

# BRAC University



## Assignment-02

**Subject title:** Digital Logic  
and Design

**Subject code:**CSE260

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**Section:**08

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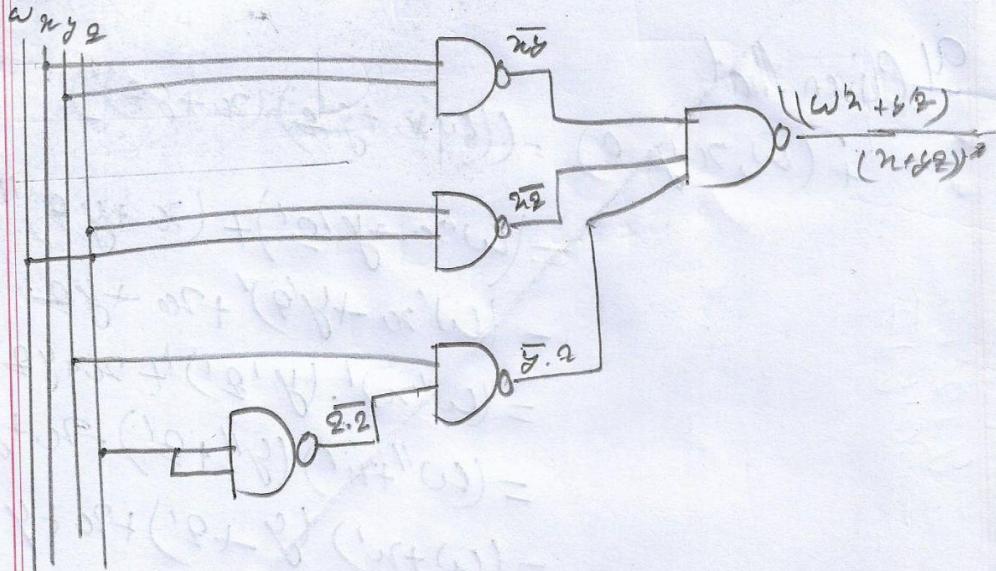
Ans to the question on - 1

Q1 Given that,

$$\begin{aligned}
 f(\omega, x, y, z) &= ((\omega'x + y'z)(x + yz))' \\
 &= (\omega'x + y'z)' + (x + yz)' \\
 &= (\omega'x + y'z)' + x + yz \\
 &= (\omega'x)' \cdot (y'z)' + x + yz \\
 &= (\omega'' + x') (y'' + z') + x + yz \\
 &= (\omega + x') (y + z') + x + yz \\
 &= (y + z')\omega + (y + z')x + x + yz \\
 &= (y + z')\omega + y + z' + x + yz \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x \\
 &= (y + z')\omega + y + z' + z' + x
 \end{aligned}$$

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$$\begin{aligned} &= \bar{y} + z' w \\ &= \bar{x} + y + \bar{z} \end{aligned}$$



Q1 Given that

$$F(w, x, y, z) = \sum(0, 1, 2, 3, 9, 11)$$

$$= \sum(0000, 0001, 0010, 0011, 1001, 1011)$$

$$= \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z + \bar{w}\bar{x}yz + \bar{w}\bar{x}y\bar{z} + w\bar{x}y\bar{z}$$

$$= \bar{w}\bar{x}\bar{y}(\bar{z} + z) + \bar{w}\bar{x}y(\bar{z} + z) + w\bar{x}z(\bar{y} + y)$$

$$= \bar{w}\bar{x}\bar{y} \cdot 1 + \bar{w}\bar{x}y \cdot 1 + w\bar{x}z \cdot 1$$

