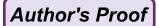
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Abstract	concurrently undergo apprehensively set synchrony of action potent and patchy connections of forming clearly defined hexagonal array, where pand less defined structure the competitive principle organisation of response effects of stimulus orientation of connections leads to superimposed spatio-tem	divide and generate action potentials, they poptosis. We propose that the ensemble on elected is that which generates the maximum stials. Consequently, local intracortical neurons emerge in "ultra-small" world configurations, a macrocolumns and patch connections in eatch connections have relatively long axons, ares elsewhere in the cortex. Extension of the to local synaptic level explains ante-natal properties in primary visual cortex, including tion, angle relative to motion, length, and speed preference. Post-natal Hebbian consolidation the mature configuration. By implication, poral images, rather than categorical feature rate of cortical information processing.		
Keywords (separated by "-")	embryogenesis - Cortica Neural small worlds - V	l patch connections - Cortical l apoptosis - Synchronous oscillation - l organization - Cortical visual responses - s - Spatio-temporal neural images		



J.J. Wright and P.D. Bourke

Abstract As neuron precursors divide and generate action potentials, they 4 concurrently undergo apoptosis. We propose that the ensemble on neurons 5 competitively selected is that which generates the maximum synchrony of action 6 potentials. Consequently, local intracortical neurons and patchy connections emerge 7 in "ultra-small" world configurations, forming clearly defined macrocolumns and 8 patch connections in hexagonal array, where patch connections have relatively 9 long axons, and less defined structures elsewhere in the cortex. Extension of 10 the competitive principle to local synaptic level explains ante-natal organisation 11 of response properties in primary visual cortex, including effects of stimulus 12 orientation, angle relative to motion, length, and speed on apparent orientation 13 preference. Post-natal Hebbian consolidation of connections leads to the mature 14 configuration. By implication, superimposed spatio-temporal images, rather than 15 categorical feature responses, form the substrate of cortical information processing. 16

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Keywords Macrocolumns • Cortical patch connections • Cortical embryogenesis 17
Cortical apoptosis • Synchronous oscillation • Neural small worlds 18
V1 organization • Cortical visual responses • Cortical feature responses 19
Spatio-temporal neural images

1 Introduction

During embryogenesis cells that become the neurons of the cerebral cortex divide 22 and migrate to their mature positions while undergoing apoptosis –the cell death 23 of a substantial fraction of their number – ultimately forming minicolumns in 24 their radial disposition, while in their surface disposition they are said to form 25

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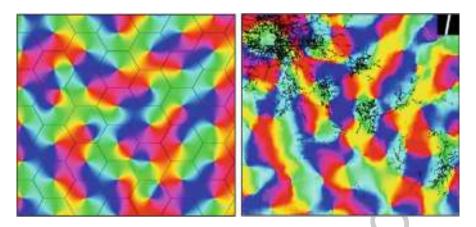
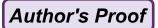


Fig. 1 *Left:* idealized diagram of organization in V1 of OP, 0–180°, about singularities, and with marginal continuity, within an hexagonal framework composed of superficial patch connections. *Right:* experimental data [18]. The *black* areas are patchy synaptic connections

macrocolumns – periodic structures that are most apparent in the primary visual 26 (V1) and somatosensory (S1) cortices, are each about 300 µm across, and are 27 roughly delineated by superficial patchy connections on the perimeter of each 28 column. Within each column, individual cells in V1 respond with an orientation 29 preference (OP) to visual lines of differing orientation [1]. The surface organization 30 of OP exhibits significant hexagonal rotational periodicity, in which each roughly 31 delineated macro- columnar unit exhibits all values of OP arrayed around a pin-32 wheel [2, 3]. Varying chirality and orientation of the pinwheels achieves continuity 33 of OP at the columnar margins, and patchy connections link areas of similar OP 34 together, "like to like" (Fig. 1).

Hubel [4], in his Nobel address, hailed Mountcastle's original proposal that 36 columns formed fundamental building blocks of cortex as "Surely the most 37 important contribution to understanding of cerebral cortex since Ramon y Cajal". 38 Enthusiasm for the explanatory power of the concept has since waned. Horton and 39 Adams [5] described the cortical column as "a structure without a function", and 40 terminology describing them has become confused [6].

