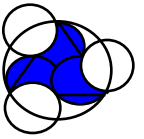


# *CLAIRE: A High-Level Programming Language for Complex Algorithms*

*Yves Caseau & al.*

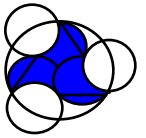
*Bouygues - Direction des Technologies Nouvelles  
Ecole Normale Supérieure*

# Outline



- ❑ *Motivations*
- ❑ *CLAIRE (short overview)*
- ❑ *Rule-based Programming*
- ❑ *Set-based Programming*
- ❑ *Conclusions*

# Background



## ■ *Combinatorial Optimization and Constraints*

- *Competitive advantages and reciprocal benefits of CO and CP techniques*
- *How to combine them: Hybrid Algorithms*

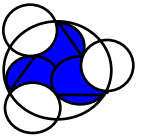
## ■ *Systematic Approach*

- *Resource Allocation, Matching*
- *Scheduling (job-shop, cumulative)*
- *Routing (TSP, VRP, VRPXX)*
- *Time-Tabling*

## ■ *Produce a Library of Hybrid Algorithm*

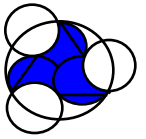
- *Building Blocks for Optimization Applications*
- *Research & Teaching*

# *CLAIRE: Specifications*



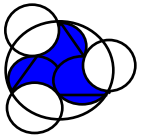
- ❑ *Simple and Readable*
  - *executable pseudo-code (teaching CO algorithms)*
  - *few simple (well-understood) concepts*
- ❑ *Multi-paradigm*
  - *Objets , Functions*
  - *Rules*
  - *Versions (search tree exploration)*
- ❑ *C++ compatibility, Freeware*
  - *generate C++ objets*
  - *efficiency similar to hand-written C++*
  - *sources and binaries available*
  - *Next release will generate Java*

# *CLAIRE at a glance*



- ❑ *Object-Oriented functional language with parametric polymorphism*
  - *mixes compiled and interpreted code, static and dynamic typing*
- ❑ *Modeling language (sets, relations, ...)*
  - *high level of abstraction, ease of use*
- ❑ *Inference engine for object-based rules*
  - *first-order logic (propagation)*
- ❑ *Tools for tree search*
  - *choice points and backtracks*

# *CLAIRE: Industrial Motivations*



## ■ *Better Productivity*

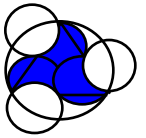
- *C++ code generator, DLL production (Windows NT)*
- *Reduction factor approximately 5*

## ■ *Simplify Maintenance*

- *more readable means easier to maintain*
- *high level of abstraction, “concise and elegant” programming*

## ■ *Support Reuse*

- *Black-box component approach is poorly suited to combinatorial optimization.*
- *We build source-code libraries*



- ❑ *Single inheritance class hierarchy*

point <: object(x:integer, y:integer)

- ❑ *Parametric Classes*

stack[of] <: thing(of:type, contents:list)

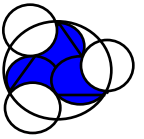
- ❑ *Class hierarchy embedded in a multiple inheritance data type lattice*

$(1 \dots 10) \subseteq (20 \dots 30) \subseteq (1 \dots 30) \subseteq \text{integer}$

$\text{stack}[\text{of} = \text{integer}] \subseteq \text{stack}[\text{of:subtype}[\text{integer}]] \subseteq \text{stack} \subseteq \text{object}$

$\text{tuple}(\text{integer}, \text{integer}) \subseteq \text{list}[\text{integer}] \subseteq \text{list}[\text{integer} \cup \text{float}] \subseteq \text{list}$

