

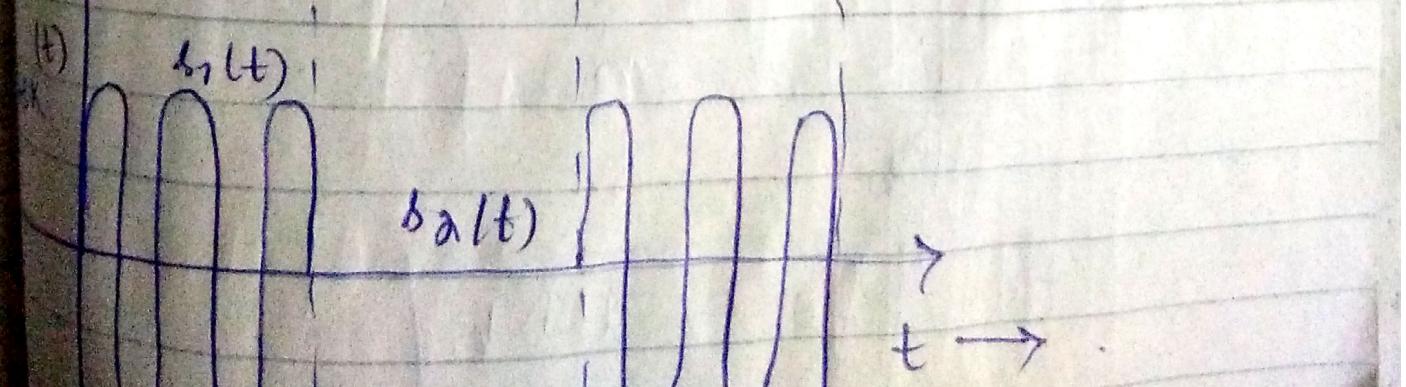
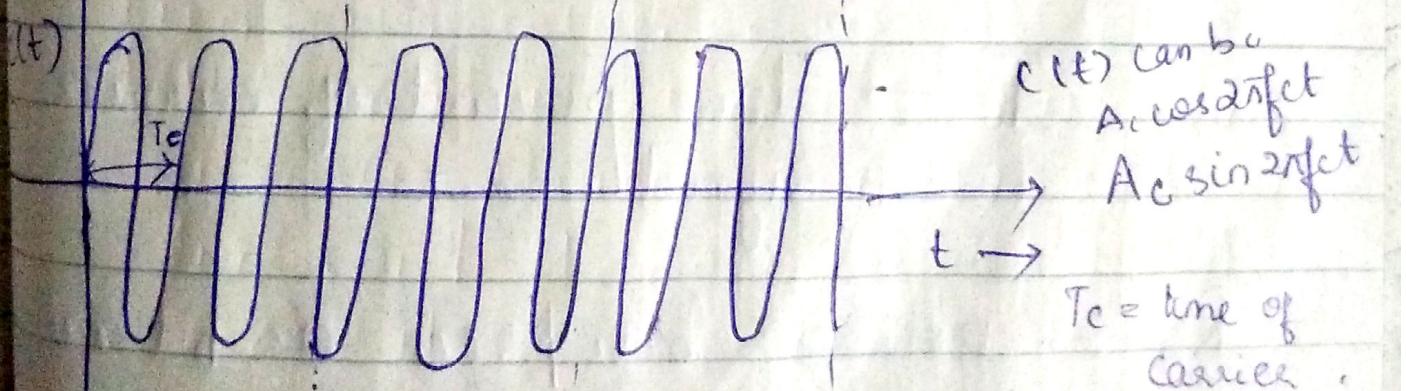
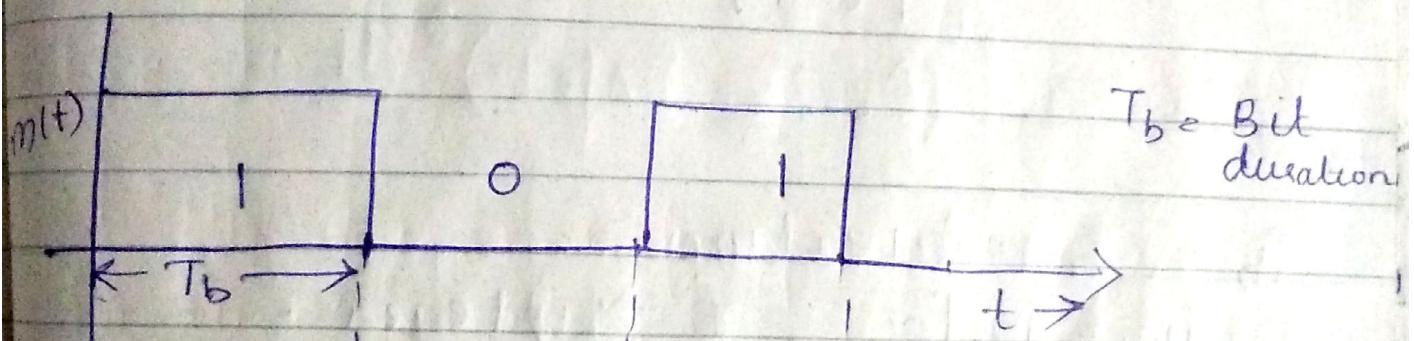
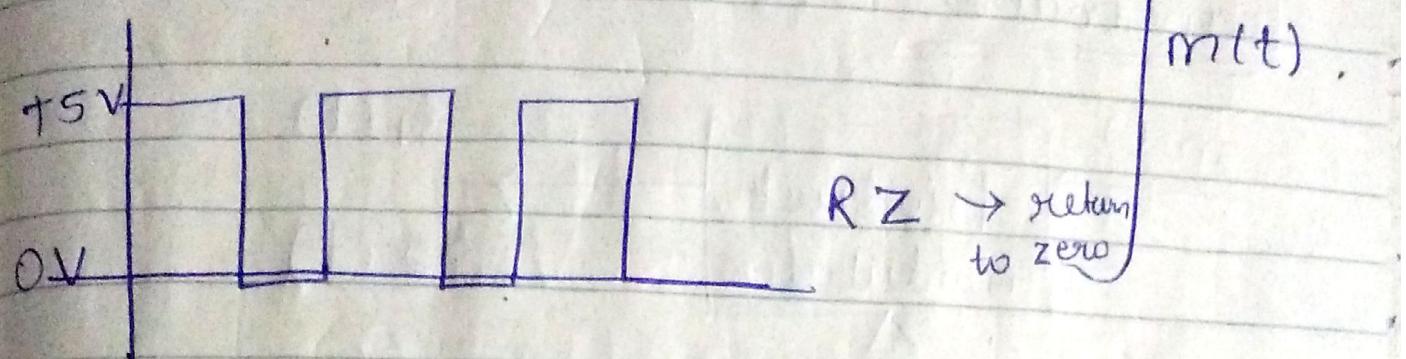
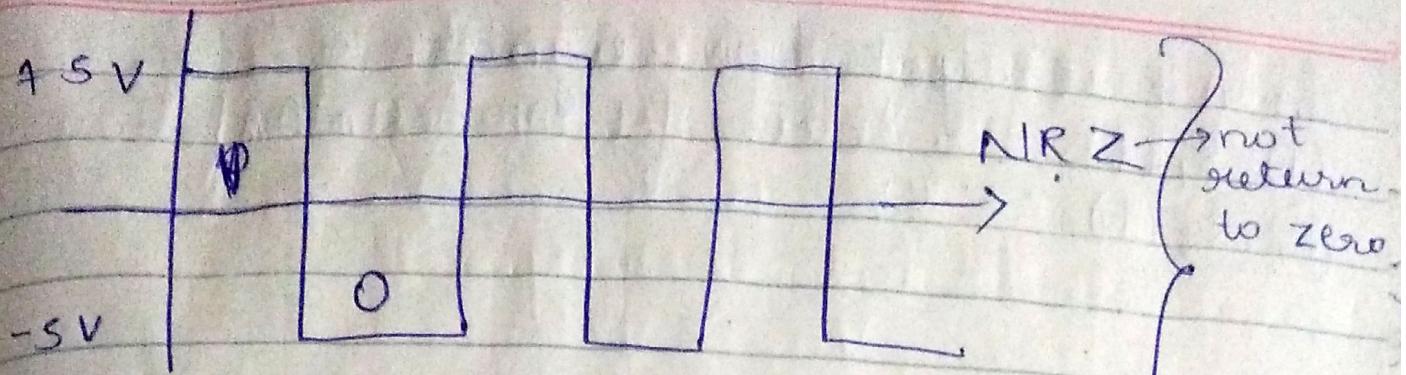
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In the wire communication the technique of modulation are:-  
PCM, DPCM, DM, ADM.

