Vegan: ecological diversity

Jari Oksanen

Abstract

This document explains diversity related methods in **vegan**. The methods are briefly described, and the equations used them are given often in more detail than in their help pages. The methods discussed include common diversity indices and rarefaction, families of diversity indices, species abundance models, species accumulation models and beta diversity, extrapolated richness and probability of being a member of the species pool. The document is still incomplete and does not cover all diversity methods in **vegan**.

Keywords: diversity, Shannon, Simpson, Rényi, Hill number, Tsallis, rarefaction, species accumulation, beta diversity, species abundance, Fisher alpha, Fisher logarithmic series, Preston log-normal model, species abundance models, Whittaker plots, extended richness, taxonomic diversity, functional diversity, species pool.

Contents

1	Diversity indices Rarefaction Taxonomic and functional diversity					
2						
3						
	3.1	Taxonomic diversity: average distance of properties	5			
	3.2	Functional diversity: the height of property tree	6			
4	Species abundance models					
	4.1	Fisher and Preston	7			
	4.2	Ranked abundance distribution	8			
5	Species accumulation and beta diversity					
	5.1	Species accumulation models	9			
	5.2	Beta diversity	11			
6	Species pool					
	6.1	Number of unseen species	13			
	6.2	Pool size from a single site	15			
	6.3	Probability of pool membership	16			

~

The **vegan** package has two major components: multivariate analysis (mainly ordination), and methods for diversity analysis of ecological communities. This document gives an introduction to the latter. Ordination methods are covered in other documents. Many of the diversity functions were written by Roeland Kindt, Bob O'Hara and Péter Sólymos.

Most diversity methods assume that data are counts of individuals. The methods are used with other data types, and some people argue that biomass or cover are more adequate than counts of individuals of variable sizes. However, this document mainly uses a data set with counts: stem counts of trees on 1 ha plots in the Barro Colorado Island. The following steps make these data available for the document:

R> library(vegan)
R> data(BCI)

1. Diversity indices

Function diversity finds the most commonly used diversity indices:

$$H = -\sum_{i=1}^{S} p_i \log_b p_i$$
 Shannon-Weaver (1)

$$D_1 = 1 - \sum_{i=1}^{S} p_i^2$$
 Simpson (2)

$$D_2 = \frac{1}{\sum_{i=1}^{S} p_i^2} \qquad \text{inverse Simpson} \tag{3}$$

where p_i is the proportion of species i, and S is the number of species so that $\sum_{i=1}^{S} p_i = 1$, and b is the base of the logarithm. It is most common to use natural logarithms (and then we mark index as H'), but b = 2 has theoretical justification. The default is to use natural logarithms. Shannon index is calculated with:

R> H <- diversity(BCI)

which finds diversity indices for all sites.

Vegan does not have indices for evenness (equitability), but the most common of these, Pielou's evenness $J = H'/\log(S)$ is easily found as:

R> J <- H/log(specnumber(BCI))</pre>

where specnumber is a simple vegan function to find the numbers of species.

vegan also can estimate series of Rényi and Tsallis diversities. Rényi diversity of order a is:

$$H_a = \frac{1}{1 - a} \log \sum_{i=1}^{S} p_i^a \tag{4}$$

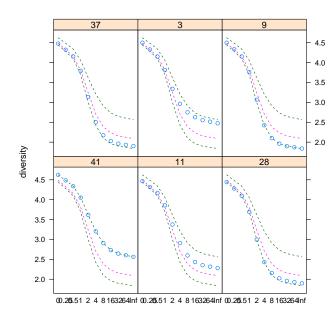


Figure 1: Rényi diversities in six randomly selected plots. The plot uses Trellis graphics with a separate panel for each site. The dots show the values for sites, and the lines the extremes and median in the data set.

