

# Grammars for Mutation Testing

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# Saarbrücken







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# Fuzzing

## Random Testing at the System Level

```
[ ;x1-GPZ+wcckc]; ,N9J+?#6^6\ e?]9lu2_%'4GX"0VUB[E/r  
~fApu6b8<{ %siq8Zh.6{V,hr?; {Ti.r3PIxMMMv6{xS^+'Hq!Ax B"YXRS@!  
Kd6;wtAMeffWM(`|J_<1~o}z3K(CCzRH JIIvHz> *. \>JrlU32~eGP?  
lR=bF3+;y$3lodQ<B89!5"W2fK*vE7v{ ' )KC-i,c{\<[~m!]o;{. ' }Gj\ (X}  
EtYetrbpbY@aGZ1{P!AZU7x#4(Rtn!q4nCwqol^y6}0|  
Ko=*JK~;zMKV=9Nai:wxu{J&UV#HaU)*BiC<),`+t*gka<W=Z.  
%T5WGHZpI30D<Pq>&]BS6R&j ?#tP7iaV}- }`\\?[_[Z^LBMPG-  
FKj '\xwuZ1=Q`^`5,$N$Q@[ !CuRzJ2D|vBy!^zkhdf3C5PAkR?V hn|  
3='i2Qx]D$qs40`1@fevnG'2\11Vf3piU37@55ap\zIyl"'f,  
$ee,J4Gw:cgNKLie3nx9(`efSlg6#[K"@WjhZ}r[Scun&sBCS,T[/  
vY'pduwgzDlVNy7'rnzxNwI)(ynBa>%|b`;`9fG]P_0hdG~$@6  
3]KAeEnQ7lU)3Pn,0)G/6N-wyzj/MTd#A;r
```

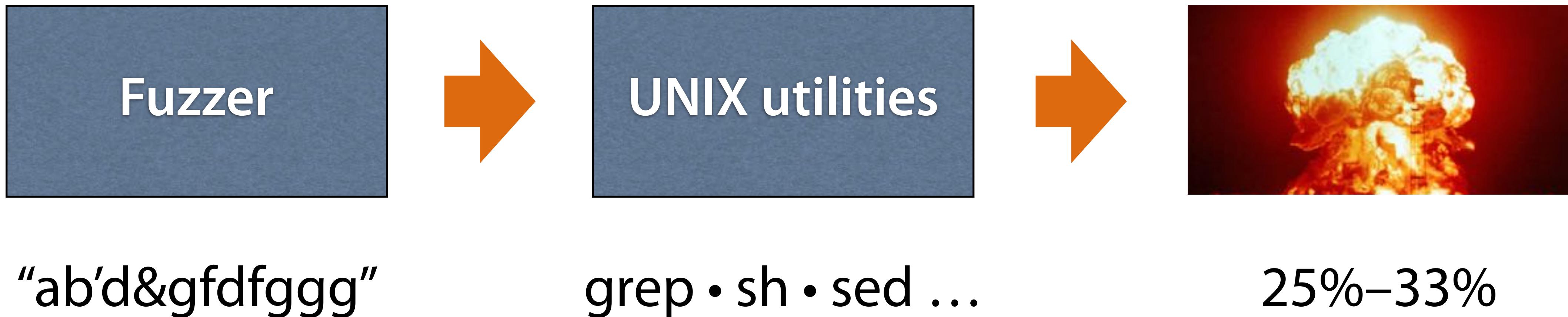
# Bart Miller

University of Wisconsin-Madison



# Fuzzing

Random Testing at the System Level



# Grammar Fuzzing

- Suppose you want to test a *parser* – to compile and execute a program
- To get deep into the program, you need *syntactically correct inputs*



Parser

# LangFuzz (2012)



- Fuzz tester for JavaScript and other languages
- Uses a full-fledged *grammar* to generate inputs

# JavaScript Grammar

## If Statement

*IfStatement*<sup>full</sup> ⇒

| **if** ParenthesizedExpression Statement<sup>full</sup>  
| **if** ParenthesizedExpression Statement<sup>noShortIf</sup> **else** Statement<sup>full</sup>

*IfStatement*<sup>noShortIf</sup> ⇒ **if** ParenthesizedExpression Statement<sup>noShortIf</sup> **else** Statement<sup>noShortIf</sup>

## Switch Statement

*SwitchStatement* ⇒

| **switch** ParenthesizedExpression { }  
| **switch** ParenthesizedExpression { CaseGroups LastCaseGroup }

*CaseGroups* ⇒

«empty»  
| CaseGroups CaseGroup

*CaseGroup* ⇒ CaseGuards BlockStatementsPrefix

# Fuzzing JavaScript

```
var haystack = "foo";
var re_text = "^foo";
haystack += "x";
re_text += "(x)";
var re = new RegExp(re_text);
re.test(haystack);
```

Reg  
prin

30 Chromium + Mozilla Security Rewards  
53,000 US\$ in Bug Bounties



JavaScript  
Parser



C. Holler

# LangFuzz (2012)



- Fuzz tester for JavaScript and other languages
- Uses a full-fledged *grammar* to generate inputs
- **Uses grammar to *parse and mutate existing inputs***

# Mutating with Grammars

To use a grammar for mutating code and data,

1. **Parse** an input into a derivation tree
2. **Mutate** the derivation tree
3. **Write** the tree out again