In wireless communication, the technique of modulation are:-  
ASK, FSK, PSK, QPSK

### Binary Signalling Schemes

ASK, PSK and FSK ~~signalling~~ <sup>scheme</sup> are used to transmit digital signal through free space schemes.  
In this ~~keeping~~ one bit is transmitted in a specific time in a specific time instant through free space.

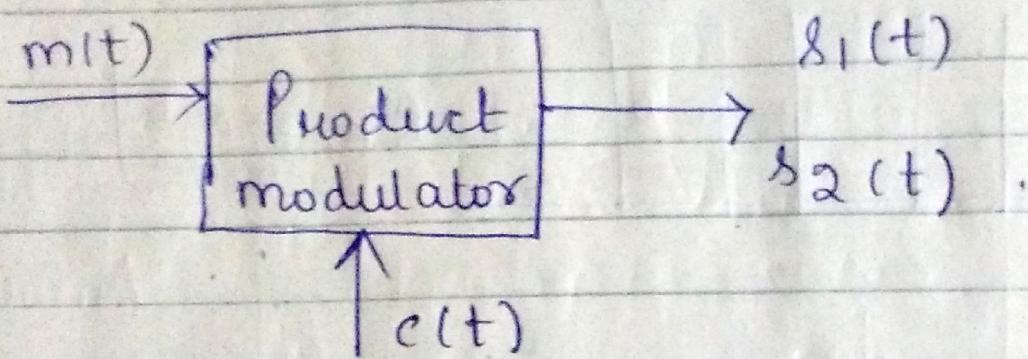
In this schemes one of the parameter of the carrier sig will be switched b/w two possible values as the message sig switches b/w 2 possible voltages so these schemes are called as signalling or switching or keying.



In ASK we got two signals -

- ①  $s_1(t) = A_c \cos 2\pi f_c t$  or  $A_c \sin 2\pi f_c t$   
②  $s_2(t) = 0$

## Transmitter



$T_b$  = bit duration

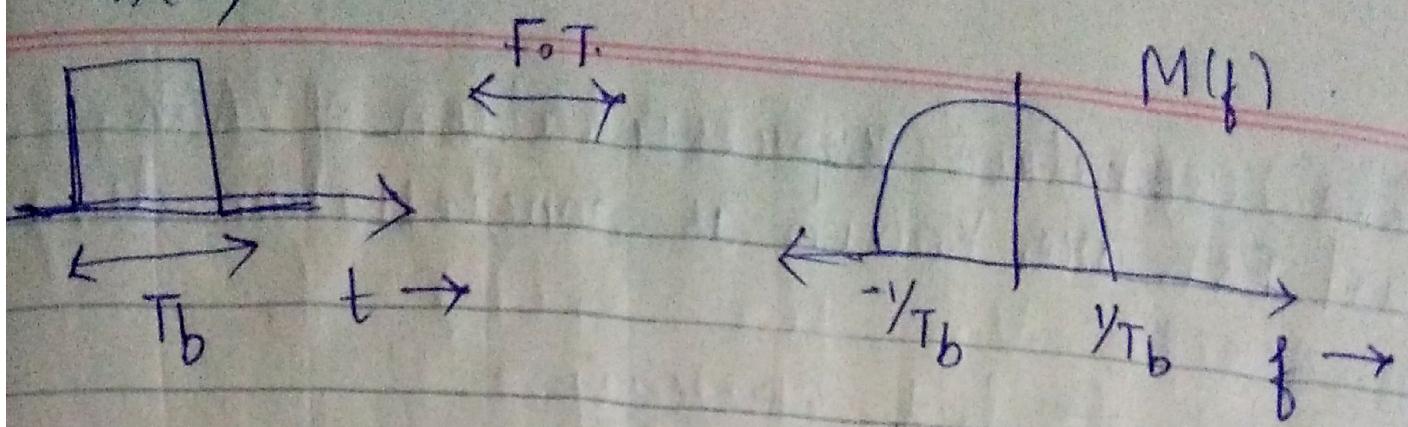
$T_b = n T_c$      $n \rightarrow$  integer .

$T_c \rightarrow$  Time period of carrier signal

$R_b \rightarrow$  no:- of bits / sec or bit rate

$$\rightarrow \frac{1}{R_b} = \frac{n}{f_c}$$

$$\rightarrow \boxed{f_c = n R_b}$$

$m(t)$ 

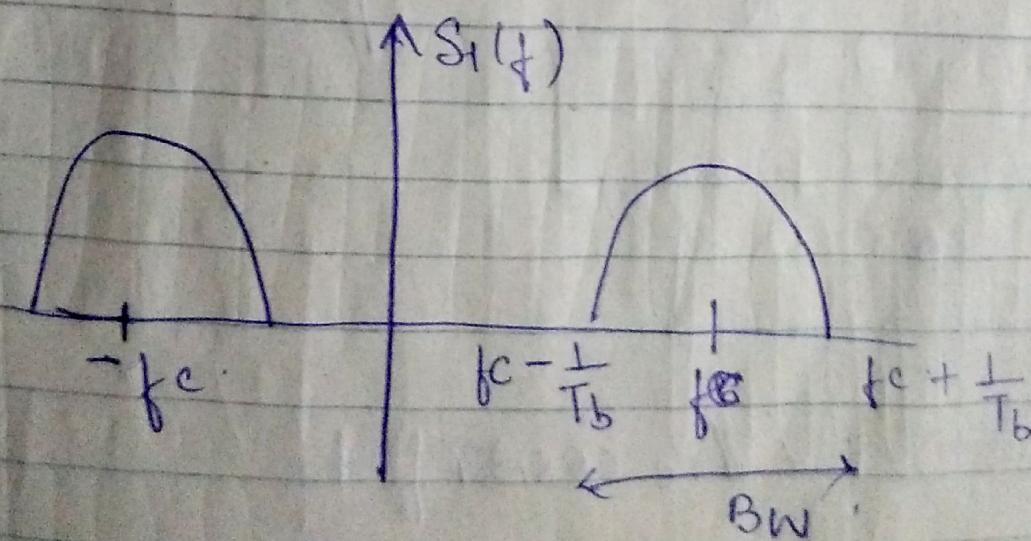
$$s(t) = c(t) m(t)$$

$$s(t) = A_c \cos 2\pi f_c t \cdot m(t)$$

$$= \frac{A_c}{2} [e^{j2\pi f_c t} + e^{-j2\pi f_c t}] \cdot m(t)$$

$$S(f) = \frac{A_c}{2} [M(f-f_c) + M(f+f_c)]$$

$$S_1(f) = S(f) ; \quad S_2(f) = 0$$



$$B_W = \frac{2}{T_b} = 2 \cdot R_b$$

The geometric representation of ASK, FSK and PSK are known as constellation diagram

For ASK:

$E_b \rightarrow$  bit energy

$$s_1(t) = A_c \cos 2\pi f_c t$$

$$s_2(t) = 0$$

$$E_b = \int_{-\infty}^{\infty} x^2(t) dt$$

$$= \int_0^{T_b} (A_c \cos 2\pi f_c t)^2 dt$$

For 1,

$$E_{b1} = \frac{A_c^2}{2} (T_b)$$

For 0,

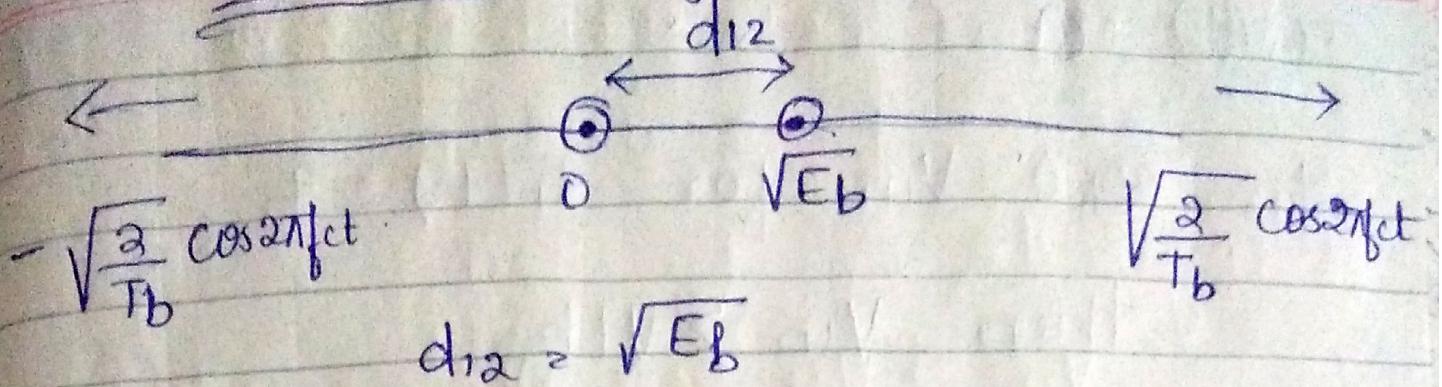
$$E_b = 0$$

$$s_1(t) = A_c \cos 2\pi f_c t$$

$$= \sqrt{\frac{2 E_b}{T_b}} \cos 2\pi f_c t$$

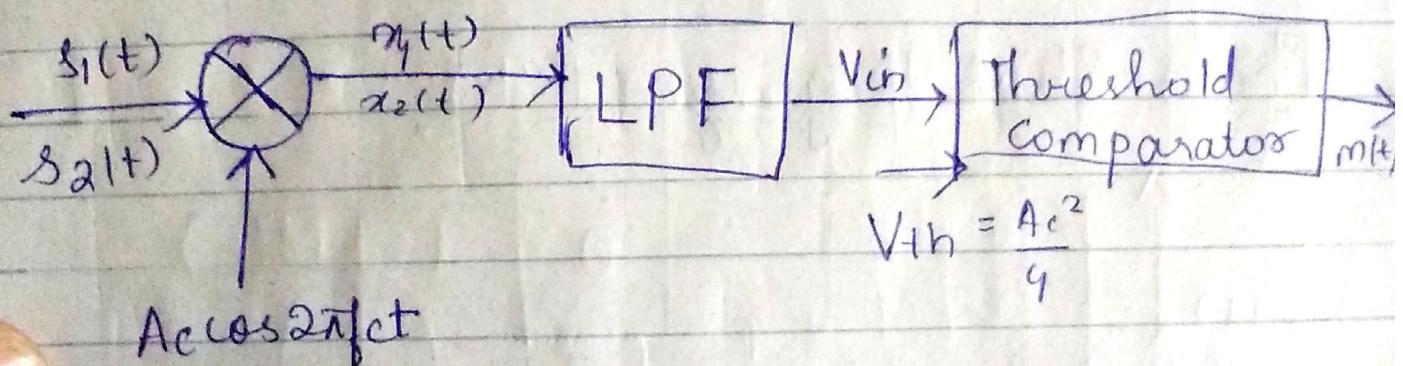
$$s_2(t) = 0$$

## Constellation diagram of ASK



$$P_e \propto \frac{1}{d_{12}} \quad (P_e = \text{probability of error})$$

## ASK Receiver



$$x(t) = A_c^2 \cos^2 2\pi fct$$

$$= \frac{A_c^2}{2} [1 + \cos 4\pi fct]$$

$$\downarrow \text{LPF} \\ \frac{A_c^2}{2}$$

$$\text{If } V_{in} > V_{th} \rightarrow 1$$

$$x_2(t) = 0$$

For ~~00~~ Vin for  $s_1(t) = 1$

then  $V_{in} > V_{th}$

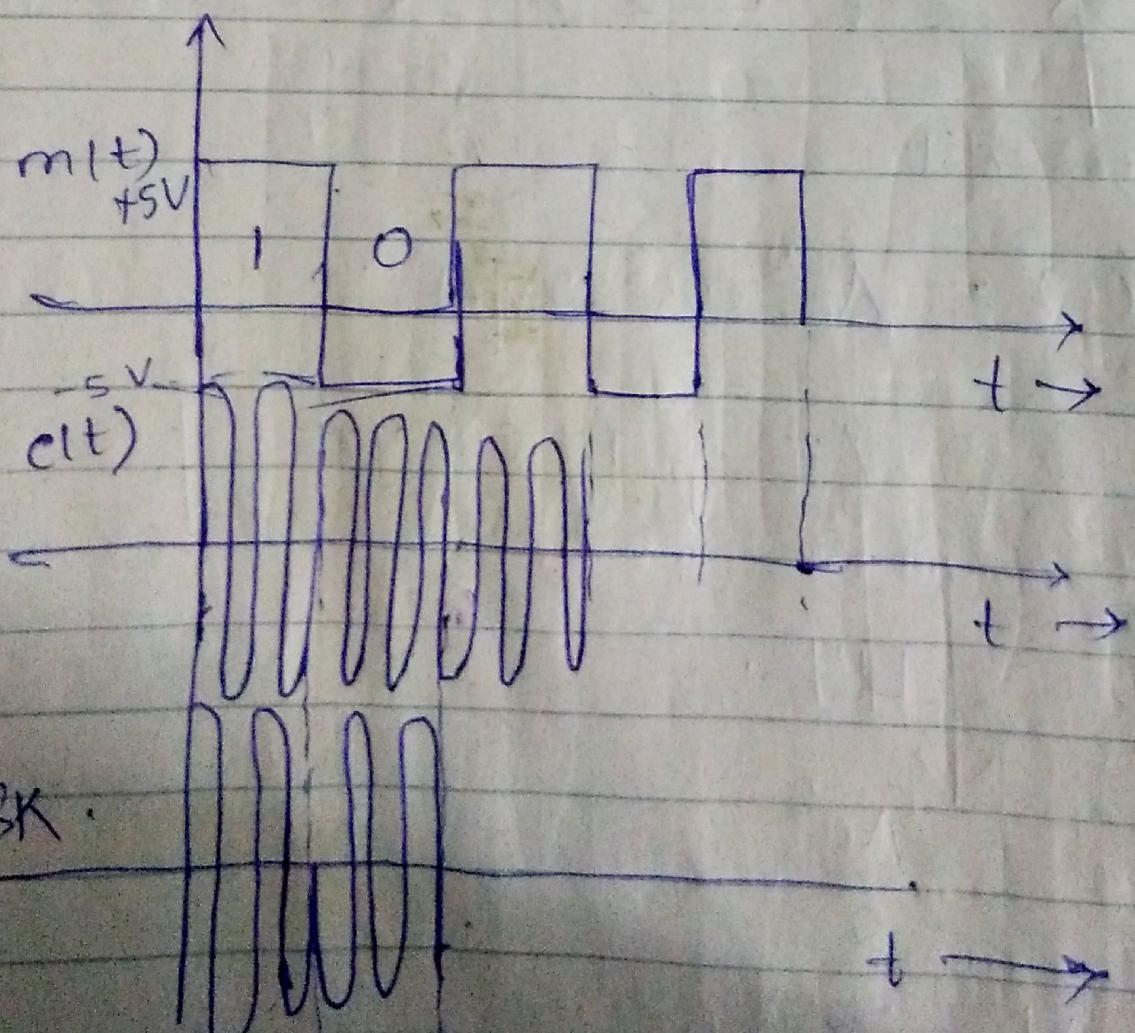
$$\text{so } m(t) = 1$$

For Vin for  $s_2(t) = 0$

then  $V_{in} < V_{th}$

$$\text{so } m(t) = 0$$

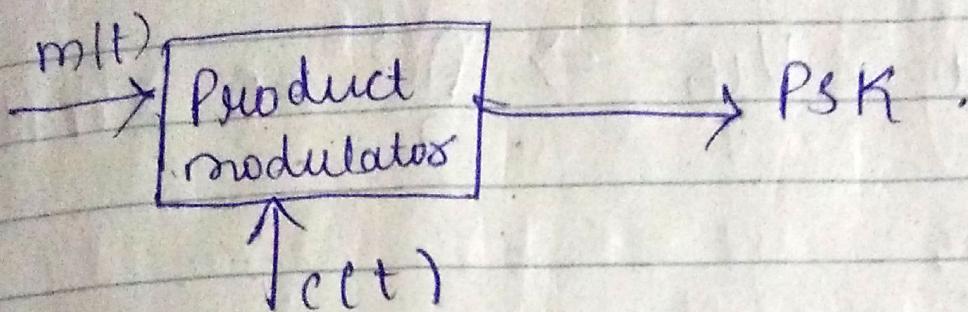
## Phase Shift Keying (PSK)