$$= \bar{w}\bar{x}\bar{y} + \bar{w}\bar{x}y + w\bar{x}z$$

$$= \bar{w}\bar{x}(y + z) + w\bar{x}z$$

$$= \bar{w}\bar{x} \cdot 1 + w\bar{x}z$$

$$= \bar{w}\bar{x} + w\bar{x}z$$

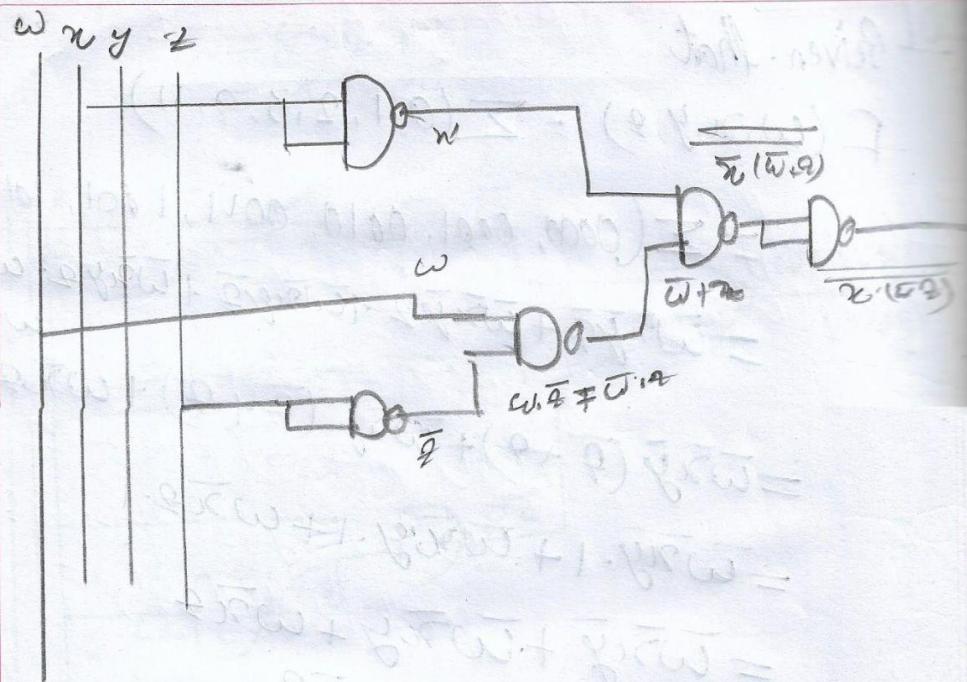
$$= \bar{x}(\bar{w} + w \cdot z)$$

$$= \bar{x}(\bar{w} + z)$$

$$= \bar{w}\bar{x} + \bar{x}z$$

$$= \bar{x}(w + z)$$

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Q1 Given that

$$f(a, b, c) = f(0, 5, 7)$$

$$= M_0 + M_5 + M_7$$

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$$= (a+b+c) \cdot (a'+b'+c') \cdot (a''+b''+c'')$$

$$= (a+b+c) (\bar{a} \cdot \bar{a} + \bar{a} \cdot b + \bar{a} \cdot c + b \cdot \bar{a})$$

$$= (a+b+c) (\bar{a} \cdot \bar{a} + \bar{a} \cdot \bar{c} + \bar{b} \cdot \bar{c} + \bar{c})$$

$$= (a+b+c) (\bar{a} + \bar{c} + \bar{a} \cdot \bar{b} + \bar{a} \cdot \bar{c} + \bar{b} \cdot \bar{c} + \bar{c})$$

$$= (a+b+c) (\bar{a} + \bar{c} + \bar{a} \cdot (\bar{b} + b) + \bar{a} \cdot \bar{c} + \bar{b} \cdot \bar{c})$$

$$= (a+b+c) (\bar{a} + \bar{c} + \bar{a} \cdot 1 + \bar{a} \cdot \bar{c} + \bar{c} \cdot (b + \bar{b}))$$