You need a *grammar*, a *parser*, and an *unparser*

# A Grammar Framework in Python

We have implemented a full-fledged *Python framework* to

1. **Specify** grammars
2. **Parse** inputs into derivation trees
3. **Mutate** derivation trees
4. **Write** the tree out again

*plus much much more;*

*e.g. testing*

This framework comes implemented as *Jupyter notebooks*

# A Grammar

```
<start>    ::= <expr>
<expr>     ::= <term> + <expr> | <term> - <expr> | <term>
<term>      ::= <term> * <factor> | <term> / <factor> | <factor>
<factor>    ::= +<factor> | -<factor> | (<expr>)
              | <integer> | <integer>. <integer>
<integer>   ::= <digit><integer> | <digit>
<digit>     ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

# A Grammar in Python

```
EXPR_GRAMMAR = {  
    "<start>": ["<expr>"],  
    "<expr>": ["<term> + <expr>", "<term> - <expr>", "<term>"],  
    "<term>": ["<factor> * <term>", "<factor> / <term>", "<factor>"],  
    "<factor>": ["+<factor>", "-<factor>", "(<expr>)",  
                  "<integer>.<integer>", "<integer>"],  
    "<integer>": ["<digit><integer>", "<digit>"],  
    "<digit>": ["0", "1", "2", "3", "4", "5", "6", "7", "8", "9"]  
}
```

# Parsing with Grammars

```
expr_input = "2 + -2"  
expr_parser = EarleyParser(EXPR_GRAMMAR)  
expr_trees = expr_parser.parse(expr_input)
```

# Mutating with Grammars

```
def swap_plus_minus(tree):
    node, children = tree
    if node == "+":
        node = "-"
    elif node == "-":
        node = "+"
    return node, children
```

```
def apply_mutator(tree, mutator):
    node, children = mutator(tree)
    return node, [apply_mutator(c, mutator) for c in children]
```

```
mutated_tree = apply_mutator(expr_tree, swap_plus_minus)
```

Demo

# Jupyter Notebooks

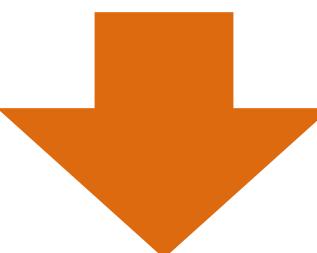
- Very fast prototyping
- Literate programming  
with examples (and tests!)
- Data visualizations



*Prototype for Python first; then go for a "serious" language like C*

# Learning Grammars

http://user:password@www.google.com:80/command?foo=bar&lorem=ipsum#fragment  
http://www.guardian.co.uk/sports/worldcup#results  
ftp://bob:12345@ftp.example.com/oss/debian7.iso



```
URL ::= PROTOCOL '://' AUTHORITY PATH ['?' QUERY] ['#' REF]
AUTHORITY ::= [USERINFO '@'] HOST [':' PORT]
PROTOCOL ::= 'http' | 'ftp'
USERINFO ::= /[a-z]+:[a-z]+/
HOST ::= /[a-z.]+/
PORT ::= '80'
PATH ::= /\[a-zA-Z0-9.\/\]*/
QUERY ::= 'foo=bar&lorem=ipsum'
REF ::= /[a-z]+/
```

# Parser-Directed Fuzzing

We track and satisfy *comparisons* in parsers to find language elements

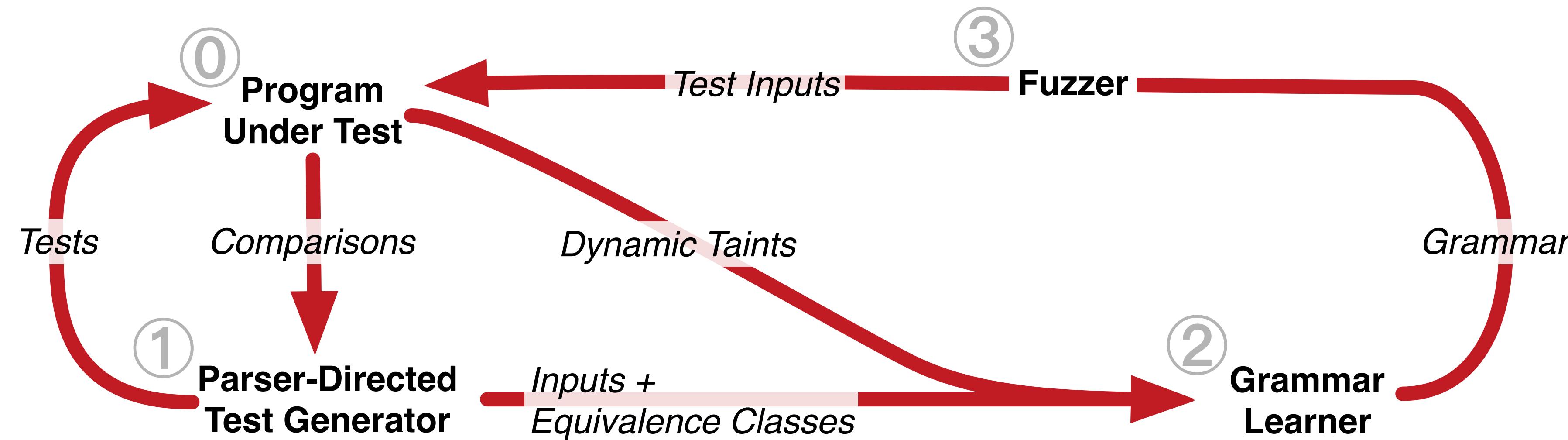
```
{ [ ( + & ? identifier number ...  
+= == ++ /= &= |= != if in string ...  
==!= <<= >>> for try let ...  
>>>= true null void with else ...  
false throw while break catch ...  
return delete typeof Object ...  
default finally indexOf  
continue function debugger  
undefined stringify  
instanceof
```

**JS tokens of length 3+ discovered**

| AFL   | KLEE  | pFuzzer |
|-------|-------|---------|
| 5,0 % | 7,5 % | 52,5 %  |

# Deep Fuzzing without Samples

PYGMALION prototype for Python programs



Perfect coverage, much faster than AFL, much better structure than KLEE

Gopinath, Mathis, Höschele, Kampmann, Zeller: "Sample-Free Learning of Input Grammars"

fuzzingbook.org

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# Generating Software Tests

## Breaking Software for Fun and Profit

by Andreas Zeller, Rahul Gopinath, Marcel Böhme, Gordon Fraser, and Christian Holler

## About this Book

Welcome to "Generating Software Tests"! Software has bugs, and catching bugs can involve lots of effort. This book addresses this problem by *automating* software testing, specifically by *generating tests automatically*. Recent years have seen the development of novel techniques that lead to dramatic improvements in test generation and software testing. They now are mature enough to be assembled in a book – even with executable code.

