

## MATH8213 ASSIGNMENT1

**Q1.** In 2D affine space endowed with orthonormal frame, given a triangle with vertices

$$A(4, 4), B(-6, -1), C(-2, 4) \rightarrow T1; \quad A(5, 4), B(-1, 2), C(5, 1) \rightarrow T2$$

$$A(-2, -3), B(1, 4), C(3, 1) \rightarrow T3; \quad A(-2, 3), B(4, 1), C(6, -5) \rightarrow T4$$

- a) Using the scalar product, find the perimeter, area and angles of the triangle
- b) Use 2D Geo-Gebra to plot the triangle

**Q2.** In 3D Euclidean space equipped with orthonormal frame, given a tetrahedron with vertices

$$A(2, -1, 1), B(5, 5, 4), C(3, 2, -1), D(4, 1, 3) \rightarrow T4, \quad A(3, -1, 0), B(0, -7, 3), C(-2, 1, -1), D(3, 2, 6) \rightarrow T3$$

$$A(2, 1, -1), B(3, 0, 2), C(5, 1, 1), D(0, -1, 3) \rightarrow T2; \quad A(2, 3, 7), B(1, 4, 9), C(-4, 0, 5), D(-2, 3, -5) \rightarrow T1$$

a) Using scalar or cross or box products, find:

- i) The perimeter, and angles of the face  $ABC$
- ii) The area and volume of the tetrahedron

b) Use 3D Geo-Gebra to plot the tetrahedron

**Q3.** The polar coordinates of the end points of the segment  $AB$  are:

$$A\left(8, \frac{-2\pi}{3}\right), B\left(6, \frac{\pi}{3}\right) \rightarrow T1 \& 4; \quad A\left(12, \frac{4\pi}{9}\right), B\left(12, \frac{4\pi}{9}\right) \rightarrow T2 \& 3$$

- a) Find the length of the segment
- b) Determine the polar coordinates of the midpoint of the segment
- c) Plot the above given line segment and its mid-point

**Q4.** Use 2D-Geogebra and plot on the same chart the graphs of the following 2d-curves expressed in polar coordinates.

$$a) r = 3(1 \pm \cos \theta); \quad r = 3(1 \pm \cos \theta); \quad b) r = 6 \cos 2\theta; \quad r = 6 \sin 2\theta$$

$$c) r = 0.125\theta; \quad r = 2^{-\theta}; \quad r = 2^{\theta}; \quad d) r = 4\sqrt{\cos 2\theta}; \quad r = 4\sqrt{\sin 2\theta} \quad \text{All teams will do Q4}$$

*Note: Teams Leaders are requested to ensure if their team members are working in team spirit way.*

**Ti stands for Team i (i=1,2,3,4)**

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**Prepared by Theoneste Hakizimana**