PSK

$$f_c = \pi R_b$$

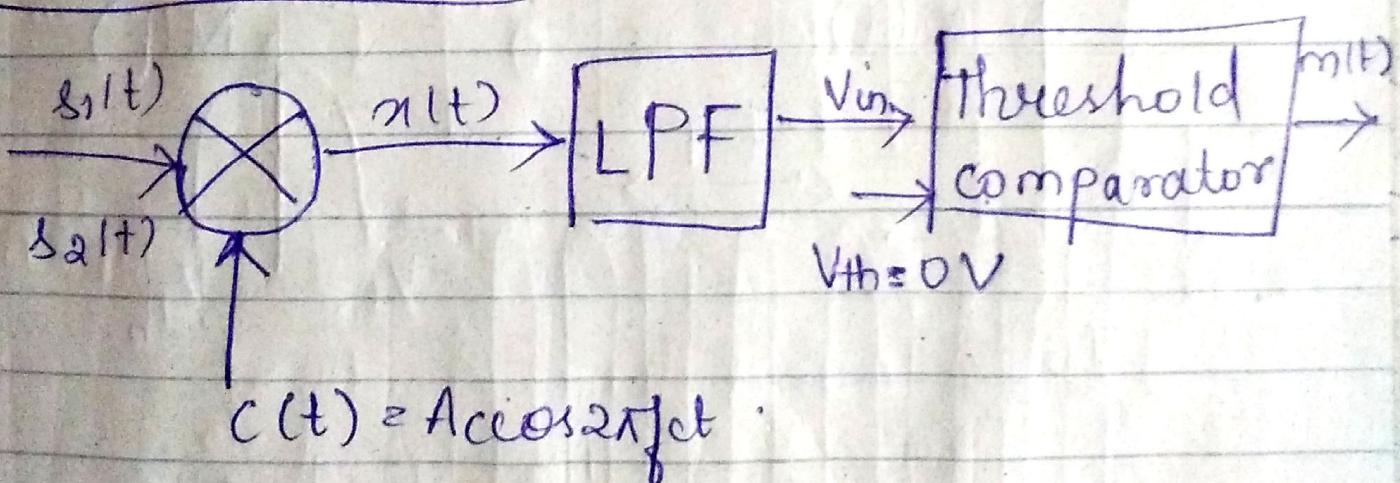
Transmitter of PSK



$$s_1(t) = A_c \cos 2\pi f_c t$$

$$s_2(t) = -A_c \cos 2\pi f_c t$$

PSK Receiver



$$n(t) = A_c^2 \cos^2 2\pi f_c t$$

$$= \frac{A_c^3}{2} \left( 1 + \frac{\cos 4\pi f_c t}{2} \right)$$

$$\text{At logic 1} \rightarrow \text{after LPF} = \frac{A_c^2}{2} = V_{in}$$

At logic 0 (after LPF)  $\Rightarrow V_{in} = -\frac{Ac^2}{2}$

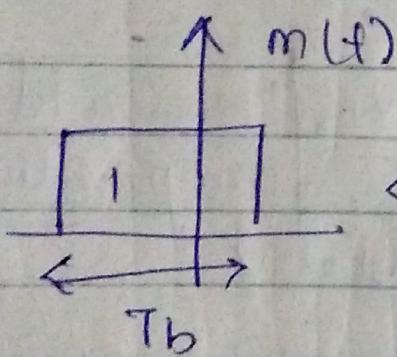
At logic 1;

$$V_{in} > V_{th} \Rightarrow \frac{Ac^2}{2} > 0 \Rightarrow m(t) = 1$$

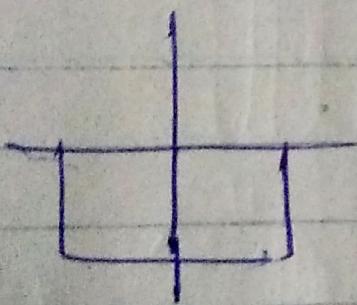
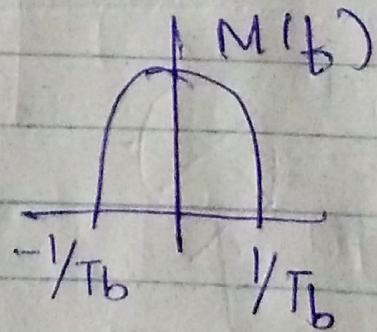
At logic 0,

$$V_{in} < V_{th} \Rightarrow \frac{Ac^2}{2} < 0 \Rightarrow m(t) = 0$$

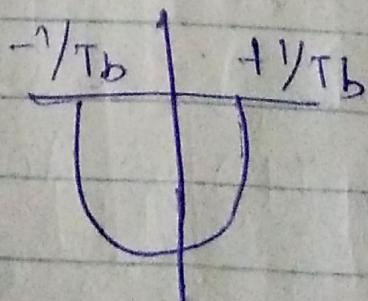
### Frequency spectrum



$\longleftrightarrow$



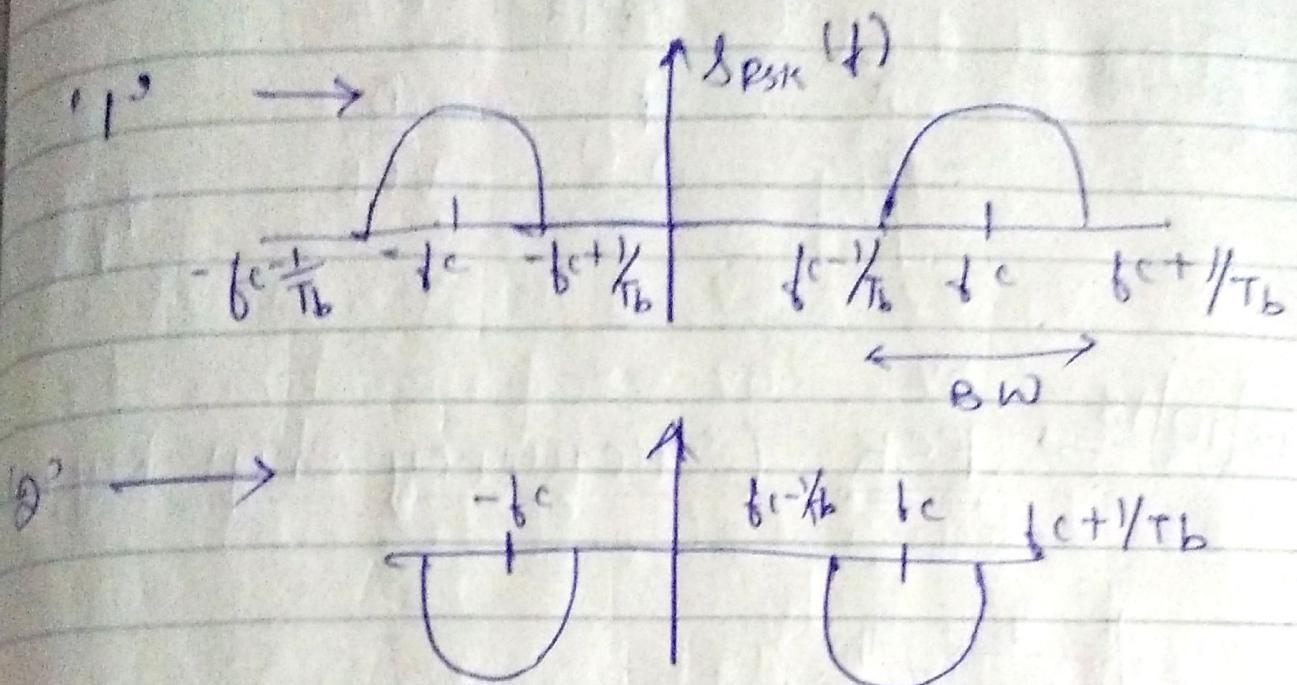
$\longleftrightarrow$



$$s(t) = c(t)m(t)$$

$$= A \cos 2\pi f_c t m(t)$$

$$= \frac{A_c}{2} [M(f-f_c) + M(f+f_c)]$$



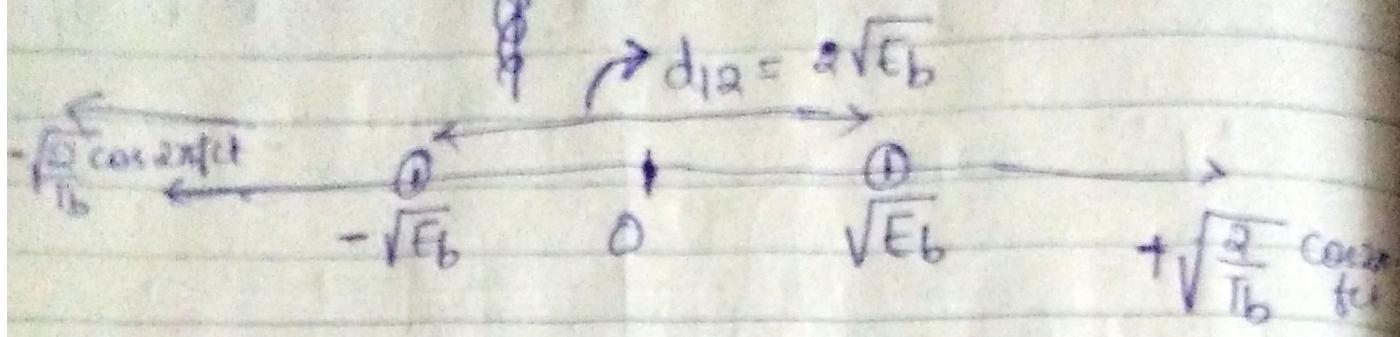
$$\boxed{\text{Bandwidth} = \frac{2}{T_b} = 2R_b}$$

