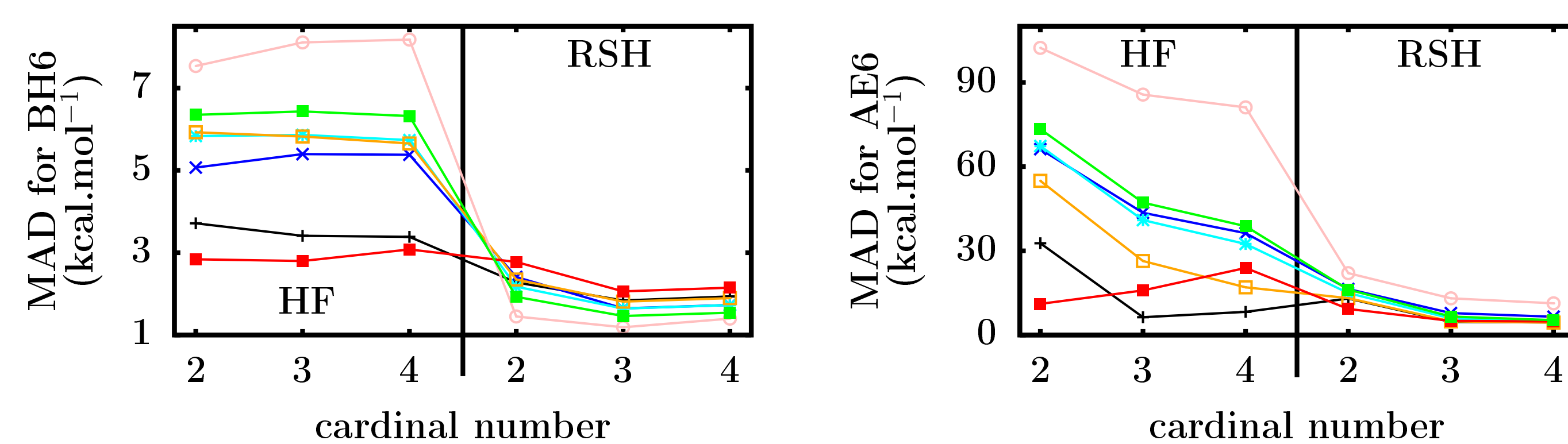


It is seen that SO2 is better for the description of van der Waals interactions<sup>[3]</sup>.

All data shown are MAD in kcal.mol<sup>-1</sup> of atomization energies of the AE6 dataset and of barrier heights of reactions of the BH6 dataset.

## Dependence on the basis set

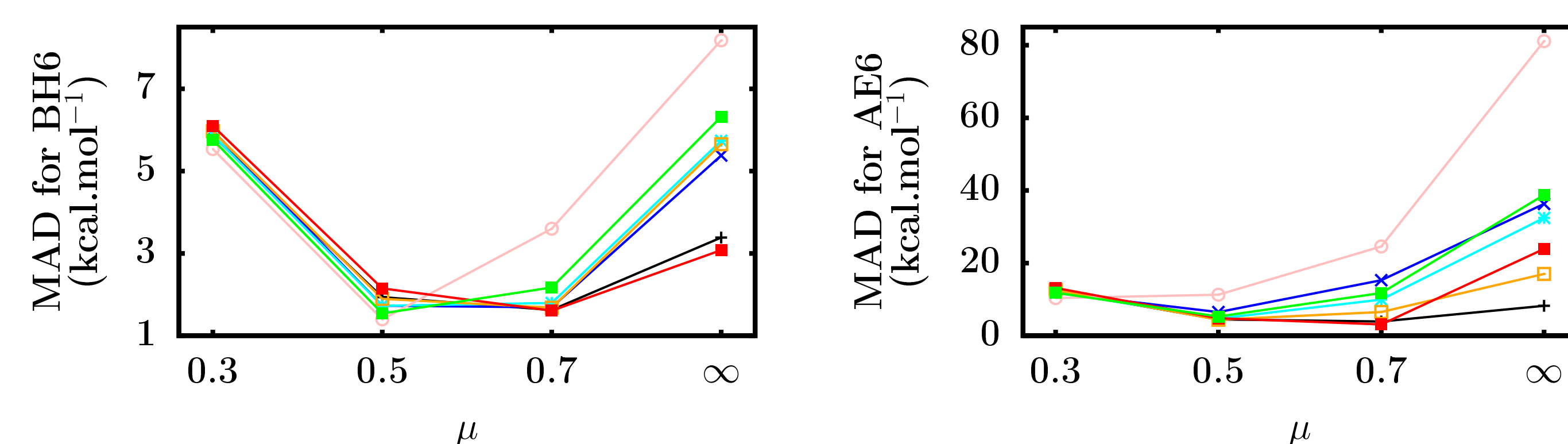
( $\mu = 0.5 \text{ bohr}^{-1}$ , srPBE functional, spin unrestricted<sup>[4]</sup>)



- ▷ As expected, the use of **range separation facilitates the convergence** with respect to the basis set.
- ▷ All range-separated methods give about the same accuracy.