# Polymorphism



## ❑ *Free Overloading (attach method to complex types)*

$f(x:\{0\}, y:(1 \dots 12)) \rightarrow 1$

$f(x:(0 \dots 10), y:\text{integer}) \rightarrow (x + y)$

$f(x:\text{integer}, y:(\{1,2\} \cup (7 \dots 10))) \rightarrow (x - y)$

## ❑ *optimization through code generation*

$\text{sum}(s:\text{subtype}[\text{integer}]) : \text{integer}$

$\rightarrow \text{let } d := 0 \text{ in } (\text{for } x \text{ in } s \text{ } d :=+ x, d)$

$\text{sum}(1 \dots 10) \dots$

$\text{let } d := 0, m := 10, x := 1 \text{ in}$

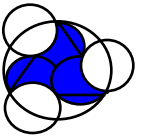
$(\text{while } (x \leq m) (d :=+ x, x :=+ 1), d)$

## ❑ *composition polymorphism*

- *Takes advantage of rules of type  $f(g(x)) = h(x)$*
- *Example :  $\det(A * B) = \det(A) * \det(B)$*



# Sets and Relations



## ❑ *Set-based Programming*

- *data types are sets (e.g., extensions)*
- *easy syntax for set expressions*

$\{x \text{ in person} \mid x.\text{age} \in (0 \dots 17)\}$

$\{x.\text{father} \mid x \text{ in person}\}$

$\text{list}\{\text{salary}(x) \mid x \text{ in } \{x \text{ in person} \mid x.\text{department} = \text{sales}\}\}$

## ❑ *Efficient Parametrization (operation/representation)*

## ❑ *Relations are first-class citizens (inverses...)*

$\text{dist}[x:(0 \dots 100), y:(0 \dots 100)] : \text{integer} := 0$

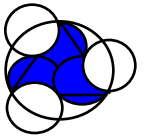
$\text{comment}[c:\text{class}] : \text{string} := ""$

## ❑ *Modeling Abilities*

$\text{meet}[s:\text{set}[\text{person}]] : \text{date} := \text{unknown}$

$\text{course}[\text{tuple}(\text{person}, \text{set}[\text{person}])] : \text{room} := \text{unknown}$

# Hypothetical Reasoning



## □ Worlds

- *world+()* creates a choice point
- *world-()* makes a backtrack
- *other derived operations*

## □ tree search

- *Trailing stack, optimized for depth-first search*

*solve()* : boolean ->

when *q* := *pick()* in

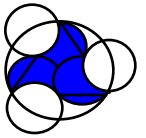
exists( *c* in *possible(q)* |

branch( (*column[q]* := *c*, *solve()*)))

else true

*branch(e) ::* (     *world+()*,  
                          ( (try *e* catch contradiction  
                          *false*) /  
                          (*world-()*, *false*) ))

# Logical Assertions



- *CLAIRE uses an “object-oriented” logic which is an extension of binary DATALOG ...*

$\text{edge}(x,y) \mid \text{exists}(z, \text{edge}(x,z) \ \& \ \text{path}(z,y))$

$\Rightarrow \text{path}(x) : \text{add } y$

- *with methods ...*

$\text{exists}(z, z = \text{salary}(x) \ \& \ z > 30000 \ \& \ z < 50000 \ \&$

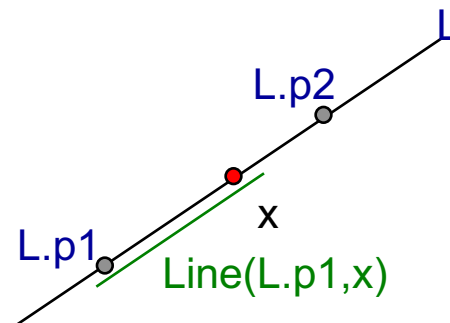
$y = 3000 + (z - 30000) * 0.28) \Rightarrow x.\text{tax} := y$

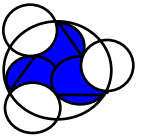
- *and the ability to create new objects and sets*

$L.p2 \in \text{Holds}(\text{line}(L.p1,x)) \Rightarrow \text{Holds}(L) : \text{add } x$