$$= (a+b+c) (\bar{a} + \bar{c} + \bar{a} \cdot \bar{c} + \bar{c})$$

$$= (a+b+c) (\bar{a} + \bar{c} \cdot (1 + \bar{a}) + \bar{c})$$

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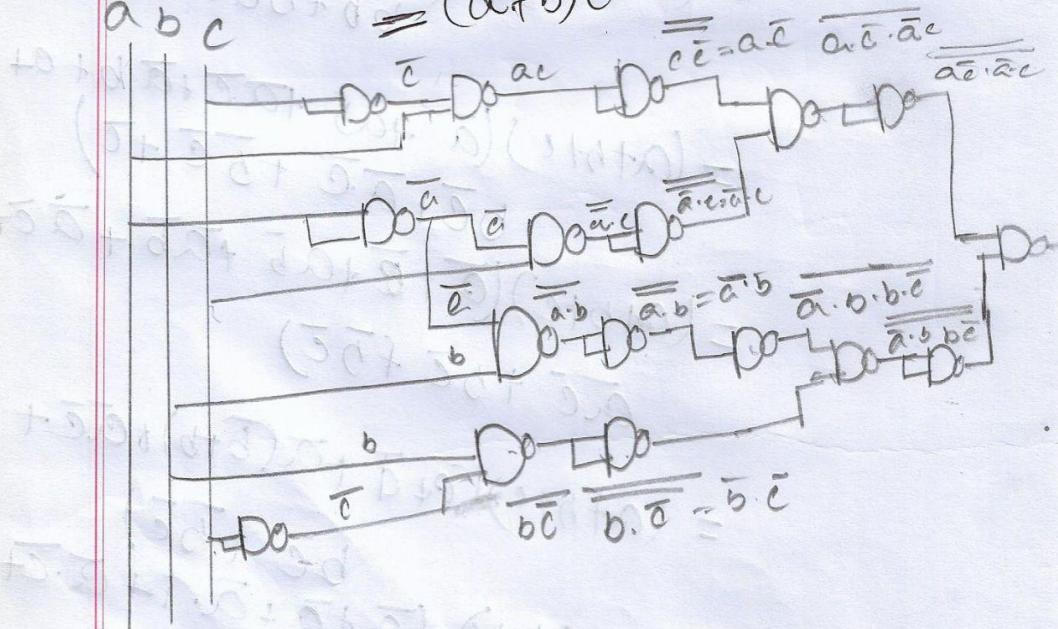
$$\begin{aligned}&= (a+b+c)(\bar{a}+\bar{c}+1+\bar{e}) \\&= (a+b+c)(\bar{a}+\bar{c})\end{aligned}$$

$$= (a\bar{a} + a\bar{c} + b\bar{a} + b\bar{e} + c\bar{a} + c\bar{e})$$

$$= (0 + a\bar{c} \cdot \bar{a}b + b\bar{c} + \bar{a}c + 0)$$

$$\begin{aligned}&= (\bar{c}\bar{c} + a\bar{c} + \bar{a}b + b\bar{c}) \\&\equiv (a+b)\bar{c} + \bar{a}(\bar{b}+b)\end{aligned}$$

a b c



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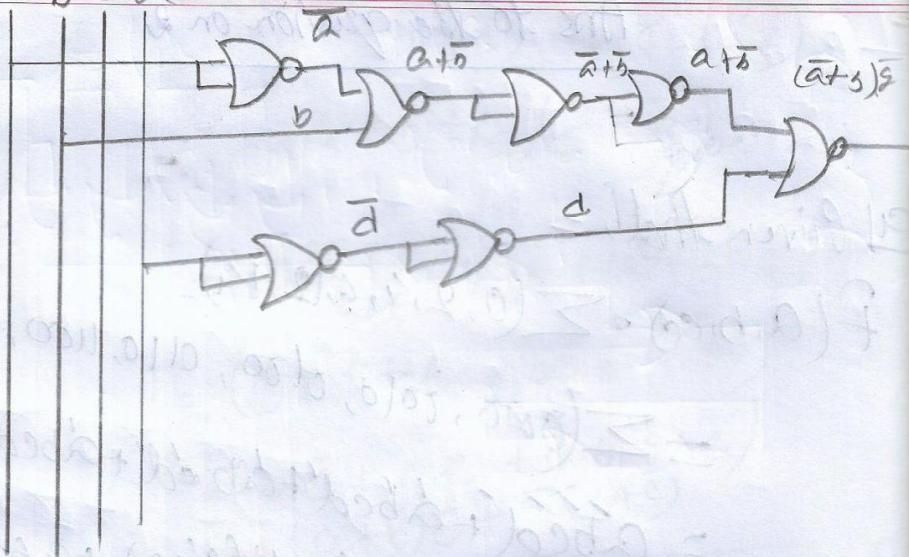
Ans to the question on 2

