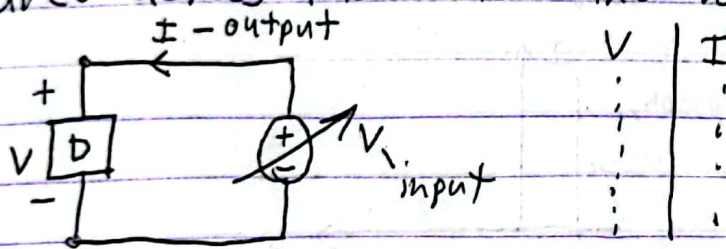
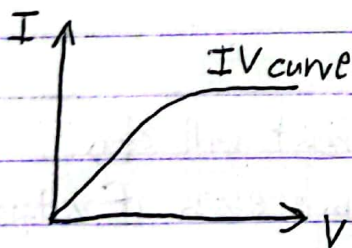


## # IV Characteristics of a device:

- It is the relationship between current and voltage across a device, it is used to describe the characteristics of the device.
- A table of  $I-V$  is made by connecting a voltage source across the device and varying the voltage. Like:



- It can also be done using a graph which would look like:

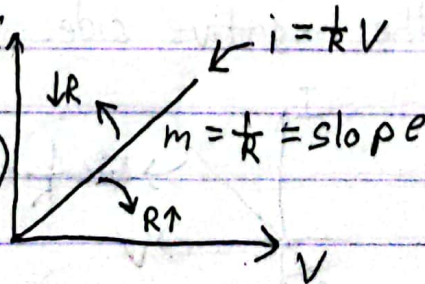


- $I-V$  Char is also known as Input-output relation of a device.

## Lecture - 3 (P - 2)

### # $I-V$ Char of simple linear elements:

- \* A device is linear if the relation between  $I-V$  is a straight line graph. eg: resistor ( $V=IR$  eqn)  $\Rightarrow V \propto I$
- \*  $I-V$  curve of resistor:  $I \propto V$
- If  $R = \infty$ ,  $m(\text{slop}) = 0$  (open circ)
- "  $R = 0$ , " " =  $\infty$  (short circ)

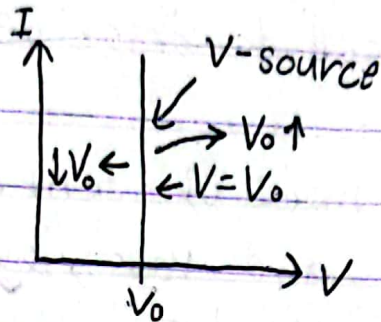
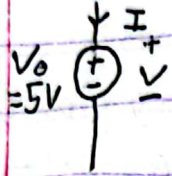




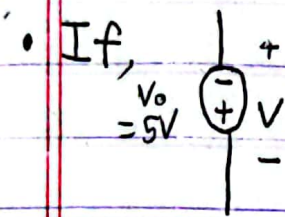
## # I-V Char of independent sources:

### \* V-source ( $V_0 = \text{constant}$ ):

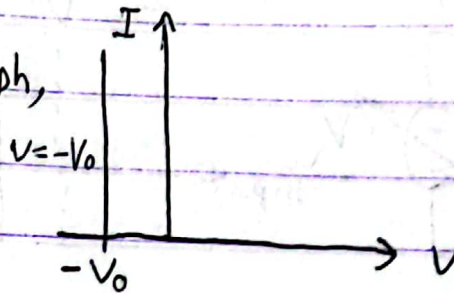
#### • Graph:



• What ever the current is, voltage will always stay the same.

