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Faculty: IT

Course Name: Digital Computer Fundamentals

Course Code: MATH 8127

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Report: Individual Assignment

Adventist University of Central Africa (AUCA)

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Department: Software Engineering

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Report: Number System, Digital Logic and Boolean Algebra

Individual Assignment

Question 1 Binary subtraction and 2's Complement Concept

a) Essential of 2's Complement in binary subtraction with signed numbers:
- 2's Complement is a method we use in computers to show a negative numbers in binary, because computers can only add easily, they are not good at subtracting directly.

So instead of subtraction, we turn it into addition using 2's complement

Example with 4 digits

$$A = 0110$$

$$B = 0110$$

If you try to subtract directly, your logic will break down and lose a focus.

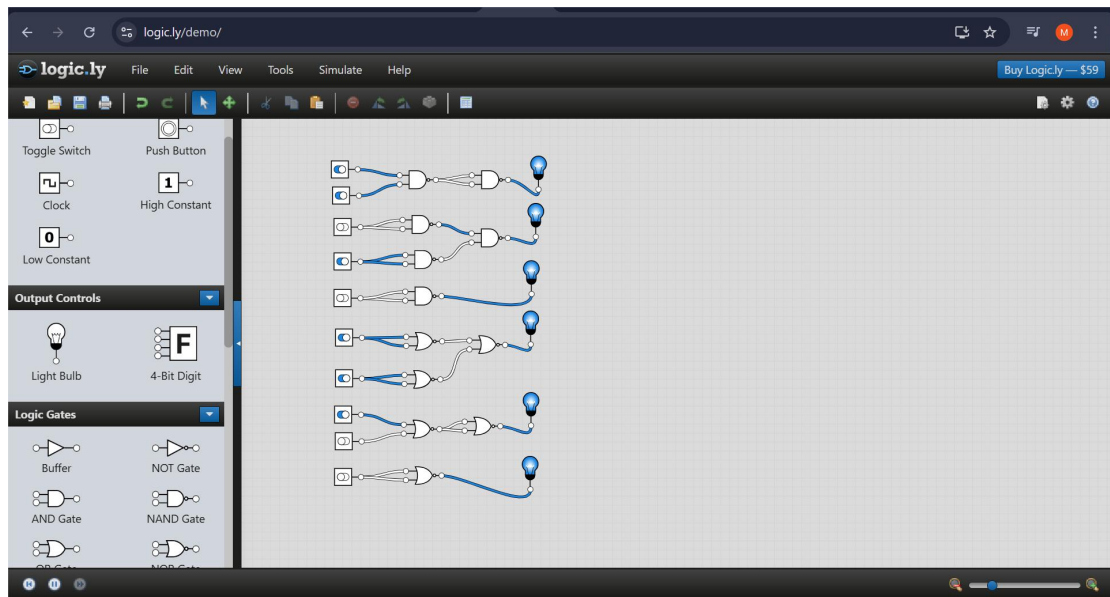
Here is best way to do it:

Step 1 turn B variable into 1's Complement, which is inversion of B values

$B = [0001]$ 1's Complement, again add 1 on 1's comp of B to get two's com

$$0001 + 1 = 0010$$

0001
+ 1
0010



Now, in our example we have $A-B$ and B is large

So if we turn it into addition, it will be $A+(-B)$ where $(-B)$ is B 's complement and 2's complement of B is 0010

So now we take value of A and add to 2's complement of B

$$A = 0110$$
$$B_{2's\text{com}} = 0010$$

$$\begin{array}{r} 0110 \\ + 0010 \\ \hline 1000 \end{array}$$

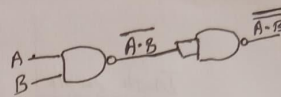
$$\text{Now } A - (-B) = 1000$$

Question 2: a) Design AND using NAND gate:

Truth table

A	B	\bar{A}	\bar{B}	$\bar{A} \cdot \bar{B}$
1	0	0	1	0
1	1	0	0	0
0	0	1	1	1
0	1	1	0	0

Logic gates

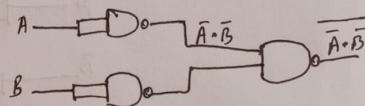


b) Design OR gate using only NAND gates:

Truth table

A	B	\bar{A}	\bar{B}	$\bar{A} \cdot \bar{B}$	$\overline{\bar{A} \cdot \bar{B}}$
0	1	1	0	0	1
0	0	1	1	1	0
1	1	0	0	0	1
1	0	0	1	0	1

Logic gate with NAND

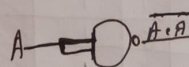


c) Design NOT gate using only NAND gate.

