

$$b) a_n = 1 + (-1)^n$$

BASE CASE: $a_1 = 0$

RECURSIVE CASE: $a_{n+1} = a_n + ?$

$$\begin{aligned} a_{n+1} &= 1 + (-1)^{n+1} \\ &= 1 + (-1)^n (-1) \\ &= 1 + (((-1)^n + 1) - 1) (-1) \\ &= 1 + (a_n - 1) (-1) \\ &= \boxed{2 - a_n} \end{aligned}$$

$$c) a_n = n(n+1)$$

base case: $a_1 = 2$

$a_{n+1} = a_n + ?$

$? = a_{n+1} - a_n$

$$\begin{aligned} &= (n+1)(n+1+1) - n(n+1) \\ &= (n+1)(n+1) + n+1 - n^2 - n \\ &= n^2 + 2n + 1 - n^2 + 1 \\ &= 2n + 2 \end{aligned}$$

$$\boxed{a_{n+1} = a_n + 2n + 2}$$

$$d) a_n = n^2$$

BASE CASE: $a_1 = 1$

RECURSIVE CASE: $a_{n+1} = a_n + ?$

$$\begin{aligned} ? &= a_{n+1} - a_n = (n+1)^2 - n^2 = n^2 + 2n + 1 - n^2 \\ &= 2n + 1 \end{aligned}$$

$$\boxed{a_{n+1} = a_n + 2n + 1}$$