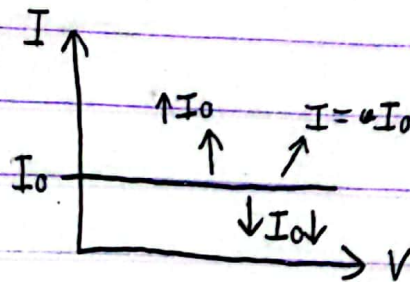
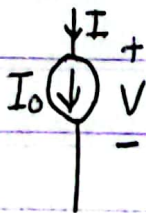


then graph,

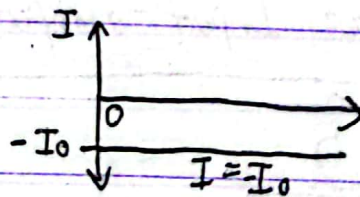
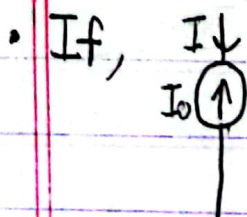


### # I-Source ( $I_0 = \text{constant}$ ):

#### • Graph:

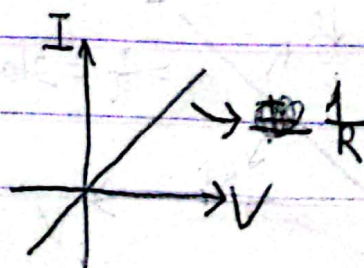


• Current will stay same even if voltage changes.



# If polarity and source direction ~~is~~ is same then the straight line will be in the positive side otherwise it will be on the negative side.

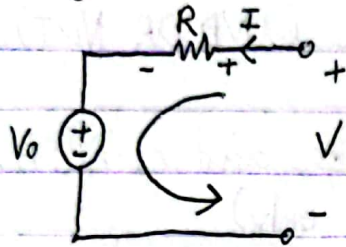
### # Resistance:



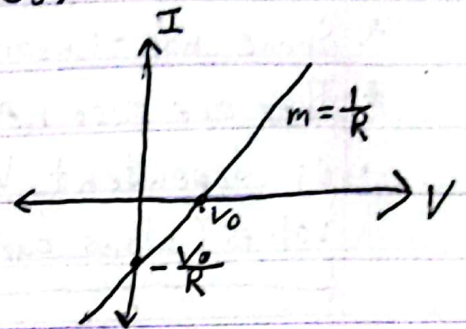


## # I-V char of Compound elements:

- \* Compound elements = combination of simple elements.
- \* Voltage source in series with resistance.

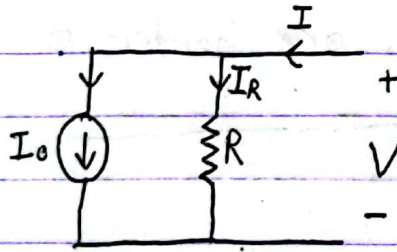


$$\begin{aligned} K \cdot V \cdot I, \\ V &= V_R + V_0 \\ \Rightarrow V &= IR + V_0 \\ \Rightarrow I &= \left(\frac{1}{R}\right)V - \frac{V_0}{R} \\ \downarrow \quad \downarrow \quad \downarrow \\ y &= m x + c \end{aligned}$$

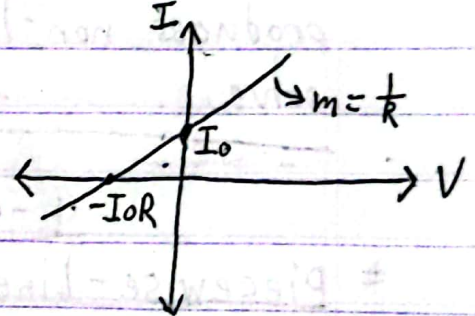


- To find the x-intercept put  $I=0$  in  $I = \left(\frac{1}{R}\right)V - \frac{V_0}{R}$ .

