

Control-Signal Crosstalk in Flip-Chip Superconducting Quantum Processors

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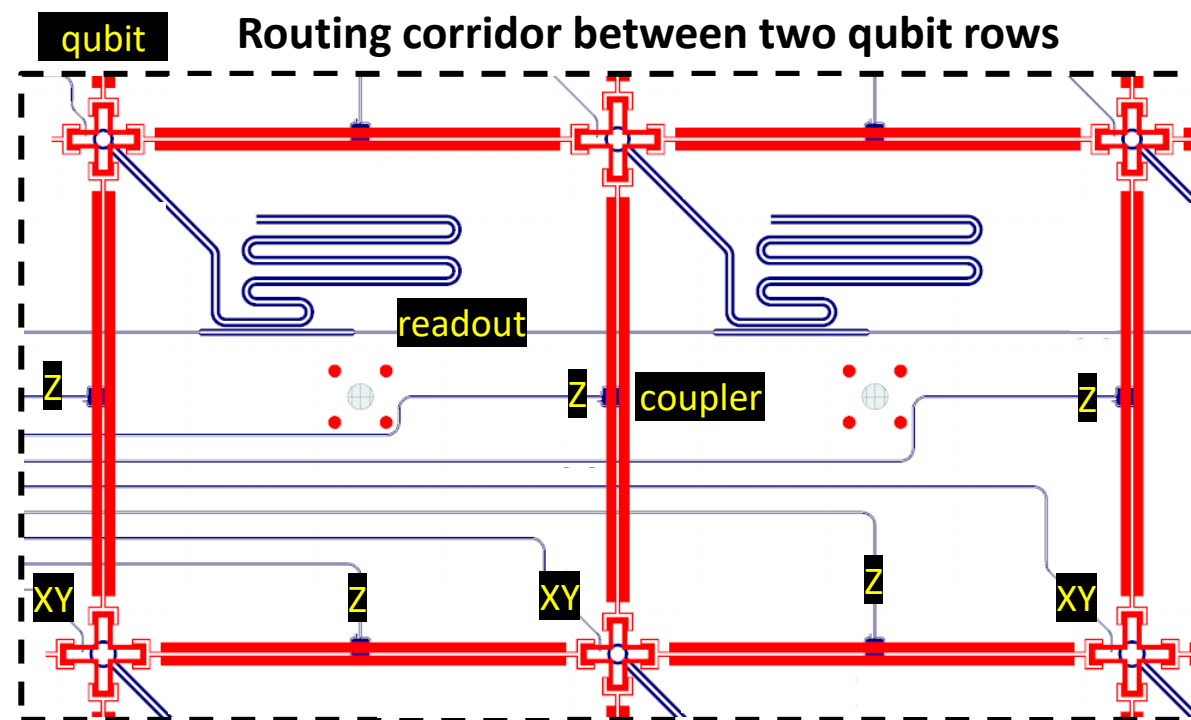
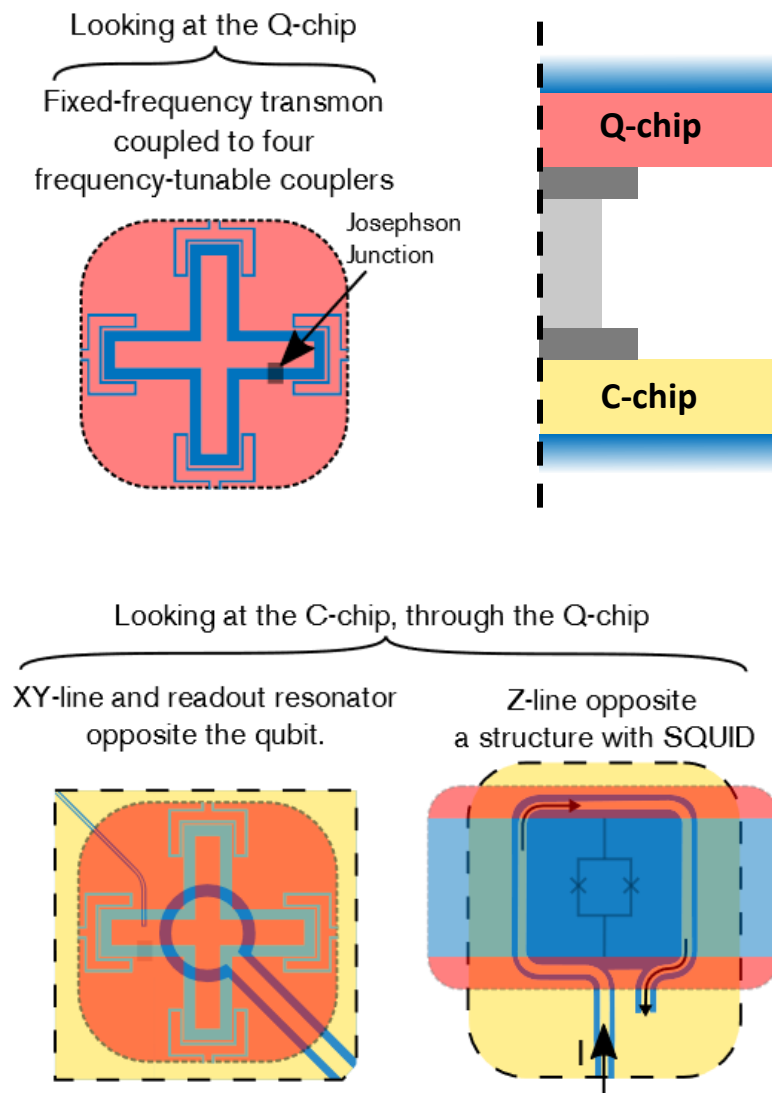
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Packaged Flip-Chip Module