```
from fuzzingbook_utils import YouTubeVideo
YouTubeVideo("w4u5gCgPlmg")
```

Generating Software Tests

Watch later Share

# Generating Software Tests

Breaking Software for Fun and Profit

# A Grammar Framework in Python

We have implemented a full-fledged *Python framework* to

1. **Specify** grammars
2. **Parse** inputs into derivation trees
3. **Mutate** derivation trees
4. **Write** the tree out again

*plus much much more;  
e.g. testing*

This framework comes implemented as *Jupyter notebooks*

## Jupyter Notebooks



- **Very fast prototyping**
- Literate programming with examples (and tests!)
- Data visualizations

*Prototype for Python first; then go for a "serious" language like C*

@FuzzingBook

[www.fuzzingbook.org](http://www.fuzzingbook.org)

# A Grammar in Python

```
EXPR_GRAMMAR = {
    "<start>": ["<expr>"],
    "<expr>": ["<term> + <expr>", "<term> - <expr>", "<term>"],
    "<term>": ["<factor> * <term>", "<factor> / <term>", "<factor>"],
    "<factor>": ["+<factor>", "-<factor>", "(<expr>)",
                  "<integer>.<integer>", "<integer>"],
    "<integer>": ["<digit><integer>", "<digit>"],
    "<digit>": ["0", "1", "2", "3", "4", "5", "6", "7", "8", "9"]
}
```

A screenshot of a Jupyter notebook interface. At the top, there's a red header bar with navigation links. Below it, the main content area has a title "Generating Software Tests" and a subtitle "Breaking Software for Fun and Profit" by Andreas Zeller, Rahul Gopinath, Marcel Böhme, Gordon Fraser, and Christian Holler. A section titled "About this Book" provides a brief overview. Below the text, there's a code cell containing Python code to play a YouTube video, followed by a video player interface. The video player shows a thumbnail of a person, the title "Generating Software Tests", and standard video controls for "Watch later" and "Share".

**Generating Software Tests**  
**Breaking Software for Fun and Profit**  
by Andreas Zeller, Rahul Gopinath, Marcel Böhme, Gordon Fraser, and Christian Holler

**About this Book**

Welcome to "Generating Software Tests"! Software has bugs, and catching bugs can involve lots of effort. This book addresses this problem by *automating* software testing, specifically by *generating tests automatically*. Recent years have seen the development of novel techniques that lead to dramatic improvements in test generation and software testing. They now are mature enough to be assembled in a book – even with executable code.

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```

Generating Software Tests  
Watch later Share

@FuzzingBook

@FuzzingBook

# Mutations with Grammars

A Chapter of “Generating Software Tests”

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Rahul Gopinath,  
Marcel Böhme,  
Gordon Fraser, and  
Christian Holler

April 22, 2019

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A chapter of **Generating Software Tests**, by Andreas Zeller, Rahul Gopinath, Marcel Böhme, Gordon Fraser, and Christian Holler.

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# 1 Mutations with Grammars

In this notebook, we make a very short and simple introduction on how to use the fuzzingbook framework for grammar-based mutation – both for data and for code.

## Prerequisites

- This chapter is meant to be self-contained.

### 1.1 Defining Grammars

We define a grammar using standard Python data structures. Suppose we want to encode this grammar:

```
<start> ::= <expr>
<expr> ::= <term> + <expr> | <term> - <expr> | <term>
<term> ::= <term> * <factor> | <term> / <factor> | <factor>
<factor> ::= +<factor> | -<factor> | (<expr>) | <integer> | <integer>. <integer>
<integer> ::= <digit><integer> | <digit>
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