Q Given that,

$$\begin{aligned}f(a, b, c, d) &= \sum(0, 2, 4, 6, 12, 14) \\&= \sum(0000, 0010, 0100, 0110, 1000, 1100) \\&= \bar{a}\bar{b}\bar{c}\bar{d} + \bar{a}\bar{b}cd' + \bar{a}b\bar{c}d' + \bar{a}bd' + ab\bar{c}d' + \\&\quad abcd' \\&= \bar{a}\bar{b}d'(c'+c) + bd'(c'+c) + abd'(c'+c) \\&= \bar{a}\bar{b}d' + bd' + abd' \\&= a'd' + abd' \\&= d'(a' + ab) \\&= d'(a' + b) \\&= a'd' + bd'\end{aligned}$$

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a b c d



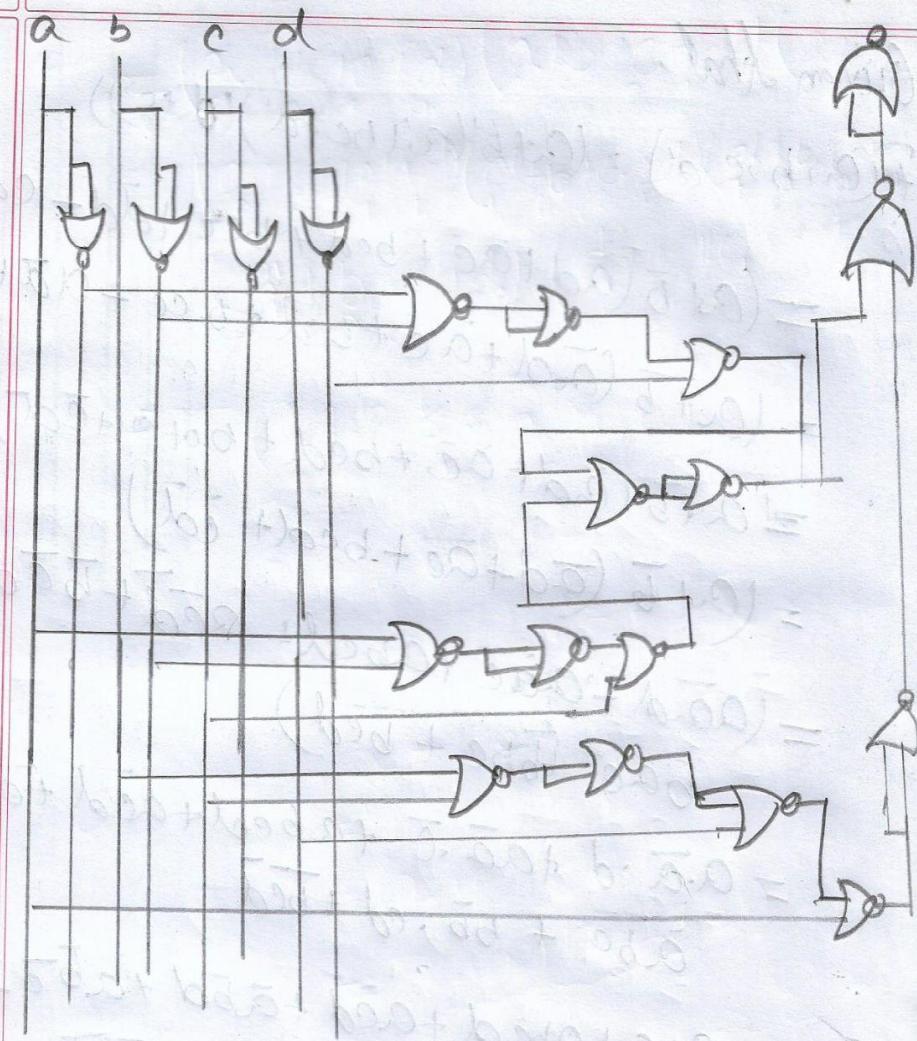
$$\begin{aligned} & \text{Stage 1: } a \oplus b = ab \\ & \text{Stage 2: } (\bar{a} \oplus \bar{b}) + ab = \bar{a}\bar{b} + ab \\ & \text{Stage 3: } (\bar{a} \oplus \bar{b}) + ab + \bar{a}\bar{b}ab = \bar{a}\bar{b}\bar{a}\bar{b} + ab\bar{a}\bar{b} + ab\bar{a}\bar{b}ab \\ & \text{Stage 4: } (\bar{a} \oplus \bar{b}) + ab + \bar{a}\bar{b}ab + \bar{a}\bar{b}\bar{a}\bar{b}ab = \bar{a}\bar{b}\bar{a}\bar{b}\bar{a}\bar{b}\bar{a}\bar{b}ab \end{aligned}$$