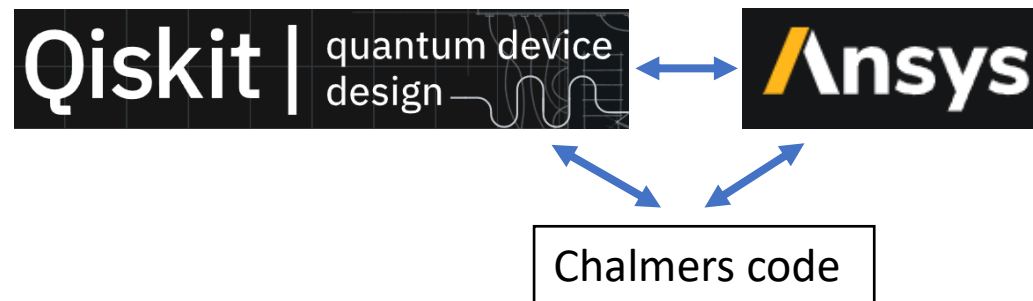
Chip Design & Fabrication by Chalmers
Flip-Chip Packaging by VTT
Sample Holder & PCB concept by Chalmers

1st generation flip-chip processors with a scalable layout and routing strategy

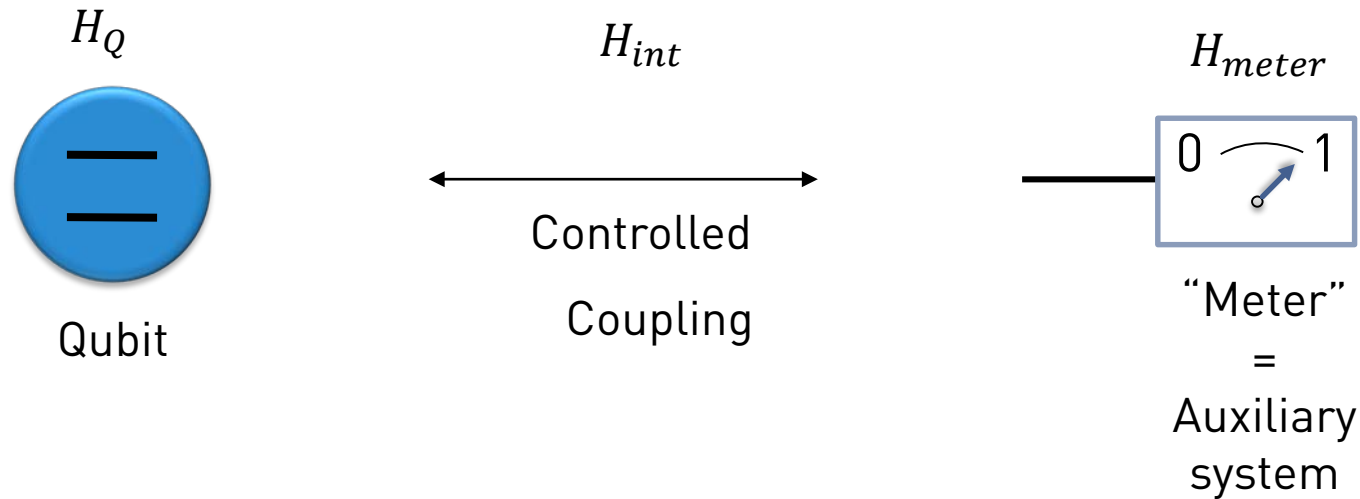
Basic elements



Automation of design and simulation



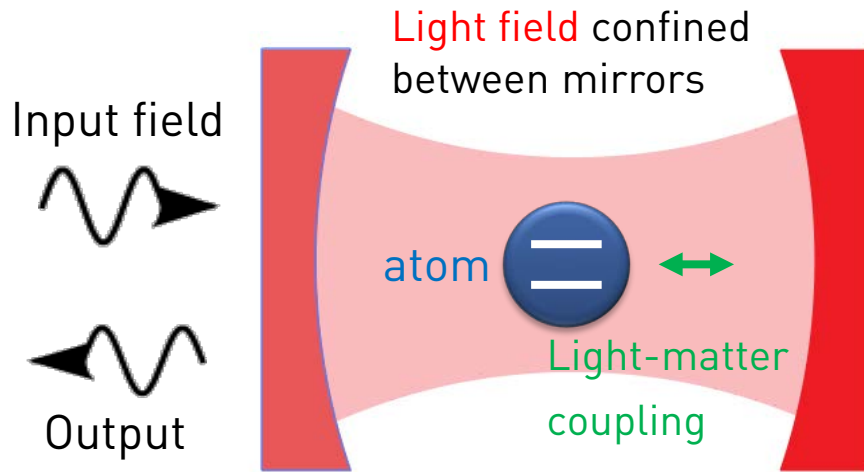
1.1 General properties of quantum measurements