$z = \text{size}(\{y \text{ in person} \mid y \in x.\text{children}\})$

$\Rightarrow x.\text{family\_size} := z + 2$





## □ *Production Rules*

```
rule1(x:person[age:(18 .. 40)]) :: rule(  
  x.salary < average({y in person | x.department = y.department}  
  ⇒ increase_salary(x) )
```

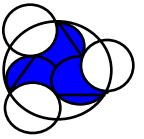
## □ *Control*

- *Rules are triggered by events (updates on slots & arrays)*
- *priorities, inheritance*
- *trigger: once/ exact / many*
- *rule sets and finer control are easy to implement*

## □ *Queries*

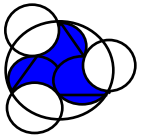
- *A query is a relation defined by a logical assertion*
- *naive top-down resolution (no recursion)*

# Goodies



- *Modules*
- *(Fast) Exceptions*
- *Memory Management*
- *Second-Order Types*

# Why Compile Rules ?



## ❑ Performance

- *much faster than best RETE-based compiler*
- *no comparison with RETE-base interpreter*

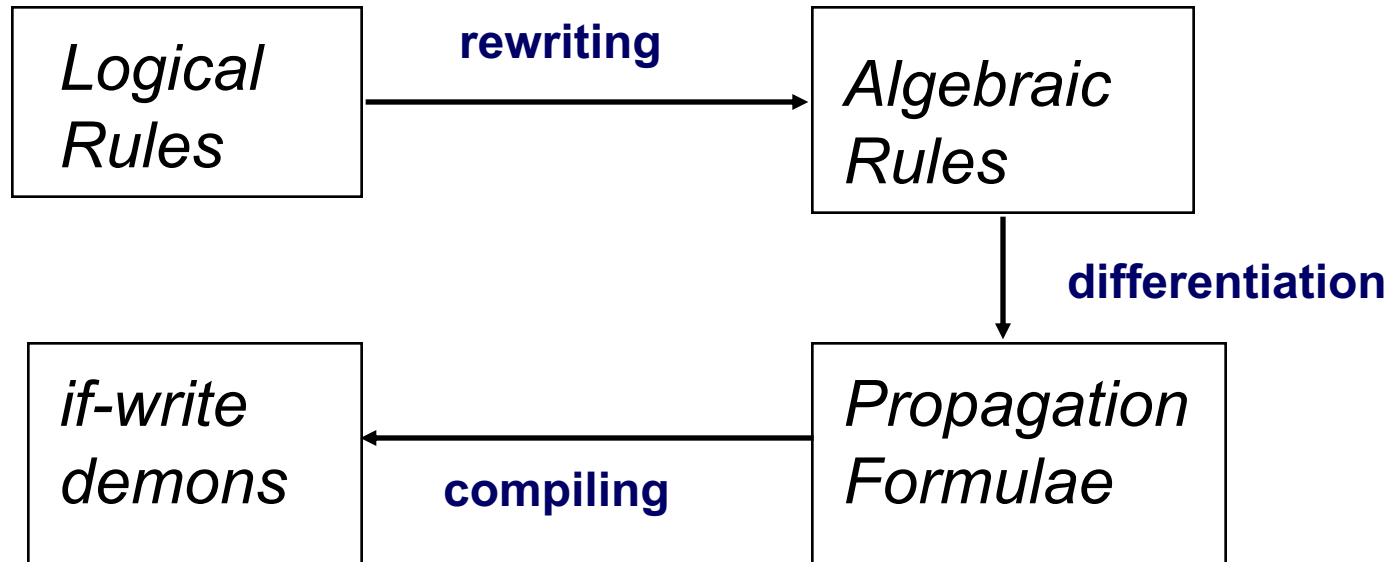
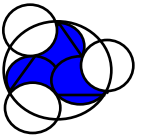
## ❑ Autonomous objects

