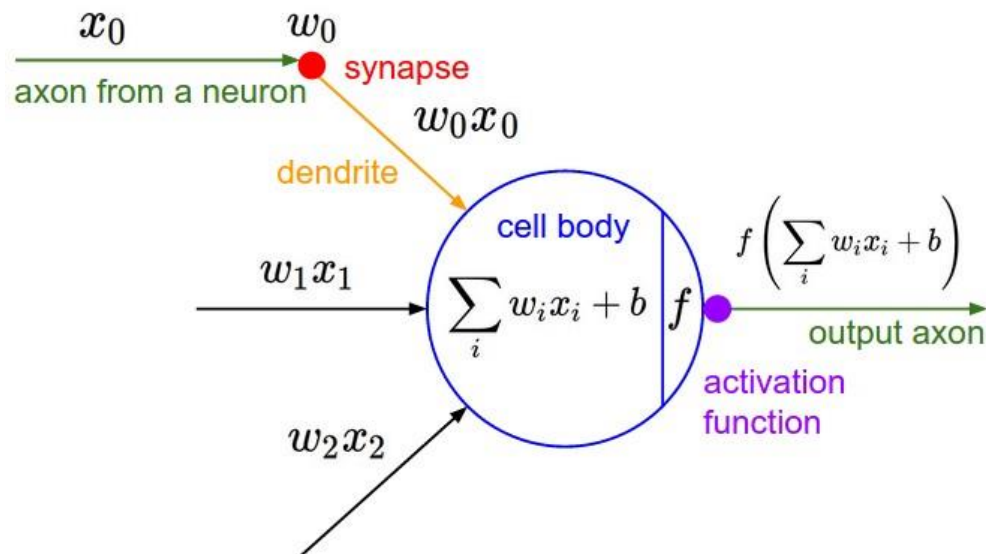


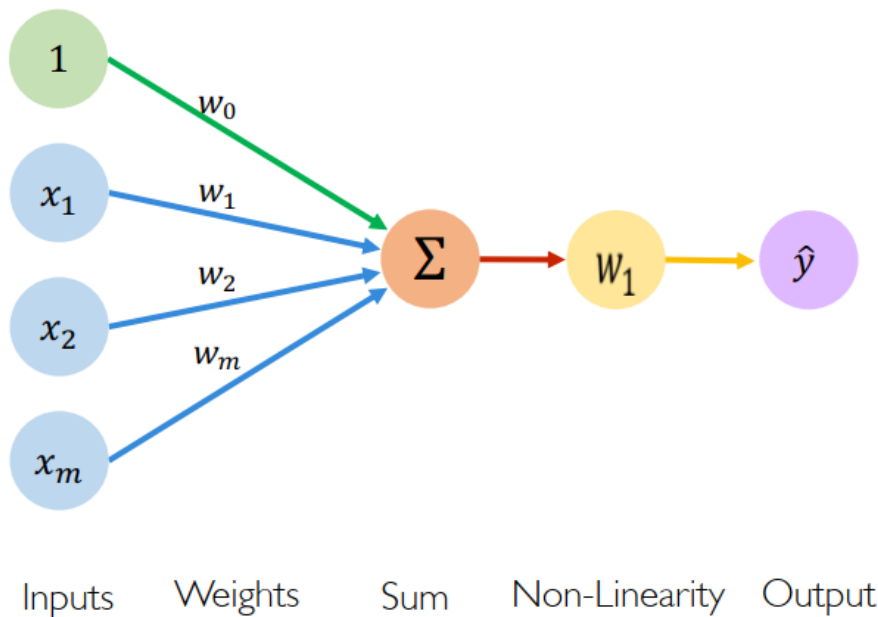
ISE 469- DERİN ÖĞRENMEYE GİRİŞ

Yapay sinir hücresi



Yapay Sinir Ağları

The Perceptron: Forward Propagation



Output

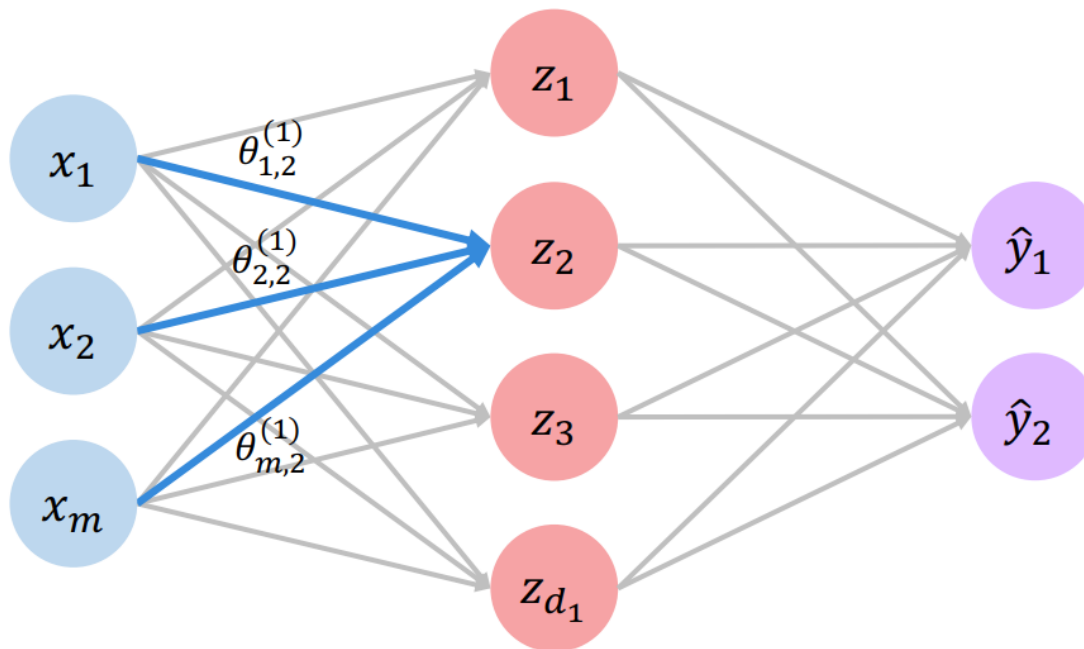
Linear combination of inputs

$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

Non-linear activation function

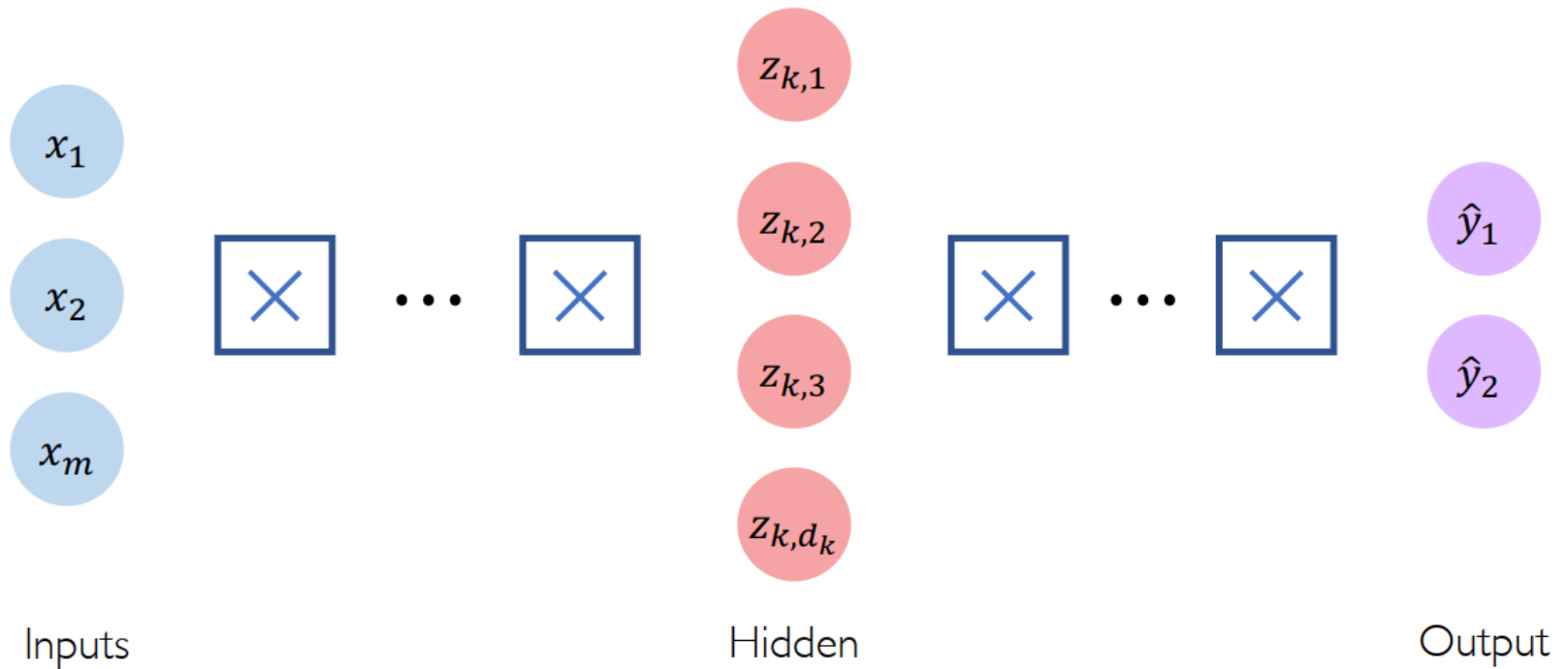
Bias

Yapay Sinir Ağları