Difficulties arise partly because columnar structure is not clearly apparent outside 42 V1 and S1, and because there is marked interspecies variation in definition of 43 columns even in V1, to the point of apparent absence in small animals. Attempts to 44 model the emergence of columnar organization of OP have also struck considerable 45 difficulty. In some species there is clear emergence of structure ante-natally, rather 46 than post-natally, yet models of the macrocolumn are generally dependent on 47 response to visual features [7]. Which "features" are regarded as fundamental is 48 also controversial, and how this relates to signal processing is problematic.



We have proposed a theory of emergence of cortical columns and their functional 50 significance [8], which differs considerably from all other explanations. We base our 51 explanation on two findings; (1) in vitro, embryonic neurons fire synchronously and 52 self-organize into "small worlds" [9] and (2) synchronous firing of neurons prevents 53 their apoptosis [10].

We assume synchrony and cell survival are causally linked – perhaps because 55 some collective pumping action allows a synchronously coupled assembly of cells 56 to increase their uptake of one or more vital metabolic substances. Therefore the 57 emergent cell network would be that selection of cell types, and their arrangement, 58 that maximizes the amplitude of synchrony for a given limit of total metabolic 59 supply. The consequences of these assumptions are as follows.

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Selection for "Small-World" Connectivity 2

Our arguments are based upon properties demonstrated in simulations of cortical 62 gamma synchrony, and travelling waves [11, 12]. Closely situated cells are able to 63 exchange synchronous pulses with smaller phase difference of afferent and efferent 64 pulses. Therefore minimization of the total axonal lengths of their interconnections 65 maximises synchrony magnitude (and uptake) while minimizing axonal metabolic 66 cost.

In the dilute network of neuronal connections, the metric distance of soma 68 separation is proportional to "degree of separation" in the topological sense. 69 Therefore maximization of synchrony, by minimizing axonal lengths, selects a 70 neural network with "ultra-small world" connectivity. This requires, in turn, that 71 the average density of synaptic connectivity decline with distance as a power 72 function [13].

A power function is the sum of exponential functions, and pre-synaptic densities 74 of cortical neurons decline roughly exponentially [14]. Therefore small-world 75 connectivity can be approximated from populations of neurons with differing 76 characteristic ranges. 77

Local Variability of Axonal Ranges in the Selected **Population**

Equal approximations to a power function can be achieved by combining different 80 relative densities of a variety of cell types, each type characterised by axonal length. 81 Simplifying to only two types, Figures 2 and 3 show where long/short axon length is 82 large $(\lambda_{\beta} \gg \lambda_{\alpha})$ approximation of a power curve requires the ratio of local neurons 83 to patch neurons be large $(N_{\beta} \gg N_{\alpha})$.

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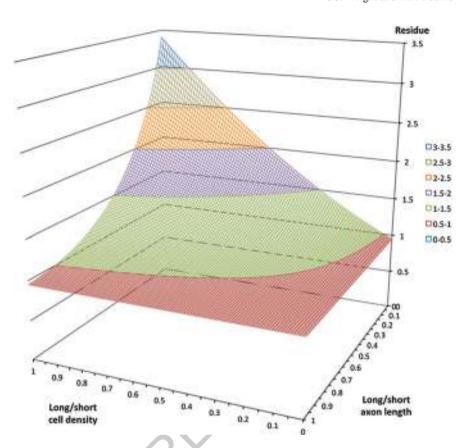


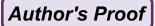
Fig. 2 Equal approximations to a power function can be achieved with a variety of combinations of cell densities and axonal ranges. *Colour margins* show fit-residual isocontours

4 Resolution into Macrocolumns

It can be shown that, where J is the magnitude of synchronous oscillation, and \mathbf{q} , \mathbf{r} 86 are positions of excitatory neurons in the cortex,

$$J \propto \int_{\mathbf{q}} \int_{\mathbf{r}} \left(N_{\alpha} \lambda_{\alpha} e^{-\lambda_{\alpha} |\mathbf{q} - \mathbf{r}|} + N_{\beta} \lambda_{\beta} e^{-\lambda_{\beta} |\mathbf{q} - \mathbf{r}|} \right) d\mathbf{q} d\mathbf{r}$$

Therefore synchrony is maximized by selection of that ensemble of cells in which 88 the cells with relatively short but dense axons are closely situated to each other. Such 89 packing forces the cells with long-range axons to form connections at longer range, 90 enforcing a "patchy" connection system. Arrangement in an hexagonal patchwork 91 optimizes this synchrony-facilitating orderliness, but a clearly demarcated arrange- 92 ment of this type is only possible where 93