Constellation diagram

$$s_1(t) = \sqrt{\frac{2E_b}{T_b}} \cos 2\pi f_c t$$

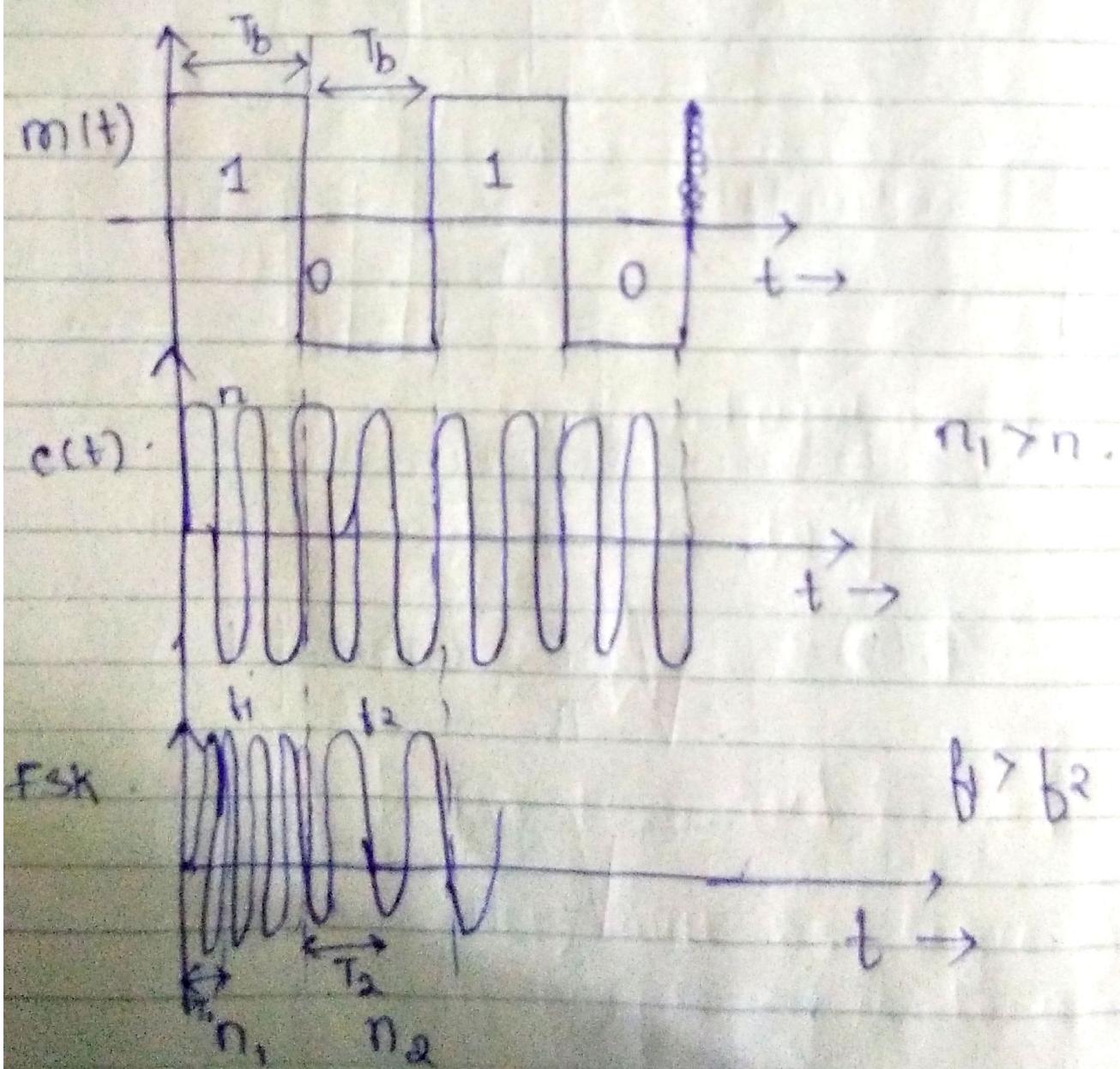
$$s_2(t) = -\sqrt{\frac{2E_b}{T_b}} \cos 2\pi f_c t$$

$$P_c \propto \frac{1}{d_{12}^2}$$



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## FSK (Frequency shift keying)



$$T_b = n_1 T_1$$

$$T_b = n_2 f_2$$

$$T_b = \frac{1}{R_b}$$

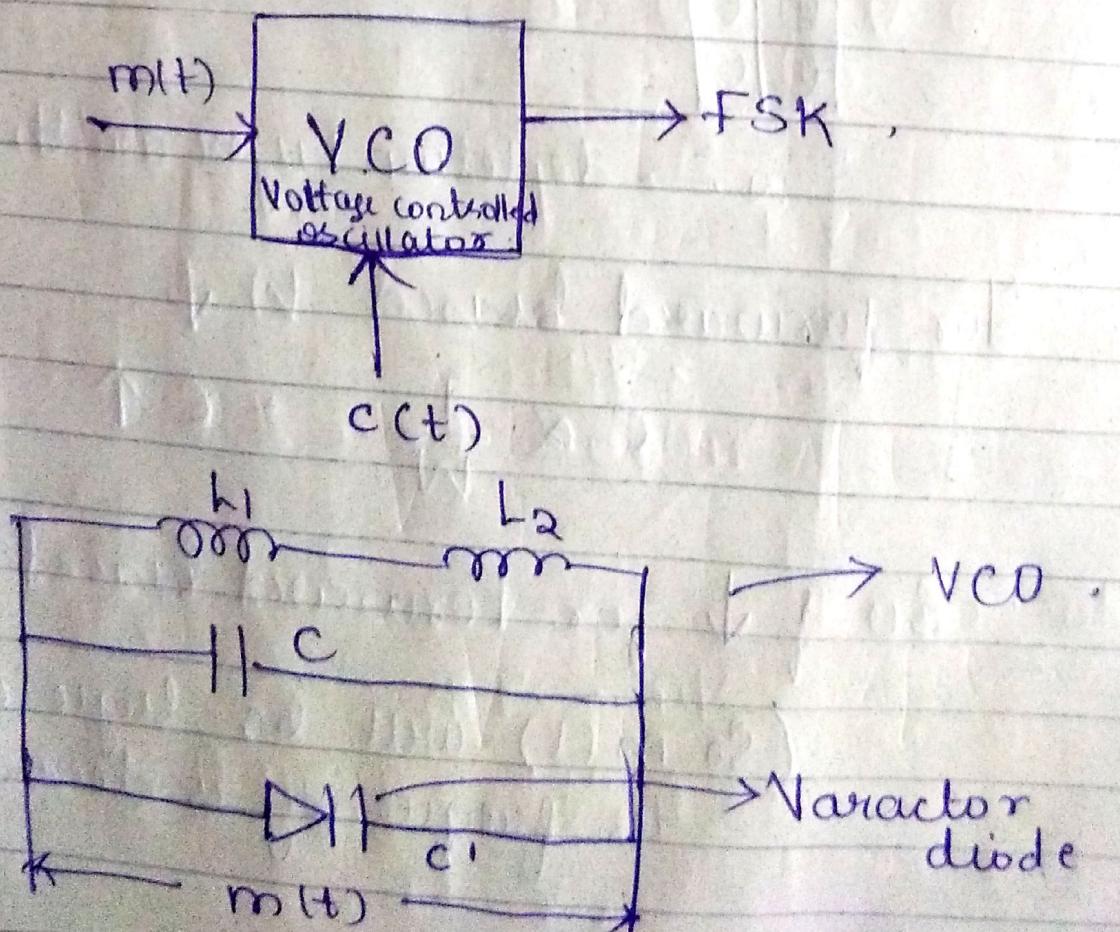
$$T_1 = \frac{1}{f_1}$$

$$f_1 = n_1 R_b$$

$$\frac{1}{R_b} = \frac{n_2}{f_2}$$

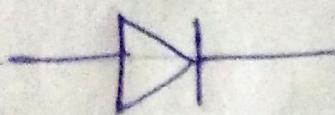
$$f_2 = R_b n_2$$

Transmitter



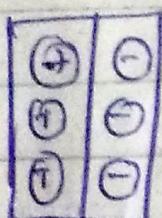
Varactor  $\rightarrow$  variable capacitor