1 import fuzzingbook_utils

1 from Grammars import syntax_diagram, is_valid_grammar,
    ↪ convert_ebnf_grammar, srange, crange
```

In Python, we encode this as a mapping (a dictionary) from nonterminal symbols to a list of possible expansions:

```
1 EXPR_GRAMMAR = {
2     "<start>":
3         [ "<expr>" ],
4
5     "<expr>":
6         [ "<term> + <expr>", "<term> - <expr>", "<term>" ],
7
8     "<term>":
9         [ "<factor> * <term>", "<factor> / <term>", "<factor>" ],
10
11    "<factor>":
12        [ "+<factor>",
13         "-<factor>",
14         "(<expr>)",
15         "<integer>. <integer>",
16         "<integer>" ],
17
18    "<integer>":
19        [ "<digit><integer>", "<digit>" ],
```

```
21     "<digit>":  
22         ["0", "1", "2", "3", "4", "5", "6", "7", "8", "9"]  
23 }
```

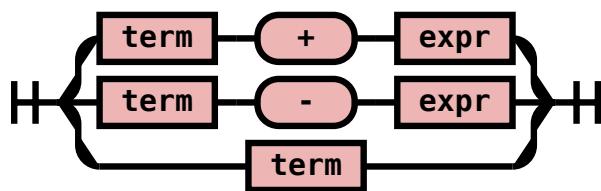
```
1 assert is_valid_grammar(EXPR_GRAMMAR)
```

```
1 syntax_diagram(EXPR_GRAMMAR)
```

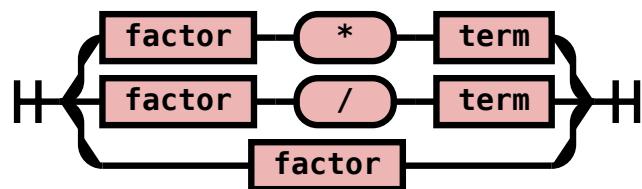
```
start
```



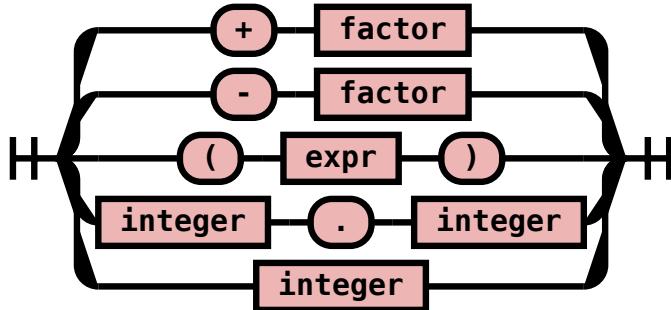
```
expr
```



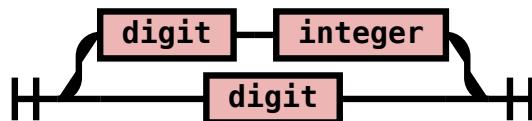
```
term
```



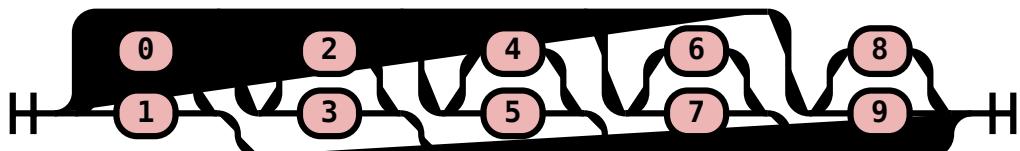
```
factor
```



integer



digit



## 1.2 Fuzzing with Grammars

We mostly use grammars for *fuzzing*, as in here:

```
1 from GrammarFuzzer import GrammarFuzzer
1 expr_fuzzer = GrammarFuzzer(EXPR_GRAMMAR)
2 for i in range(10):
3     print(expr_fuzzer.fuzz())
```

```
3.8 + --62.912 - ++4 - +5 * 3.0 * 4
7 * (75.5 - -6 + 5 - 4) + -(8 - 1) / 5 * 2
(-(9) * +6 + 9 / 3 * 8 - 9 * 8 / 7) / +-+65
(9 + 8) * 2 * (6 + 6 + 9) * 0 * 1.9 * 0
(1 * 7 - 9 + 5) * 5 / 0 * 5 + 7 * 5 * 7
```