$$\begin{aligned} z_2 &= w_{0,2}^{(1)} + \sum_{j=1}^m x_j w_{j,2}^{(1)} \\ &= w_{0,2}^{(1)} + x_1 w_{1,2}^{(1)} + x_2 w_{2,2}^{(1)} + x_m w_{m,2}^{(1)} \end{aligned}$$

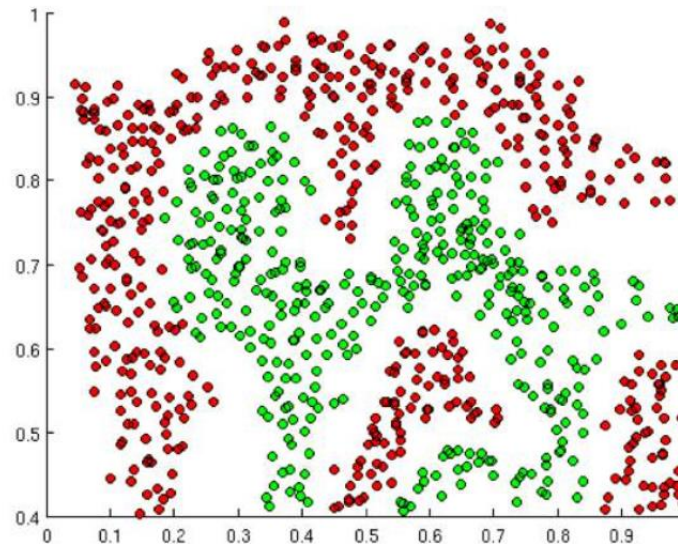
Deep Neural Network



$$z_{k,i} = w_{0,i}^{(k)} + \sum_{j=1}^{d_{k-1}} g(z_{k-1,j}) w_{j,i}^{(k)}$$

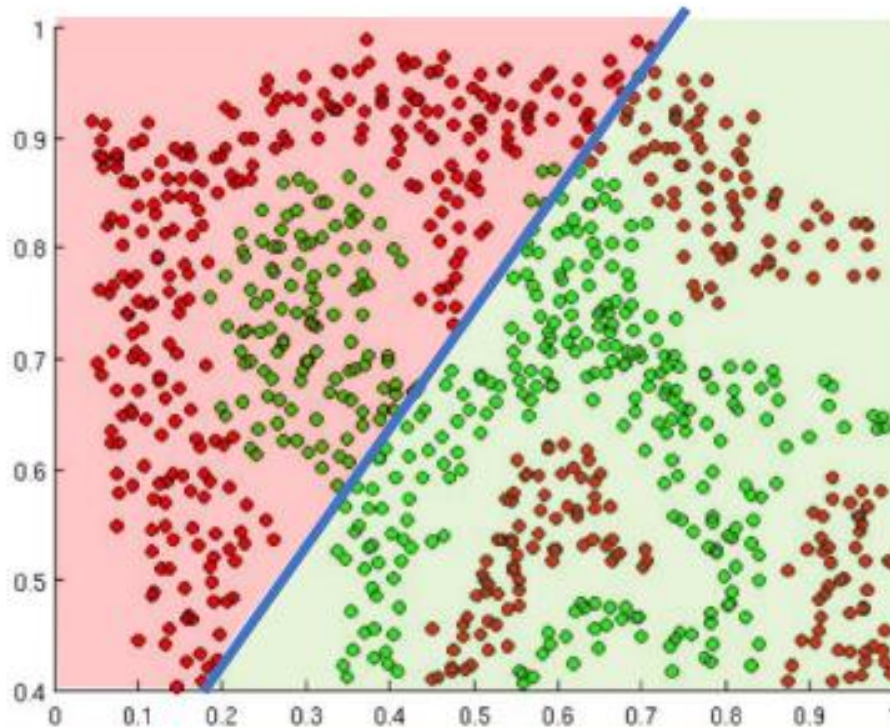
Aktivasyon fonksiyonunun önemi

The purpose of activation functions is to **introduce non-linearities** into the network



