Division of Science



Department of Mathematics

The City College of New York

MATH195 – Precalculus

Fall 2024 Final Exam Date:

December 17th, 2024

First Name: Last Name:

EMPLID: ___

Circle your section (for example, XX, Instructor, Days, Hours):

AB, Bharathan; M,W 8:00 AM to 9:40 AM BC, Chung Lo; M,W 10:00 AM to 11:40 AM BC2, Gadsby; M,W 10:00 AM to 11:40 AM CD, Scott; M, W 12:00 PM to 1:40 PM EF, Dacanay, M, W 2:00 PM to 3:40 PM FG, Okpo; M, W 4:00 PM to 5:40 PM GH, Ortiz; M, W 6:00 PM to 7:40 PM

KL, Rutter; T, R 8:00 AM to 9:40 AM LM, Bam; T, R 10:00 AM to 11:40 AM (LM2, Mim; T, R 10:00 AM to 11:40 AM PR, Videen; T, R 2:00 PM to 3:40 PM RS, Nussenzveig; T, R 4:00 PM to 5:40 PM ST, Ajarar; T, R 6:00 PM to 7:40 PM

Directions:

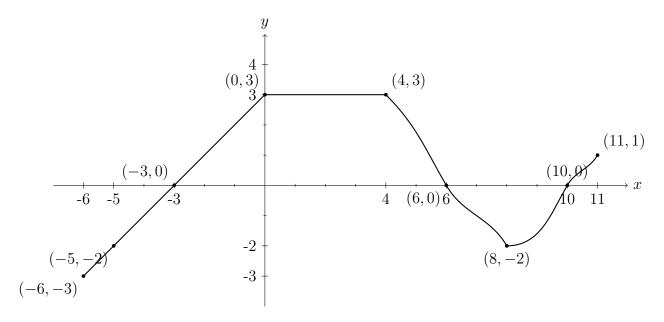
- NO notes, calculators, or other electronic devices allowed. All electronic devices must be turned off and placed out of sight or they will be confiscated for the duration of the exam.
- Read each problem carefully. Unless otherwise instructed, be sure to show your work.
- Remember that it is your **responsibility** to answer each question clearly and in a way that convinces the grader that you understand how to solve each problem.

- GOOD LUCK!

You can use this page as scrap.	However any work	done on this page wi	ll not be graded.

Answer all 21 questions. You **must show all of your work** as neatly and clearly as possible and **indicate** the final answer in the box for each non-graph question. For all graph questions, you should sketch your graph on the grid provided.

1. (4 points) The graph of y = f(x) is given below. Use the graph to find the domain of f. Express your answer using interval notation.



Write your answer in the box below:

2. (4 points) Let
$$f(x) = \begin{cases} x - 1 & \text{if } x \ge 0 \\ -x^2 & \text{if } x < 0 \end{cases}$$
 and let $g(x) = \ln(x + 2)$ for $x > -2$. Find $f(g(-1))$.

Write your answer in the box below:



- 3. (4 points) Let $f(x) = -2\sin(x \frac{\pi}{2}) + 1$.
 - (a) $(1\frac{1}{2} \text{ point})$ Find the amplitude of f(x). Write your answer in the box below:



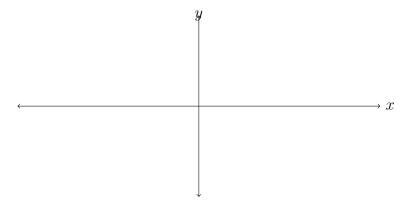
(b) $(1\frac{1}{2} \text{ point})$ Find the period of f(x). Write your answer in the box below:



(c) (1 point) Find the horizontal shift b of f(x). Write your answer in the box below:

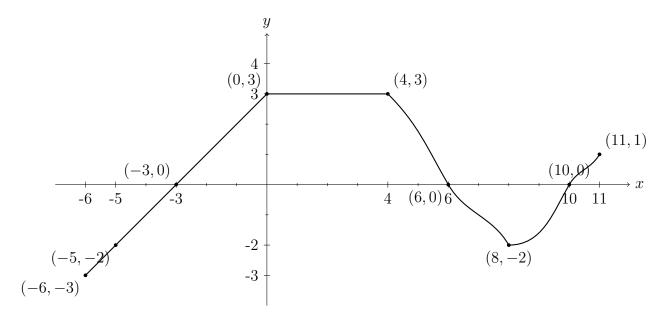


(d) (2 points) Sketch one complete period of the graph of f(x) in the appropriate interval $\left[b,b+\frac{2\pi}{k}\right]$.



4. (4 points) Find the radian angle θ circular arc is 25.	when the radius r of t	the circle is 10 and the lengt	sh s of the
Write your answer in the box below:			
5. (4 points) Evaluate $\sin\left(\frac{\pi}{3} + \frac{\pi}{6}\right)$. Write your answer in the box below:			
			Page 3

6. (4 points) Use the graph of the function f below to find the average rate of change of f between x = 0 and x = 4.



Write your answer in the box below:



7. (4 points) Find $\sin 2\theta + \cos \theta$ if $\tan \theta = \frac{3}{4}$ and θ is in Quadrant III.

Write your answer in the box below:



	Theorem to sho	by that $x + 2$ is	a factor of $P(x)$.	Show your w	ork in
) Using the resulting the box b		, factor $P(x)$ con	mpletely.		
		, factor $P(x)$ con	mpletely.		
		, factor $P(x)$ con	mpletely.		