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Q Given that,

$$\begin{aligned}
 P(a, b, c, d) &= (a+b)(a'+b'c+d')(d+c') \\
 &= (a+b)(\bar{a}d + \bar{a}\bar{c} + bcd + b\bar{c}\bar{e} + \bar{b}\bar{d}d + \bar{c}\bar{d}) \\
 &= (a+b)(\bar{a}d + \bar{a}\bar{c} + bcd + b\cdot\bar{c}\bar{e} + a\bar{d} + \bar{c}\bar{d}) \\
 &= (a+b)(\bar{a}d + \bar{a}\bar{c} + bcd + b\cdot\bar{c}\bar{e} + 0 + 0 + \bar{c}\bar{d}) \\
 &= (a+b)(\bar{a}d + \bar{a}\bar{c} + bcd + \bar{c}\bar{d}) \\
 &= (a+b)(\bar{a}d + \bar{a}\bar{c} + bcd + \bar{c}\bar{d}) \\
 &= (\bar{a}d + a\bar{c} + abcd + \bar{a}\bar{c}\bar{d} + \bar{b}\bar{a}\bar{d} + \\
 &\quad \bar{b}\bar{a}\bar{c} + \bar{b}bc + \bar{b}\bar{c}\bar{d}) \\
 &= a\bar{a}\cdot d + a\bar{a}\cdot\bar{c} + abcd + \bar{a}\bar{c}\bar{d} + \bar{a}\bar{b}\bar{d} + \\
 &\quad \bar{a}\bar{b}\bar{c} + b\bar{b}\cdot\bar{c}\bar{d} + \bar{b}\bar{c}\bar{d} \\
 &= 0 + 0 + abcd + a\bar{c}\bar{d} + \bar{a}\bar{b}\bar{d} + \bar{a}\bar{b}\bar{c} + 0 + \\
 &= abcd + a\bar{c}\bar{d} + \bar{a}\bar{b}\bar{d} + \bar{a}\bar{b}\bar{c} + \bar{b}\bar{c}\bar{d}
 \end{aligned}$$

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$$a \cdot b \cdot c \cdot d + a \cdot b \cdot \bar{c} \cdot \bar{d} + a \cdot \bar{b} \cdot c \cdot \bar{d} + \bar{a} \cdot b \cdot c \cdot d =$$

$$a \cdot b \cdot c \cdot d + a \cdot b \cdot \bar{c} \cdot \bar{d} + a \cdot \bar{b} \cdot c \cdot \bar{d} + \bar{a} \cdot b \cdot c \cdot d =$$