or the corresponding Hill numbers $N_a = \exp(H_a)$. Many common diversity indices are special cases of Hill numbers: $N_0 = S$, $N_1 = \exp(H')$, $N_2 = D_2$, and $N_\infty = 1/(\max p_i)$. The corresponding Rényi diversities are $H_0 = \log(S)$, $H_1 = H'$, $H_2 = -\log(\sum p_i^2)$, and $H_\infty = -\log(\max p_i)$. Tsallis diversity of order q is:

$$H_q = \frac{1}{q-1} \left(1 - \sum_{i=1}^{S} p^q \right) . {5}$$

This corresponds to common diversity indices: $H_0 = S - 1$, $H_1 = H'$, and $H_2 = D_2$, and can be converted to the Hill number:

$$N_q = (1 - (q - 1)H_q)^{\frac{1}{1 - q}}. (6)$$

We select a random subset of five sites for Rényi diversities:

R> k <- sample(nrow(BCI), 6)
R> R <- renyi(BCI[k,])</pre>

We can really regard a site more diverse if all of its Rényi diversities are higher than in another site. We can inspect this graphically using the standard plot function for the renyi result (Fig. 1).

Finally, the α parameter of Fisher's log-series can be used as a diversity index:

R> alpha <- fisher.alpha(BCI)</pre>

2. Rarefaction

Species richness increases with sample size, and differences in richness actually may be caused by differences in sample size. To solve this problem, we may try to rarefy species richness to the same number of individuals. Expected number of species in a community rarefied from N to n individuals is:

$$\hat{S}_n = \sum_{i=1}^{S} (1 - q_i), \quad \text{where} \quad q_i = \binom{N - x_i}{n} / \binom{N}{n}$$
 (7)

where x_i is the count of species i, and $\binom{N}{n}$ is the binomial coefficient, or the number of ways we can choose n from N, and q_i give the probabilities that species i does not occur in a sample of size n. This is defined only when $N-x_i>n$, but for other cases $q_i=0$ or the species is sure to occur in the sample. The variance of rarefied richness is:

$$s^{2} = q_{i}(1 - q_{i}) + 2\sum_{i=1}^{S} \sum_{j>i} \left[\binom{N - x_{i} - x_{j}}{n} / \binom{N}{n} - q_{i}q_{j} \right]$$
 (8)

Equation 8 actually is of the same form as the variance of sum of correlated variables:

$$VAR\left(\sum x_i\right) = \sum VAR(x_i) + 2\sum_{i=1}^{S} \sum_{j>i} COV(x_i, x_j)$$
(9)

The number of stems per hectare varies in our data set:

R> quantile(rowSums(BCI))

```
0% 25% 50% 75% 100% 340.0 409.0 428.0 443.5 601.0
```

To express richness for the same number of individuals, we can use:

```
R> Srar <- rarefy(BCI, min(rowSums(BCI)))</pre>
```

Rarefaction curves often are seen as an objective solution for comparing species richness with different sample sizes. However, rank orders typically differ among different rarefaction sample sizes, rarefaction curves can cross.

As an extreme case we may rarefy sample size to two individuals:

```
R> S2 <- rarefy(BCI, 2)
```

This will not give equal rank order with the previous rarefaction richness:

[1] FALSE

Moreover, the rarefied richness for two individuals is a finite sample variant of Simpson's diversity index (or, more precisely of $D_1 + 1$), and these two are almost identical in BCI:

R> range(diversity(BCI, "simp") - (S2 -1))

[1] -0.002868298 -0.001330663

Rarefaction is sometimes presented as an ecologically meaningful alternative to dubious diversity indices, but the differences really seem to be small.

3. Taxonomic and functional diversity

Simple diversity indices only consider species identity: all different species are equally different. In contrast, taxonomic and functional diversity indices judge the differences of species are. Taxonomic and functional diversities are used in different fields of science, but they really have very similar reasoning, and either could be used either with taxonomic or functional properties of species.

