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Operator Precedence Grammar

① ~~∅~~ You cannot have two non-terminal consecutively in RHS.

② ~~∅~~ It cannot have ϵ production.

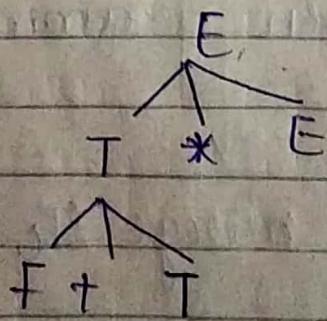
$$E \rightarrow TF(X)$$

$$E \rightarrow \epsilon(X)$$

Eg:-

$$\begin{array}{l} E \rightarrow T * E \\ T \rightarrow F + T \\ F \rightarrow id \end{array}$$

→ The operator that appears on the lower level have higher precedence.



So here $+$ has more precedence than $*$.

Associativity of $*$ is Right
" " $+$ is "

④ size of operator precedence grammar
 $= (\# \text{ terminals} + 1)^2$

		id	+	*	\$	\Rightarrow (Input)
↑ (stack)	id	> noti.	>	>	>	
	+	<	>	<	>	
	*	<	>	>	>	
	\$	<	<	<	accept	

table
 This is drawn
 accordingly
 to bodmas

→ Precedence of + in stack > + is Input

→ Precedence of \$ is the least

→ Precedence of id is the greatest

→ Comparison of operator is always depend on grammar.

$$\begin{array}{l}
 \text{Q} \\
 \hline
 \begin{array}{l}
 A \rightarrow B * A \mid B \\
 B \rightarrow B + C \mid C \\
 C \rightarrow D / C \mid D \\
 D \rightarrow \text{id}
 \end{array}
 \end{array}$$

	*	+	/	id	\$
*	<		<	<	>
+	>	>	<	<	>
/	>	>	<	<	>
id	>	>	>	nothing	>
\$	<	<	<	<	accept

Precedence for this table:-

$$id > / > + > * > id.$$

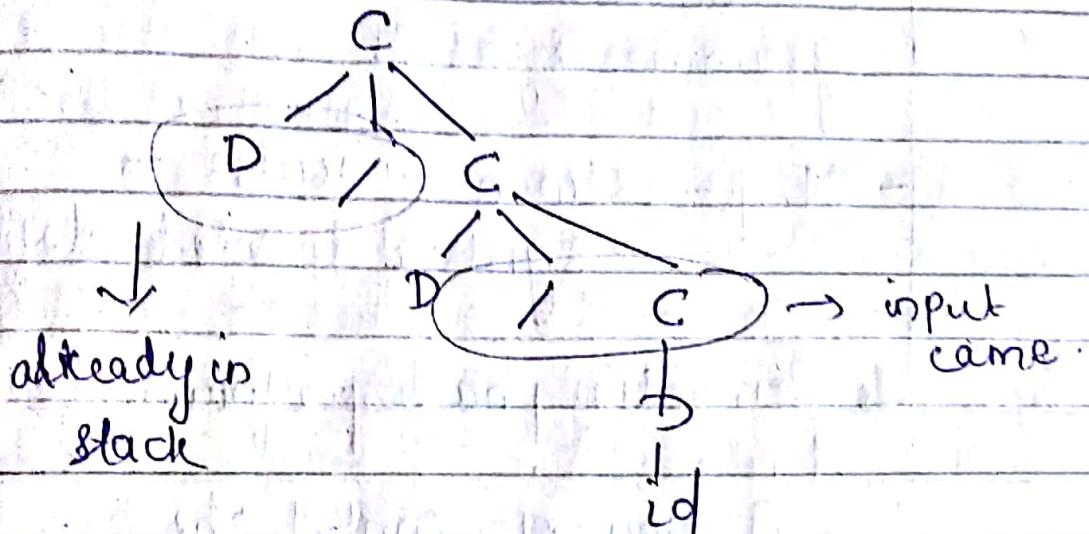
→ Associativity is necessary when we have same operator in the stack if input.

→ When right associative, we have to first shift i.e., we have to give precedence to the incoming operator (input).

→ When left associative, we have to first reduce i.e., we have to give precedence to the operator.