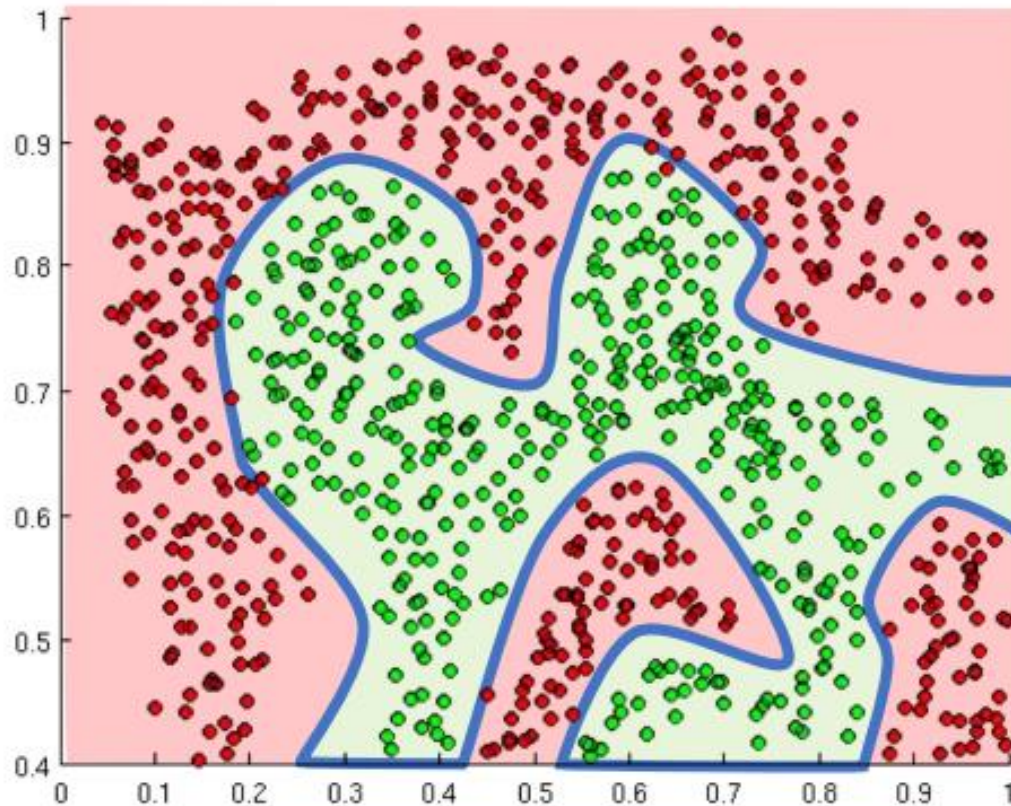
What if we wanted to build a Neural Network to distinguish green vs red points?

Doğrusal (Linear) aktivasyon fonksiyonu



Linear Activation functions produce linear decisions no matter the network size

Doğrusal olmayan (Linear) aktivasyon fonksiyonu



Non-linearities allow us to approximate
arbitrarily complex functions

Aktivasyon fonksiyonları

linear

```
keras.activations.linear(x)
```

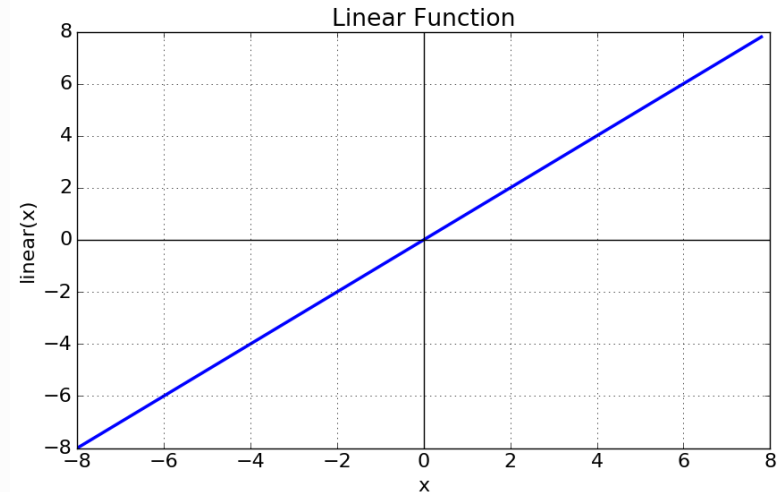
Linear (i.e. identity) activation function.

Arguments

- **x**: Input tensor.

Returns

Input tensor, unchanged.



Kaynak: <https://keras.io/activations/>

Kaynak: https://ml-cheatsheet.readthedocs.io/en/latest/activation_functions.html

Aktivasyon fonksiyonları

relu

```
keras.activations.relu(x, alpha=0.0, max_value=None, threshold=0.0)
```

Rectified Linear Unit.

With default values, it returns element-wise $\max(x, 0)$.

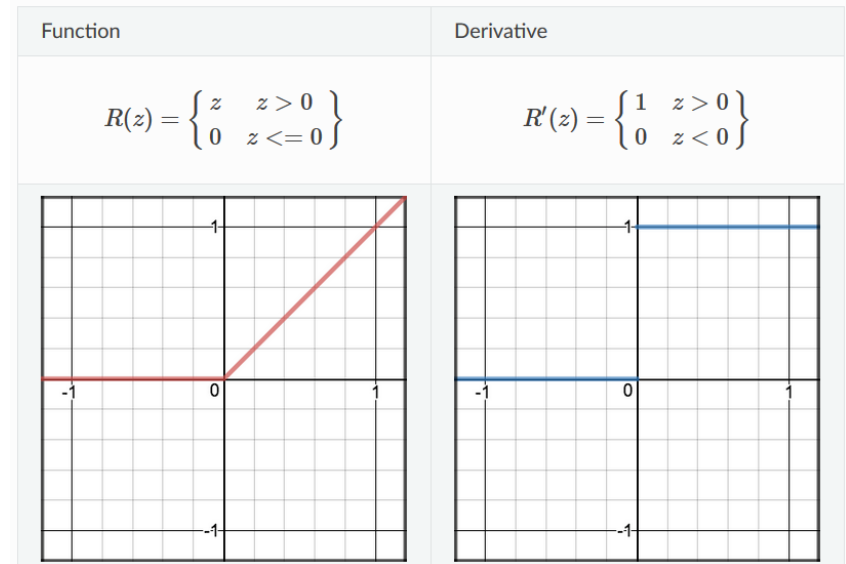
Otherwise, it follows: $f(x) = \max_value$ for $x \geq \max_value$, $f(x) = x$ for $\text{threshold} \leq x < \max_value$, $f(x) = \alpha * (x - \text{threshold})$ otherwise.

Arguments

- **x**: Input tensor.
- **alpha**: float. Slope of the negative part. Defaults to zero.
- **max_value**: float. Saturation threshold.
- **threshold**: float. Threshold value for thresholded activation.

Returns

A tensor.



Kaynak: <https://keras.io/activations/>

Kaynak: https://ml-cheatsheet.readthedocs.io/en/latest/activation_functions.html

Aktivasyon fonksiyonları

sigmoid

```
keras.activations.sigmoid(x)
```

Sigmoid activation function.

Arguments

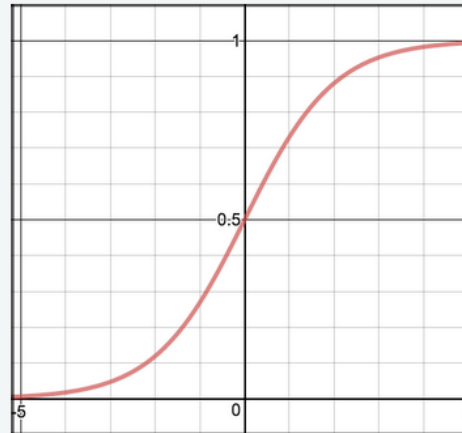
- x: Input tensor.