3.1. Taxonomic diversity: average distance of properties

The two basic indices are called taxonomic diversity (Δ) and taxonomic distinctness (Δ^*):

$$\Delta = \frac{\sum \sum_{i < j} \omega_{ij} x_i x_j}{n(n-1)/2} \tag{10}$$

$$\Delta^* = \frac{\sum \sum_{i < j} \omega_{ij} x_i x_j}{\sum \sum_{i < j} x_i x_j}$$
(11)

These equations give the index values for a single site, and summation goes over species i and j, and ω are the taxonomic distances among taxa, x are species abundances, and n is the total abundance for a site. With presence—absence data, both indices reduce to the same index called Δ^+ , and for this it is possible to estimate standard deviation. There are two indices derived from Δ^+ : it can be multiplied with species richness 1 to give $s\Delta^+$, or it can be used to estimate an index of variation in taxonomic distinctness Λ^+ :

$$\Lambda^{+} = \frac{\sum \sum_{i < j} \omega_{ij}^{2}}{n(n-1)/2} - (\Delta^{+})^{2}$$
(12)

We still need the taxonomic differences among species (ω) to calculate the indices. These can be any distance structure among species, but usually it is found from established hierarchic taxonomy. Typical coding is that differences among species in the same genus is 1, among the same family it is 2 etc. However, the taxonomic differences are scaled to maximum 100 for easier comparison between different data sets and taxonomies. Alternatively, it is possible to scale steps between taxonomic level proportional to the reduction in the number of categories: if almost all genera have only one species, it does not make a great difference if two individuals belong to a different species or to a different genus.

Function taxondive implements indices of taxonomic diversity, and taxa2dist can be used to convert classification tables to taxonomic distances either with constant or variable step

¹This text normally uses upper case letter S for species richness, but lower case s is used here in accordance with the original papers on taxonomic diversity

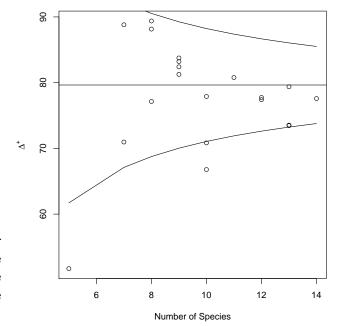


Figure \sim 2: Taxonomic diversity Δ^+ for the dune meadow data. The points are diversity values of single sites, and the funnel is their approximate confidence intervals (2× standard error).

lengths between successive categories. There is no taxonomic table for the BCI data in **vegan**² but there is such a table for the Dune meadow data (Fig. 2):

```
R> data(dune)
R> data(dune.taxon)
R> taxdis <- taxa2dist(dune.taxon, varstep=TRUE)
R> mod <- taxondive(dune, taxdis)</pre>
```

3.2. Functional diversity: the height of property tree

In taxonomic diversity the primary data were taxonomic trees which were transformed to pairwise distances among species. In functional diversity the primary data are species properties which are translated to pairwise distances among species and then to clustering trees of species properties. The argument for trees is that in this way a single deviant species will have a small influence, since its difference is evaluated only once instead of evaluating its distance to all other species.

Function treedive implements functional diversity defined as the total branch length in a trait dendrogram connecting all species, but excluding the unnecessary root segments of the tree. The example uses the taxonomic distances of the previous chapter. These are first converted to a hierarchic clustering (which actually were their original form before taxa2dist converted them into distances)

```
R> tr <- hclust(taxdis, "aver")
R> mod <- treedive(dune, tr)</pre>
```

²Actually I made such a classification, but taxonomic differences proved to be of little use in the Barro Colorado data: they only singled out sites with Monocots (palm trees) in the data.

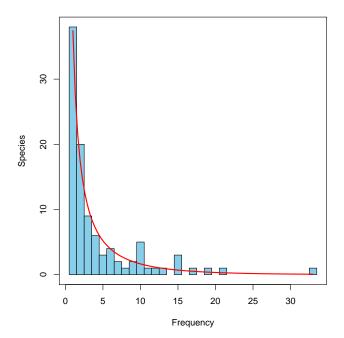


Figure 3: Fisher's log-series fitted to one randomly selected site (20).

4. Species abundance models

Diversity indices may be regarded as variance measures of species abundance distribution. We may wish to inspect abundance distributions more directly. **Vegan** has functions for Fisher's log-series and Preston's log-normal models, and in addition several models for species abundance distribution.