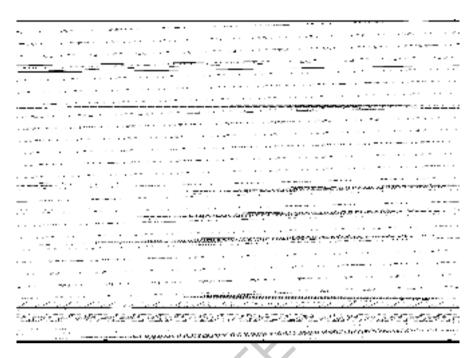


Fig. 3 Cell densities and axonal ranges of local and patch neurons vary approximately inversely for equivalent fits to a power function obtained along the lowest-residual iso-contour in Fig. 2. Intersingularity distance (cp Fig. 4) is comparatively invariant over this range

$$\frac{local\ cells}{local\ cells\ +\ patch\ cells} = \frac{N_{\beta}}{N_{\alpha} + N_{\beta}} \ge \frac{\pi}{2\sqrt{3}}$$

This follows simply from the ratio of area of a circle to a hexagon, when local 94 cells are enclosed within an hexagonal patch-connection frame. Therefore the 95 absence of a clearly columnar arrangement does not imply a loss of the small 96 world organization, nor does it deny that both short-range local connections, and 97 longer-range functional connections are present – the distinct types are merely more 98 entangled with each other (See Fig. 4).

Thus, variation of the clarity of demarcation of columns in differing cortical areas, and between species, need not reflect major differences in function.

5 A Mobius Map Within Macrocolumns

Restated in physical terms, the maximization of J requires the populations of cells 103 of differing axonal range be geometrically arranged so as to permit maximum 104 resonance throughout the system. Since the amplitude of synchronous oscillation 105

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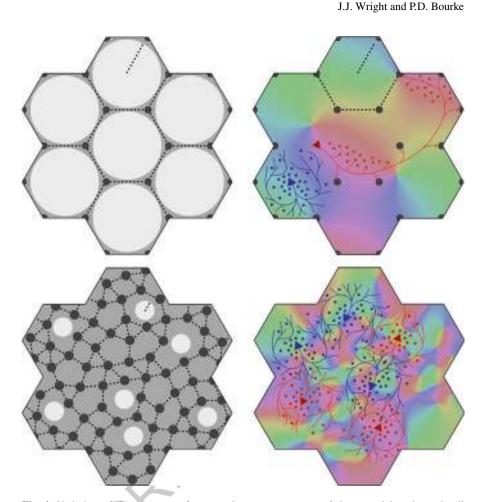


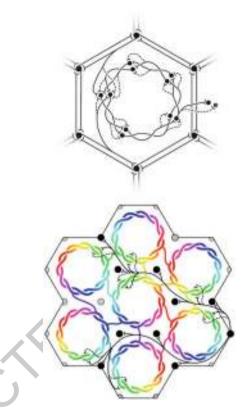
Fig. 4 Variation of the structure of macrocolumns at extremes of the axonal lengths and cell numbers in Fig. 3. *Top*: With large long/short axon length ratio, clearly resolved hexagonal organization emerges, with long (*red*) patch connections linking "like to like", and highly clustered short intracortical axons (*blue*). *Bottom*: near-complete loss of resolution when long/short axon ratio approaches 1

declines with distance of separation of cell bodies, then the system of patch 106 connections and the local neurons within each macrocolumn must achieve a 1:1 107 connection system, promoting resonance between cells in each macrocolumn, and 108 the surrounding patch system, and thus forming an input map of the cortical 109 surround, projected onto each macrocolumn. If it is additionally assumed that the 110 competition for crucial resources is not simply between individual neurons, but also 111 between closely situated pre-synapses arising from the same cell, then "winner take 112 all" competition between closely situated synaptic connections would develop, and 113 at equilibrium each cell would then require high firing correlation with some of its 114 neighbors, and low firing correlation with other neighbors – and be correspondingly 115

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Fig. 5 Maximization of synchrony with local synaptic competition leads to Mobius ordering, within macrocolumns. Top: Equilibrium disposition of saturated (solid) and sensitive (dashed) synapses in the developing neocortex. Bottom: "Like to like" saturated patchy connections map the same part of the surrounding cortical field onto homologous cell positions on the Möbius configuration