- \* Current source in parallel with resistance.



$$\begin{aligned} K \cdot C \cdot I, \\ I &= I_0 + I_R \\ I &= \left(\frac{1}{R}\right)V + I_0 \\ \downarrow \quad \downarrow \quad \downarrow \\ y &= m x + c \end{aligned}$$

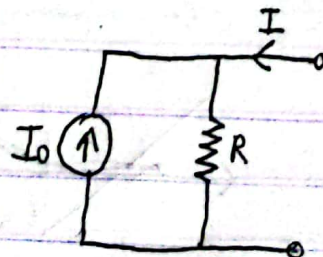
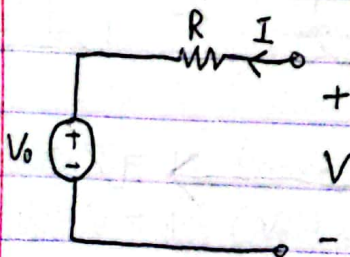


- To find the x-intercept put  $I=0$  in  $I = \left(\frac{1}{R}\right)V + I_0$ .
- If I-source is reversed, The eqn becomes,  $I = \left(\frac{1}{R}\right)V - I_0$ .
- \* If V-source is " , " " " ,  $I = \left(\frac{1}{R}\right)V + \frac{V_0}{R}$ .

## L-3 (P-5)

### # Equivalent Circuit:

- \* If 2 devices have the same I-V relation they are called equivalent circuit



if  $V_0 = I_0 R$ , this is also known as source transformation.



## # Non-Linear Devices:

- \* Devices whose  $I$ - $V$  <sup>graph</sup> ~~curve~~ is not a <sup>single</sup> straight line.
  - \* They are required to implement non-Linear operations.
  - \* Some non-linear devices are logic gates (AND, OR, NOT)
  - \* They are also needed to control  $I/V$ .
  - eg: dependent  $V$ -sources and  $I$ -sources, and switch, valves (allows current to flow in 1 direction only).
- 

### L-4 (P-2)

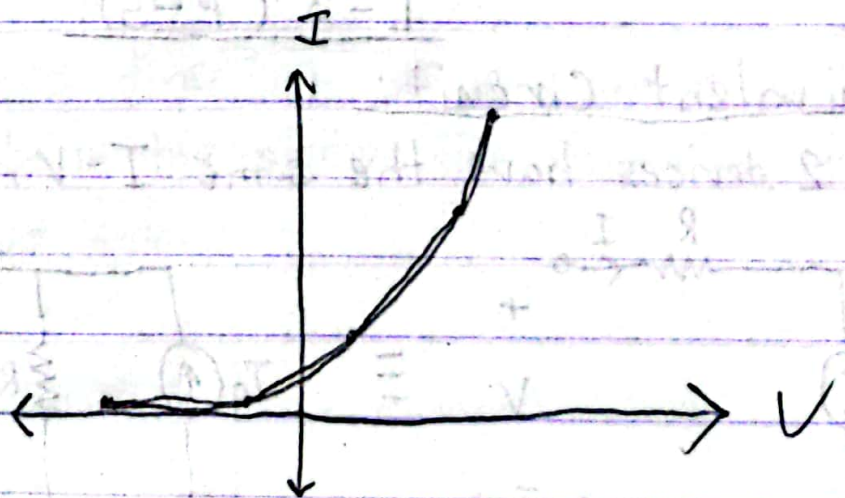
## # Problems with Non-Linear devices:

- \* They produce non-linear  $I$ - $V$  which ~~intern~~ inturn produces non-linear equation which are harder to solve.
- 

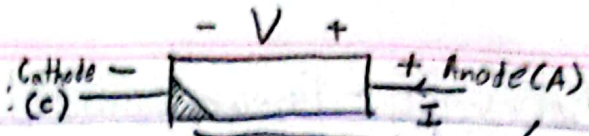
### L-4 (P-3)

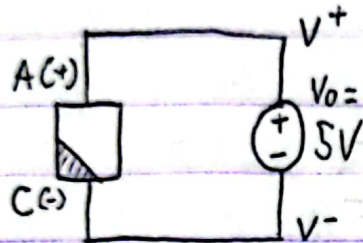
## # Piecewise-Linear approximation:

- \* It is a technique used to solve non-linear eqn.
- \* Here a curve is divided into segments of straight lines.
- \* The more pieces the graph is broken into the more accurate it is.