Returns

The sigmoid activation: $1 / (1 + \exp(-x))$.

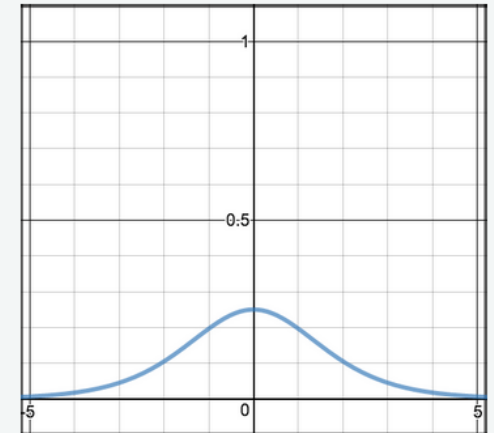
Function

$$S(z) = \frac{1}{1 + e^{-z}}$$



Derivative

$$S'(z) = S(z) \cdot (1 - S(z))$$



Kaynak: <https://keras.io/activations/>

Kaynak: https://ml-cheatsheet.readthedocs.io/en/latest/activation_functions.html

Aktivasyon fonksiyonları

softmax

```
keras.activations.softmax(x, axis=-1)
```

Softmax activation function.

Arguments

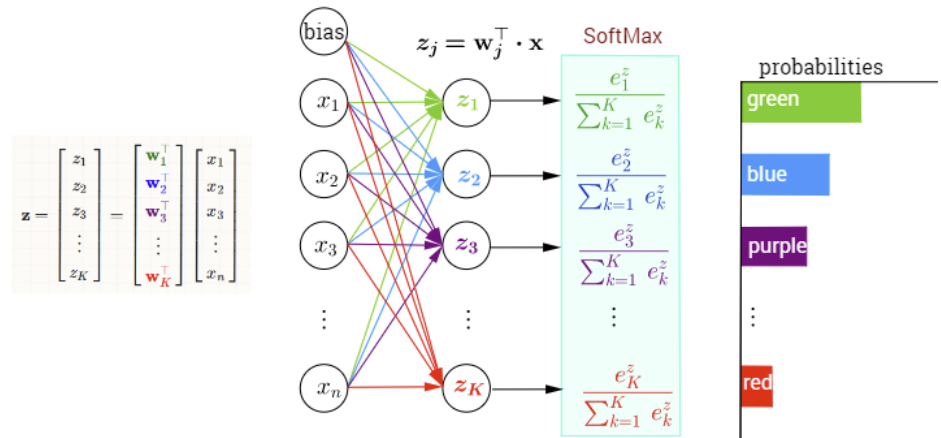
- **x**: Input tensor.
- **axis**: Integer, axis along which the softmax normalization is applied.

Returns

Tensor, output of softmax transformation.

Raises

- **ValueError**: In case `dim(x) == 1`.



Kaynak: <https://keras.io/activations/>

Kaynak: https://ml-cheatsheet.readthedocs.io/en/latest/activation_functions.html

Aktivasyon fonksiyonları

tanh

```
keras.activations.tanh(x)
```

Hyperbolic tangent activation function.

Arguments

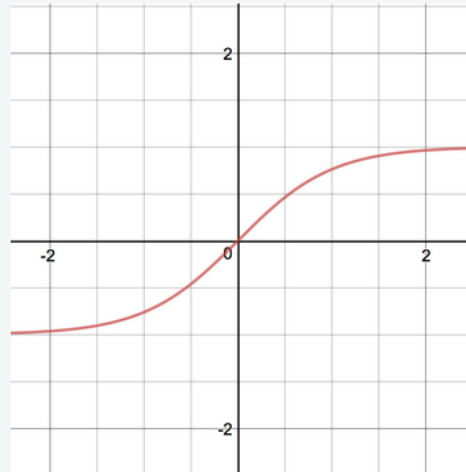
- **x**: Input tensor.

Returns

The hyperbolic activation: $\tanh(x) = (\exp(x) - \exp(-x)) / (\exp(x) + \exp(-x))$

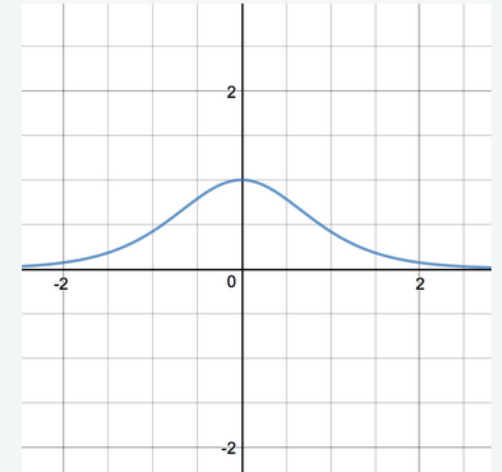
Function

$$\tanh(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}$$



Derivative

$$\tanh'(z) = 1 - \tanh(z)^2$$



Kaynak: <https://keras.io/activations/>

Kaynak: <https://towardsdatascience.com/activation-functions-neural-networks-1cbd9f8d91d6>

Aktivasyon fonksiyonları

elu

```
keras.activations.elu(x, alpha=1.0)
```

Exponential linear unit.

Arguments

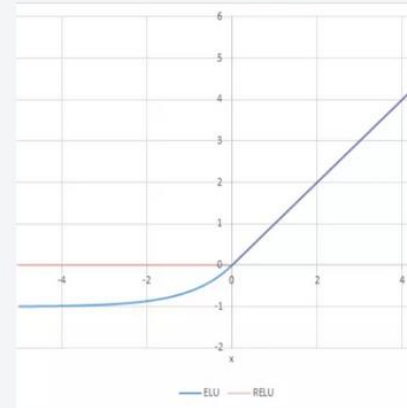
- **x**: Input tensor.
- **alpha**: A scalar, slope of negative section.

Returns

The exponential linear activation: x if $x > 0$ and $\alpha * (\exp(x)-1)$ if $x < 0$.

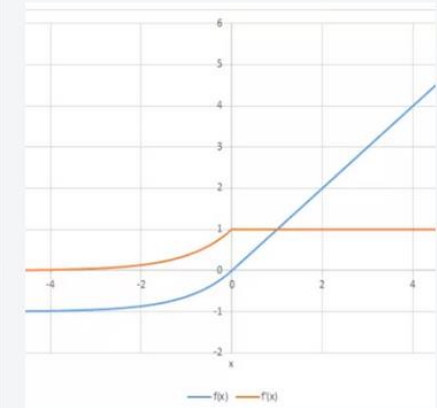
Function

$$R(z) = \begin{cases} z & z > 0 \\ \alpha \cdot (e^z - 1) & z \leq 0 \end{cases}$$



Derivative

$$R'(z) = \begin{cases} 1 & z > 0 \\ \alpha \cdot e^z & z \leq 0 \end{cases}$$



Aktivasyon fonksiyonları

selu

```
keras.activations.selu(x)
```

Scaled Exponential Linear Unit (SELU).