Truth table

A	\bar{A}	$\bar{A} \cdot \bar{A}$
1	0	0
0	1	1

Logic gate

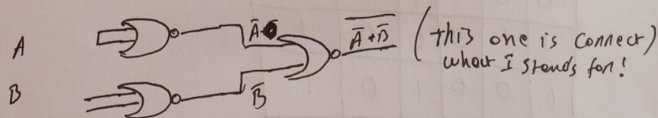
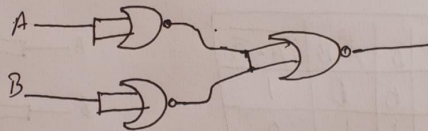


d) Design an AND gate using NOR gate

Truth table

A	B	\bar{A}	\bar{B}	$\bar{A} + \bar{B}$	$\bar{B} + \bar{A}$	$(\bar{A} + \bar{B}) + (\bar{B} + \bar{A})$	$(\bar{A} + \bar{B}) + (\bar{B} + \bar{A})$
0	0	1	1	1	1	1	0
0	1	1	0	1	0	1	0
1	0	0	1	0	1	1	0
1	1	0	0	0	0	0	1

Logic gate

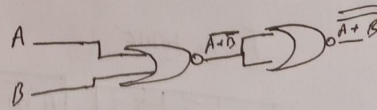


e) Design OR gate using NOR gates

Truth table

A	B	\bar{A}	\bar{B}	$\bar{A} + \bar{B}$	$\overline{\bar{A} + \bar{B}}$
0	0	1	1	1	0
0	1	1	0	1	1
1	0	0	1	1	1
1	1	0	0	0	1

Logic gates



Truth table

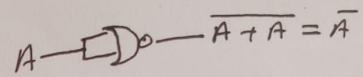
A	B	A + B	$\bar{A} + \bar{B}$	$\overline{\bar{A} + \bar{B}}$
0	0	0	1	0
0	1	1	0	1
1	0	1	0	1
1	1	1	0	1

f) Design ~~and~~ NOT gate using only NOR

Truth table

A	\bar{A}	$\overline{A+A}$
0	1	1
1	0	0

Logic gate



Question 3 Boolean Algebra - Simplifying Expression

$$a) AB + A\bar{B} + \bar{A}B$$

$$\Rightarrow A(B + \bar{B}) + \bar{A}B \quad [\text{by factoring } A \text{ as common factor}]$$

$$= A(1) + \bar{A}B \quad [\text{by } B + \bar{B} = 1]$$

$$= A + \bar{A}B \quad [\text{by } A \cdot 1 = A \text{ Identity Law}]$$

$$= A + B(A + \bar{A}) \quad [\text{by Complement}]$$

$$= A + B(1) \quad [\text{by } A + \bar{A} = 1]$$

$$= \boxed{A + B} \quad [\text{by } B(1) = B]$$

$$\boxed{AB + A\bar{B} + \bar{A}B = A + B}$$

$$b) (A+B)(A+\bar{B})(\bar{A}+B) =$$

$$(AA + A\bar{B} + BA + B\bar{B})(\bar{A} + B) \quad [\text{by distributive law}]$$

$$(A + A\bar{B} + BA + 0)(\bar{A} + B) \quad [\text{by Complement law, where } A \cdot A = A, B \cdot \bar{B} = 0]$$

$$A(\bar{B} + B)(\bar{A} + B) \quad [\text{by distributive law}]$$

$$A(1)(\bar{A} + B) \quad [\text{Complement law } \bar{B} + B = 1]$$

$$A(\bar{A} + B) \quad [\text{by identity law } A \cdot 1 = A]$$

$$A\bar{A} + AB \quad [\text{by distributive law}]$$

$$0 + AB \quad [\text{by identity law } A \cdot \bar{A} = 0]$$

$$\boxed{AB} \quad [\text{by identity law } 0 + AB = AB]$$

$$\boxed{AB} \Rightarrow \boxed{(A+B)(A+\bar{B})(\bar{A}+B) = AB}$$

$$c) \overline{A+BC} + A\bar{B}$$

$$\bar{A} \cdot \bar{B}C + A\bar{B} \quad [\text{by De Morgan's Law}]$$

$$(\bar{A} \cdot (\bar{B} + C)) + A\bar{B} \quad [\text{by De Morgan's Law}]$$

$$\bar{A} \cdot \bar{B} + \bar{A}C + A\bar{B} \quad [\text{by distributive}]$$

$$\bar{A} \cdot \bar{B} + A\bar{B} + \bar{A}C \quad [\text{by Commutative Law}]$$