Normal diode:



0V      5V  $\rightarrow$  reverse biased (open circuit)  
5V      0V  $\rightarrow$  forward biased (short circuit)

$$f = \frac{1}{2\pi\sqrt{(L_1+L_2)(C'+C)}}$$



$\xleftarrow{\quad w \quad} \rightarrow$  depletion layer width

For forward biased  $w \downarrow$ .

$$C \propto \frac{1}{w}, C \uparrow$$

So  $f \downarrow$  for Forward biased

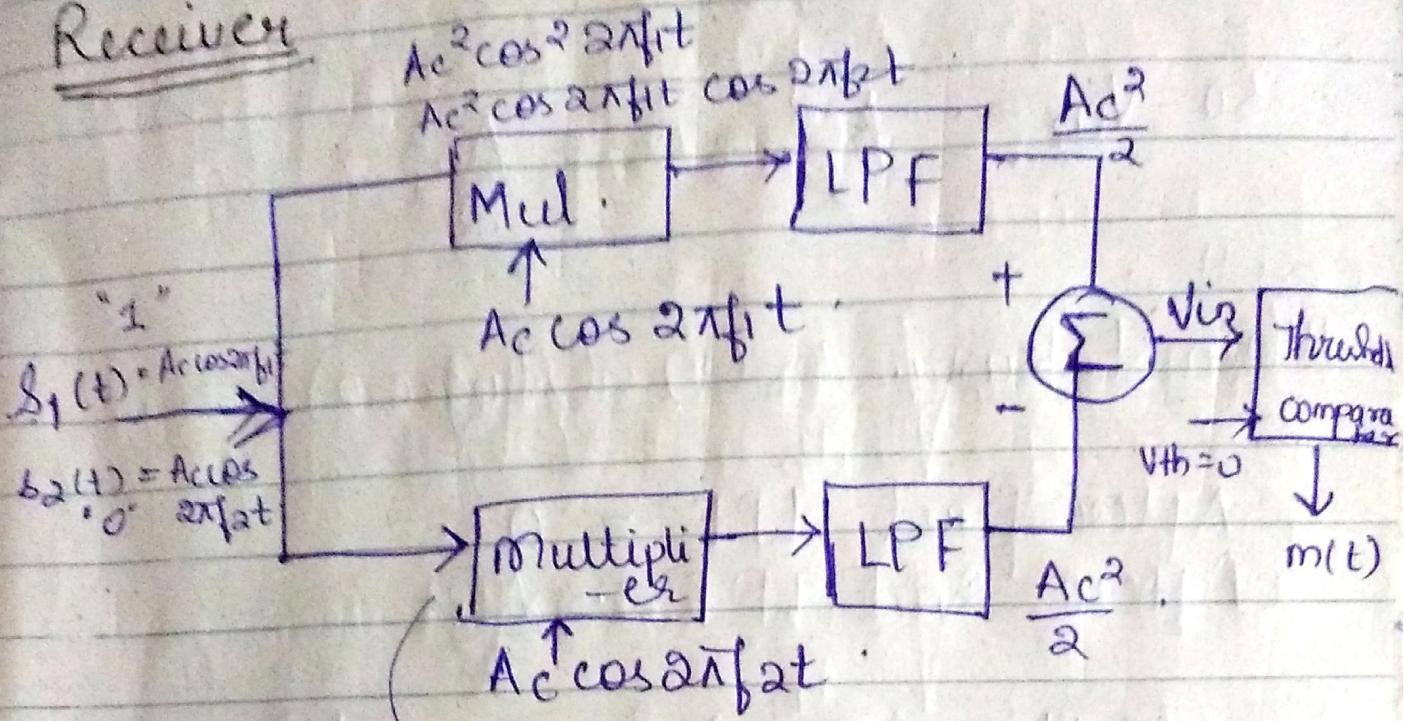
(So m(t) will be logic 0)

as frequency is decreased

For revenue biased,  $W \uparrow, C \downarrow, f \uparrow$

(so  $m(t)$  will be logic 1  
as frequency is increased)

Receiver



$$Ac^2 \cos^2 2\pi f_1 t = \frac{Ac^2}{2} [1 + \cos 4\pi f_1 t]$$

$$\begin{aligned} & Ac^2 \cos 2\pi f_1 t \cos 2\pi f_2 t \\ &= \frac{Ac^2}{2} [\cos 2\pi(f_1 + f_2)t + \\ & \quad \cos 2\pi(f_1 - f_2)t] \end{aligned}$$

LPF → only pass the constant value.

When  $s_1(t) \rightarrow$  For first LPF,  $\frac{Ac^2}{2}$

$s_2(t) \rightarrow n \cdot n = 0$ .

When  $s_1(t) \rightarrow$  For second LPF = 0

$s_2(t) \rightarrow n \cdot n = Ac^2/2$

Case I

When taking logic 1

$$\text{For first LPF} = \frac{Ac^2}{2}$$

$$\text{After second } \text{ " } = 0$$

$$\text{So } V_{in} = \frac{Ac^2}{2} - 0 = \frac{Ac^2}{2}$$

Case II

When taking } s\_a(t) (Logic 0)

$$\text{After first LPF} = 0$$

$$\text{After second LPF} = \frac{Ac^2}{2}$$

$$\text{So } V_{in} = 0 - \frac{Ac^2}{2} = -\frac{Ac^2}{2}$$

For Case I

$$V_{in} > V_{th}$$

$$m(t) = \text{logic 1}$$

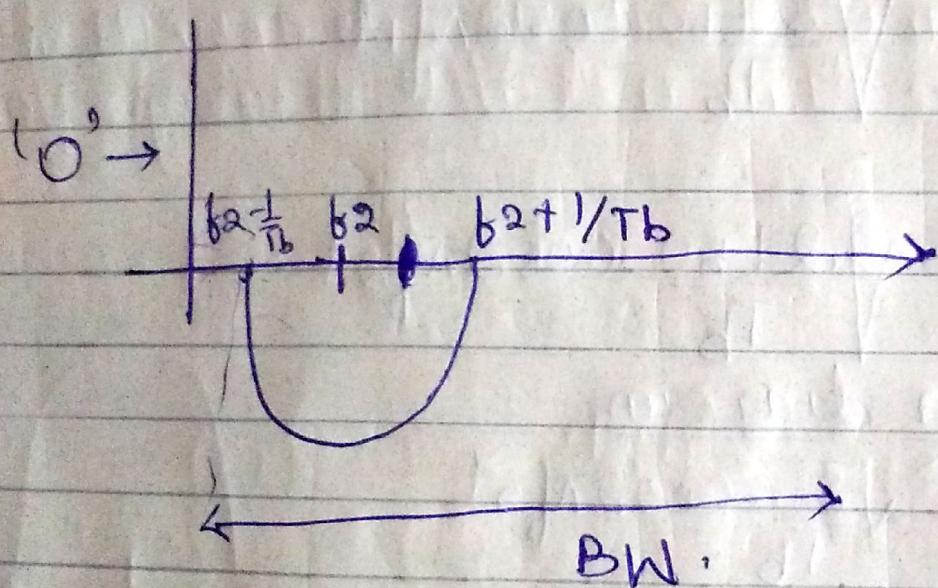
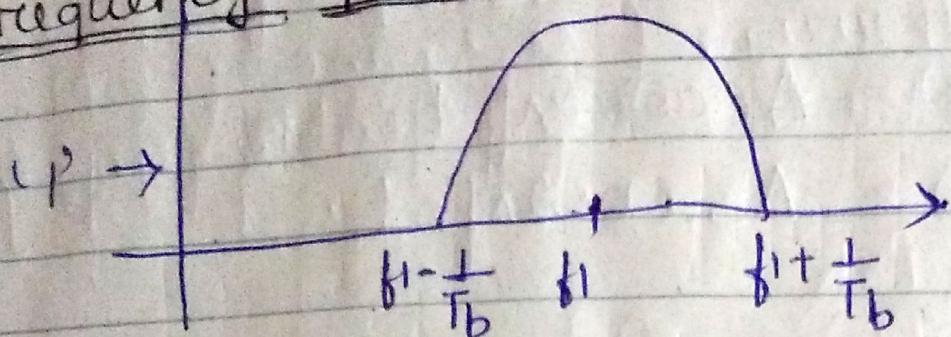
For Case II

$$V_{in} < V_{th}$$

$$m(t) = \text{logic 0}$$

So, we got  $m(t)$  same as we have been given.