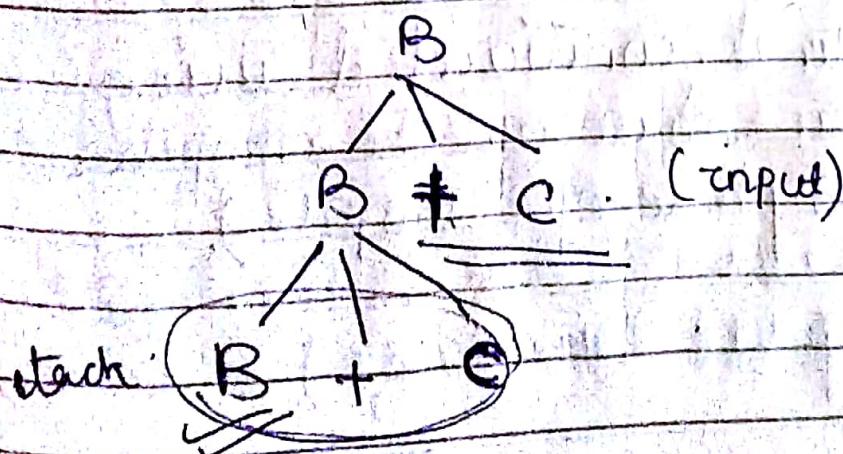
already in stack.

Here / is right associative.



So first we will evaluate input then stack. (first shift then reduce).

Here + is left associative.



So first we will evaluate stack then input. (first reduce then shift).

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Semantic Analysis

- attributes are attached to the grammar symbols
- $CFG + \text{semantic rules} =$
syntax directed definition

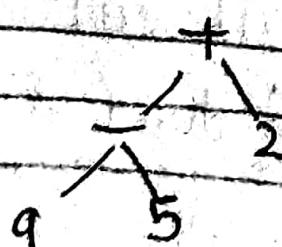
→ Semantic phase performs following tasks:-

- (1) Flow-of - Control check.
- (2) Type Check
- (3) Scope resolution
- (4) Array out of bound check

* Symbol table is constructed using the analysis phase of the compiler (ie, first 3 phase of compiler).

Abstract Syntax Tree (AST)

$9 - 5 + 2$



→ It hides the implementation part & just gives the overview struct.

Semantic errors:-

- ① Type mismatch.
- ② Accessing an out of scope variable.
- ③ Formal & Actual parameter mismatch.
- ④ Undeclared variable.
- ⑤ Multiple declaration of a variable in a scope.

Synthesized Attributes :

$S \rightarrow ABC$ attribute /
→ The node can take value only by its children or node.

Inherited attributes :

→ node can take the value from parent, its siblings and the node itself.

$S \rightarrow ABCS$.

$E_1 : E \rightarrow E + T$

We write attribute as $E \cdot val$.

$$E \cdot val = E_0 \cdot val + T \cdot val.$$

* Here $\cdot val \rightarrow$ represent the attribute attached with that node.

Here we have written E_1 just to differentiate that E can take value from someone else (which is E itself).

S-attributed SDT.

- ① uses only synthesized attribute
- ② bottom-up parsing.
- ③ semantic rules are present at the end.



$$E \cdot val = E \cdot val \parallel T \cdot val \parallel \{ \}$$

semantic rules
written at the
end.

L-attributed SDT

- ① uses synthesized attributes
- ② uses inherited attributes but with the restriction that node cannot take value from its right sibling
- ③ Depth-first order and left-to-right parsing

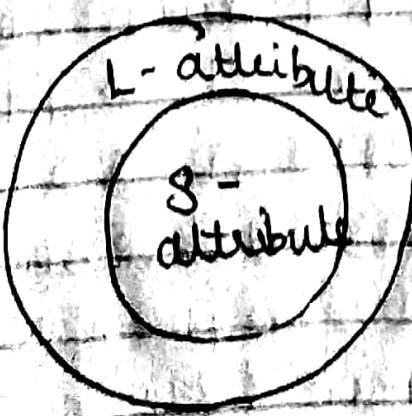
$S \rightarrow ABC$

A can only take value from S

B can only take value from S & A

C " " " " " " " " " " S, A and B

→ S can take value from ABC



SDD → Syntax directed definition

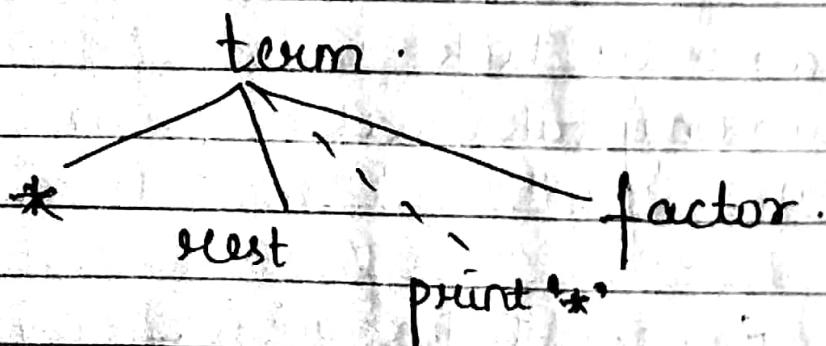
SDT → " " " " " " " " " " translation

semantic

In SDT, ~~attribute~~ rules can come in b/w but in SDD it always come in last.