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Q1 Given that:

$$f(a, b, c) = M(0, 5, 7)$$

$$= M_0 + M_5 + M_7$$

$$= (a+b+c) \cdot (a'+b+c') \cdot (a'+b'+c)$$

$$= (a+b+c) (\overline{a} \cdot \overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{b} + b \cdot \overline{c} + \overline{c} \cdot \overline{a} + \overline{c} \cdot \overline{b} + \overline{c} \cdot \overline{c})$$

$$= (a+b+c) (\overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{c} + \overline{c} \cdot \overline{b} + \overline{c})$$

$$= (a+b+c) (\overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{c} + \overline{c} \cdot \overline{b} + \overline{c})$$

$$= (a+b+c) (\overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{c} + \overline{c} \cdot \overline{b} + \overline{c})$$

$$= (a+b+c) (\overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{c} + \overline{c} \cdot \overline{b} + \overline{c})$$

$$= (a+b+c) (\overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{c} + \overline{c} \cdot \overline{b} + \overline{c})$$

$$= (a+b+c) (\overline{a} + \overline{a} \cdot \overline{b} + \overline{a} \cdot \overline{c} + b \cdot \overline{a} + b \cdot \overline{c} + \overline{c} \cdot \overline{b} + \overline{c})$$

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$$= (a+b+c)(\bar{a}+\bar{c}-1+\bar{e})$$

$$= (a+b+c)(\bar{a}+\bar{c})$$

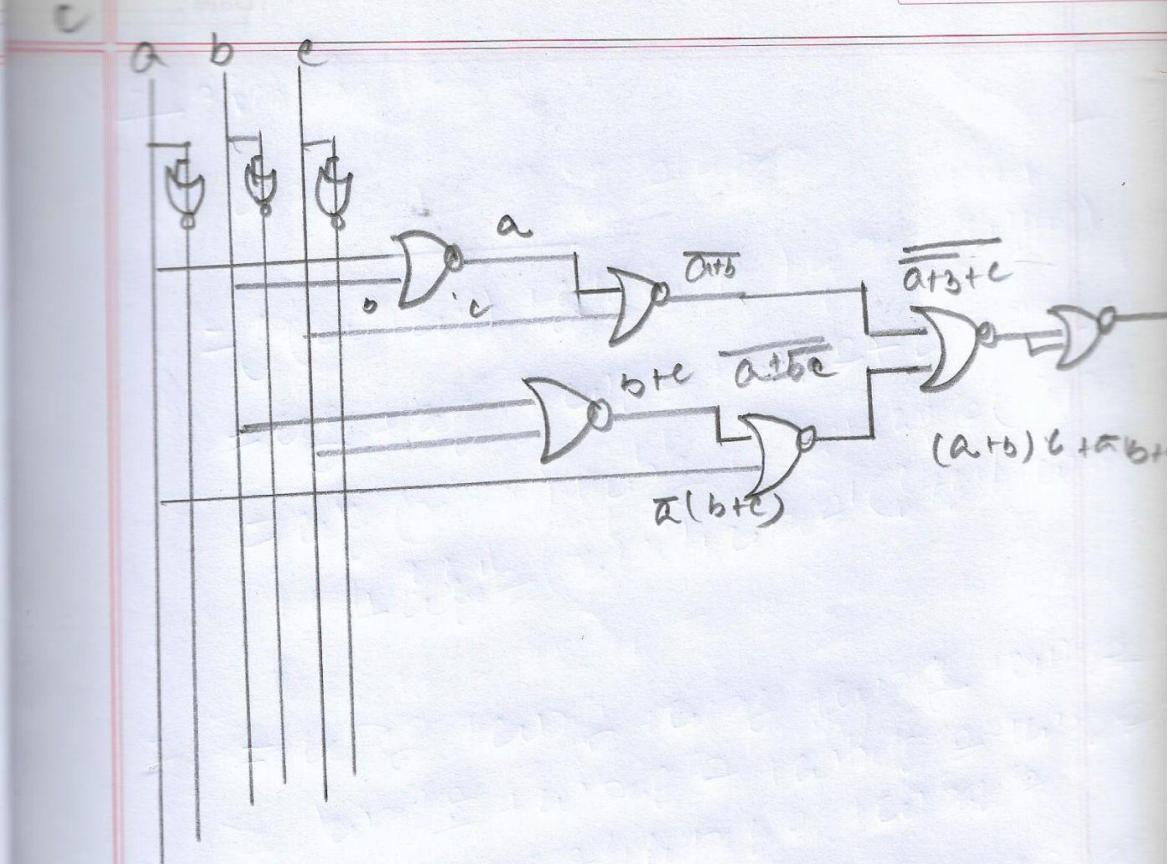
$$= (a\bar{a} + a\bar{c} + b\bar{a} + b\bar{e} + c\bar{a} + c\bar{e})$$