SELU is equal to: $\text{scale} * \text{elu}(x, \alpha)$, where α and scale are predefined constants. The values of α and scale are chosen so that the mean and variance of the inputs are preserved between two consecutive layers as long as the weights are initialized correctly (see `lecun_normal` initialization) and the number of inputs is "large enough" (see references for more information).

Arguments

- **x**: A tensor or variable to compute the activation function for.

Returns

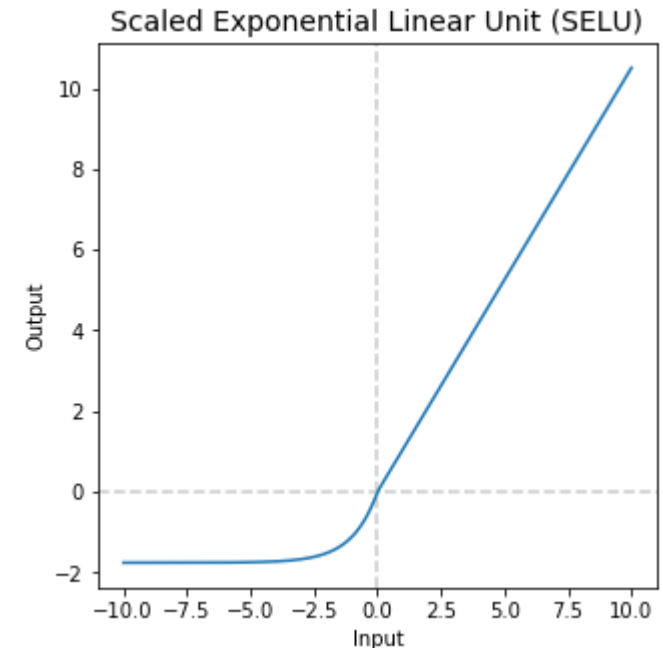
The scaled exponential unit activation: $\text{scale} * \text{elu}(x, \alpha)$.

Note

- To be used together with the initialization "lecun_normal".
- To be used together with the dropout variant "AlphaDropout".

Kaynak: <https://keras.io/activations/>

Kaynak: <https://towardsdatascience.com/deep-study-of-a-not-very-deep-neural-network-part-2-activation-functions-fd9bd8d406fc>



Aktivasyon fonksiyonları

hard_sigmoid

```
keras.activations.hard_sigmoid(x)
```

Hard sigmoid activation function.

Faster to compute than sigmoid activation.

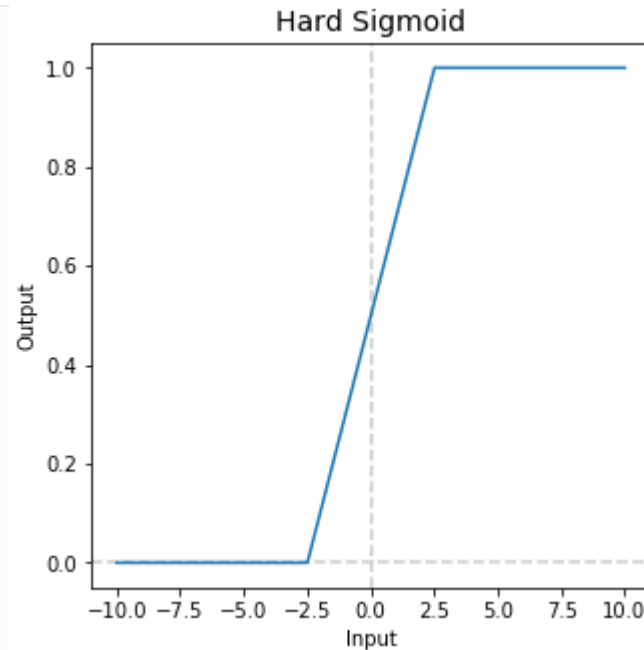
Arguments

- x: Input tensor.

Returns

Hard sigmoid activation:

- 0 if $x < -2.5$
- 1 if $x > 2.5$
- $0.2 * x + 0.5$ if $-2.5 \leq x \leq 2.5$.



Kaynak: <https://keras.io/activations/>

Kaynak: <https://towardsdatascience.com/deep-study-of-a-not-very-deep-neural-network-part-2-activation-functions-fd9bd8d406fc>

Aktivasyon fonksiyonları

softplus

```
keras.activations.softplus(x)
```

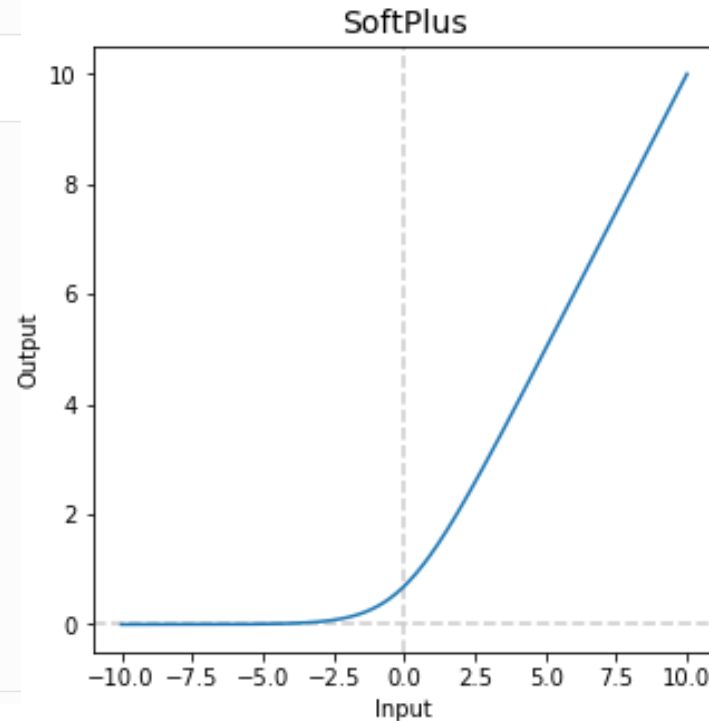
Softplus activation function.

Arguments

- **x**: Input tensor.

Returns

The softplus activation: $\log(\exp(x) + 1)$.