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strongly linked to some neighbors by "saturated" synapses, and weakly to others 116 by "sensitive" synapses. This intra-cellular constraint, along with the requirement 117 to form a 1:1 map of connections between each macrocolumn and its patchy- 118 connection surround, can be met if the connections within the macrocolumn form 119 a closed system analogous to a Mobius strip. Figure 5 (top) shows how a dynamic 120 equilibrium of synaptic connections can thus be struck. The mapping of the patch 121 system onto the macrocolumn can be expressed as

$$\mathbf{P}\left(\left|\mathbf{R}-\mathbf{C}_{j}\right|,\vartheta\right)\rightarrow\mathbf{p}^{[2]}\left(\left|\mathbf{r}-\mathbf{C}_{j}\right|,\pm\vartheta+\varphi\right)$$

where P is the plane of the patchy connections, and R are cortical positions with 123 reference to these, while **P** and **r** are corresponding plane and positions within a 124 macrocolumn. The square brackets (here [2]) indicate the map's resemblance, if 125 viewed from a third dimension, to a 2:1 map formed by squaring a complex vector. 126 C_i is the origin of both **P** and $\mathbf{p}^{[2]}$ for the j-th local map, and corresponds to 127 the position of the OP singularity in that macrocolumn. ϑ is the polar angle of R, 128 chirality of the local map is indicated by $\pm \vartheta$, and φ is the orientation of the local 129 map relative to the global map.

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Figure 5 (bottom) shows further requirements for synchrony maximization. On 131 the input map, radial lines on the surrounding cortex must map about a centre, 132 analogous to an OP singularity. The Mobius strip-like folding of connections means 133 that "OP" from 0 to 180° is mapped 0 to 360° about the singularity – concealing 134 a superposition of diametrically opposite lines projected from the cortex to the 135 macrocolumn. To further increase resonance, patch connections must link "like to 136 like" OP in forming multiple 1:1 maps, and adjacent macrocolumns must also be so 137 arranged as to increase resonance by linking "like to like" map positions on adjacent 138 macrocolumns, as closely as possible within a roughly hexagonal framework. Thus, 139 the properties of V1 sketched in Fig. 1 are reproduced.

These considerations apply to the development of the cortex prior to the 141 beginning of vision at birth.

Consequences of Eye-Opening and Development of Responses to Stimuli

The dynamic equilibrium of synaptic activity described above presumably gives 145 rise to some persistence of the structure on Hebbian principles, but subsequent to 146 birth, inputs from the direct visual pathway must produce strong perturbations from 147 equilibrium, and overwriting of the Mobius structure by later learning.

To fire rapidly in the mature brain, individual neurons in V1 require direct visual 149 input from their receptive fields, in summation with "contextual" signals transferred 150 laterally by the patch system – and on firing, they give rise to further, laterally spreading, contextual signals, forming travelling waves.

The transfer of these waves from the wider cortex to each macrocolumn, 153 considered as transfer to a Mobius-like map, is then a mapping with time lags of 154 an image, O, given by

$$O\left(\mathbf{P},t\right) \to O\left(\mathbf{p}^{[2]},t+\frac{|\mathbf{R}-\mathbf{r}|}{v}\right)$$

where v is the wave speed.

This permits the simulation of V1 neuron responses to visual moving lines, by 157 calculating the corollary inputs reaching a macrocolumn at the time the direct visual 158 input reaches the same macrocolumn, as shown in Fig. 6. 159

The results match the experimental data of Basole et al. [15] – data considered 160 incompatible with earlier notions of V1 neuron OP specificity.

In the case of a visual line of given length, the selective neuron responses vary 162 not only with line orientation, but also with its inclination to the direction of travel, 163 and speed, as shown in Fig. 7. Notably, the "classic" property of elementary OP is 164 seen only for low stimulus speeds.

The results of Basole et al. have been otherwise explained by assuming V1 neu- 166 rons show specific tuning to combinations of object orientation, spatial frequency 167

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Neural Field Dynamics and the Development of the Cerebral Cortex

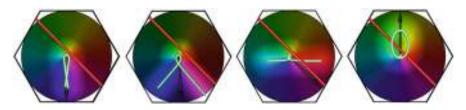


Fig. 6 In V1, lateral transmission via patchy connections, plus input from direct visual pathway, summates above threshold for action potentials. Results for a line moving from left to right, and oriented at 45° to the line of passage, with stimulus speed/wave speed, left to right, 0.1, 0.5, 1.0, 1.5