$$\bar{B}(\bar{A} + A) + \bar{A}C \quad [\text{by Distributive Law}]$$

$$\bar{B}(1) + \bar{A}C \quad [\text{by Complement } \bar{A} + A = 1]$$

$$\bar{B} + \bar{A}C \quad [\text{by identity } \bar{B}(1) = \bar{B}]$$

$$\boxed{\bar{B} + \bar{A}C}$$

$$\boxed{\overline{A+BC} + A\bar{B} = \bar{B} + \bar{A}C}$$

$$d) AB + A\bar{B} + \bar{A}B + A\bar{B}$$

$$A(B + \bar{B}) + \bar{A}B + A\bar{B} \quad [\text{by distributive}]$$

$$A(1) + \bar{A}B + A\bar{B} \quad [\text{by Complement } B + \bar{B} = 1]$$

$$A + \bar{A}B + A\bar{B} \quad [\text{by identity } A(1) = A]$$

$$A + B(\bar{A} + A) \quad [\text{by distributive}]$$

$$A + B(1) \quad [\text{by Complement } \bar{A} + A = 1]$$

$$\boxed{A + B}$$

$$[\text{by identity } B \cdot 1 = B]$$

$$e) \overline{\overline{A+B}} + \overline{\overline{C+D}}$$

$$\overline{\overline{A+B}} \cdot \overline{\overline{C+D}} \quad [\text{by De Morgan's Law}]$$

$$\overline{\overline{A}} \cdot \overline{\overline{B}} \cdot \overline{\overline{C}} \cdot \overline{\overline{D}} \quad [\text{by De Morgan's Law}]$$

$$A \cdot B \cdot C \cdot D \quad [\text{Negation Cancels}]$$

$$\boxed{A \cdot B \cdot C \cdot D}$$

$$f) \overline{\overline{A+B} \cdot \overline{C+D}}$$

$$\overline{\overline{A+B}} + \overline{\overline{C+D}} \quad [\text{by De Morgan's Law}]$$

$$\overline{\overline{A+B}} + \overline{\overline{C+D}} \quad [\text{by De Morgan's Law}]$$

$$\boxed{A+B+C+D} \quad [\text{by Negation Cancels}]$$

$$g) \overline{\overline{A \cdot (\overline{B+C})} + \overline{D+E}}$$

$$\overline{\overline{A \cdot (\overline{B+C})}} \cdot \overline{\overline{D+E}} \quad [\text{by De Morgan's Law}]$$

$$\overline{\overline{A \cdot (\overline{B+C})}} \cdot \overline{\overline{D+E}} \quad [\text{by De Morgan's Law}]$$

$$A \cdot \overline{\overline{B+C}} \cdot \overline{\overline{D+E}} \quad [\text{by De Morgan's Law}]$$

$$A \cdot \overline{B+C} \cdot \overline{D+E} \quad [\text{by Negation Cancels}]$$

$$h) \overline{\overline{(\overline{A+B}) \cdot (\overline{C+D})} + \overline{E}}$$

$$\overline{\overline{(\overline{A+B}) \cdot (\overline{C+D})}} + \overline{\overline{E}} \quad [\text{by De Morgan's Law}]$$

$$\overline{\overline{(\overline{A+B}) \cdot (\overline{C+D})}} + \overline{\overline{E}} \quad [\text{by De Morgan's Law}]$$

$$(\overline{\overline{A+B}}) \cdot (\overline{\overline{C+D}}) + \overline{\overline{E}} \quad [\text{by De Morgan's Law}]$$

$$\overline{A+B} \cdot \overline{C+D} + \overline{E} \quad [\text{by Complement}]$$

$$\boxed{\overline{A+B} \cdot \overline{C+D} + \overline{E}}$$