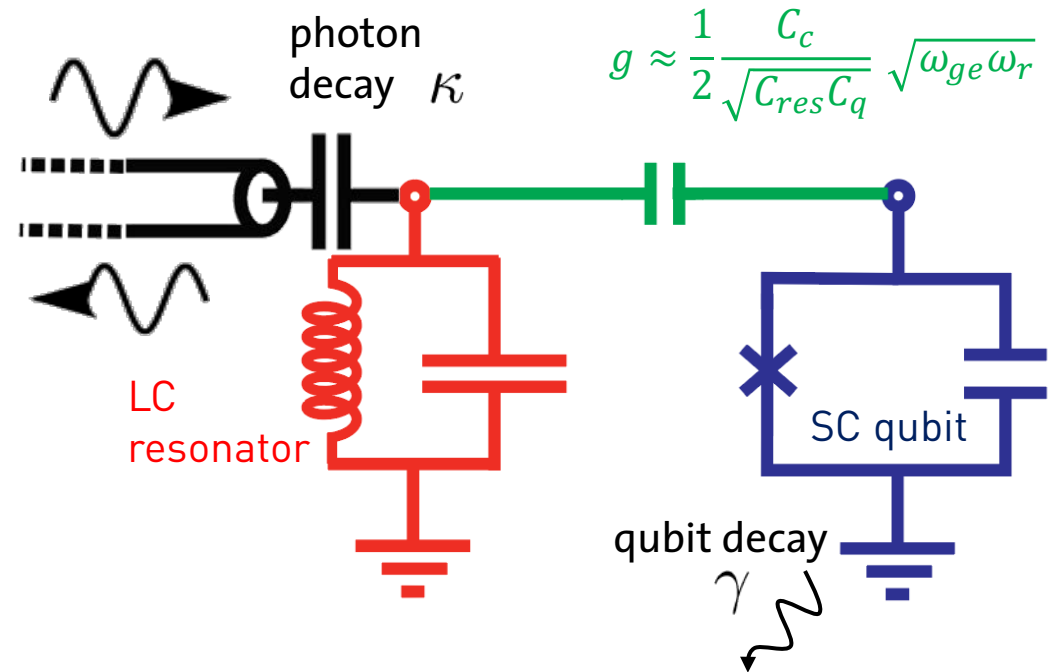
Desirable properties:

- Projective and Quantum non-demolition (QND)
 - Coupling to the meter does not change the state of the qubit $[H_Q, H_{int}] = 0$.
 - Repeated measurement yields the same outcome.
- Good ON/OFF ratio
 - $[H_{int}, H_{meter}] = 0$ during "OFF"
 - $[H_{int}, H_{meter}] \neq 0$ during "ON"
- No spontaneous decay/excitation due to measurement apparatus
- Fast and high fidelity

