Graph Theory: Lecture No. 29

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If G is a graph with n vertices and degrees $d_1 \leq d_2 \leq \ldots \leq d_n$ then the n-tuple (d_1, \ldots, d_n) is called the degree sequence of G. An arbitrary integer sequence (a_1, a_2, \ldots, a_n) is called Hamiltonian, if every graph with n vertices and a degree sequence pointwise greater than (a_1, a_2, \ldots, a_n) is hamiltonian. An integer sequence $(a_1, a_2, ..., a_n)$ such that $0 \le a_1 \le a_2 \le ... a_n < n$ and $n \ge 3$ is hamiltonian if and only if the following holds for every i < n/2: $a_i \le i \to a_{n-i} \ge n-i$.