```
- (6 / 9 - 5 - 3 - 1) - -1 / +1 + (9) / (8) * 6
(+-(0 - (1) * 7 / 3)) / ((1 * 3 + 8) + 9 - +1 / --0) - 5 *
(-+939.491)
+2.9 * 0 / 501.19814 / ---+(6.05002)
+-8.8 / (1) * -+1 + -8 + 9 - 3 / 8 * 6 + 4 * 3 * 5
(+ (8 / 9 - 1 - 7)) + ---06.30 / +4.39
```

### 1.3 Parsing with Grammars

We can parse a given input using a grammar:

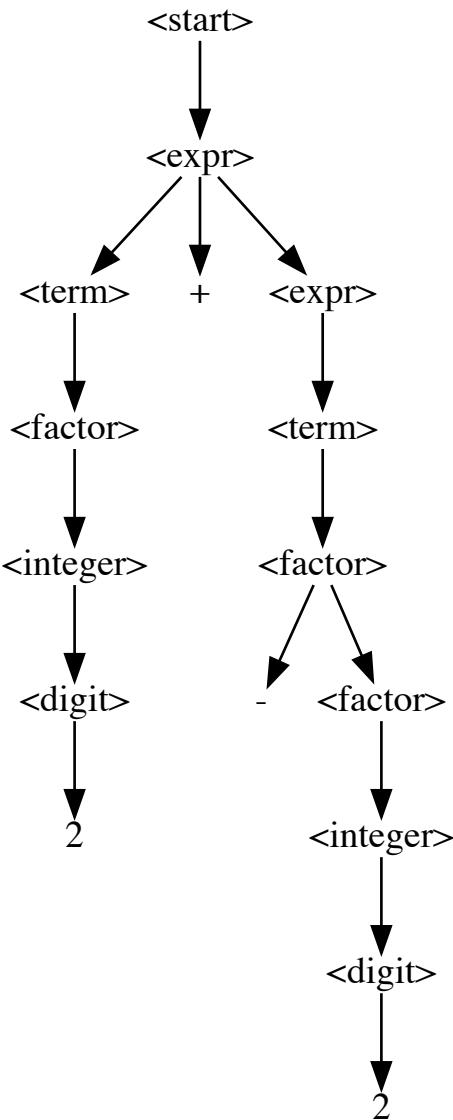
```
1 expr_input = "2 + -2"
```

```
1 from Parser import EarleyParser, display_tree, tree_to_string
```

```
1 expr_parser = EarleyParser(EXPR_GRAMMAR)
```

```
1 expr_tree = list(expr_parser.parse(expr_input))[0]
```

```
1 display_tree(expr_tree)
```



Internally, each subtree is a pair of a node and a list of children (subtrees)

```
1 expr_tree
```

```
('<start>',
 [('<expr>',
   [('<term>',
     [('<factor>',
       [('<integer>',
         [('<digit>',
           [('2', [])])])])]),
    ('+', []),
   ('<expr>',
     [('<term>',
       [('<factor>',
         [('‐', [])])])]))]
```

```
('<factor>', [('<integer>', [('<digit>', [('2', [])])])])])])])
```

## 1.4 Mutating a Tree

We define a simple mutator that traverses an AST to mutate it.

```
1 def swap_plus_minus(tree):
2     node, children = tree
3     if node == "+":
4         node = "-"
5     elif node == "-":
6         node = "+"
7     return node, children
```

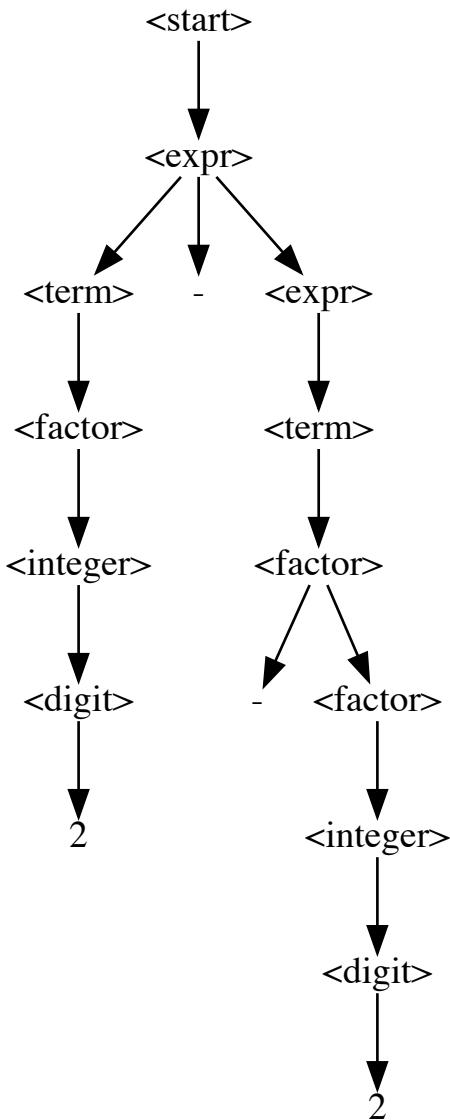
```
1 def apply_mutator(tree, mutator):
2     node, children = mutator(tree)
3     return node, [apply_mutator(c, mutator) for c in children]
```

```
1 mutated_tree = apply_mutator(expr_tree, swap_plus_minus)
```

```
1 display_tree(mutated_tree)
```



## 1.5 Unparsing the Mutated Tree

To unparse, we traverse the tree and look at all terminal symbols:

```

1 tree_to_string(mutated_tree)
'2 - -2'
  
```

## 1.6 Lots of mutations

```

1 for i in range(10):
2     s = expr_fuzzer.fuzz()
3     s_tree = list(expr_parser.parse(s))[0]
4     s_mutated_tree = apply_mutator(s_tree, swap_plus_minus)
  
```

```

5     s_mutated = tree_to_string(s_mutated_tree)
6     print('    ' + s + '\n->  ' + s_mutated + '\n')

8786.82 - +01.170 / 9.2 - +(7) + 1 * 9 - 0
-> 8786.82 + +01.170 / 9.2 + +(7) - 1 * 9 + 0