1.2 Circuit QED



Circuit
equivalent



System Hamiltonian (compare chapter 2):

$$H_{\text{sys}}/\hbar = \omega_r a^\dagger a + \omega_{ge} b^\dagger b - \frac{\alpha}{2} (b^\dagger)^2 b^2 - g(a - a^\dagger)(b - b^\dagger)$$

$$= \boxed{\omega_r a^\dagger a} + \boxed{\frac{\omega_{ge}}{2} \sigma^z} + \boxed{g(a^\dagger \sigma^- + a \sigma^+)}$$

Resonator field

qubit

coupling

Jaynes-Cummings
Hamiltonian

- Rotating wave approximation (RWA)
- Two-level approximation

1.3 Circuit QED: Resonant case and dispersive limit

Jaynes-Cummings Hamiltonian:

$$H/\hbar = \underbrace{\omega_r a^\dagger a}_{\text{quantized field}} + \underbrace{\frac{\omega_{ge}}{2} \sigma^z}_{\text{qubit}} + \underbrace{g(a^\dagger \sigma^- + a \sigma^+)}_{\text{coupling}}$$

Strong coupling regime: $g > \gamma, \kappa$

What happens
in the limit of large detuning?

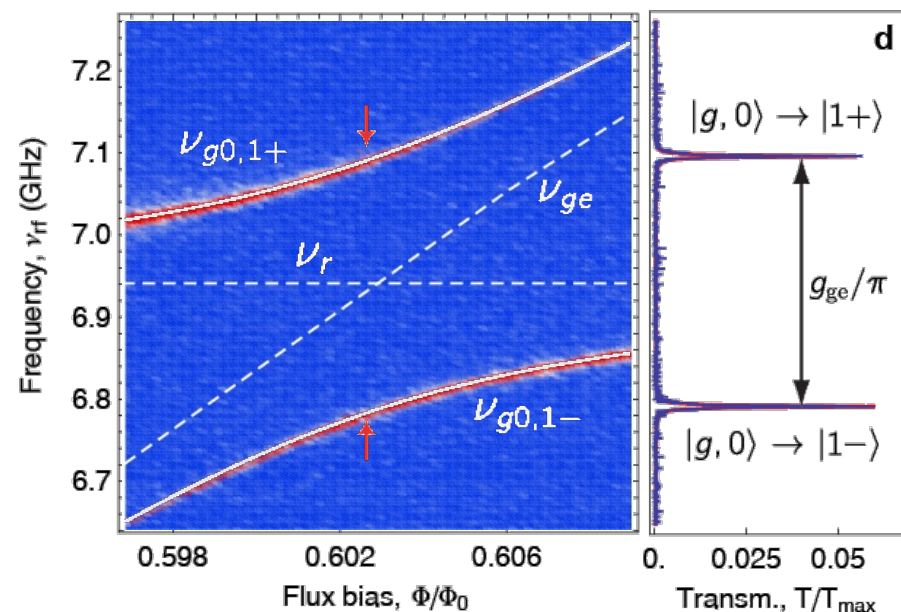
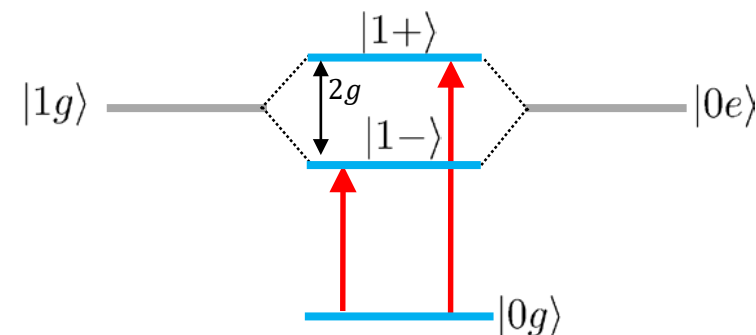
$$|\Delta| = |\omega_{ge} - \omega_r| \gg g$$