→ In SDT we have to attach a different node for semantic rule as follow:-

term → * rest { print '*' } factor



→ Till now we have ~~been~~ been writing as $E \rightarrow T + E$ but now in SDD and SDT we are writing ~~and~~ attributes along with the flow of information in the parse tree.

Type checking

$E \rightarrow E_1 + E_2 \{ \text{if } (E_1.\text{type} == E_2.\text{type}) \& \& (E_1.\text{type} == \text{int}) \text{ then}$

$E \cdot \text{type} = \text{int}$
else
 error (" ");

$E \rightarrow (E_1) \{ E \cdot \text{type} = E_1 \cdot \text{type} \}$

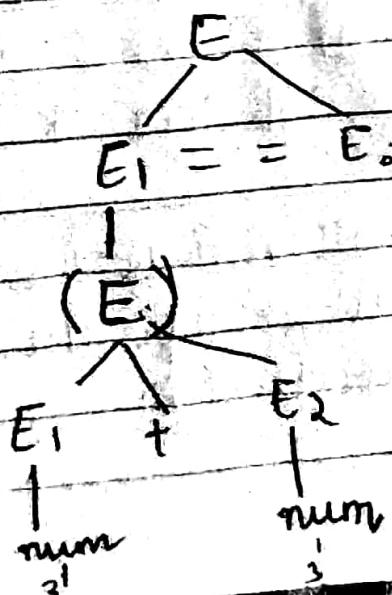
$E \rightarrow E_1 == E_2 \left\{ \begin{array}{l} \text{if } (E_1 \cdot \text{type}) == (E_2 \cdot \text{type}) \\ \& \& (E_1 \cdot \text{type} == \text{int} / \text{bool}) \\ \text{then } E \cdot \text{type} = \text{boolean} \\ \text{else error (" ")}; \end{array} \right.$

$E \rightarrow \text{num} \{ E \cdot \text{type} = \text{num_type} \}$

$E \rightarrow \text{true} \{ E \cdot \text{type} = \text{boolean} \}$

$E \rightarrow \text{false} \{ E \cdot \text{type} = \text{boolean} \}$

Eg:- $(3+2) == 6$



(Something like this
will be drawn,
not exactly)

↑ info. will flow
from bottom to up

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Tutorial

Ambiguous Grammar

$$E \rightarrow E+E \mid E * E \mid a$$

Resolve Ambiguity

(Operator grammar)

There will come a state,

$$\begin{aligned} E &\rightarrow E+E \\ E &\rightarrow E\cdot+E \\ E &\rightarrow E\cdot * E \end{aligned}$$

In Normal, there will be S/R conflict for SLR.

but for first Prod \rightarrow Reduce
and Prod \rightarrow Shift

R/S conflict

As + is left associative so we will perform reduce.

Similarly there is a S/R for *

As * precedence is higher
so shift will perform first
and then reduction

Similarly

$$E \rightarrow E * E$$

$$E \rightarrow E + E$$

$$E \rightarrow E \cdot E$$

Here also for + we have a S/R conflict.
As * precedence is higher than +,
we will perform reduce.

For * there is also a conflict, and
* left associative so we will
perform reduce first.

→ So generally for SLR we have
S/R conflict but if we associate
operators operations then this can
be resolved.

→ When we cannot tell from the grammar
its associativity so we will use assumption
(BODMAS).

$$S \rightarrow iSe.S | iS | a$$

$$\begin{aligned} S &\rightarrow iS \cdot eS \\ S &\rightarrow iS \cdot \end{aligned}$$

Here also
we have a S/R
conflict.

* We generally give shift more importance
than reduce, so we will do shift here.

→ This is not an operator grammar,
ie, dangling if statement so here
Shift & has higher precedence
than reduce.

Q) Because our objective is to take
the higher length input so we perform
shift operation.

* There are different methods to cope
up errors

We
will
study

this
part
later
(Not
for
error)

① panic error → as soon as it
come leave ~~everything~~

② Statement error → If at a partial
input ^{character} error comes then we leave
some input character till the
error is gone.

③ Pop every element from the stack
and then start from that particular
I/P character ~~and~~ where there is
no error.

Annotated Parse Tree

A parse tree showing attribute value at each node

$E \cdot \text{type} = \text{boolean}$

$E_1 \cdot \text{type} = \text{int}$

$= =$

$E_2 \cdot \text{type} = \text{int}$

$(E \cdot \text{type} = \text{int})$

6

$E \cdot \text{type} = +$

int

$E_2 \cdot \text{type} = \text{int}$

2

3.

$$(3 + 2) = 6$$

$$(3 = 6) + 2$$

E
 $E_1 + E_2$
(boolean) (integer)

base (E)

2.

$E_1 = E_2$
3 6

Type Equivalence :

Structural equivalence

Name equivalence

Structural equivalence

under naming

struct type 1 { int a ; int b ; } ;

struct type 2 { int c ; int d ; } ;

struct type 3 { int a ; int b ; } ;

→ In structural equivalence, structure should be same ~~and~~ (basic type) and number of components.