9. (4 points) Evaluate and simplify sin	$n^{-1}\left(\frac{\sqrt{2}}{2}\right) + \cos^{-1}\left(\frac{\sqrt{2}}{2}\right)$. Express your answer in radians.
Write your answer in the box below:		
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10. (4 points) Evaluate the difference quotient $\frac{f(1+h)-f(1)}{h}$ when $f(x)=x^2+2x$. Write your answer in the box below:



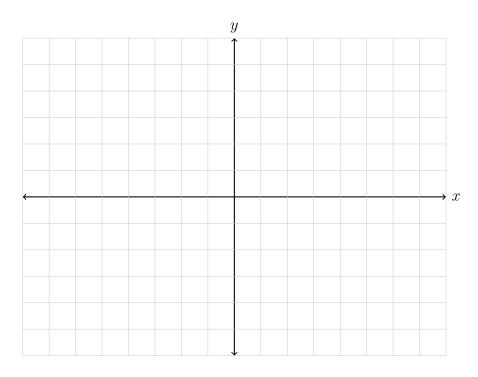
11. (8 points) Consider the equation of the ellipse $x^2 + 4x + 4y^2 - 8y + 4 = 0$.

(a) (4 points) Write the equation in standard form.

Write your answer in the box below:



(b) (4 points) Graph the ellipse on the axes below.



12. (4 points) Solve the trigonometric equation $4\sin\theta + 3\sqrt{3} = \sqrt{3}$, for all values of	θ on the interval
$0 \le \theta \le 2\pi$. Write your answer in the box below:	

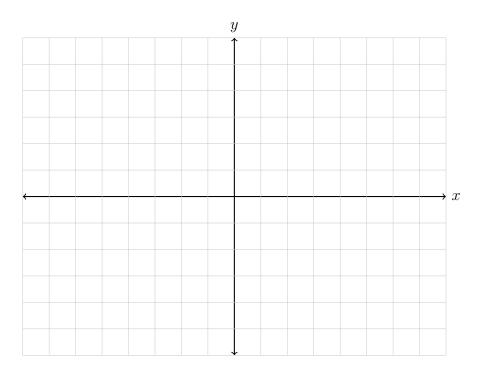


13. (4 points) Use the table below to solve the equation $f(x) = \frac{\sqrt{3}}{2}$.

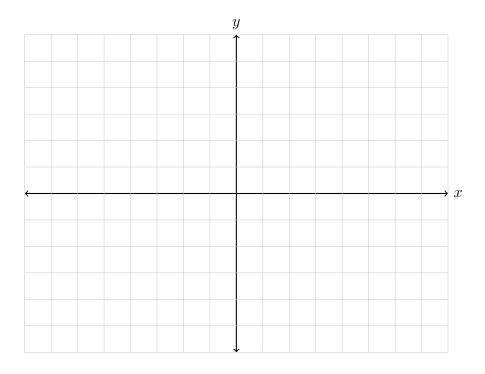
x	0	$\frac{\pi}{6}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{5\pi}{6}$	π
f(x)	0	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	0

Write your answer in the box below:

14. (4 points) Make a rough sketch of the graph $g(x) = x^3 - 2x^2 - 3x$. Label all intercepts on your graph.



15. (4 points) Graph the function $f(x) = -\log_3(x+3)$ by transforming the graph of $y = \log_3(x)$. Label the vertical asymptote and all intercepts on your graph.

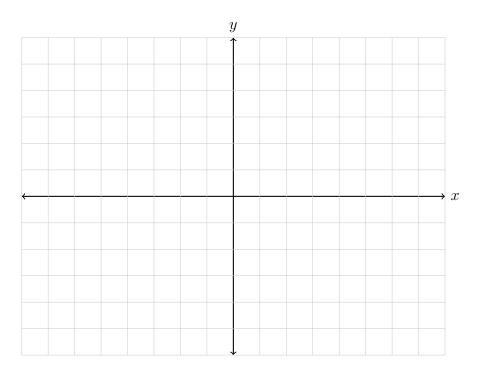


16. (4 points) Let $f(x) = \frac{4}{4-x}$. Find $f^{-1}(2)$.

Write your answer in the box below:

1			

17. (4 points) Sketch the graph of $f(x) = -e^x + 2$. Label the horizontal asymptote and intercepts on your graph.



18. $(4 points)$ Find the distance betw	veen the points $(-2,5)$ and $(10,0)$.
Write your answer in the box below:	
19. (4 points) Solve the exponential ed of logarithms.	quation $2(5+3^{x+1}) = 100$ for x . Express your answer in terms
Write your answer in the box below:	

20. (8 points) Consider the system of nonlinear equations.

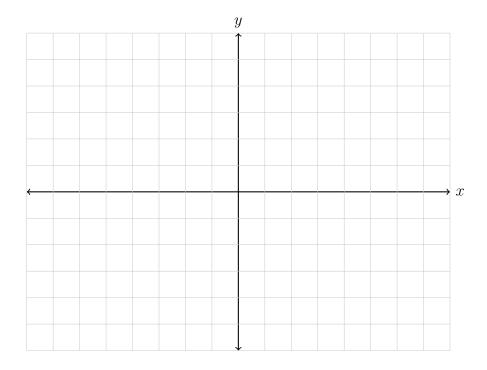
$$\begin{cases} x^2 + y^2 = 1\\ y - x = 1 \end{cases}$$

(a) (4 points) Solve the system of equations. Write your answers in coordinate point form.

Write your answer in the box below:



(b) (4 points) Graph the system on the axes below. Clearly label the solutions to the system.



21. (8 points) The grey squirrel popurate of 8 percent per year. It is estimated	_	,	growth
(a) (4 points) Find a function that	models the population	t years after 2013 ($t = 0$ for 20)	13).
Write your answer in the box below:			
(b) (4 points) After how many year	s will the grey squirrel	population reach 25,000?	
Write your answer in the box below:			
		P	age 13

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