Kaynak: <https://keras.io/activations/>

Kaynak: <https://towardsdatascience.com/deep-study-of-a-not-very-deep-neural-network-part-2-activation-functions-fd9bd8d406fc>

Aktivasyon fonksiyonları

softsign

```
keras.activations.softsign(x)
```

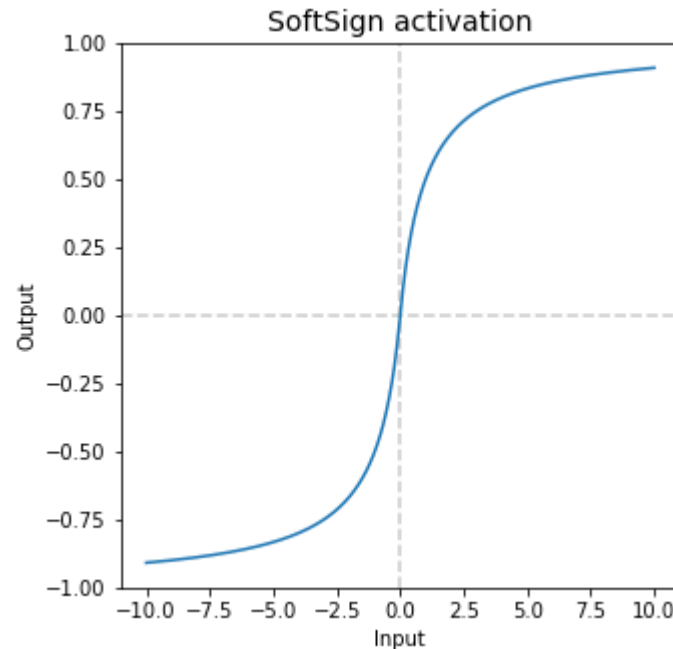
Softsign activation function.

Arguments

- **x**: Input tensor.

Returns

The softsign activation: $x / (|x| + 1)$.



Kaynak: <https://keras.io/activations/>

Kaynak: <https://towardsdatascience.com/deep-study-of-a-not-very-deep-neural-network-part-2-activation-functions-fd9bd8d406fc>

Kaynak: <https://keras.io/activations/>

Aktivasyon fonksiyonları

exponential

```
keras.activations.exponential(x)
```

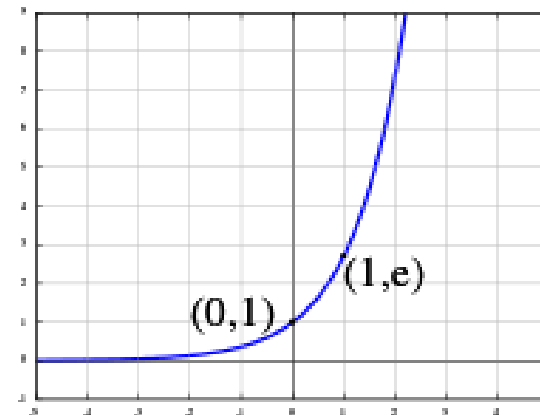
Exponential (base e) activation function.

Arguments

- x: Input tensor.

Returns

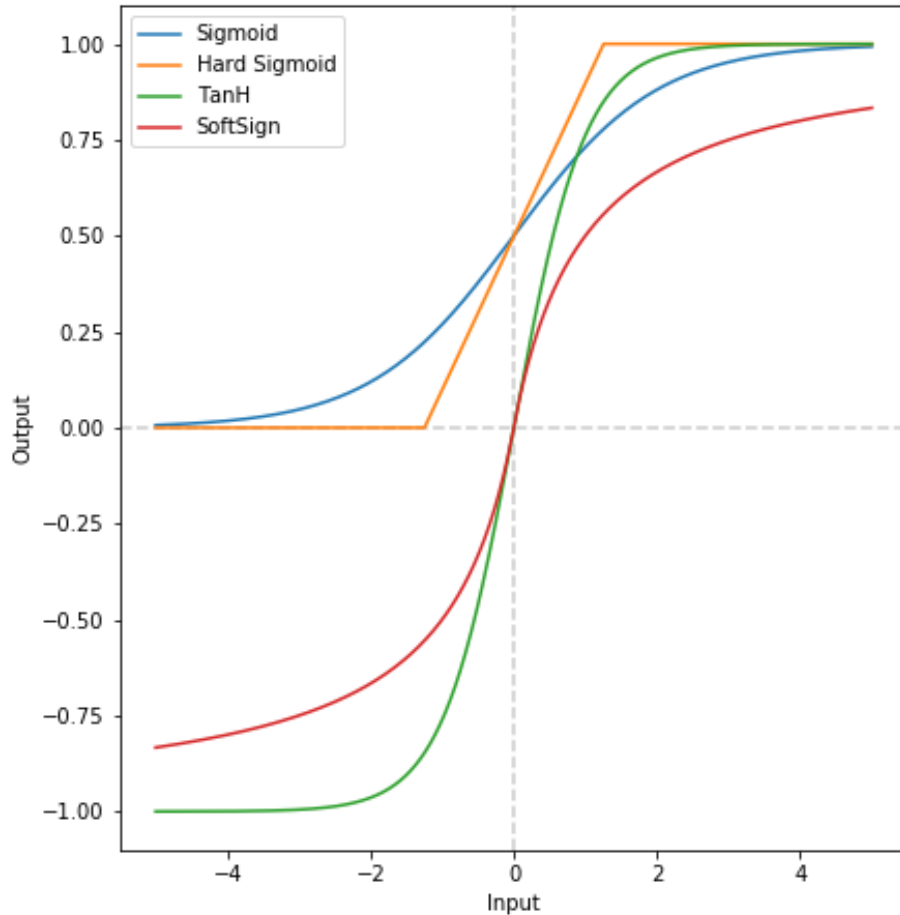
Exponential activation: $\exp(x)$.