So in the above example all three → are structural equivalence.

→ 1 & 3 are structural equivalence under naming (structure is same and the name of components same).

→ In name equivalence → structure

can be different but name should be same.

Eg:- struct type 1 { int a ; int b ; }

array type 1

name
same .

Type Conversion

Type conversion ← Implicit

Explicit

(Eg:- upgrading
int to float
and then perform
operations).

Eg:- changing
int to
char

(there will
be loss of
information)

(changing char to int,
there will be no loss
of information).

Eg:-
S → axw { print('1') }
 S → y { print('3') }
 W → Sz { print('2') } y .

I/P = axwxyz .

Bottom - Up Parser

O/P

3 2 1 2 1

x x x x y z z

x x x x S z z

x x x x w z z

x x x x S z z

x x x x w z z

x x x x S z z

x x x x w z z

x x x x S z z

x x x x w z z

x x x x S z z

S

↑

mx w

mx S z

1
2

1

2

3

Top - Down

O/P

3 2 1 2 1

x x x x y z z

x x x x S z z

x x x x w z z

x x x x S z z

S

—
x x w

print(1) ;

—
x x z

print(2) ;

—
x x w

print(1,y);

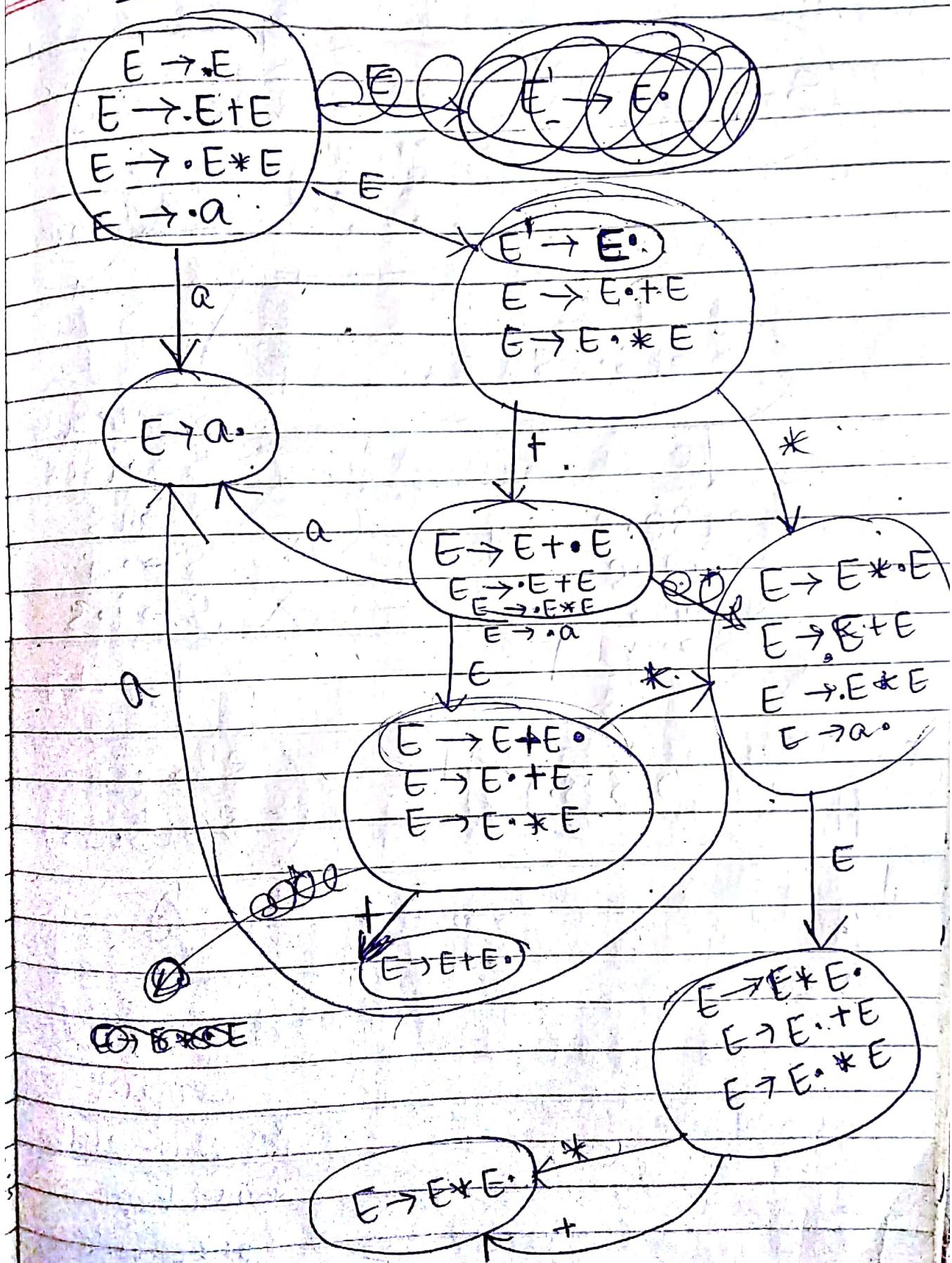
—
x x z

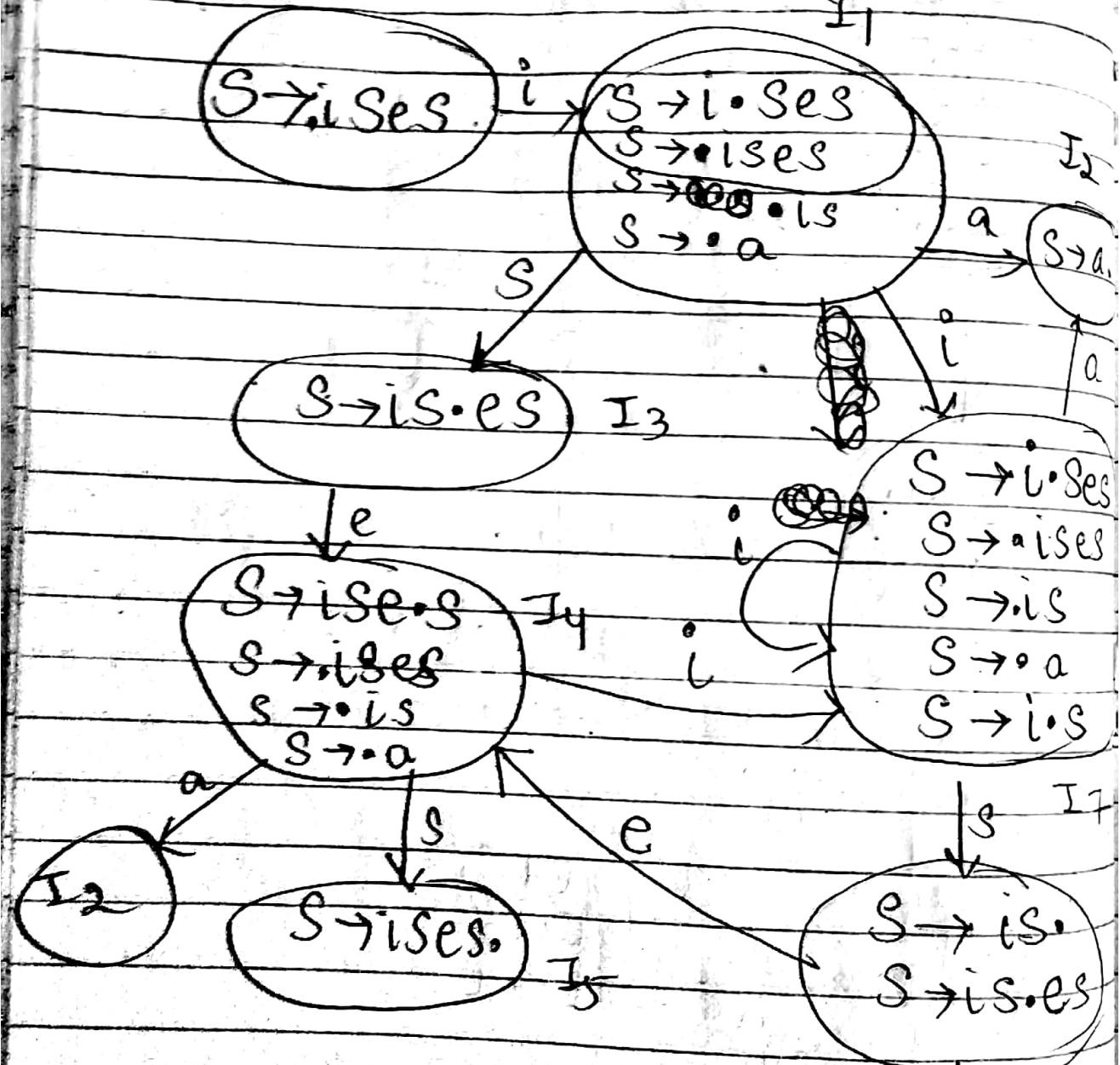
print(2);

—
x y z

print(3,y);

Tutorial Ques:





Shift reduce conflict
 so shift will have high precedence over reduce

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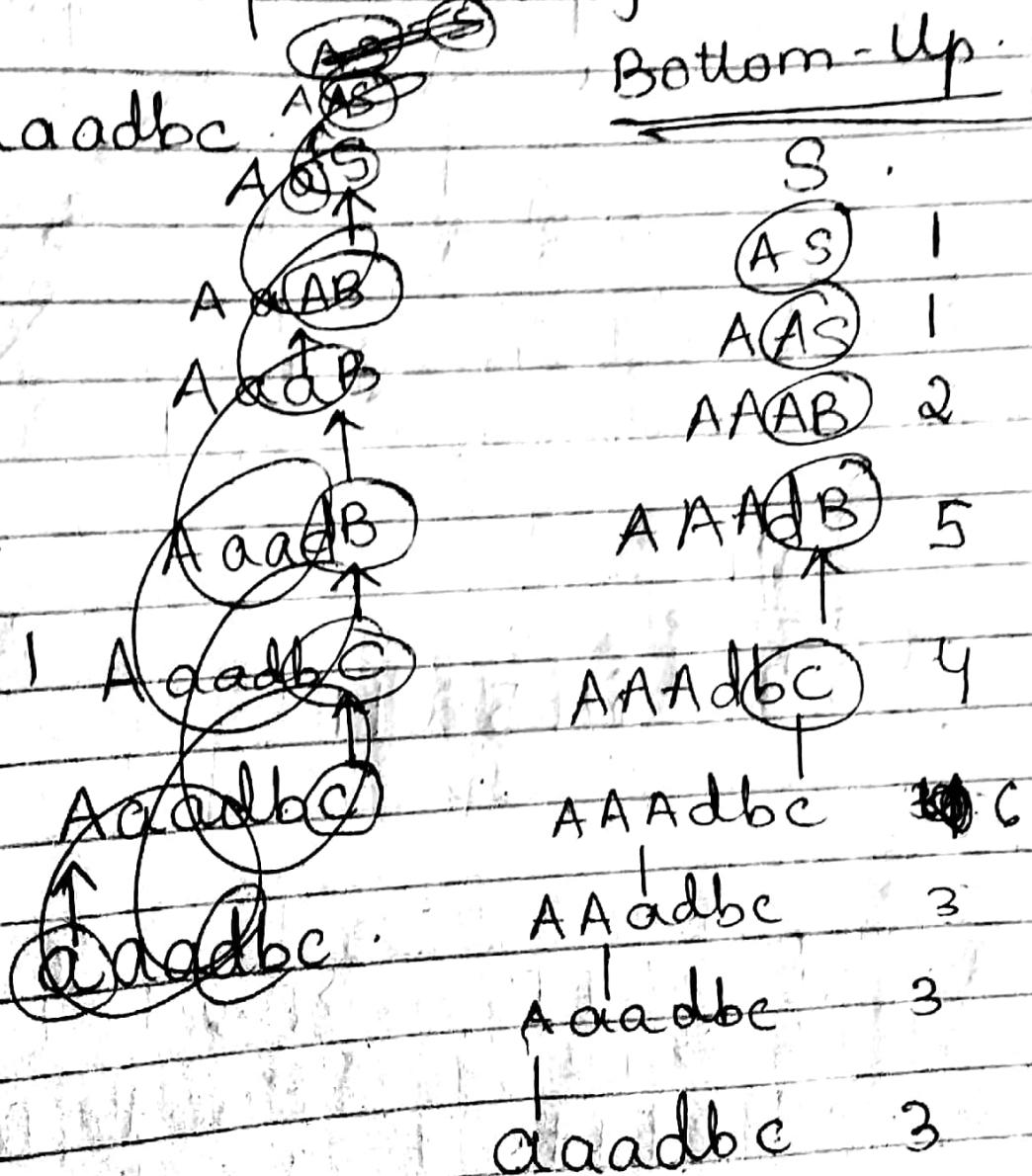
<u>S</u>	$S \rightarrow AS$	{ print ("1") }
	$S \rightarrow AB$	{ print ("2") }
	$A \rightarrow a$	{ print ("3") }
	$B \rightarrow bC$	{ print ("4") }
	$B \rightarrow dB$	{ print ("5") }
	$C \rightarrow c$	{ print ("6") }