- *The generated code is purely procedural*
- *no need for additional engine or data structures*
- *Ideally suited for Java Beans concept*

## ❑ Dynamic Rules

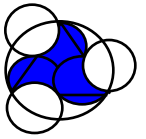
- *Dynamic Libraries*
- *Consistency-checking at compile-time*
- *through interpreter (50 times slower)*

# *Principles for Compiling Rules*



*CLAIRE compiles a set of rules into a set of demons (procedural attachment). Java observable mechanism could be used.*

# Rules Compilation



## ■ Complete compilation

- *totally procedural C++ code (no auxiliary data structures)*
- *Sets/Lists/Vectors handling is thoroughly optimized*

## ■ Benchmarks

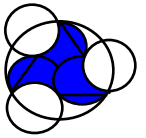
- *Standard benchmarks are easy to translate (inverse is not true)*
- *State-of-the-art results (600K to 3Mips on a P166)*
- *but no inter-rule optimization is performed*

## ■ Empirical Results

- *10 to 50% penalty compared with hand-optimized procedural code*
- *source code reduction factor from 4 to 30.*



# Code Example



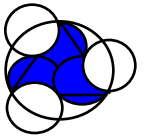
## □ *The Airline scheduler:*

```
city <: thing(  
  time_zone:integer = 0,  
  previous_request:set[request],  
  starting:set[flight],  
  arriving:set[flight],  
  starting_plan:set[travel_plan],  
  arriving_plan:set[travel_plan] )
```

```
7 == (9:(AF401):13, 8:(AF301, LU401):12)  
8 == (9:(AF401):13, 8:(AF301, LU401):12)  
9 == (9:(AF401):13)  
10 == (12:(AF011, BA401):19,  
       10:(AF311, LU511, LU411):16)  
11 == (12:(AF011, BA401):19)  
12 == (12:(AF011, BA401):19)
```

```
complex_plan(r:request, f:flight) :: rule(  
  (f.fromc = r.start & f.to != r.arrive &  
   f.depart >= r.depart & (f.depart + f.time) <= r.end_at )  
⇒ let r2 := request!(f.to, r.arrive ,(f.depart + f.time), r.end_at) in  
  (if not(r2 ∈ f.to.previous_request)  
   (f.to.previous_request :add r2,  
    r2.start := f.to,  
    r2.arrive := r.arrive)) )
```

# Rules Applications



## ❑ *Crane scheduling application*

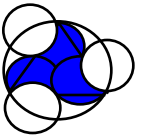
- *Propagation of resource constraint*
- *Complex propagation patterns*
  - 1 week to implement 3 rules with methods
- *minimal performance degradation*

## ❑ *Television Advertising Optimization*

- *very large bin packing with constraints*
- *Ad-hoc limited tree search with heuristics*
- *Rules are used for defining heuristic control parameters*

$(x.\text{satisfaction} < \text{minsat} \ \& \ x.\text{productline} = \dots \ \& \ y \in x.\text{products}$   
 $\ \& \ y.\text{satisfaction} < (\text{minsat} / 2) \dots) \Rightarrow \text{priority}(y) :^* 2$

# Set-Based Programming



*Set-based Programming is the combination of:*

- *sets are "first-class citizens" with a choice of multiple representations (abstraction)*
- *abstract sets may be used to capture "design patterns"*

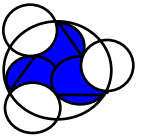
`for x in {p.father | p in person} ...`

`for y in {p in person | p.father.retired? = true} ...`

`sum({f(x) | x in {y in (1 .. 10) but 5 | p(y) >0}})`

`min( i but t, <Atleast, TE)`

# Concrete and Abstract Sets



## ■ Concrete Sets

- *classes* `for x in person print(x), size(person)`
- *sets, lists* `set(1,2,3,4), list(Peter, Paul, Mary)`
- *data structure library* (*Bitvectors, Hset, ...*)