$$\chi \sigma_z a^\dagger a$$

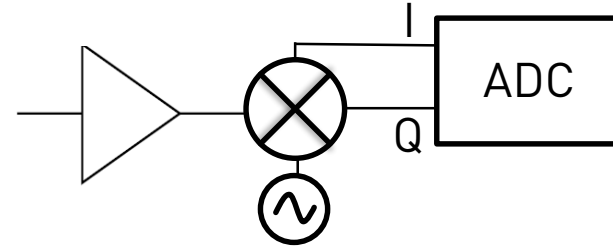
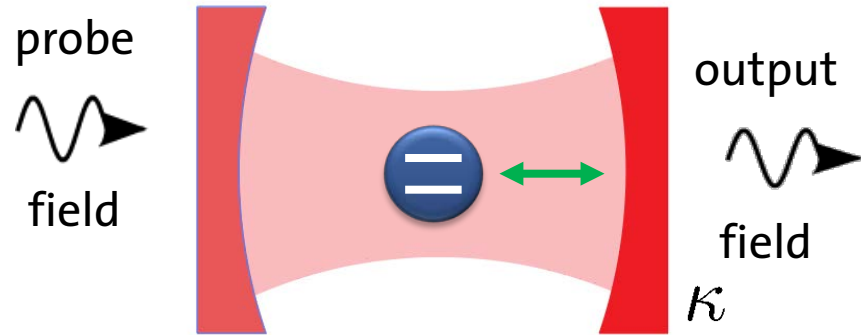
Dispersive coupling

- Limit of large detuning is referred to as the dispersive limit. No resonant exchange of excitations.
- In the dispersive regime coupling Hamiltonian commutes with qubit Hamiltonian.

Energy level diagram for resonant case $\omega_r = \omega_{ge}$:



1.4 Principle of Dispersive Qubit Measurement



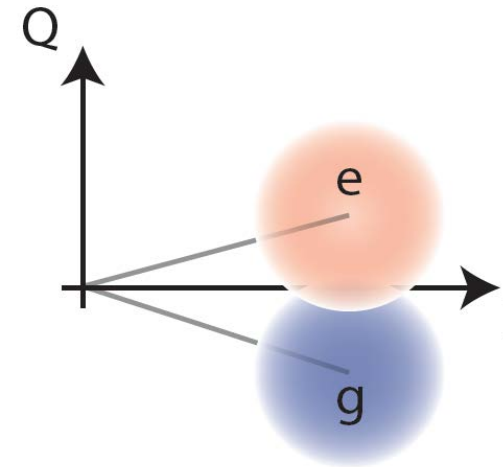
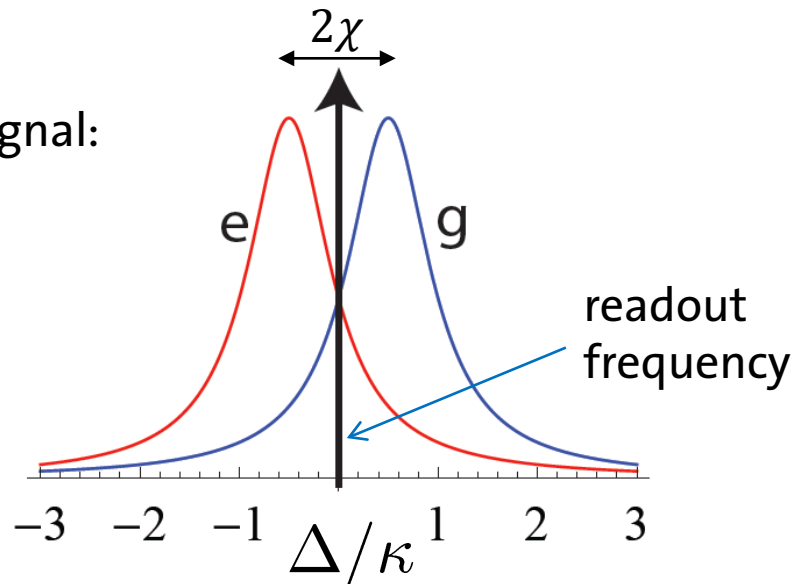
$$A e^{i\phi} = I + iQ$$

↑ ↑ ↑
 signal Phase In-phase and
 amplitude components

In the limit of large detuning $\omega_r - \omega_{ge} \gg g$:

$$H/\hbar \approx (\omega_r + \chi\sigma_z)a^\dagger a, \text{ with } \chi \approx -\alpha \frac{g^2}{\Delta(\Delta - \alpha)}$$