+-6 * 0 / 5 * (-(1.7 * +(-1 / +4.9 * 5 * 1 * 2) + -4.2 + (6 +
-5) / (4 * 3 + 4)))
-> +-6 * 0 / 5 * (-(1.7 * +(-1 / +4.9 * 5 * 1 * 2) - -4.2 - (6 -
-5) / (4 * 3 - 4)))

(6 * 2 + 5) * -(5) / (0 + 7) / 7 - -075 / 2
-> (6 * 2 - 5) * -(5) / (0 - 7) / 7 + -075 / 2

6 + 9 * 3 * 7 - 6 / 0 * 5 - 7 * 5 + 3 - 0
-> 6 - 9 * 3 * 7 + 6 / 0 * 5 + 7 * 5 - 3 + 0

93 * +- (0 / 0 - 0 - 4) / (2) / 1 - 2.49 - (7.0 / 9.1)
-> 93 * +- (0 / 0 + 0 + 4) / (2) / 1 + 2.49 + (7.0 / 9.1)

+0.6 * 1.62 * 3 / 7 * 5 - 645 / (3 * 4 - 2) / 7
-> +0.6 * 1.62 * 3 / 7 * 5 + 645 / (3 * 4 + 2) / 7

(1 * 8 * 4 + 1) - +-+(2 - 8) / 0.76 * 3
-> (1 * 8 * 4 - 1) + +-+(2 + 8) / 0.76 * 3

-+--(0 - 0) / 1 / 3 / 5 * 9 * 2 + +5.0 / ((+5) * 8 * 7)
-> -+--(0 + 0) / 1 / 3 / 5 * 9 * 2 - +5.0 / ((+5) * 8 * 7)

1 * ++6 - -(5 + 7 + 5 - 6 - 4) - 5.4 / 2 - +5 / 9
-> 1 * ++6 + -(5 - 7 - 5 + 6 + 4) + 5.4 / 2 + +5 / 9

(1.5 * 1 + 9 - 3 + 3) - 6 / 6 + 1 + 0
-> (1.5 * 1 - 9 + 3 - 3) + 6 / 6 - 1 - 0

```

## 1.7 Another Example: JSON

```

1 import string

1 CHARACTERS_WITHOUT_QUOTE = (string.digits
2                             + string.ascii_letters
3                             + string.punctuation.replace('"', ''))
4     .replace('\\', '\\')
        + ' ')

1 JSON_EBNF_GRAMMAR = {
2     "<start>": ["<json>"],
3     "<json>": ["<element>"],

```

```

4     "<element>": ["<ws><value><ws>"],
5     "<value>": [<object>, <array>, <string>, <number>, "
6     ↪ true", "false", "null"],
7     "<object>": [{"<ws>}", {"<members>"}],
8     "<members>": [<member>(<members>)*],
9     "<member>": [<ws><string><ws>:<element>],
10    "<array>": [<ws>][<elements>],
11    "<elements>": [<element>(<elements>)*],
12    "<element>": [<ws><value><ws>],
13    "<string>": ['' + <characters> + '''],
14    "<characters>": [<character>*],
15    "<character>": strange(CHARACTERS_WITHOUT_QUOTE),
16    "<number>": [<int><frac><exp>],
17    "<int>": [<digit>, <onenine><digits>, "-<digits>", "-<
18     ↪ onenine><digits>"],
19    "<digits>": [<digit>+],
20    "<digit>": ['0', <onenine>],
21    "<onenine>": crange('1', '9'),
22    "<frac>": [", ".<digits>],
23    "<exp>": [", "E<sign><digits>", "e<sign><digits>"],
24    "<sign>": [", '+', '-'],
25    "<ws>": ["( )*"]
26 }
27
28 assert is_valid_grammar(JSON_EBNF_GRAMMAR)

```