$$= (0 + a\bar{c} + \bar{a}b + b\bar{e} + \bar{a}c + 0)$$

$$= (a\bar{c} + a\bar{e} + \bar{a}b + b\bar{c})$$

$$= (a+b)\bar{c} + \bar{a}(b+c)$$

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Ans to the questions

a) Given that,

$$\begin{aligned}f(a, b, c, d) &= a'b + b(a+c) \\&= b(a' + a + c) \\&= b(1 + c) \\&= b \cdot 1 \\&= b \\&= b + a \cdot c' \\&= (a+b)(a'+b) \\&= (a+b+c \cdot c')(a'+b+c'c) \\&= (a+b+c)(a+b+c')(a'+b+c') \\&= (a+b+c+d)(a+b+c'+d+d') \\&\quad (a'+b+c+d+d')(a'+b+c'+d+d')\end{aligned}$$

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$$= (a_0 + b_0 + c_0 + d_0) (a'_0 + b'_0 + c'_0 + d'_0) (a''_0 + b''_0 + c''_0 + d''_0)$$
$$(a_1 + b_1 + c_1 + d_1) (a'_1 + b'_1 + c'_1 + d'_1) (a''_1 + b''_1 + c''_1 + d''_1)$$
$$(a_2 + b_2 + c_2 + d_2) (a'_2 + b'_2 + c'_2 + d'_2) (a''_2 + b''_2 + c''_2 + d''_2)$$
$$\dots$$
$$= \prod \{0, 1, 2, 3, 8, 9, 10, 11\}$$

$$(d+10)(a+b+c+d) =$$
$$(a+b+c+d)(a+b+c+d+10) =$$
$$(a+b+c+d)(a+b+c+d+10) =$$
$$(a+b+c+d)(a+b+c+d+10) =$$
$$(a+b+c+d)(a+b+c+d+10) =$$

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b) Given that,

$$\begin{aligned}f(a, b, c) &= a' + ab(b' + c') \\&= a' + abb' + abc' \\&= a' + a \cdot a' + abc' \\&= a' + abc' \\&= (a' + a)(a' + bc') \\&= (a' + bc') \\&= a' + bc' \\&= (a' + b)(a' + c') \\&= (a' + b + c')(a' + c') \\&= (a' + b + c')(a' + b + c') \\&\quad (a' + b + c')(a' + b + c') \\&= (a' + b + c') (a' + b + c') \\&\quad (a' + b + c') \\&= \begin{pmatrix} a' & b & c \\ 1 & 0 & 0 \end{pmatrix} \begin{pmatrix} a' & b & c \\ 1 & 0 & 0 \end{pmatrix} \\&= \begin{pmatrix} a' + b' + c' \\ 1 & 1 & 1 \end{pmatrix} \\&= \Pi(4, 5, 7)\end{aligned}$$

C1

Given that,

$$f(w, x, y, z) = xy + y'(z + w)$$

$$= xy + y'(z + w)(z + z')$$

$$= xy + y'(z + w)$$

$$= xy + y'z + wy'$$

$$= xy + wy' + y'z$$

$$= x(y + z') + y'z$$

$$= xw + y'z$$

$$= (x + z')(x + z)$$

$$= (x + y' + z')(x + z + yz')$$

$$= (x + z')(x + y' + z')(x + z + z')$$

$$= (x + z')(x + y' + z')(x + z + z')$$

$$= x + z' + z + zw(x + y' + z') \\ (x + z + z')$$

$$= (x + z' + z + zw)(x + y' + z')$$

$$= (w + x + y' + z)(w + x + y' + z)(w + x + y' + z) \\ (w + x + y' + z)(w + x + y' + z)(w + x + y' + z) \\ (w + x + y' + z)(w + x + y' + z)$$