## Dependence on $\mu$

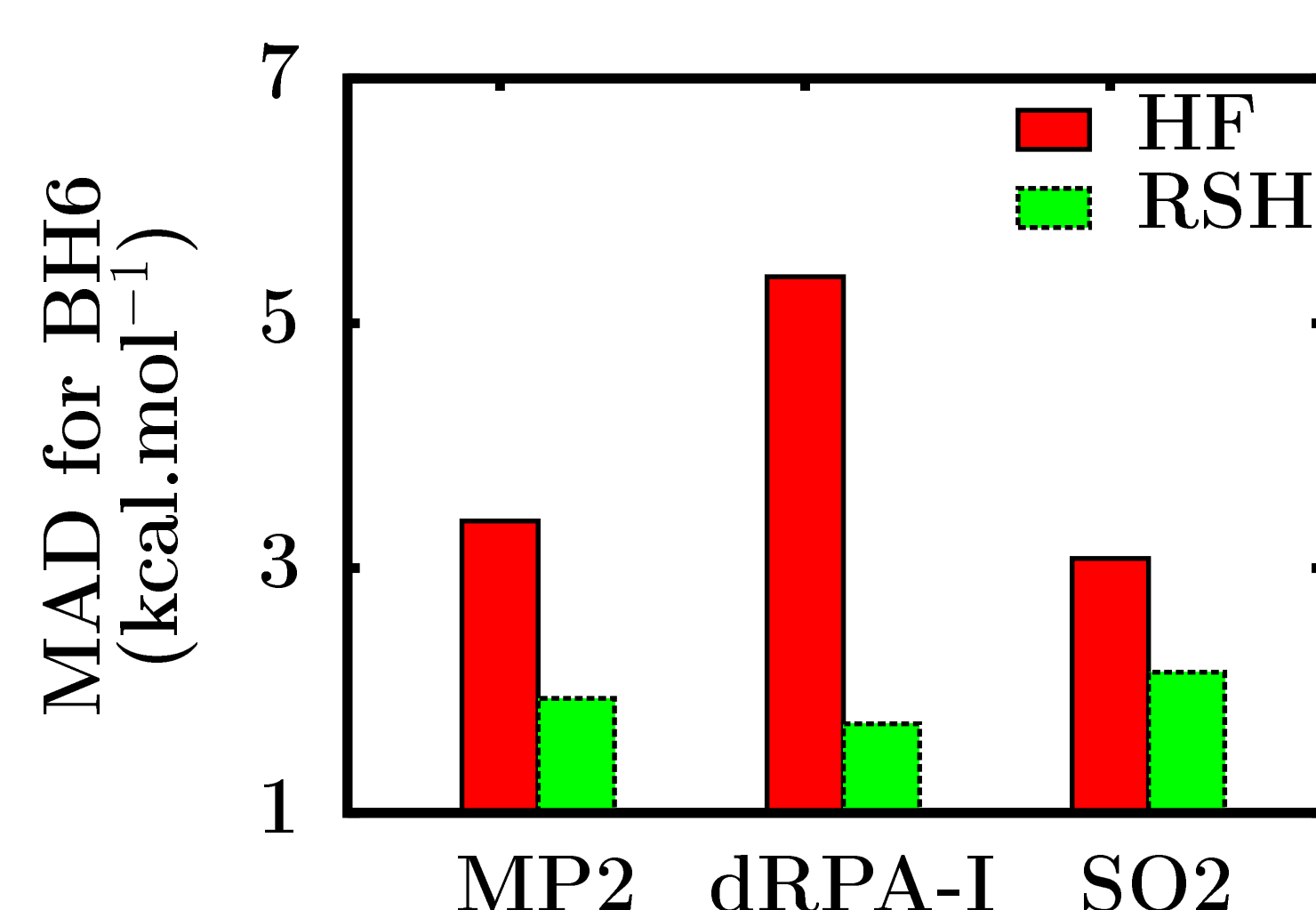
(cc-pVQZ, srPBE functional, spin unrestricted<sup>[4]</sup>)