4.1. Fisher and Preston

In Fisher's log-series, the expected number of species \hat{f} with n individuals is:

$$\hat{f}_n = \frac{\alpha x^n}{n} \tag{13}$$

where α is the diversity parameter, and x is a nuisance parameter defined by α and total number of individuals N in the site, $x = N/(N - \alpha)$. Fisher's log-series for a randomly selected plot is (Fig. 3):

We already saw α as a diversity index. Now we also obtained estimate of standard error of α (these also are optionally available in fisher.alpha). The standard errors are based on the

second derivatives (curvature) of log-likelihood at the solution of α . The distribution of α is often non-normal and skewed, and standard errors are of not much use. However, fisherfit has a profile method that can be used to inspect the validity of normal assumptions, and will be used in calculations of confidence intervals from profile deviance:

```
R> confint(fish)
```

```
2.5 % 97.5 % 31.84517 52.29146
```

Preston's log-normal model is the main challenger to Fisher's log-series. Instead of plotting species by frequencies, it bins species into frequency classes of increasing sizes. As a result, upper bins with high range of frequencies become more common, and sometimes the result looks similar to Gaussian distribution truncated at the left.

There are two alternative functions for the log-normal model: prestonfit and prestondistr. Function prestonfit uses traditionally binning approach, and is burdened with arbitrary choices of binning limits and treatment of ties. It seems that Preston split ties between adjacent octaves: only half of the species observed once were in the first octave, and half were transferred to the next octave, and the same for all species at the octave limits occuring 2, 4, 8, 16...times. Function prestonfit can either split the ties or keep all limit cases in the lower octave. Function prestondistr directly maximizes truncated log-normal likelihood without binning data, and it is the recommended alternative. Log-normal models usually fit poorly to the BCI data, but here our random plot (number 20):

```
R> prestondistr(BCI[k,])
```

```
Preston lognormal model
```

Method: maximized likelihood to log2 abundances

No. of species: 100

```
mode width S0
0.9849822 1.6642110 27.1323499
```

```
Frequencies by Octave
```

```
0 1 2 3 4 5 6
Observed 19.00000 29.00000 22.00000 12.500 13.500000 3.000000 1.00000000
Fitted 22.77303 27.13125 22.52739 13.036 5.257389 1.477706 0.2894664
```

4.2. Ranked abundance distribution

An alternative approach to species abundance distribution is to plot logarithmic abundances in decreasing order, or against ranks of species. These are known as ranked abundance distribution curves, species abundance curves, dominance—diversity curves or Whittaker plots.

Function radfit fits some of the most popular models using maximum likelihood estimation:

$$\hat{a}_r = \frac{N}{S} \sum_{k=r}^{S} \frac{1}{k}$$
 brokenstick (14)

$$\hat{a}_r = N\alpha (1 - \alpha)^{r-1}$$
 preemption (15)

$$\hat{a}_r = \exp\left[\log(\mu) + \log(\sigma)\Phi\right]$$
 log-normal (16)

$$\hat{a}_r = N\hat{p}_1 r^{\gamma}$$
 Zipf (17)

$$\hat{a}_r = Nc(r+\beta)^{\gamma}$$
 Zipf-Mandelbrot (18)

Where \hat{a}_r is the expected abundance of species at rank r, S is the number of species, N is the number of individuals, Φ is a standard normal function, \hat{p}_1 is the estimated proportion of the most abundant species, and α , μ , σ , γ , β and c are the estimated parameters in each model.