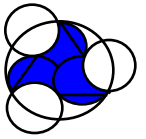
## ■ Data Types

- *Intervals* `1 .. n, "abc" .. "abd"`
- *Union, Intersection* `array U property, list ^ subtype[char]`
- *Parameterized Types*  
`for x in person[age:(15 .. 18)] print(x)`

## ■ Set Expressions

- *image*  
`{age(x) | x in person}, list{i + 1 | i in (1 .. 10)}`
- *selection*  
`{x in person | x.age > 0}, list{i in (1 .. n) | f(i) > 0}`

# Extensibility



## ■ *Classes*

- *extending the data structure library*

```
Hset[of] <: set_class(of:type,content:list,index:integer)
```

```
add(s:Hset[X], y:X) : void
```

```
-> let i := hash(s.content,y) in ....
```

```
set!(s:Hset) -> {x in s.content | known?(x)}
```

## ■ *Patterns*

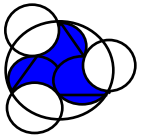
- *a pattern is a function call that is dealt with lazily*

```
but(x:abstract_set,y:any) : set -> {z in x | z != y}
```

```
%(x:any, y:but[tuple(abstract_set,any)])
```

```
=> (x % y.args[1] & x != y.args(2))
```

# Explicit Iteration



## ■ *Lazy evaluation directed by set type*

```
for x in person print(x)
for y in (1 .. n) f(y)
```

## ■ *Optimization through source code generation*

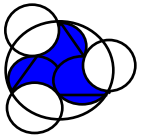
```
for c in person.descendent
  for x in c.instances print(x)
let y := 1 in
  (while (y <= n) (f(y), y :=+ 1))
```

## ■ *Iteration mechanism is extensible*

```
iterate(x:Hset,v:Variable,e:any)
=> for v in x.content (if known?(v) e)
```

```
iterate(x:but[tuple(abstract_set,any)],v:Variable,e:any)
=> for v in x.args[1] (if (v != x.args[2]) e)
```

# *Implicit Iteration*



## ■ *Image/selection expressions imply iterations*

```
{x in (1 .. 10) | f(x) > 0}
```

```
{length(c.subclass) | c in (class but class)}
```

```
let s := {}, x := 1 in
```

```
  (while (x <= 10) (if (f(x) > 0) s :add x, x :+ 1),  
   s)
```

## ■ *The iteration of such an expression is also lazy :*

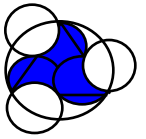
```
for x in {x in (1 .. 10) | f(x) > 0} print(x)
```

```
for y in {c.slots | c in (class \ relation.ancestors)} print(y)
```

```
for c in class.instances
```

```
  if not(c % relation.ancestors) print(c.slots)
```

# *Abstraction: A Tradeoff*



## ■ *CLAIRE supports true abstraction:*

- *One may substitute a representation by another and not have to change a line of code*
- *On the other hand, re-compiling is necessary*

## ■ *CLAIRE supports efficient generic methods*

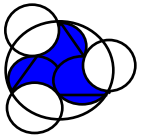
```
sum(s:subtype[integer]) : integer  
=> let d := 0 in (for x in s d :=+ x, d)
```

```
count(s:subtype[integer]) : integer  
=> let d := 0 in (for x in s d :=+ 1, d)
```

```
min(s:abstract_set,p:property,default:any) ....
```



# *Application: Embedded Linked List*



- *Embedding (using slots) is more efficient*

```
Task <: object( ....  
                next:Task, prev:Task, ....)
```

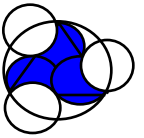
- *Patterns may represent « virtual linked lists »*

```
chain(x:Task) : list[Task]  
  -> let l := list(x), in  
      (while known?(next,x) (x := x.next, l :add x),  
       l)  
insert(x:Task,y:list[Task]) => ...  
iterate(x:chain[tuple(Task)],v:Variable,e:any) => ...
```

