

104. Maximum Depth of Binary Tree

<https://leetcode.com/problems/maximum-depth-of-binary-tree/description/>

Problem Summary

Given the root of a binary tree, return the **maximum depth** of the tree.

- The **maximum depth** is the number of nodes **along the longest path** from the root down to the farthest leaf.

Note: In this problem, depth = number of nodes on the path (not number of edges), so the root itself contributes 1.



Recursive Approach



Base Case:

- If the tree is empty (root == None), return 0.



Recursive Step:

- For any node, compute the depth of its left subtree: $\text{left} = \text{maxDepth}(\text{root.left})$
- Compute the depth of its right subtree: $\text{right} = \text{maxDepth}(\text{root.right})$
- Return $\max(\text{left}, \text{right}) + 1$ because:
 - You want the deeper side.
 - And you add 1 to include the current node.



Python Code

```
# Definition for a binary tree node.
```

```
class TreeNode:
```

```
    def __init__(self, val=0, left=None, right=None):
        self.val = val
        self.left = left
        self.right = right
```

```

class Solution:

def maxDepth(self, root: Optional[TreeNode]) -> int:
    if not root:
        return 0

    left = self.maxDepth(root.left)
    right = self.maxDepth(root.right)

    return max(left, right) + 1

```

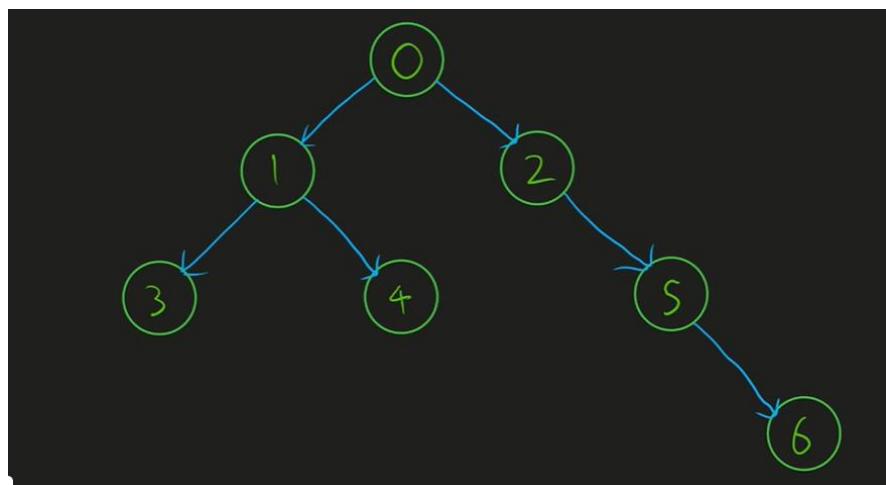
⌚ Time and Space Complexity

Metrics	Values
Time	$O(n)$ — every node is visited once
Space	$O(h)$ — recursion stack goes up to height of the tree (h)

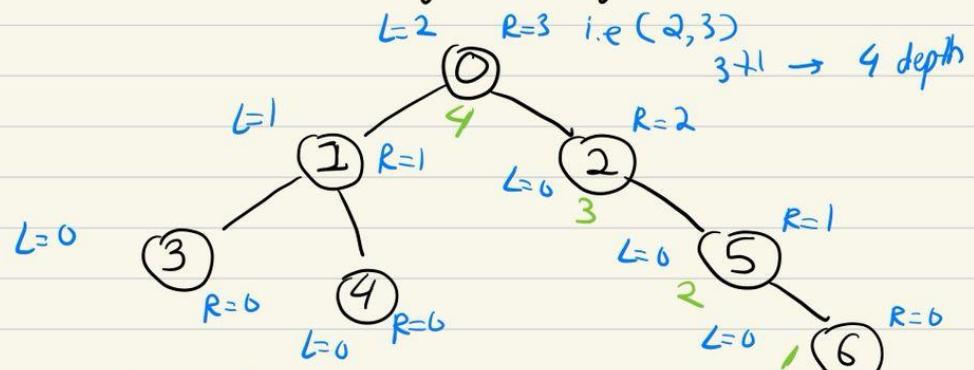
🧠 Conceptual Notes

- The function is **recursive**, and every call is isolated with its own left and right values.
- This is why you can think of every subtree as a small problem being solved independently — a key recursive idea in tree problems.