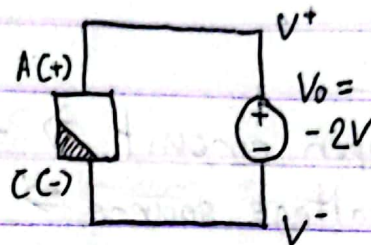


- \* Symbol of non-linear device:  ,  $V = V_A - V_C$
- \* They have polarity, The (-ve) side is always marked.
- \* If  $V > 0 \Rightarrow V_A > V_C \Rightarrow$  Forward Bias
- "  $V \leq 0 \Rightarrow V_A \leq V_C \Rightarrow$  Reverse "



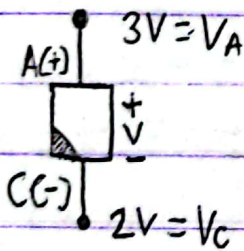
Forward Bias

$$\begin{aligned} V_0 &= V^+ - V^- \\ &= V_A - V_C \\ &= 5V \end{aligned}$$

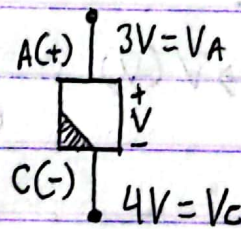


Reverse Bias

$$\begin{aligned} V_0 &= V^+ - V^- \\ &= V_A - V_C \\ &= -2V \end{aligned}$$



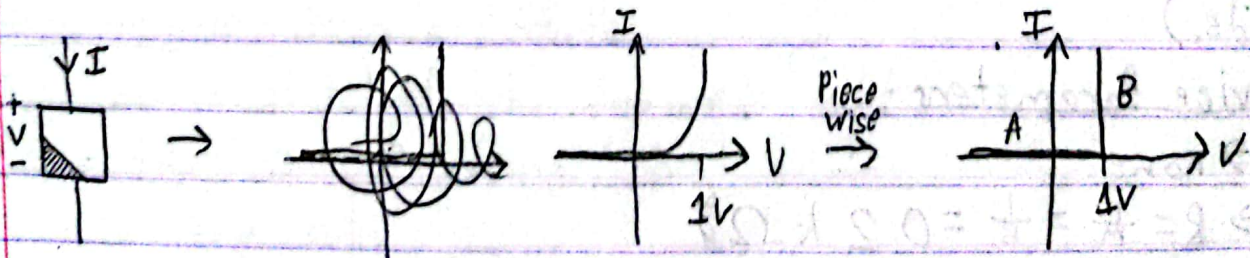
$$\begin{aligned} V &= V_A - V_C \\ &= 1V \text{ (F.B)} \end{aligned}$$



$$\begin{aligned} V &= V_A - V_C \\ &= -1V \text{ (R.B)} \end{aligned}$$

- \* In a non-linear device 'I' enters through the anode.

\*

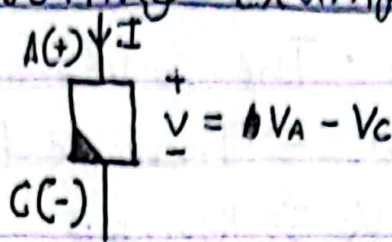
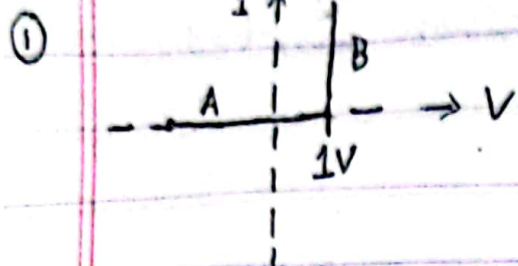


A  $\Rightarrow I = 0$ , (Open circuit)

B  $\Rightarrow V = 1$ , (Voltage source)