- *These lists may be used as usual :*

```
count(chain(t1)), sum({x.weight | x in chain(t0)}), ...
```

# Feature Combination



```
iterate(s:Interval, v:Variable, e:any)
  => for v in s.use.users (if SET(v)[v.index] e)

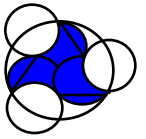
<atleast(x:Task, y:Task) => (x.atleast <= y.atleast)

min(s:any, f:property, default:any) : any
  => let x := default in
      (for y in s (if f(x,y) x := y), x)
```

*// the task with the smallest earliest start date in i, different from t*  
`min(i but t, <atleast, TEnd)`

*let x := TEnd in*  
*(for y in i.use.users*  
*(if SET(i)[y.index]*  
*(if (y != t) (if (y.atleast <= x.atleast) x := y))),*  
*x)*

# Structure Iterators



- *Combining iterators and patterns is useful to iterate more complex data structures such as trees :*

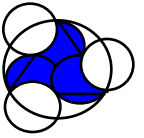
```
Tree <: object(value:any,right:Tree,left:Tree)
TreeIterator <: object(tosee:list, status:boolean)
iterate(x:by[tuple(Tree,TreeIterator)], v:Variable, e:any)
  => let v := start(x.args[2], x.args[1]) in
      while (v != unknown)
        (e, v := next(x.args[2], x.args[1]))
```

```
TreeIteratorDFS <: TreeIterator()
start(x:TreeIteratorDFS, y:Tree) -> ...
next(x:TreeIteratorDFS, y:Tree) -> ...
DFS :: TreeIteratorDFS()
```

```
TreeIteratorBFS <: TreeIterator() ...
```

```
for x in (myTree by DFS) print(x)
{y.weight | y in (myTree by BFS)}
```

# A Real-Life Example (I)



*// builds a maximum weight complete matching*

match()

-> (... , *// initialization*

while (HN != N) (if not(grow()) dual\_change()))

*// a step repeats until the forest is hungarian (return value is false)*

*// or the matching is improved (return value is true)*

*// explore is the stack of even nodes that have not been explored yet*

grow() : boolean

-> let i := pop(explore) in

( exists( j in {j in GpiSet(i, LastExplored[j] + 1, LastValid[j]) | not(odd?[j])} |

(if (sol-[j] != 0)

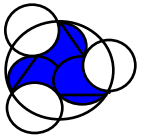
(//[SPEAK] grow: add (~S, ~S) to forest// i, j,

odd?[j] := true, pushEven+(sol-[j]), tree[j] := i, false)

else (augment(i, j), true))) |

(if (explore[0] != 0) grow()) )

# Hungarian Algorithm (II)



*// change the dual feasible solution, throw a contradiction if there are no perfect matching*

dual\_change() : integer

-> let e := Min( list{vclose[i] | i in {j in Dom | not(odd?[j])}}) in

*(//[SPEAK] DUAL CHANGE: we pick epsilon = ~S // e,*

if (e = NMAX) contradiction!(),

for k in stack(even) (pi+[k] := + e, LastExplored[k] := LastValid[k]),

for j in {j in Dom | odd?[j]} (pi-[j] := - e, vclose[j] := NMAX)),

clear(explore),

for i in stack(even)

let l := Gpi[i], k := size(l), toExplore := false in

(while (LastValid[i] < k) (k, toExplore) := reduceStep(i,j,l,k,toexplore),

if toExplore push(explore,i)))

*// look at edges outside the valid set one at a time*

reduceStep(i:Dom,j:Dom,l:list,k:integer,toExplore:boolean) : tuple(integer,boolean)

-> let j := l[k], c := Cpi(i,j) in

(if (c = 0) (*//[SPEAK] dual\_change: Add edge ~S, ~S // i,j,*

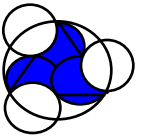
Gpiadd(l,i,j,k), toExplore := true)

else (vclose[j] := min c, k := k - 1)),

list(k,toExplore))