Dry Run following Tree for example:



Q2 Maximum Depth of Binary Tree



`def maxDepth(self, root: Optional[TreeNode]) → int`

If not root: — check 1
return 0

`left = self.maxDepth(root.left)` → check 2

`right = self.maxDepth(root.right)` → check 3

`return max(left, right)`

#1 `root i.e. 0 ≠ null` check 1

`left = maxDepth(root.left i.e. 0.left)` check 2
→ 1

1.1

`root i.e. 1 ≠ null`

`left = maxDepth(root.left i.e. 1.left)` check 2
1 → 3

1.1.1 \nearrow_{root} i.e 3 $\maxDepth(\text{self}, 3)$

$3 \neq \text{null} \checkmark$

$\text{left} = \text{self}. \maxDepth(3. \text{left})$
 $3 \rightarrow \text{null}$

1.1.1.L

\nearrow_{root} i.e. null

null = null \checkmark

$\text{return } 0$

Goes back to # 1.1.1 left=0

$\nearrow_{\text{right}} = \text{self}. \maxDepth(3. \nearrow_{\text{right}})$
 $3 \rightarrow \text{null}$

1.1.1.R

$\nearrow_{\text{root}} \text{ null}$ i.e. null = null \checkmark return

Goes back to 1.1 $\nearrow_{\text{right}} = 0$

$\text{return } \max(\text{left}, \nearrow_{\text{right}}) + 1$
 $(0, 0) + 1$

$\text{return } 1$

Goes back to 1.1 $\nearrow_{\text{left}} = 1$

$\nearrow_{\text{right}} = \text{self}. \maxDepth(\text{self}. \nearrow_{\text{right}})$
 $1 \rightarrow 4$

i.e. by the whole flow we got this

1.1.R $\text{root} = 4$

$4 \neq \text{null}$

$\text{left} = \text{self.maxDepth}(\text{root.left})$
 $4 \rightarrow \text{null}$)

1.1.R.L

$\text{root} = \text{null}$

i.e. $\text{null} = \text{null} \checkmark$ return 0

Go back to 1.1.R $\text{left} = 0$

$\text{right} = \text{self.maxDepth}(\text{root.right})$
 $4 \rightarrow \text{null}$

1.1.R.R

$\text{root} \Rightarrow \text{null}$ i.e. $\text{null} = \text{null}$ return 0

Go back to 1.1.R $\text{Right} = 0$

return $\max(\text{left}, \text{right}) + 1$
 $0, 0 + 1$

return 1

because it got
its
call from
 right

Go back to 1.1 $\text{Right} = 1$

return $\max(\text{left}, \text{right}) + 1$
 $1, 1 + 1$

return 2

Goers back to 1 left = 2

from the whole detailed recursive call

$\pi_{right} = self \cdot MaxDepth(\underline{self \cdot \pi_{right}})$
 $1 \rightarrow 2$

1.R

$\pi_{root} = 2$ i.e. $2 \neq null$

$\pi_{left} = self \cdot maxDepth(\underline{\pi_{root \cdot \pi_{left}}})$
 $2 \rightarrow null$

1.R.1

$\pi_{root} \rightarrow null = null$ return 0

Goers back to 1.R left = 0

$\pi_{right} = self \cdot \pi_{right} (\underline{2 \cdot \pi_{right}})$
 $2 \rightarrow 5$

1.R.R

π_{root} i.e. $5 \neq null$

$\pi_{left} = self \cdot \pi_{left} (\underline{5 \cdot \pi_{left}})$
 $5 \rightarrow null$)

1.R.R.1

π_{root} i.e. $null = null$

Goers back to 1.RR left = 0

$\pi_{right} = self \cdot \pi_{right} (\underline{5 \cdot \pi_{right}})$
 $5 \rightarrow 6$

I.R.R.R $\text{root} = 6$ i.e. $6 \neq \text{null}$

$\text{left} = \text{self.maxDepth}(6.\text{root})$
 $6 \rightarrow \text{null}$

I.R.R.R.] $\text{null} = \text{null}$ $\text{return } 0$

Goes back to I.R.R.R $\text{left} = 0$

$\text{right} = \text{self.maxDepth}(6.\text{root})$
 $6 \rightarrow \text{null}$

I.R.R.R.I

$\text{null} = \text{null}$ $\text{return } 0$

Goes back to I.R.R.R $\text{right} = 0$

$\text{return } \max(\text{right}, \text{left})$
 $0, 0 + 1$
I

Goes back to I.R.R $\text{right} = 1$

$\text{return } \max(0, 1)$
0 + 1

$\text{return } 2$

Goes back to I.R $\text{right} = 2$

$\text{return } \max(\text{left}, \text{right})$
0, 2 + 1

$\text{return } 3$

Goes back to 1

return $\max(\text{left}, \text{right})$
 $2, 3 + 1$

return 4

max depth = 4