Bottom-Up

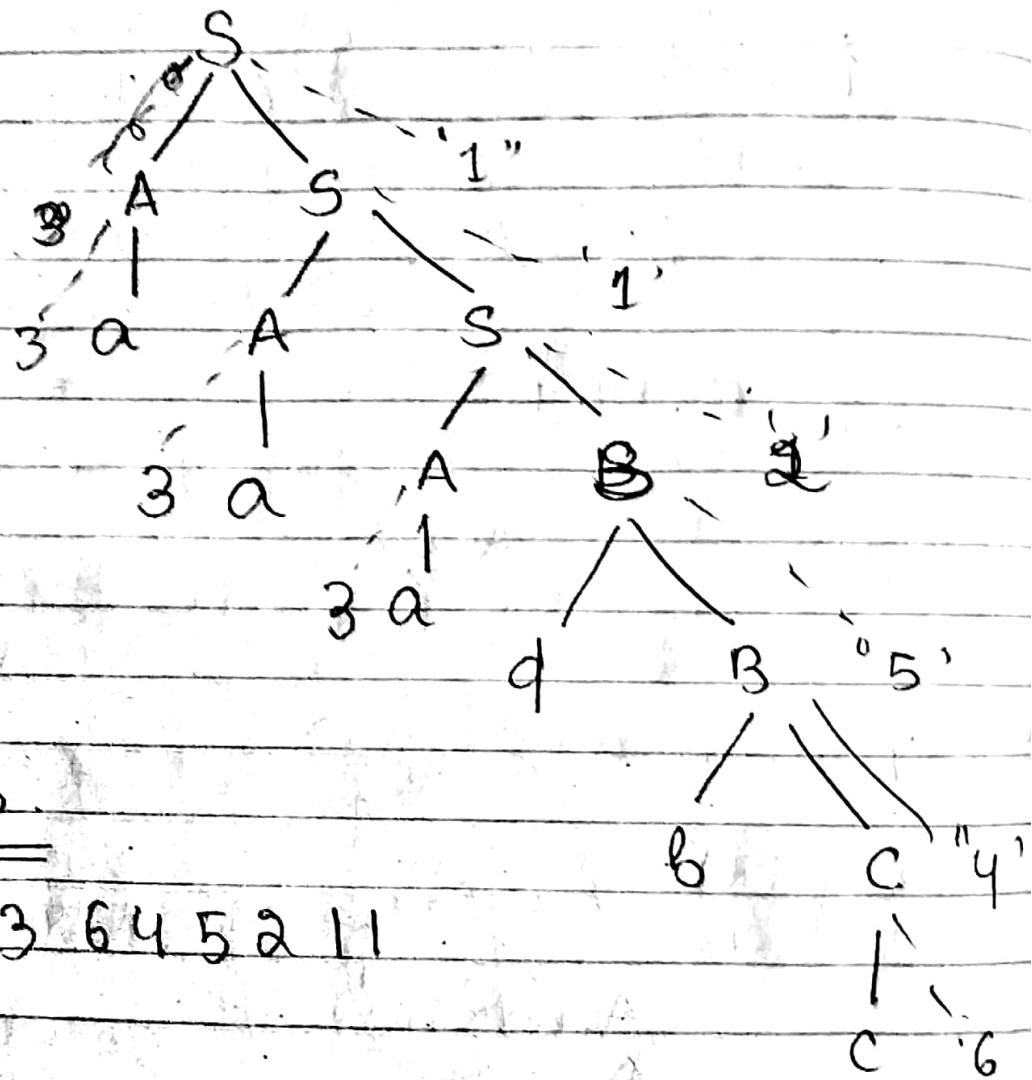
I/P caadbc

O/P =

33 3645211

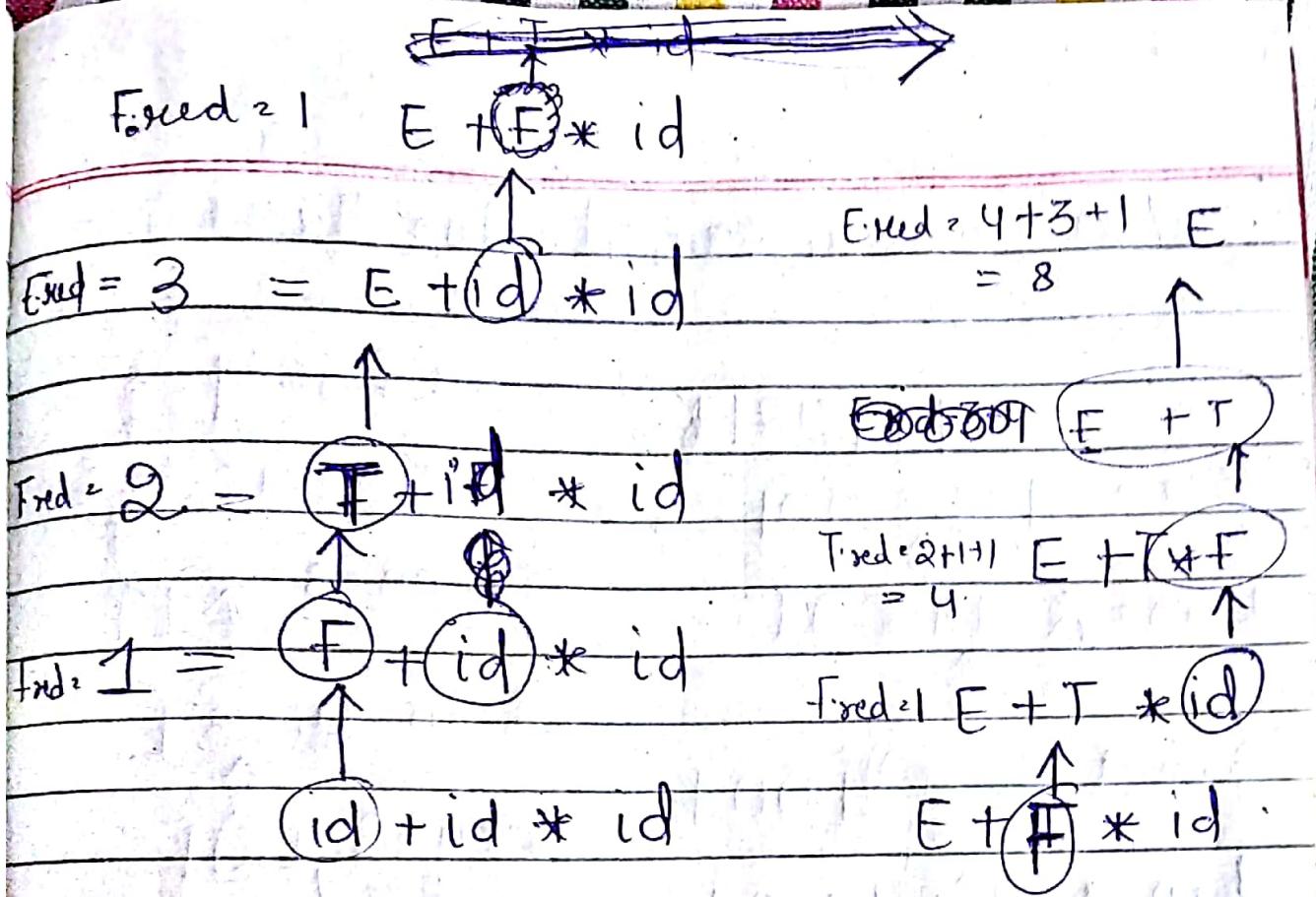


Top down



$E \rightarrow E + T$	$\{E \cdot \text{red} = E \cdot \text{red} + T \cdot \text{red} + 1\}$
$E \rightarrow T$	$\{E \cdot \text{red} = T \cdot \text{red} + 1\}$
$T \rightarrow T * F$	$\{T \cdot \text{red} = T \cdot \text{red} + F \cdot \text{red} + 1\}$
$T \rightarrow F$	$\{T \cdot \text{red} = F \cdot \text{red} + 1\}$
$F \rightarrow \text{id}$	$\{F \cdot \text{red} = 1\}$

Q Calculate the no. of reductions used in the parsing of "id + id * id".

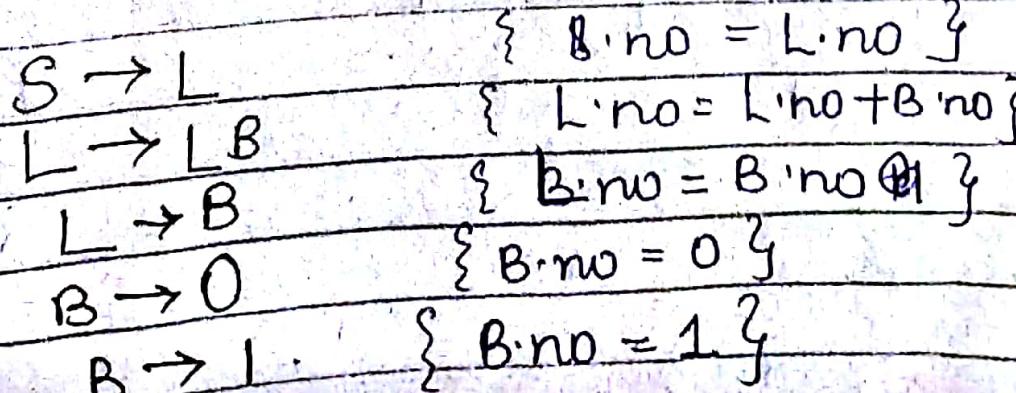


We have used 8 reductions.

Now we will perform reduction using semantic rules. \rightarrow we are getting 8 reductions.

Ans
 \because This is S-attributed SDT.

Q Draw SDT to count the no. of 1's in the grammar :-



Also give an example for the same.

111001
B.no = 1 LB 001

L.no = 2 L 1 001

B.no = 1 L(B) 1 001

B.no = 1 L(1) 1 001

B.no = 1 B 1 1 001

00001 1 0 1 0 0 1 1

L.no = 4 L

B.no = 1 LB

L.no = 3 L 1

B.no = 1 LB 1

L.no = 3 L 0 1

B.no = 0 LB 0 1

L.no = 3 L 0 0 1

LB 0 0 1

Total number of 1's = 4.

According to annotated parse tree
no. of 1's = 4.

101 S=2 01

L=2 B=1

T=L G=0

1-B 0

S=1 ✓

L=1

O=L B=1

O-B 1

Annotated parse tree can be bottom-up & top-down. But preferably draw top-down.