# # Piecewise-linear modelling example:



## \* Device modelling:

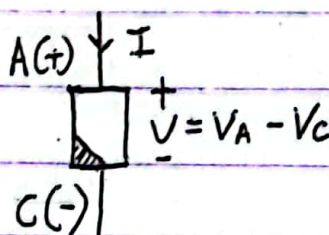
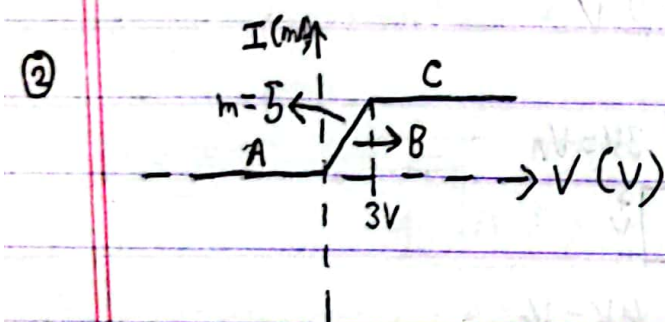
A  $\Rightarrow V < 1 \Rightarrow$  open circuit  $\Rightarrow$

B  $\Rightarrow I > 0 \Rightarrow$  voltage source  $\Rightarrow$

## \* Device parameters:

A  $\Rightarrow$  no parameters

B  $\Rightarrow V_0 = 1V$



## \* Dev modelling:

A  $\Rightarrow V \leq 0V \Rightarrow$

B  $\Rightarrow 0 < V < 3V \Rightarrow$  ( $R = \frac{1}{m} = \frac{1}{5} = 0.2 k\Omega$ )

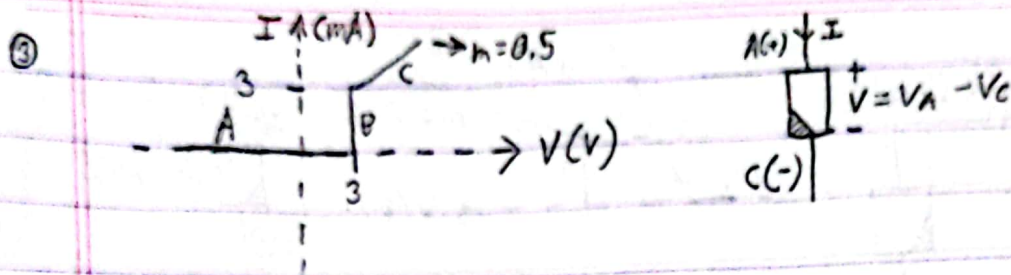
C  $\Rightarrow V > 3V \Rightarrow$  (Direction of I is Anode to cathode because the line 'C' intercepts the y-axis in the positive side.)

## \* Device Parameters:

A  $\Rightarrow$  none

B  $\Rightarrow R = \frac{1}{m} = \frac{1}{5} = 0.2 k\Omega$

C  $\Rightarrow y = m x = 5 \times 3 = 15 mA$



### \* Device Model:

A  $\Rightarrow V \leq 3V \Rightarrow$

B  $\Rightarrow 0 < I \leq 3 \text{ mA} \Rightarrow$

C  $\Rightarrow V > 3V \Rightarrow$

### \* Parameters:

A  $\Rightarrow$  none

B  $\Rightarrow V_0 = 3V$

C  $\Rightarrow y = mx + c \Rightarrow 3 = 0.5 \times 3 + c \Rightarrow c = 1.5, \therefore y = 0.5x + 1.5$   
 $R = \frac{1}{m} = \frac{1}{0.5} = 2 \text{ k}\Omega$

- For current source with parallel resistor, put  $x = 0$  in  $y = 0.5x + 1.5$   
 $\therefore y = 1.5, \therefore I = 1.5 \text{ mA}$
- For voltage source with resistor in series, put  $y = 0$  in  $y = 0.5x + 1.5$   
 $\therefore x = -3V$