### Frequency Spectrum



$$\begin{aligned} BW &= \left( f_1 + \frac{1}{T_b} \right) - \left( f_2 - \frac{1}{T_b} \right) \\ &= (f_1 - f_2) + \frac{2}{T_b} \end{aligned}$$

$$BW = f_1 - f_2 + 2R_b$$

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$$E_b = \frac{A_c^2}{2} T_b$$

$$\Rightarrow A_c = \sqrt{\frac{2 E_b}{T_b}}$$

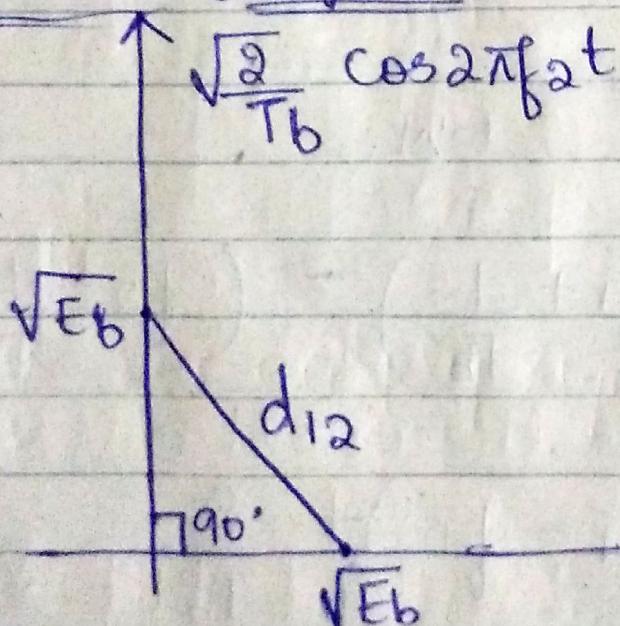
$$s_1(t) = A_c \cos 2\pi f_1 t \quad \{ f_1 > f_2 \}$$

$$s_2(t) = A_c \cos 2\pi f_2 t$$

$$s_1(t) = \sqrt{\frac{2 E_b}{T_b}} \cos 2\pi f_1 t$$

$$s_2(t) = \sqrt{\frac{2 E_b}{T_b}} \cos 2\pi f_2 t$$

Constellation diagram



$$\sqrt{\frac{2}{T_b}} \cos 2\pi f_1 t$$

$$\begin{aligned} d_{12} &= \sqrt{E_b + E_b} \\ &= \sqrt{2 E_b} \end{aligned}$$

$$P_e \propto \frac{1}{d_{12}}$$

(Assuming that  $s_1(t)$  and  $s_2(t)$  are orthogonal to each other, so we are taking  $90^\circ$  between them).

These two functions ( $s_1(t)$  and  $s_2(t)$ ) are harmonically related to each other. These functions are orthogonal to each other.

Now we have use 1 bit for transmitting, either 0 or 1 i.e., we have studied Binary ASK, FSK and PSK.

### M-Array signalling

$$M = 2^N \quad (N \rightarrow \text{no:- of bits transmitted at time instant})$$

In our syllabus we have 4-PSK or quadrature PSK.

$$4 = 2^2 \rightarrow 2 \text{ bits is transmitted}$$

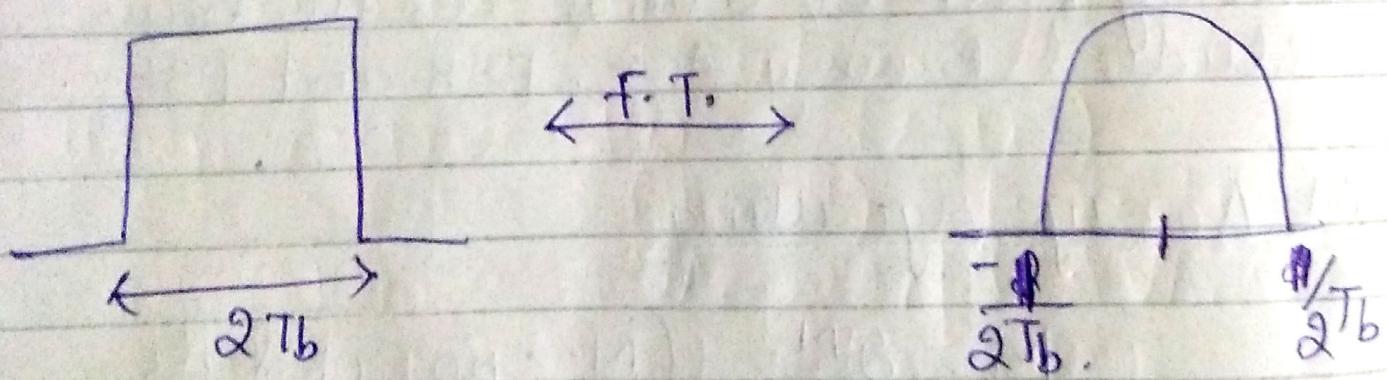
## M-array signalling

ASK, PSK and FSK, in these keyings one bit is transmitted in a specific time instant through free space i.e.,  $N = 1$ . where,  $N$  is no:- of possible symbols.

## 4-array PSK

In this scheme 2 bit are transmitted in a specific time instant through free space.

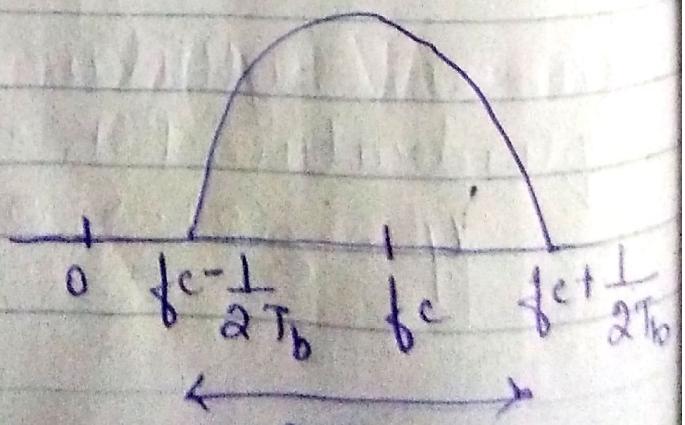
$$n = 2 \text{ so } M = 4.$$



This is for empty signal but for QPSK:

$$BW = \frac{1}{T_b}$$

$$BW = R_b$$



When,

$$M = 2$$

$$BW = 2R_b$$

$$M = 4$$

$$BW = R_b$$

$$M = 8$$

$$BW = \frac{2}{3} R_b$$

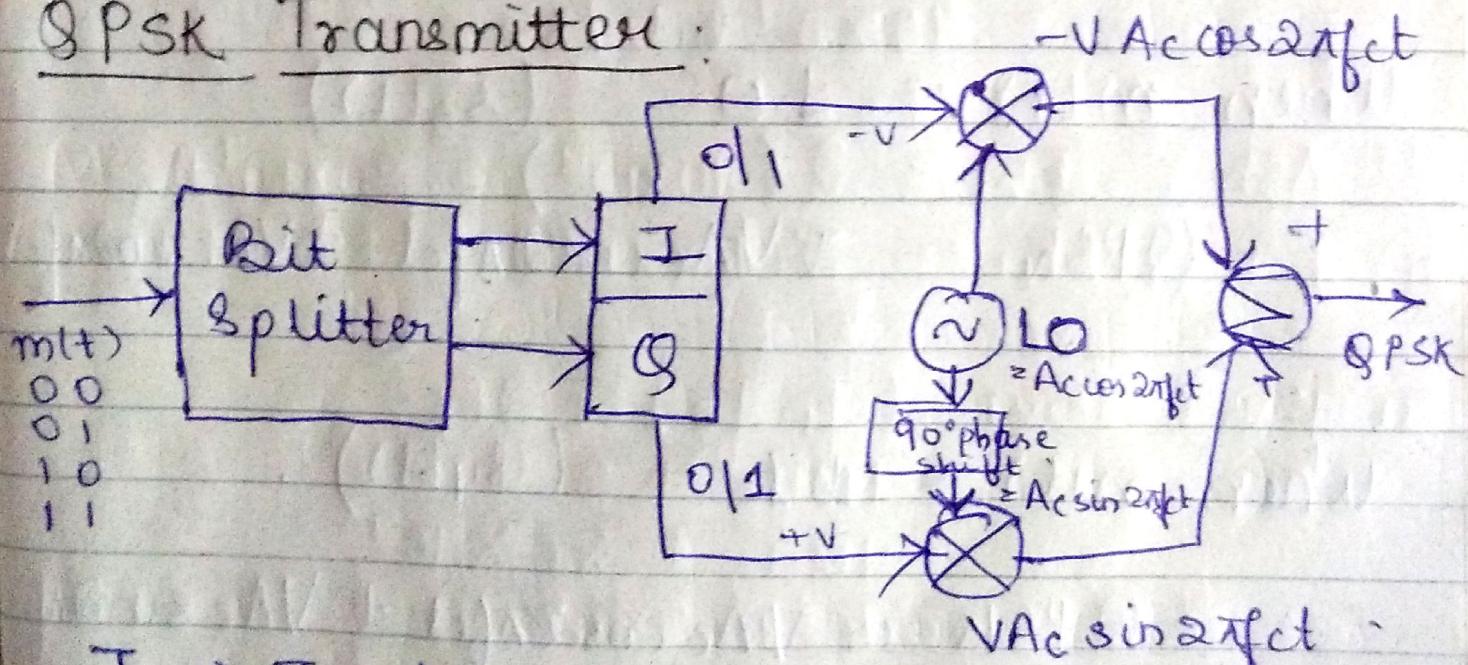
$$\approx 0.667 R_b$$

$$= 0.667 R_b = 0.6 R_b$$

As the number of bits to be transmitted goes on increasing then channel BW requirement will be decreased but the system complexity will be increased

4-array PSK is also called Quadrature PSK. (QPSK).

### QPSK Transmitter:



I  $\rightarrow$  In phase

Q  $\rightarrow$  Quadrature phase

0  $\rightarrow$  -V

1  $\rightarrow$  +V

LO  $\rightarrow$  local oscillator

=  $\text{Ac} \cos 2\pi f_{\text{ct}}$

(Here we are assuming not return to zero that's why for '0' we have taken -V)

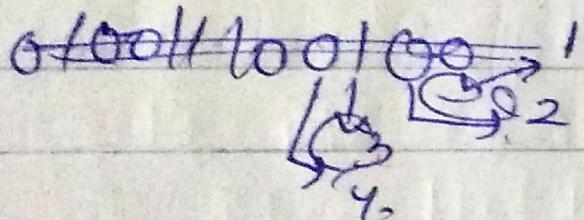
When  $m(t) = 0$  ( $s_1(t)$ )

1st O will <sup>and</sup> go to I  
2nd O will go to Q.

$$QPSK = -V_A c \cos 2\pi f_c t - V_A c \sin 2\pi f_c t$$

When  $m(t) = 0.5$  ( $s_2(t)$ )

$$QPSK = +V_A c \cos 2\pi f_c t - V_A c \sin 2\pi f_c t$$



when  $m(t) = 10$  ( $s_3(t)$ )

$$QPSK = -V_A c \cos 2\pi f_c t + V_A c \sin 2\pi f_c t$$

when  $m(t) = 11$  ( $s_4(t)$ )

$$QPSK = V_A c \cos 2\pi f_c t + V_A c \sin 2\pi f_c t$$

(Here we are assuming not return to zero that's why for '0' we have taken  $-V$ )

When  $m(t) = 00 \cdot (\delta_1(t))$

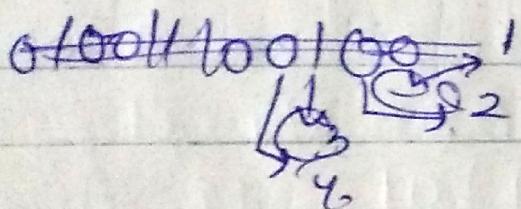
1st O will go to I

2nd O will go to Q.

$$QPSK = -V_{AC} \cos 2\pi fct - V_{AC} \sin 2\pi fct$$

When  $m(t) = 01 \cdot (\delta_2(t))$

$$QPSK = +V_{AC} \cos 2\pi fct - V_{AC} \sin 2\pi fct$$

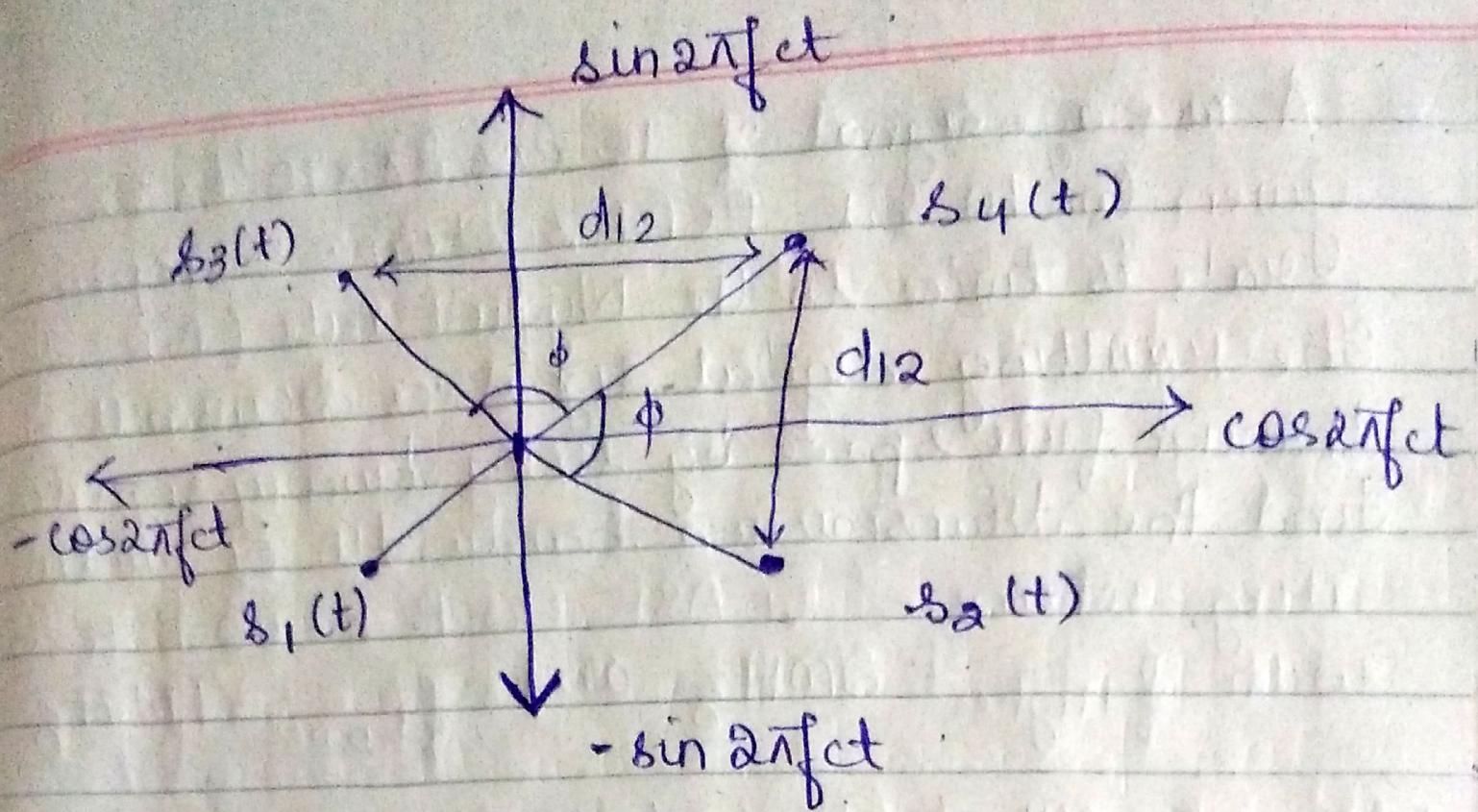


When  $m(t) = 10 \cdot (\delta_3(t))$

$$QPSK = -V_{AC} \cos 2\pi fct + V_{AC} \sin 2\pi fct$$

When  $m(t) = 11 \cdot (\delta_4(t))$

$$QPSK = V_{AC} \cos 2\pi fct + V_{AC} \sin 2\pi fct$$



General formula for any array PSK  
are :-

$$E_s = N E_b \quad M = 2^N$$

$$d_{12} = \sqrt{2E_s} \sin\left(\frac{\pi}{M}\right)$$

$$BW = \frac{2R_b}{N}$$

$$\phi = \frac{2\pi}{M}$$

★ As receiver section is complex, so we need not have to do it.