# CLAIRE Strategy

---



## □ Phase I: 95 - 97

- *Free Academic Software*
- *Support-as-you-use approach*
- *Productivity gains for R&D projects*
- *Algorithm libraries*

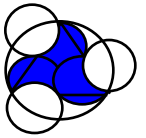
## □ Phase II: 98 - 99

- *Deployed Applications*
- *Industrial Users Club*
- *Industrial Support for CLAIRE run-time library*
- *libraries: ECLAIR, Schedule, LP, ...*

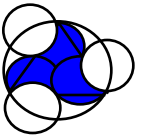
## □ Phase III: 99 onwards

- *part of development tools suite*
- *looking for collaborations*

# Conclusion



- ❑ *CLAIRE is a powerful tool for processing business rules:*
  - *State-of-the-art inference engine*
  - *Expressive Power*
- ❑ *CLAIRE is a good tool to implement complex algorithms for decision aid*
  - *multi-paradigm*
  - *high level of abstraction*
  - *readability*
- ❑ *CLAIRE is available*
  - *compiler, interpreter, tools for tracing and debugging*
  - *UNIX and Windows NT: <http://www.ens.fr/~laburthe/claire.html>*
  - *complete system: (20000 lines), compiler (executable ) 1.5 Mb*
    - *run-time: 5000 lines of code (100K) [Java: 1000 lines]*



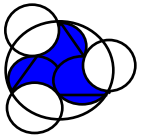
# *Industrial Applications*

---

- *4 applications written with CLAIRE have been deployed*
  - *Construction Equipment Inventory*
  - *Crane Daily Planning*
  - *Call Center Scheduling*
  - *Advertising Resource Optimization*
- *A BOUYGUES library of reusable components is being developed (business objects)*
- *A public library (ENS) of classical algorithms is also being developed (forthcoming book)*