It is customary to define the models for proportions p_r instead of abundances a_r , but there is no reason for this, and radfit is able to work with the original abundance data. We have count data, and the default Poisson error looks appropriate, and our example data set gives (Fig. 4):

```
R> rad <- radfit(BCI[k,])
R> rad
```

RAD models, family poisson No. of species 100, total abundance 429

	par1	par2	par3	Deviance	AIC	BIC
Null				45.067	331.756	331.756
Preemption	0.039794			33.728	322.417	325.022
Lognormal	0.93253	1.0384		19.018	309.707	314.917
Zipf	0.11174	-0.76181		42.503	333.192	338.402
Mandelbrot	8.5711	-1.7894	14.87	7.286	299.975	307.790

Function radfit compares the models using alternatively Akaike's or Schwartz's Bayesian information criteria. These are based on log-likelihood, but penalized by the number of estimated parameters. The penalty per parameter is 2 in AIC, and log S in BIC. Brokenstick is regarded as a null model and has no estimated parameters in **vegan**. Preemption model has one estimated parameter (α) , log-normal and Zipf models two $(\mu, \sigma, \text{ or } \hat{p}_1, \gamma, \text{ resp.})$, and Zipf-Mandelbrot model has three (c, β, γ) .

Function radfit also works with data frames, and fits models for each site. It is curious that log-normal model rarely is the choice, although it generally is regarded as the canonical model, in particular in data sets like Barro Colorado tropical forests.

5. Species accumulation and beta diversity

Species accumulation models and species pool models study collections of sites, and their species richness, or try to estimate the number of unseen species.

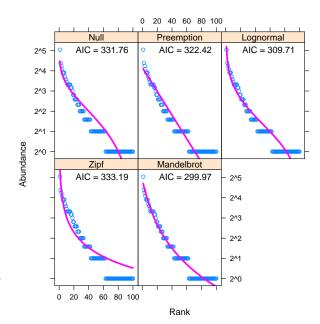


Figure 4: Ranked abundance distribution models for a random plot (no. 20). The best model has the lowest AIC.

5.1. Species accumulation models

Species accumulation models are similar to rarefaction: they study the accumulation of species when the number of sites increases. There are several alternative methods, including accumulating sites in the order they happen to be, and repeated accumulation in random order. In addition, there are three analytic models. Rarefaction pools individuals together, and applies rarefaction equation (7) to these individuals. Kindt's exact accumulator resembles rarefaction:

$$\hat{S}_n = \sum_{i=1}^{S} (1 - p_i), \text{ where } p_i = \binom{N - f_i}{n} / \binom{N}{n}$$
(19)

where f_i is the frequency of species i. Approximate variance estimator is:

$$s^{2} = p_{i}(1 - p_{i}) + 2\sum_{i=1}^{S} \sum_{j>i} \left(r_{ij} \sqrt{p_{i}(1 - p_{i})} \sqrt{p_{j}(1 - p_{j})} \right)$$
(20)

where r_{ij} is the correlation coefficient between species i and j. Both of these are unpublished: eq. 19 was developed by Roeland Kindt, and eq. 20 by Jari Oksanen. The third analytic method was suggested by Coleman:

$$S_n = \sum_{i=1}^{S} (1 - p_i), \text{ where } p_i = \left(1 - \frac{1}{n}\right)^{f_i}$$
 (21)

and he suggested variance $s^2 = p_i(1-p_i)$ which ignores the covariance component. In addition, eq. 21 does not properly handle sampling without replacement and underestimates the species accumulation curve.

The recommended is Kindt's exact method (Fig. 5):

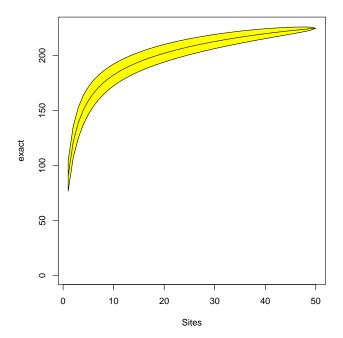


Figure 5: Species accumulation curve for the BCI data; exact method.

R> sac <- specaccum(BCI)
R> plot(sac, ci.type="polygon", ci.col="yellow")

5.2. Beta diversity

Whittaker divided diversity into various components. The best known are diversity in one spot that he called alpha diversity, and the diversity along gradients that he called beta diversity. The basic diversity indices are indices of alpha diversity. Beta diversity should be studied with respect to gradients, but almost everybody understand that as a measure of general heterogeneity: how many more species do you have in a collection of sites compared to an average site.