```
1 JSON_GRAMMAR = convert_ebnf_grammar(JSON_EBNF_GRAMMAR)
```

```
1 syntax_diagram(JSON_GRAMMAR)
```

```
start
```



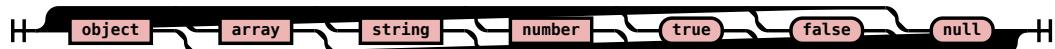
```
json
```



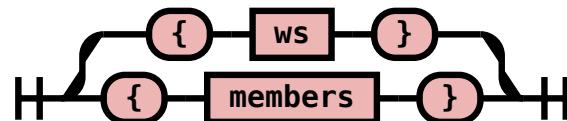
element



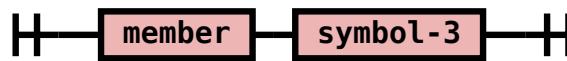
value



object



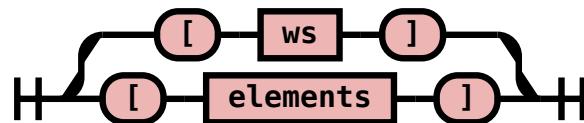
members



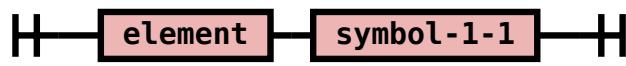
member



array



elements



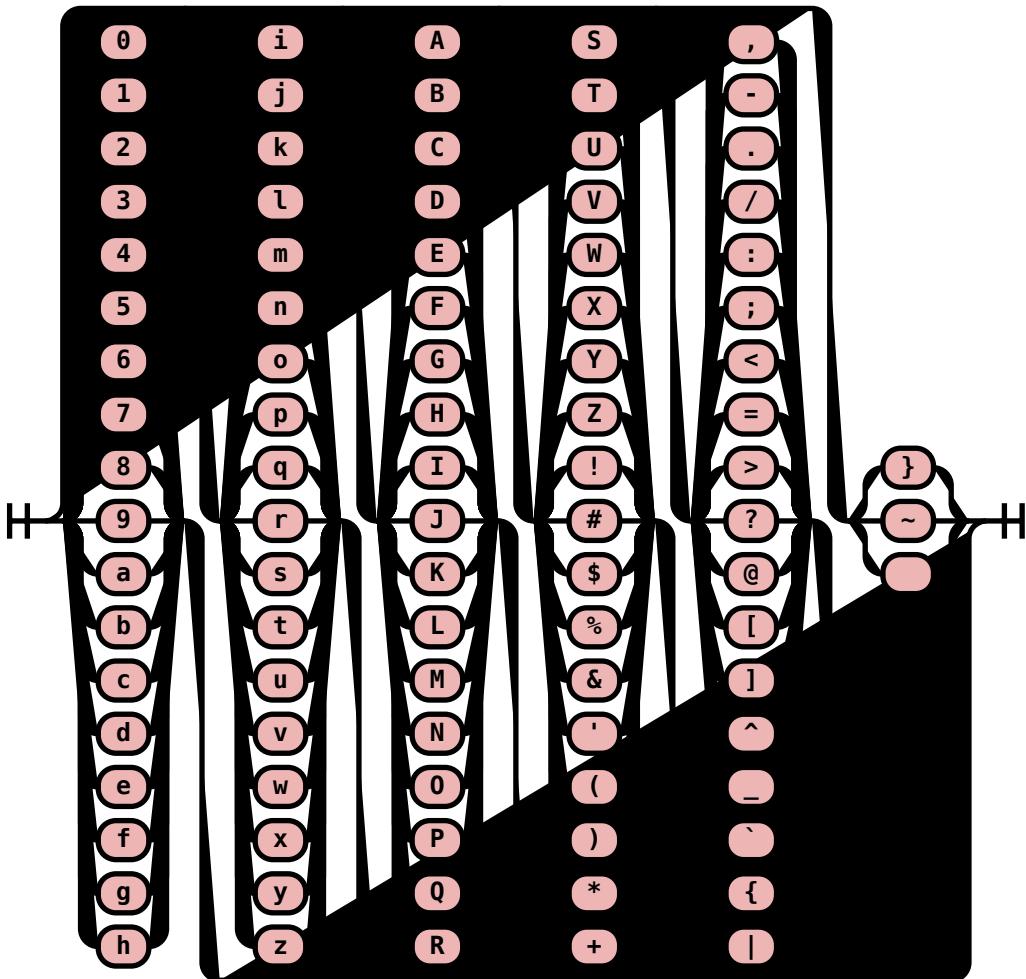
string



characters



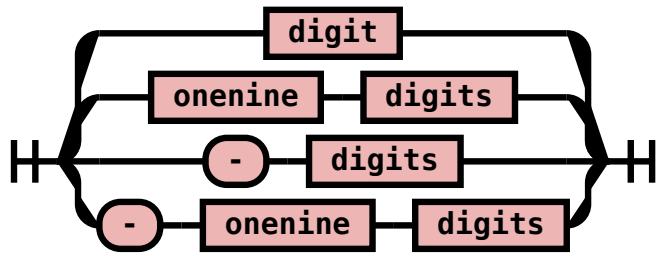
character



number



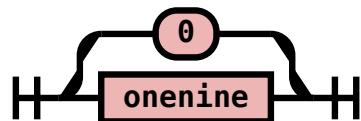
int



digits



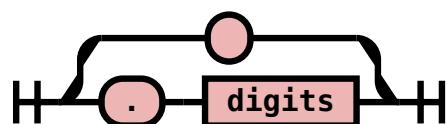
digit



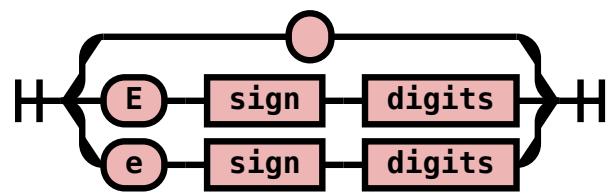
onenine



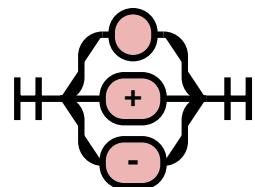
frac



exp



sign



ws



symbol



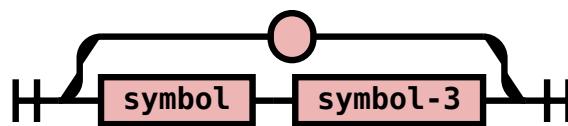