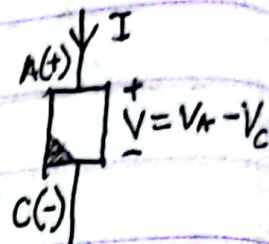
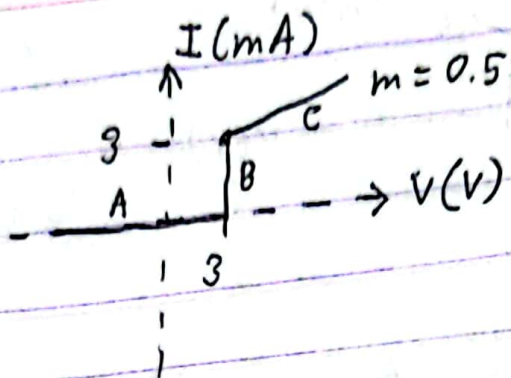
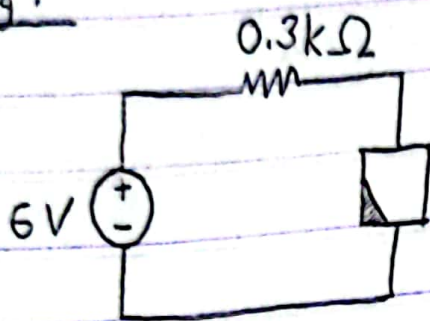
### L-4 (P-7)

### # Methode of Assumed State:

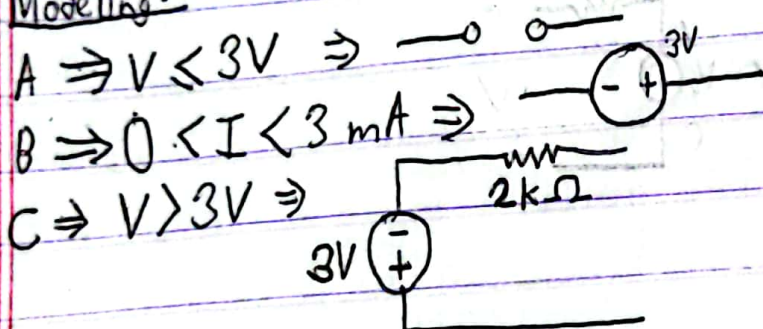
- Assume a state of the device.
- Solve the circuit using that model.
- Check the soln.
- Repeat (1-3) if mismatch.



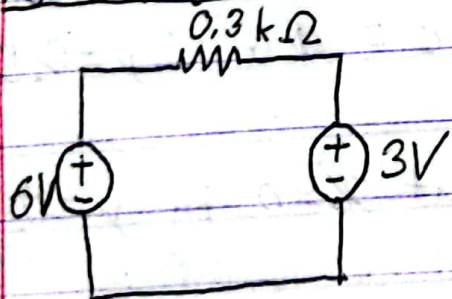
Eg:



Modeling:



① Assuming device working in B region:

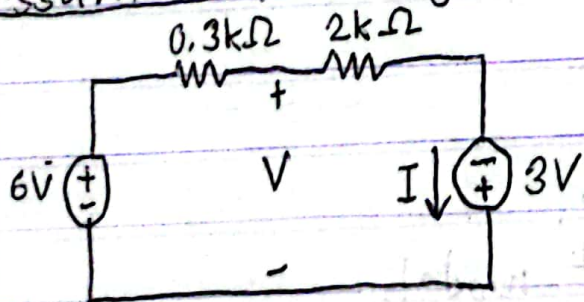


$$I = \frac{6-3}{0.3} = 10 \text{ mA}$$

$$V = 3 \text{ V}$$

• Soln not correct because  $0 < I < 3 \text{ mA}$ , as it should have been in the B region.  
 $\therefore$  Assumption is wrong.

② Assume in C region:



$$I = \frac{6+3}{0.3+2} = 3.6 \text{ mA}$$

$$\text{K.V.L} \Rightarrow V = 2I - 3 = 4.2 \text{ V}$$

Assumption correct as  $V > 3V$  in C region.