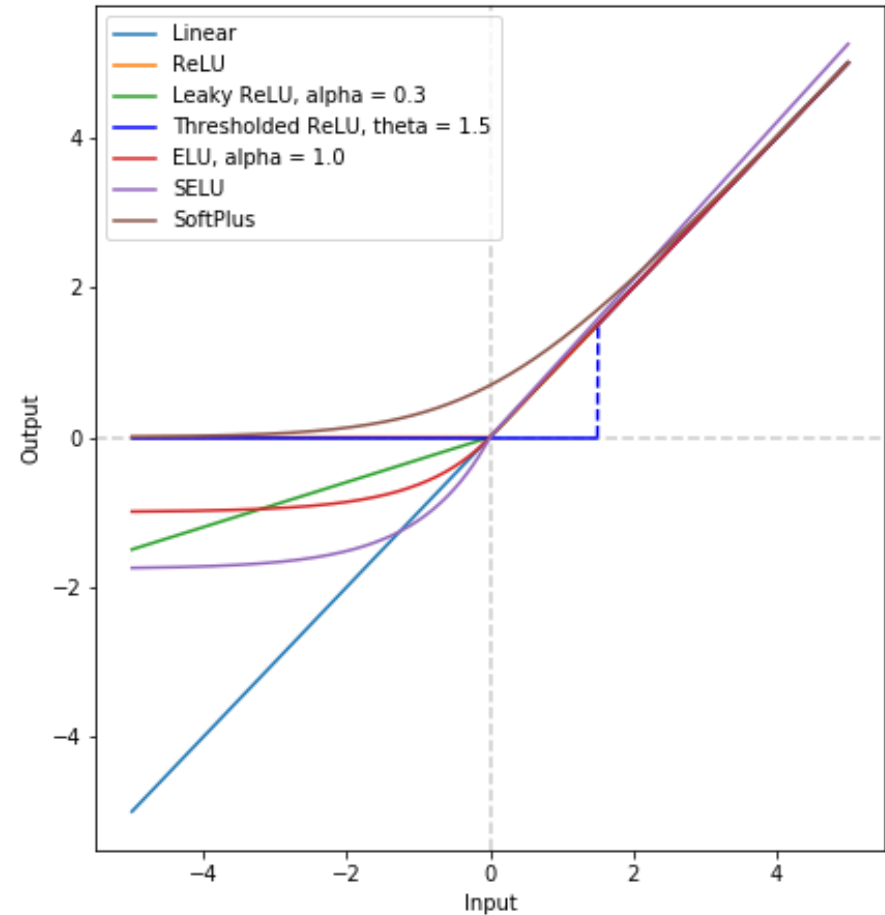
Aktivasyon fonksiyonları

Comparing activation functions

Sigmoid-like activations



Linear and Rectified activations



Applying Neural Networks

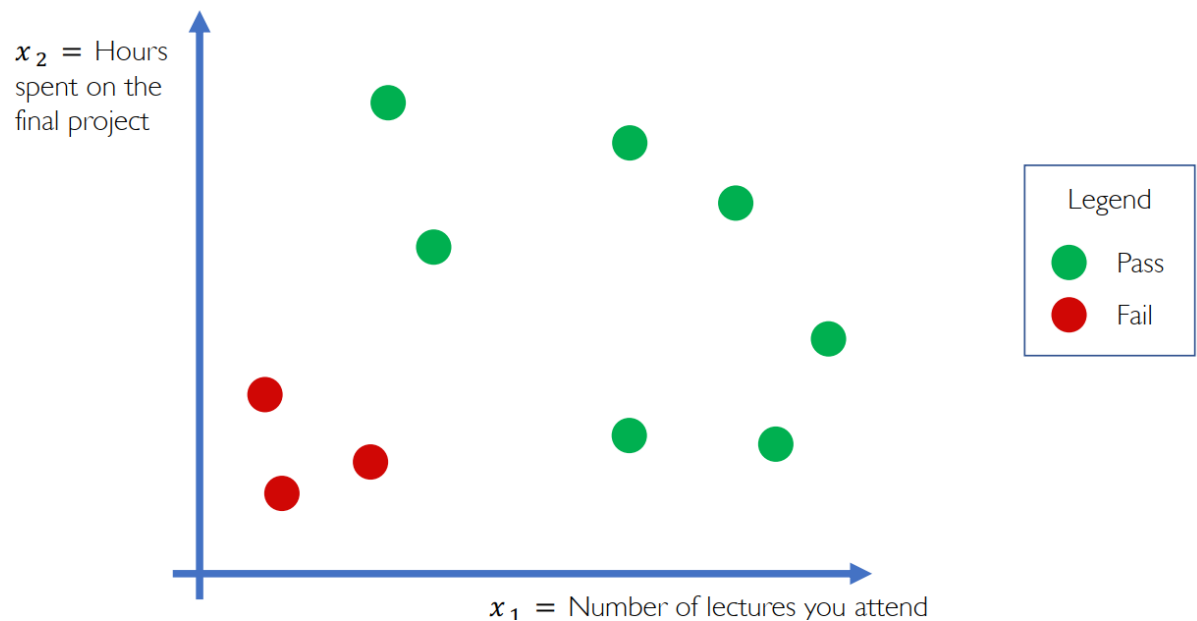
Example Problem

Will I pass this class?