symbol-1



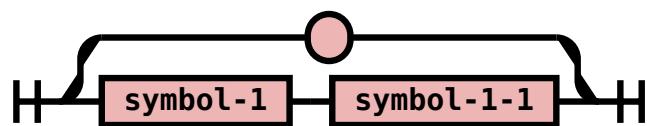
symbol-2



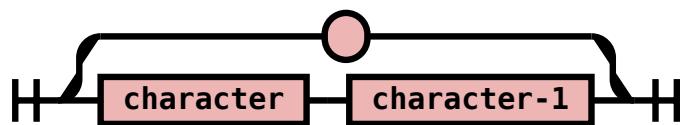
symbol-3



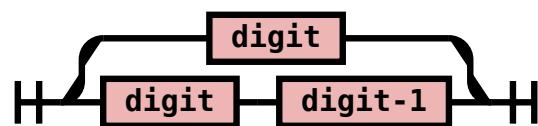
symbol-1-1



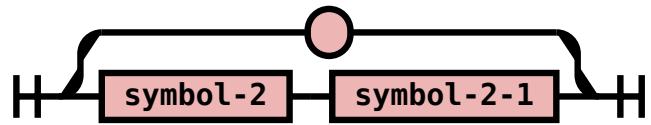
character-1



digit-1



## symbol-2-1

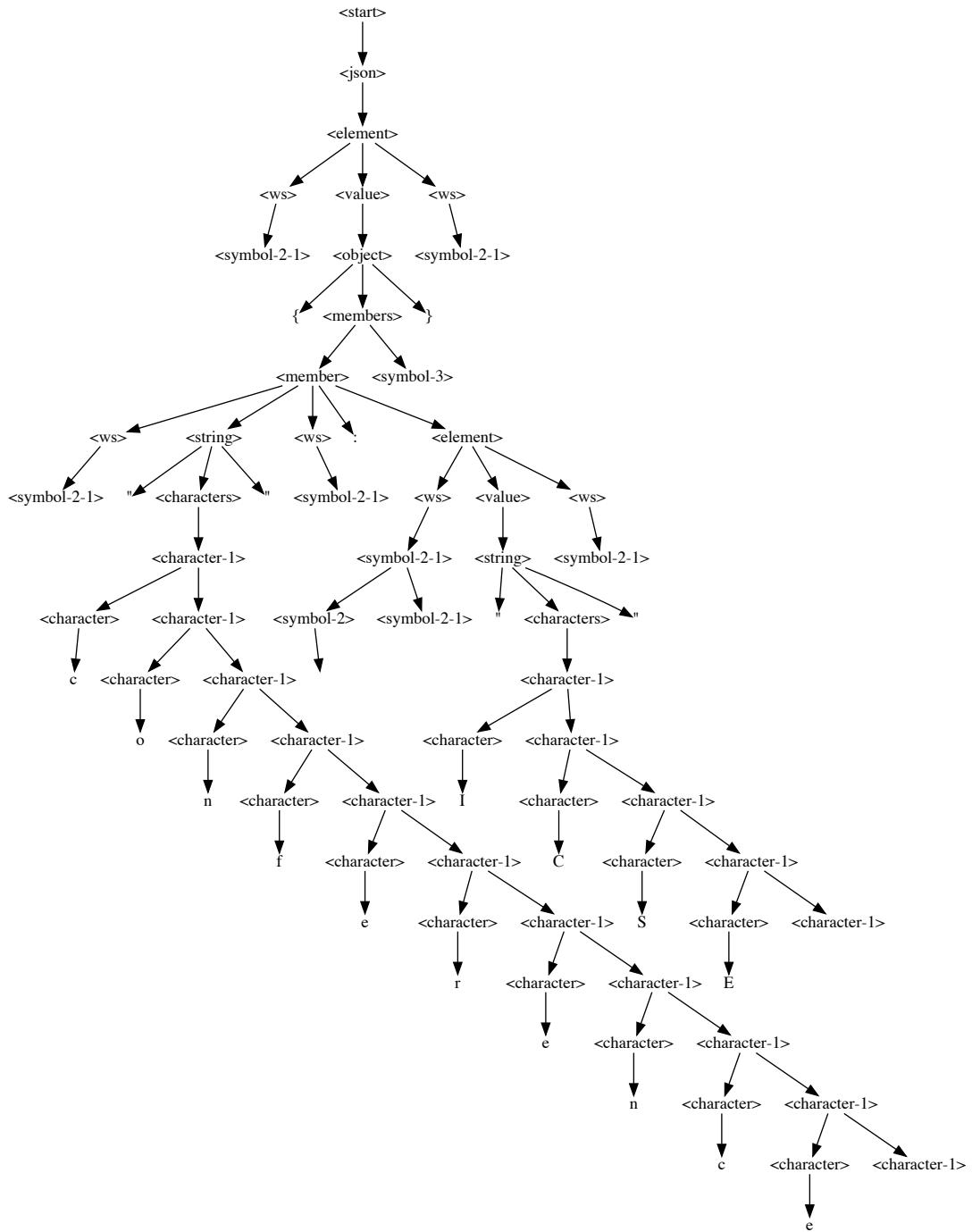


```
1 json_input = '{"conference": "ICSE"}'
```

```
1 json_parser = EarleyParser(JSON_GRAMMAR)
```

```
1 json_tree = list(json_parser.parse(json_input))[0]
```

```
1 display_tree(json_tree)
```



```

1 def swap_venue(tree):
2     if tree_to_string(tree) == '"ICSE"':
3         tree = list(json_parser.parse('"ICST"))[0]
4     return tree

```

```

1 mutated_tree = apply_mutator(json_tree, swap_venue)

```

```
1 tree_to_string(mutated_tree)
```

```
' {"conference": "ICST"}'
```

## **2 References**