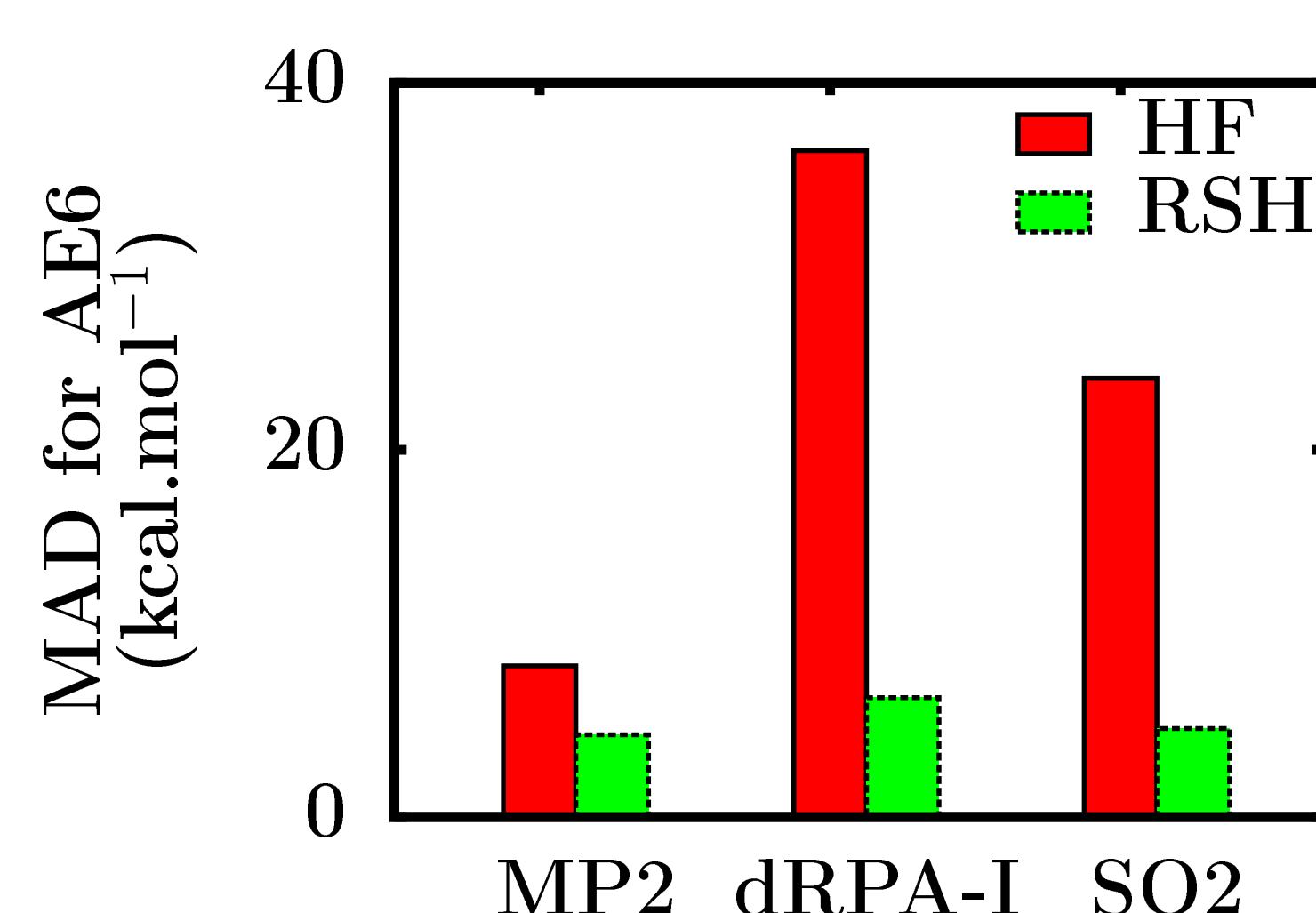
- ▷ The canonical value of  $\mu = 0.5 \text{ bohr}^{-1}$  is here again a sound choice.

## RSH+SO2 is a good method

( $\mu = 0.5 \text{ bohr}^{-1}$ , cc-pVQZ, srPBE functional, spin unrestricted<sup>[4]</sup>)



- ▷ Range-separation generally improves the results.



- ▷ Szabo-Ostlund 2 confirms it's position of leader in the RSH+RPA categories of methods.

## CONCLUSION AND OUTLOOK

- ▷ Most RPA formulations and variants have been **generalized to open-shell** expressions.
- ▷ Working implementation as been done in **MOLPRO**<sup>[5]</sup>.
- ▷ Open-shell (RSH+)RPA calculations have successfully been applied to the **AE6 and BH6 dataset**.
- ▷ Results confirm that **RSH+SO2 is a good method** to calculate :
  - interaction energies
  - atomization energies
  - barrier heights
- ▷ Future developments could include a way to estimate **spin-contamination** in these RPA calculations and a **spin-adapted open-shell RPA** formulation.

## References

1. Toulouse, Gerber, Jansen, Savin, Ángyán, PRL, 2009
2. Ángyán, Liu, Toulouse, Jansen, JCTC, 2011
3. Toulouse, Zhu, Savin, Jansen, Ángyán, JCP, 2011
4. Mussard, Toulouse, Luppi, Reinhardt, *to be published*
5. MOLPRO 2012.1, Werner, Knowles, Knizia, Manby, Schütz