

Assignment - 2

Solution

1. Simplify:

$$\begin{aligned} \text{a. } & (P + Q + R)(P + Q')(P' + R) \\ & = (PP + PQ' + PQ + QQ' + PR + Q'R)(P' + R) \\ & = (P + P(Q' + Q) + PR + Q'R)(P' + R) \\ & = (P(1 + R) + Q'R)(P' + R) \\ & = (P + Q'R)(P' + R) \\ & = PP' + PR + Q'RP' + Q'RR \\ & = PR + Q'R(P' + 1) \\ & = PR + Q'R \\ \text{b. } & A'B'C + (A+B+C)' + A'B'C' \\ & = A'B'C + A'B'C' + A'B'C' \\ & = A'B'C + A'B'C' \\ & = A'B'(C + C') \\ & = A'B'(1) = A'B' \end{aligned}$$

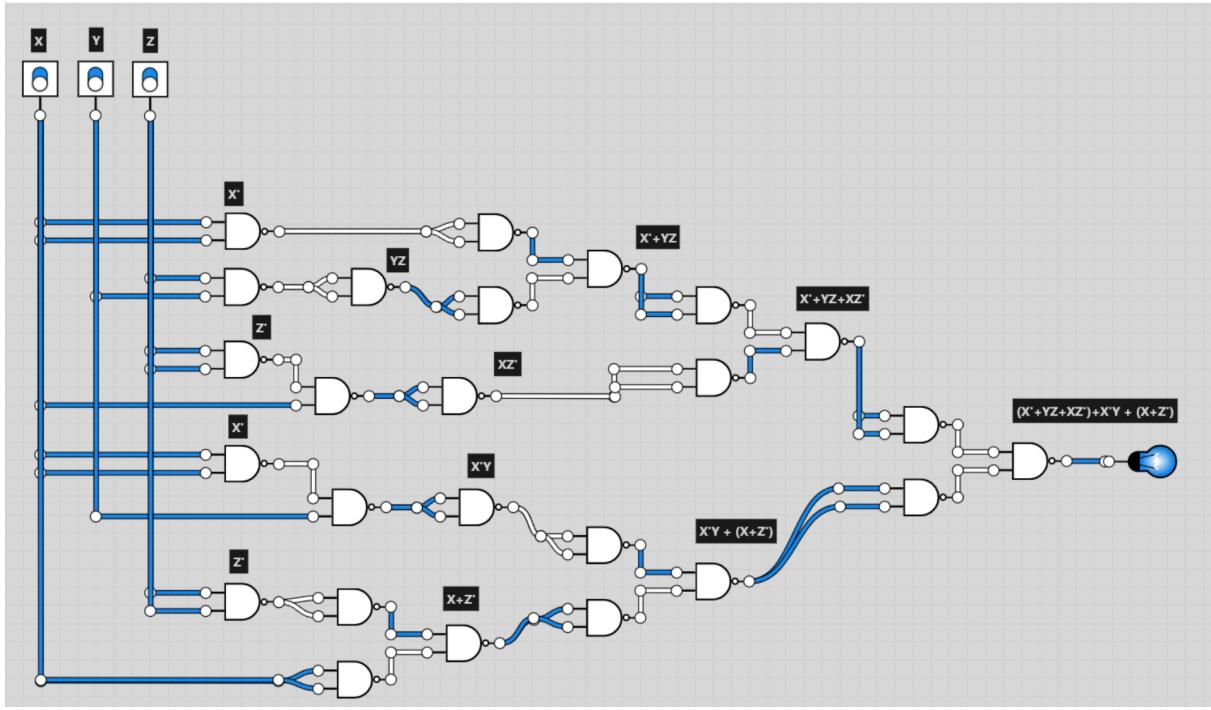
2. Complement:

$$\begin{aligned} \text{a. } & A' + C(B + C')(A' + B')(A + C') \\ & = A' \cdot [C + (B \cdot C') + (A' \cdot B') + (A \cdot C')] \\ & = A [C' + (B'C) + (A B) + (A'C)] \end{aligned}$$

3. POS: $F = \prod(000, 010, 111)$

$$= (A + B + C)(A + B' + C)(A' + B' + C')$$

4. Draw using NAND gates only:



5. Find SOP and POS:

SOP:

$$\begin{aligned}
 F(P, Q, R, S) &= P + QR'S \\
 &= P(Q+Q')(R+R')(S+S') + (P+P')QR'S \\
 &= (PQ + PQ')(R+R')(S+S') + PQR'S + P'QR'S \\
 &= (PQR + PQR' + PQ'R + PQ'R')(S+S') + PQR'S + P'QR'S \\
 &= PQRS + PQR'S + PQ'RS + PQ'R'S + PQRS' + PQR'S' + PQ'RS' + \\
 &\quad PQ'R'S' + PQR'S + P'QR'S \\
 &= PQRS + PQR'S + PQ'RS + PQ'R'S + PQRS' + PQR'S' + PQ'RS' + \\
 &\quad PQ'R'S' + P'QR'S \\
 &= \sum (1111, 1101, 1011, 1001, 1110, 1100, 1010, 1000, 0101) \\
 &= \sum (15, 13, 11, 9, 14, 12, 10, 8, 5) \\
 &= \sum (5, 8, 9, 10, 11, 12, 13, 14, 15)
 \end{aligned}$$