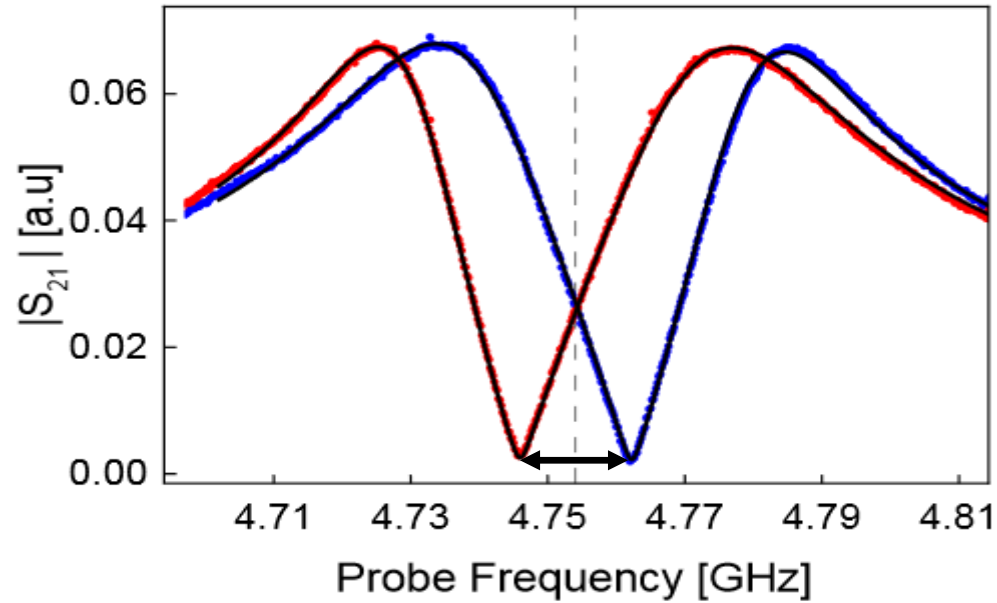
Amplitude of
transmitted signal:



A. Wallraff *et al.*, *Phys. Rev. Lett.* 95, 060501 (2005).
 R. Vijay *et al.*, *Phys. Rev. Lett.* 106, 110502 (2011).

1.5 Readout Resonator Response

Transmission amplitude or readout resonator extracted through Purcell filter for qubit prepared in **ground (g)** or **excited (e)** state :



In **ground/excited** state:

Data measured after state prep. (*,*)

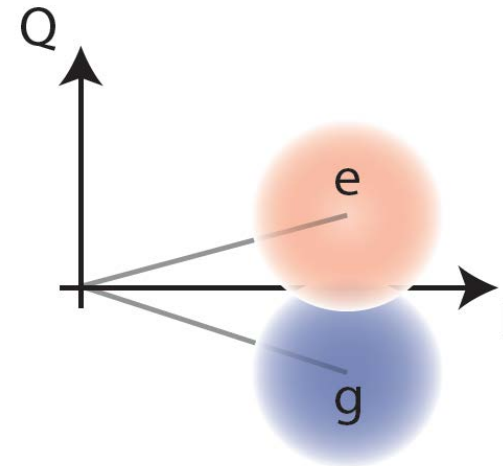
Fit to resonator response model (-)

Parameter fit (input-output model):

Readout resonator $\kappa_r/2\pi = 37.5$ MHz

State dependent resonator shift

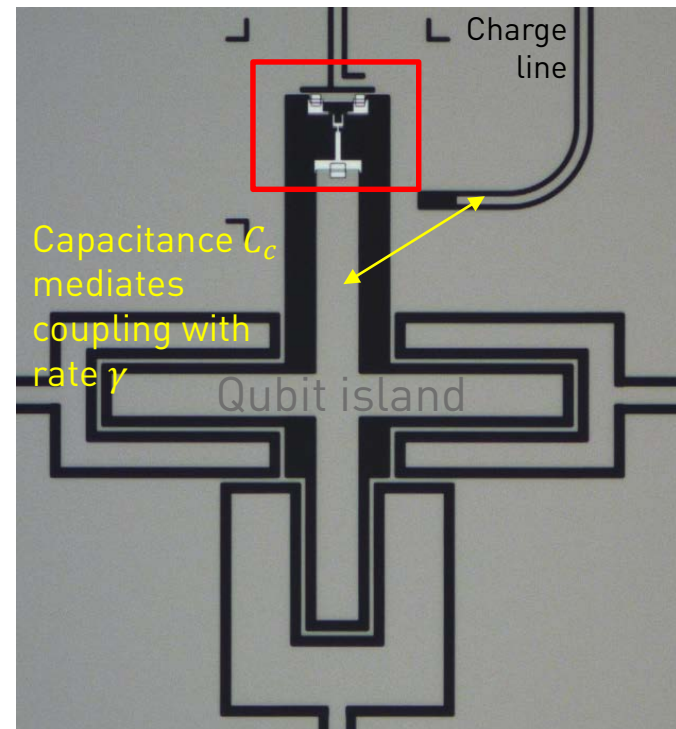
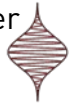
$2\chi/2\pi \simeq -16$ MHz