The best known index of beta diversity is based on the ratio of total number of species in a collection of sites (S) and the average richness per one site $(\bar{\alpha})$:

$$\beta = S/\bar{\alpha} - 1 \tag{22}$$

Subtraction of one means that $\beta = 0$ when there are no excess species or no heterogeneity between sites. For this index, no specific functions are needed, but this index can be easily found with the help of **vegan** function **specnumber**:

R> ncol(BCI)/mean(specnumber(BCI)) - 1

Γ17 1.478519

The index of eq. 22 is problematic because S increases with the number of sites even when sites are all subsets of the same community. Whittaker noticed this, and suggested the index to be found from pairwise comparison of sites. If the number of shared species in two sites is

a, and the numbers of species unique to each site are b and c, then $\bar{\alpha} = (2a + b + c)/2$ and S = a + b + c, and index 22 can be expressed as:

$$\beta = \frac{a+b+c}{(2a+b+c)/2} - 1 = \frac{b+c}{2a+b+c}$$
 (23)

This is the Sørensen index of dissimilarity, and it can be found for all sites using **vegan** function **vegdist** with binary data:

```
R> beta <- vegdist(BCI, binary=TRUE)
R> mean(beta)
[1] 0.3399075
```

There are many other definitions of beta diversity in addition to eq. 22. All commonly used indices can be found using betadiver. The indices in betadiver can be referred to by subscript name, or index number:

R> betadiver(help=TRUE)

```
1 \text{ "w"} = (b+c)/(2*a+b+c)
2"-1" = (b+c)/(2*a+b+c)
3 \text{ "c"} = (b+c)/2
4 \text{ "wb"} = b+c
5 \text{ "r"} = 2*b*c/((a+b+c)^2-2*b*c)
6 "I" = \log(2*a+b+c)-2*a*\log(2)/(2*a+b+c)-((a+b)*\log(a+b)+(a+c)*\log(a+c))/(2*a+b+c)
7 "e" = \exp(\log(2*a+b+c)-2*a*\log(2)/(2*a+b+c)-((a+b)*\log(a+b)+(a+c)*\log(a+c))/(2*a+b+c))-1
8 "t" = (b+c)/(2*a+b+c)
9 \text{ "me"} = (b+c)/(2*a+b+c)
10 "j" = a/(a+b+c)
11 "sor" = 2*a/(2*a+b+c)
12 "m" = (2*a+b+c)*(b+c)/(a+b+c)
13 "-2" = pmin(b,c)/(pmax(b,c)+a)
14 "co" = (a*c+a*b+2*b*c)/(2*(a+b)*(a+c))
15 "cc" = (b+c)/(a+b+c)
16 \text{ "g"} = (b+c)/(a+b+c)
17 "-3" = pmin(b,c)/(a+b+c)
18 "1" = (b+c)/2
19 "19" = 2*(b*c+1)/((a+b+c)^2+(a+b+c))
20 "hk" = (b+c)/(2*a+b+c)
21 "rlb" = a/(a+c)
22 "sim" = pmin(b,c)/(pmin(b,c)+a)
23 "gl" = 2*abs(b-c)/(2*a+b+c)
z'' = (\log(2) - \log(2*a+b+c) + \log(a+b+c))/\log(2)
```

Some of these indices are duplicates, and many of them are well known dissimilarity indices. One of the more interesting indices is based on the Arrhenius species—area model

$$\hat{S} = cX^z \tag{24}$$

where X is the area (size) of the patch or site, and c and z are parameters. Parameter c is uninteresting, but z gives the steepness of the species area curve and is a measure of beta

diversity. In islands typically $z \approx 0.3$. This kind of islands can be regarded as subsets of the same community, indicating that we really should talk about gradient differences if $z \gtrsim 0.3$. We can find the value of z for a pair of plots using function betadiver:

The size X and parameter c cancel out, and the index gives the estimate z for any pair of sites.