Let's start with a simple two feature model

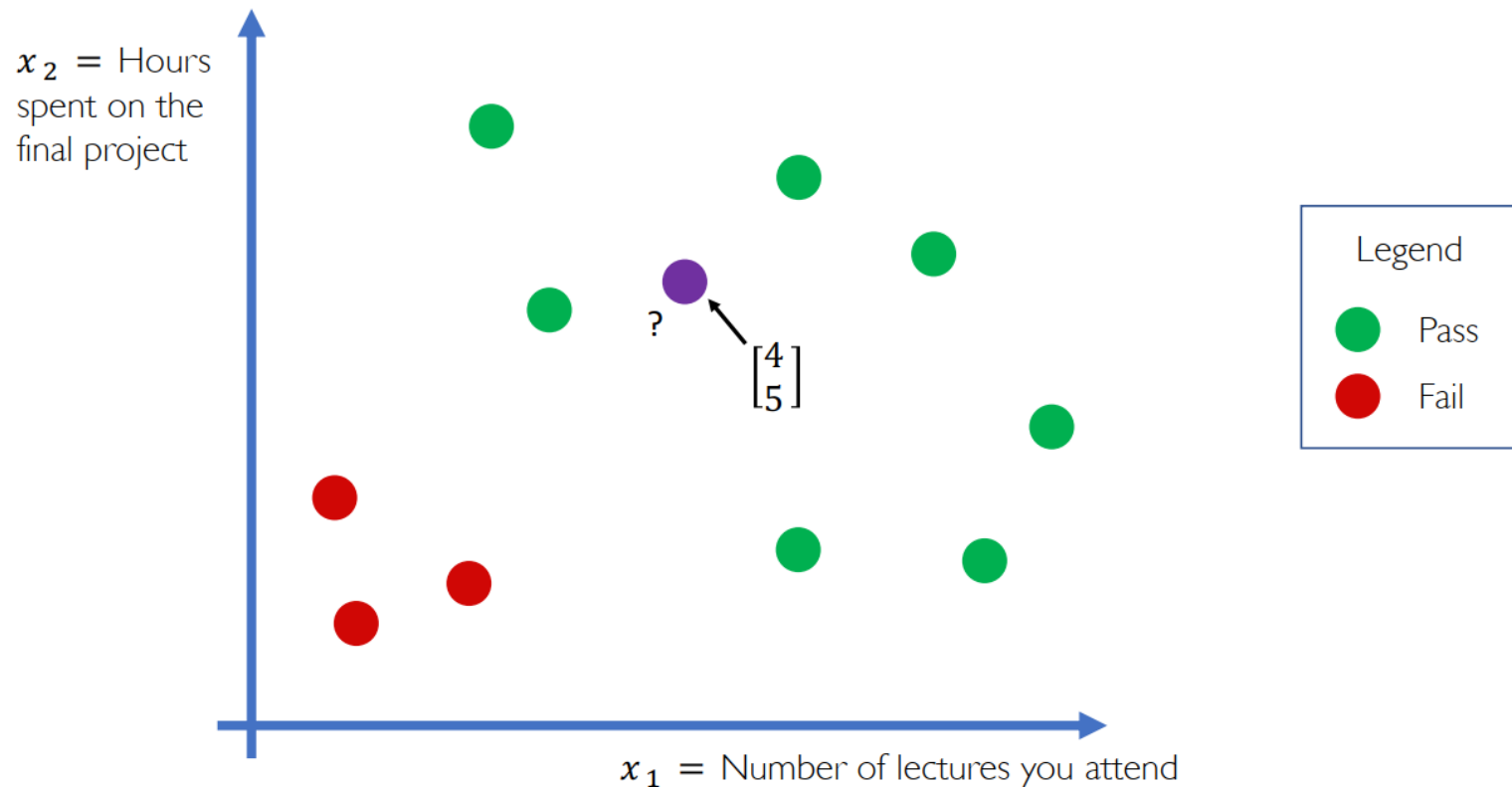
x_1 = Number of lectures you attend

x_2 = Hours spent on the final project

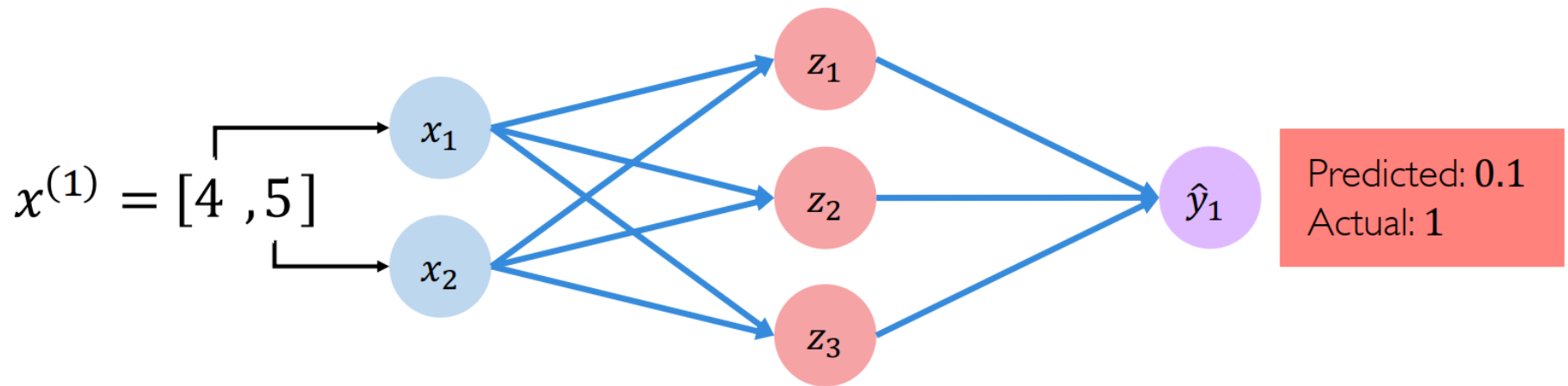


Applying Neural Networks

Example Problem: Will I pass this class?

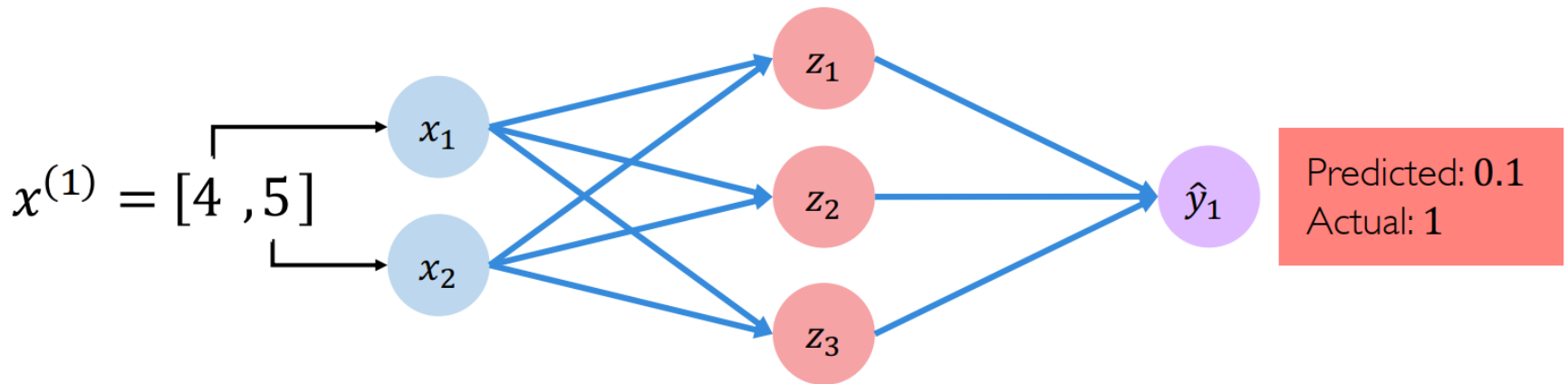


Applying Neural Networks



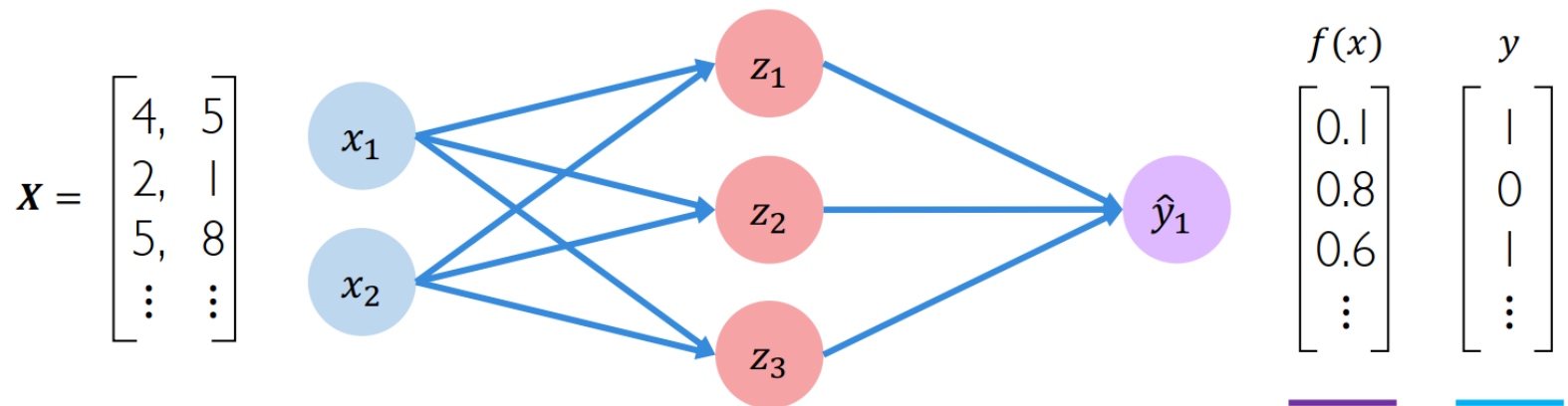
Quantifying Loss

The **loss** of our network measures the cost incurred from incorrect predictions



$$\mathcal{L}(\underbrace{f(x^{(i)}; \mathbf{W})}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}})$$

The **empirical loss** measures the total loss over our entire dataset



- Also known as:
- Objective function
 - Cost function
 - Empirical Risk

$$J(\mathbf{W}) = \frac{1}{n} \sum_{i=1}^n \mathcal{L}(\underbrace{f(x^{(i)}; \mathbf{W})}_{\text{Predicted}}, \underbrace{y^{(i)}}_{\text{Actual}})$$