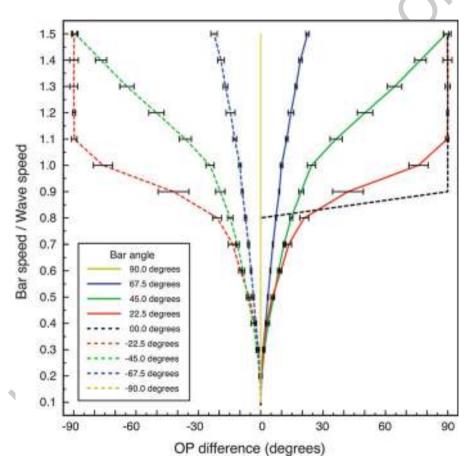


Fig. 7 Simulation results: change in apparent OP, and standard error of the estimate, as a function of bar speed to wave speed, for lines at different orientations to their directions of motion. Bar length 6 macrocolumn diameters

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and temporal frequency [16]. We have shown that Issa et al.'s description is 168 equivalent to the effect of Hebbian learning upon the properties demonstrated in 169 our simulation. Overwriting of the pre-natal Mobius maps by post-natal Hebbian 170 learning also explains the consolidation of "like to like" patchy connections, and 171 the continuity and completeness required by dimension-reduction models [7] of 172 response maps.

Interactions Between Cortical Areas

The same principles of self-organization should apply widely in the cortex. If so, 175 then cortical areas self-organized into patchy connections and macrocolumns could 176 also interact with other cortical areas via cortico-cortical fibers. Favorov and Kursun 177 [17] have demonstrated the potential of neocortical layer 4 to permit near-linear 178 superposition of impulses relayed via cortico-cortical fibers. Co-resonance among 179 sets of macrocolumns at multiple scales would thus be possible. With such an ante- 180 natal organization, after birth, signals from the environment could then produce 181 complex contextual superpositions of waves relayed between groups of Mobius 182 maps.

One such instance is modeled in Fig. 8, showing how neuron responses to com- 184 pound aspects of moving visual stimuli could arise. Similarly, return transmission 185 from higher to lower cortical areas might mediate some aspects of attention.

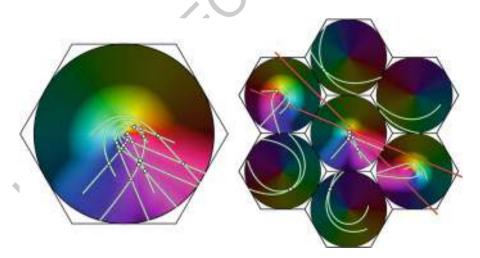


Fig. 8 Inter-areal interactions. Right: a complex of macrocolumns in V1, three of which are concurrently activated by a moving visual line. Left: A column in a higher visual area, which is co-resonant at equilibrium with the lower-centre complex. Transient signals from the lower to the higher system, result in superposition of signals representing different positions on, and times of passage of, the moving line



Conclusions 8 187

Our account emphasizes the importance of cooperative and competitive processes 188 in embryonic development, in addition to genetically programmed developmental 189 cascades. It explains diverse aspects of neural architecture and function in a 190 unified way, including the ante-natal emergence of functional structures in V1, 191 the origin of macrocolumns and superficial patch connections, their tendency to 192 hexagonal periodicity, their interareal and interspecies variation, and the response 193 properties of V1 neurons, including the post-natal abnormalities produced by visual 194 deprivation. The model can also be combined with models utilizing Turing pattern 195 formation, to account for the origin of OD columns. The principles may (with 196 appropriate adjustment for local cell forms and the organization of input pathways) 197 be applicable to other sensory modes, and even motor cortex. At the time of writing 198 preliminary evidence has been obtained of the existence of Mobius-like organization 199 in macrocolumns of the sensorimotor cortex.

As well as the capacity to explain empirical data, there are interesting implica- 201 tions for theories of neural information processing. The ultra-small-world configura- 202 tion implies that the organization is near a maximum for speed and energy-efficiency 203 of processing. Synaptic storage capacity can reach theoretical maximum entropy, 204 under the assumption that available metabolic resources are sufficient to sustain 205 only 50 % of synapses at maximum saturation. The modular organization offers a 206 potential for the rapid expansion of the cerebral cortex seen in its evolution.

Perhaps most importantly, the model indicates that brain function may be built 208 upon a primary, ab initio, spatial organization that can act as a reference framework 209 for sensory inputs from the environment as well as for internal dynamics of the 210 Freeman type. Not abstract features, but superimposed spatio-temporal images, may form the kernel of cerebral information processing.

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