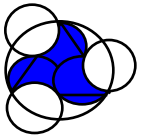


# *Future Directions*



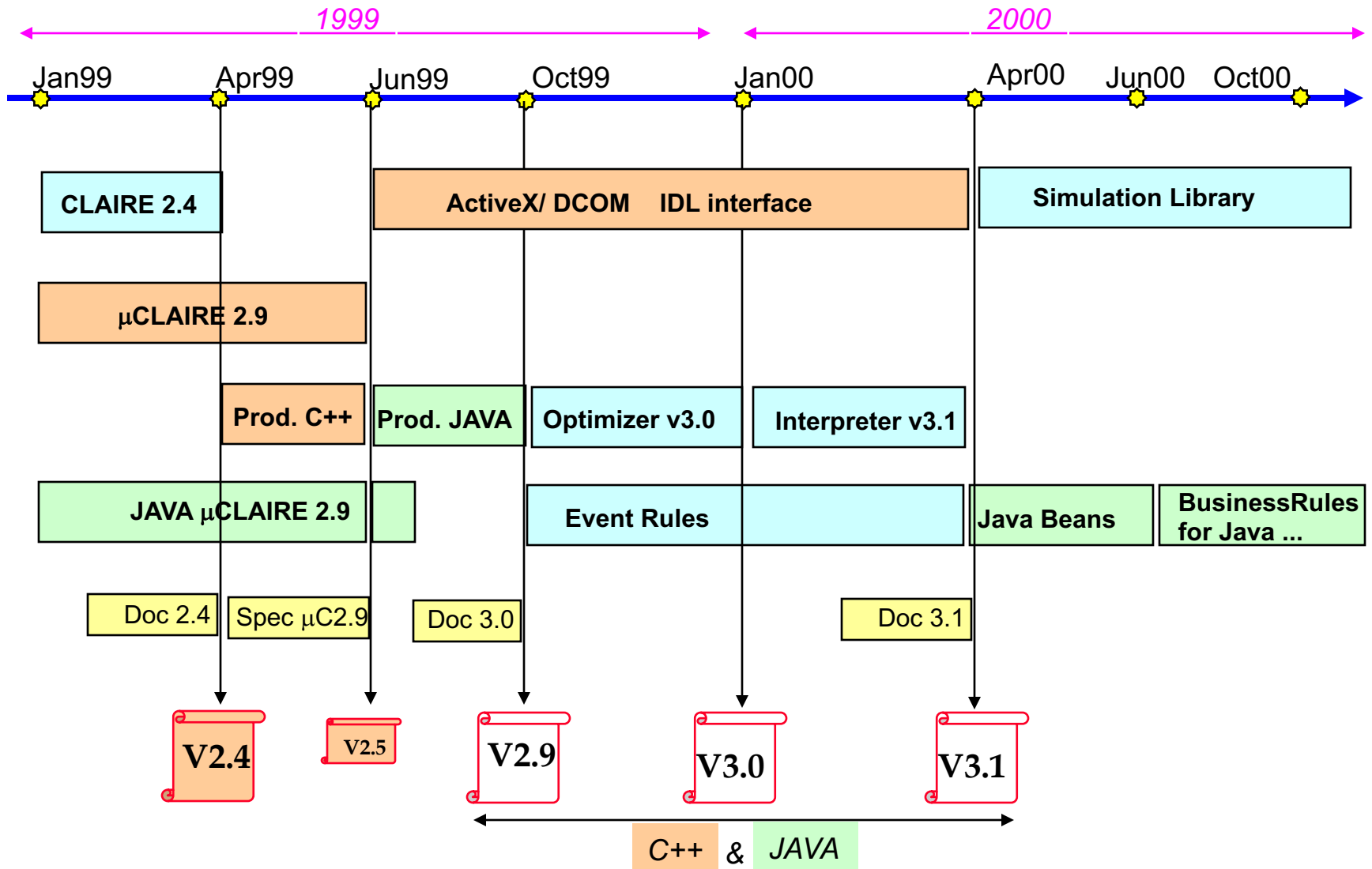
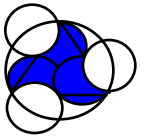
- *Component generator*
  - *Stripped Objects (no reflective descriptions)*
  - *Message Interface (DCOM/ CORBA/ ...)*
- *Java-based version of CLAIRE*
  - *Simpler Run-time (almost none)*
  - *Generate Human-maintenable code*
  - *Exit Strategy*
- *Simulation Environment*
  - *Finite Event simulation for stochastic optimization*
  - *Agent- based*
- *Optimization Software Platform*
  - *Do not extend CLAIRE but build software components*
  - *Business objects for call center scheduling or routing*

# *Future Releases*

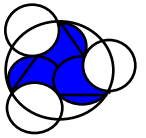


- v2.4
  - *Arrays (dynamic but constant length)*
  - *Improved compiler for floats*
- v2.5 (?)
  - *Re-usable C++ Kernel (shorter -simpler -faster)*
  - *Simplified Type System (safer)*
- v2.9
  - *Java Compiler (beta version)*
- v3.0
  - *Component Compiler (COM ?)*
  - *Improved Code Optimizer*

# RoadMap



# *$\mu$ CLAIRE: what's up ?*



## ■ *C++ Kernel*

- C++ Namespaces
- C++ class components
- Separated Reflective Description

## ■ *Type System*

- *Integer Intervals Only*
- *list[t] replaced by list (LISP) and list<t> (C++, C<t> = C[of = t])*
  - lists as objects vs. lists as values
  - safer (uniform for lists, sets and arrays)

## ■ *Optimization*

- *Native Floats*
- *Uniform C++ Object implementation (but integers)*
  - simpler debugging
  - faster generic methods
  - easier maintenance (takes more from C++: e.g., streams)