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$$= (\omega + \alpha + \beta + \gamma) (\omega' + \alpha' + \beta' + \gamma') (\omega'' + \alpha'' + \beta'' + \gamma'')$$

$$= \prod (0, 2, 3, 8, 10, 11)$$

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Ans to the question on 4

Q Given that,

$$P(w, x, y, z) = yz + 2(y+z)$$

$$= yz + 2y + 2z$$

$$= yz(w+z) + 2y(w+z) + 2z(w+z)$$

$$= wyz + wz^2 + wyz + w'yz + wz^2 + w'z^2$$

$$= wyz'(w+z) + w'yz'(w+z) + wz^2 \text{ (Ans)} \\ + w'yz(w+z) + wz^2(y+z) + wz^2(y+z)$$

$$= wnyz + wnyz' + wnyz + wnyz'$$

$$wnyz + wnz^2 + wnyz + wnyz' + wnyz + wnyz' + wnyz + wnyz'$$

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$$= \cancel{w_{10}y_0} + \cancel{w_{10}y_1} + w_{10}y_2$$

$$= w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + \\ w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + \\ w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2' + w_{10}y_2'$$

$$= \sum (11100, 10100, 01100, 1111, 1011, 0111, 0011)$$

$$1001, 0001, 0010)$$

$$1, 2, 3, 6, 7, 9, 10, 11, 14, 15)$$

$$= \sum (14, 10, 0, 15, 11, 7, 3, 3, 9, 1, 2)$$

$$= \sum (1, 2, 3, 6, 7, 9, 10, 11, 14, 15)$$

b1 Given that,

$$P(a,b,c) = b + c'(a'b'e)$$

$$= b + ca' + cb'e$$

$$= b + ca' + c'e \cdot b'$$

$$= b + ac' + 0$$

$$= b + ac'$$

$$= b(a + a') + cd(b + b')$$

$$= ab + ab' + a'b + a'b'e$$

$$= ab(a + c') + a'b(c + c') \text{ take } (c + c')$$

$$= abc + abc' + abc + abc' + abc + abc'$$

$$= abc + abc' + abc + abc' + abc + abc'$$

$$= \sum(7, 0, 3, 2, 0)$$

$$\therefore \bar{\Sigma} (0, 2, 3, 6, 7)$$

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Given that

$$\begin{aligned}
 f(w, x, y, z) &= y + y'z + zy' \\
 &= y(w+w') + y'z(w+w') + zy'(w+w') \\
 &= wy + w'y + wz'y' + w'yz + wz'y + w'yz \\
 &= wy(x+u) + w'y(x+u) + w'yz(x+u) + w'yz \\
 &\quad + w'yz'(x+u) + wz'y'(y+z') + wz'y \\
 &= wxy + wxyz' + w'xy + w'xyz' + w'yz \\
 &\quad + wxyz' + w'yz' + wz'y'z + wz'y'z \\
 &= wxy(z+z') + wxyz'(z+z') + w'yz(z+z') \\
 &\quad + w'xyz'(z+z') + w'xyz + w'xyz' + \\
 &\quad wxyz' + wxyz' + wxyz' + wxyz' + wxyz' \\
 &\quad + wxyz' + wxyz' + wxyz' + wxyz' + wxyz'
 \end{aligned}$$

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$$\begin{aligned} &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2' + w_{12}^2 g_2 + w_{21}^2 g_2' + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \end{aligned}$$

$$= \sum (1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14)$$

$$\begin{aligned} &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \end{aligned}$$

$$\begin{aligned} &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \\ &= w_{11}^2 g_2 + w_{12}^2 g_2' + w_{21}^2 g_2 + \end{aligned}$$