Function betadisper can be used to analyse beta diversities with respect to classes or factors. There is no such classification available for the Barro Colorado Island data, and the example studies beta diversities in the management classes of the dune meadows (Fig. 6):

```
R> data(dune)
R> data(dune.env)
R> z <- betadiver(dune, "z")</pre>
R> mod <- with(dune.env, betadisper(z, Management))</pre>
R> mod
       Homogeneity of multivariate dispersions
Call: betadisper(d = z, group = Management)
No. of Positive Eigenvalues: 12
No. of Negative Eigenvalues: 7
Average distance to centroid:
          ΗF
                NM
0.3080 0.2512 0.4406 0.3635
Eigenvalues for PCoA axes:
 PCoA1
                PCoA3
                        PCoA4
                               PCoA5
                                       PCoA6
                                              PCoA7
                                                      PCoA8
                                                             PCoA9
         PCoA2
 1.6547
        0.8870 0.5334
                       0.3744
                              0.2873
                                      0.2245
                                            0.1613
                                                    0.0810
                                                            0.0652
 PCoA10
        PCoA11 PCoA12 PCoA13 PCoA14
                                      PCoA15 PCoA16
                                                    PCoA17
        0.0353
 PCoA19
-0.0828
```

6. Species pool

6.1. Number of unseen species

Species accumulation models indicate that not all species were seen in any site. These unseen species also belong to the species pool. Functions specpool and estimateR implement some methods of estimating the number of unseen species. Function specpool studies a collection of sites, and estimateR works with counts of individuals, and can be used with a single site.

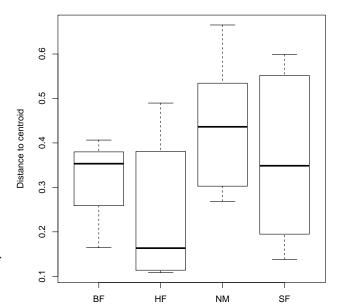


Figure 6: Box plots of beta diversity measured as the average steepness (z) of the species area curve in the Arrhenius model $S = cX^z$ in Management classes of dune meadows.

Both functions assume that the number of unseen species is related to the number of rare species, or species seen only once or twice.

Function specpool implements the following models to estimate the pool size S_p :

$$S_p = S_o + \frac{f_1^2}{2f_2}$$
 Chao (25)

$$S_p = S_o + f_1 \frac{N-1}{N}$$
 1st order Jackknife (26)

$$S_p = S_o + f_1 \frac{2N - 3}{N} + f_2 \frac{(N - 2)^2}{N(N - 1)}$$
 2nd order Jackknife (27)

$$S_p = S_o + \sum_{i=1}^{S_o} (1 - p_i)^N$$
 Bootstrap (28)

Here S_o is the observed number of species, f_1 and f_2 are the numbers of species observed once or twice, N is the number of sites, and p_i are proportions of species. The idea in jackknife seems to be that we missed about as many species as we saw only once, and the idea in bootstrap that if we repeat sampling (with replacement) from the same data, we miss as many species as we missed originally.

The variance estimators of Chao is:

$$s^2 = f_2 \left(\frac{G^4}{4} + G^3 + \frac{G^2}{2} \right), \text{ where } G = \frac{f_1}{f_2}$$
 (29)

The variance of the first-order jackknife is based on the number of "singletons" r (species occurring only once in the data) in sample plots:

$$s^{2} = \left(\sum_{i=1}^{N} r_{i}^{2} - \frac{f_{1}}{N}\right) \frac{N-1}{N} \tag{30}$$

Variance of the second-order jackknife is not evaluated in specpool (but contributions are welcome). For the variance of bootstrap estimator, it is practical to define a new variable $q_i = (1 - p_i)^N$ for each species:

$$s^{2} = \sum_{i=1}^{S_{o}} q_{i}(1 - q_{i}) + 2 \sum \sum Z_{p}, \text{ where}$$

$$Z_{p} = \dots$$
(31)

The extrapolated richness values for the whole BCI data are:

R> specpool(BCI)

```
Species chao chao.se jack1 jack1.se jack2 boot
All 225 236.6053 6.659395 245.58 5.650522 247.8722 235.6862
boot.se n
All 3.468888 50
```

If the estimation of pool size really works, we should get the same values of estimated richness if we take a random subset of a half of the plots (but this is rarely true):

6.2. Pool size from a single site

The specpool function needs a collection of sites, but there are some methods that estimate the number of unseen species for each single site. These functions need counts of individuals, and species seen only once or twice, or other rare species, take the place of species with low frequencies. Function estimateR implements two of these methods:

R> estimateR(BCI[k,])

```
20
S.obs 100.000000
S.chao1 133.476190
se.chao1 15.441519
S.ACE 147.592810
se.ACE 6.621289
```

Chao's method is similar as above, but uses another, "unbiased" equation. ACE is based on

rare species also:

$$S_p = S_{\text{abund}} + \frac{S_{\text{rare}}}{C_{\text{ACE}}} + \frac{a_1}{C_{\text{ACE}}} \gamma^2 \quad \text{where}$$

$$C_{\text{ACE}} = 1 - \frac{a_1}{N_{\text{rare}}}$$

$$\gamma^2 = \frac{S_{\text{rare}}}{C_{\text{ACE}}} \sum_{i=1}^{10} i(i-1)a_1 \frac{N_{\text{rare}} - 1}{N_{\text{rare}}}$$
(32)

Now a_1 takes the place of f_1 above, and means the number of species with only one individual. Here $S_{\rm abund}$ and $S_{\rm rare}$ are the numbers of species of abundant and rare species, with an arbitrary upper limit of 10 individuals for a rare species, and $N_{\rm rare}$ is the total number of individuals in rare species.

The pool size is estimated separately for each site, but if input is a data frame, each site will be analysed.

If log-normal abundance model is appropriate, it can be used to estimate the pool size. Log-normal model has a finite number of species which can be found integrating the log-normal:

$$S_p = S_\mu \sigma \sqrt{2\pi} \tag{33}$$

where S_{μ} is the modal height or the expected number of species at maximum (at μ), and σ is the width. Function veiledspec estimates this integral from a model fitted either with prestondistr or prestonfit, and fits the latter if raw site data are given. Log-normal model may fit poorly, but we can try:

R> veiledspec(prestondistr(BCI[k,]))

Extrapolated Observed Veiled 113.18418 100.00000 13.18418

R> veiledspec(BCI[k,])

Extrapolated Observed Veiled 122.24639 100.00000 22.24639

6.3. Probability of pool membership

Beals smoothing was originally suggested as a tool of regularizing data for ordination. It regularizes data too strongly, but it has been suggested as a method of estimating which of the missing species could occur in a site, or which sites are suitable for a species. The probability for each species at each site is assessed from other species occurring on the site.

Function beals implement Beals smoothing:

R> smo <- beals(BCI)

We may see how the estimated probability of occurrence and observed numbers of stems relate in one of the more familiar species. We study only one species, and to avoid circular reasoning we do not include the target species in the smoothing (Fig. 7):

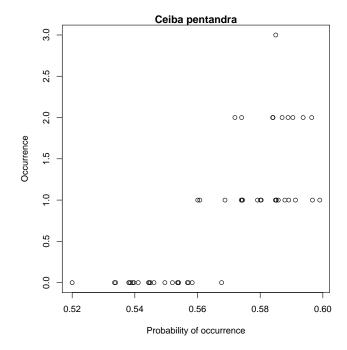


Figure 7: Beals smoothing for *Ceiba* pentandra.

R> j <- which(colnames(BCI) == "Ceiba.pentandra")R> plot(beals(BCI, species=j, include=FALSE), BCI[,j], main="Ceiba pentandra", xlab="Probability of occ

About this version:

Id: diversity-vegan. Rnw 2259 2012-08-23 15:13:58Z jarioksa processed with vegan 2.0-5 in R Under development (unstable) (2012-10-08 r60901) on October 8, 2012