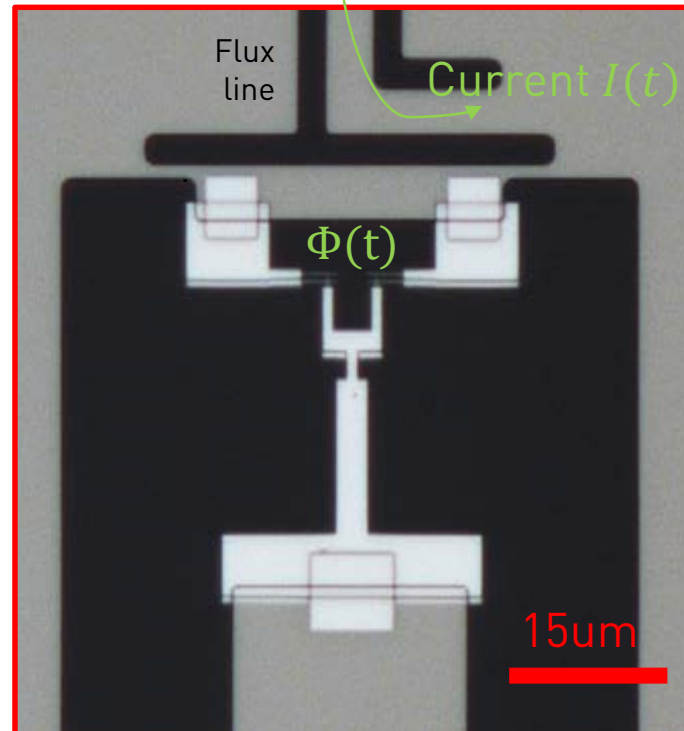
2.1 Control and Characterization of superconducting qubits

XY control

Drive $b_{in}(t)$ at carrier frequency ω_{ge}



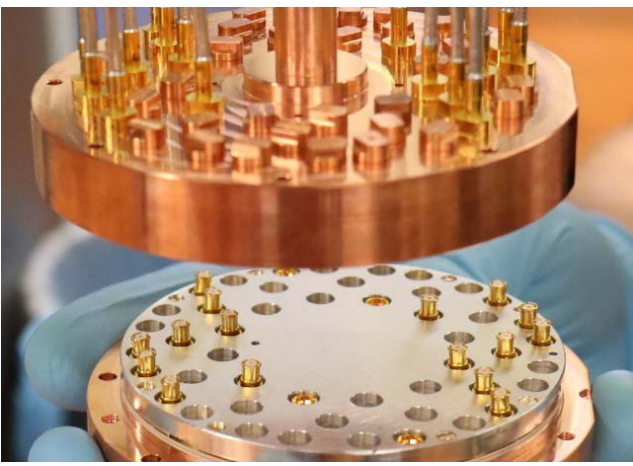
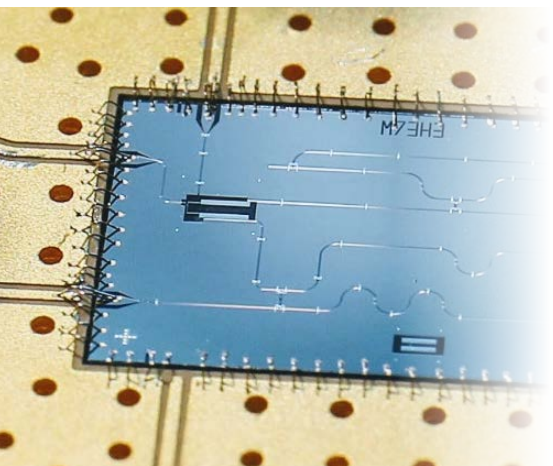
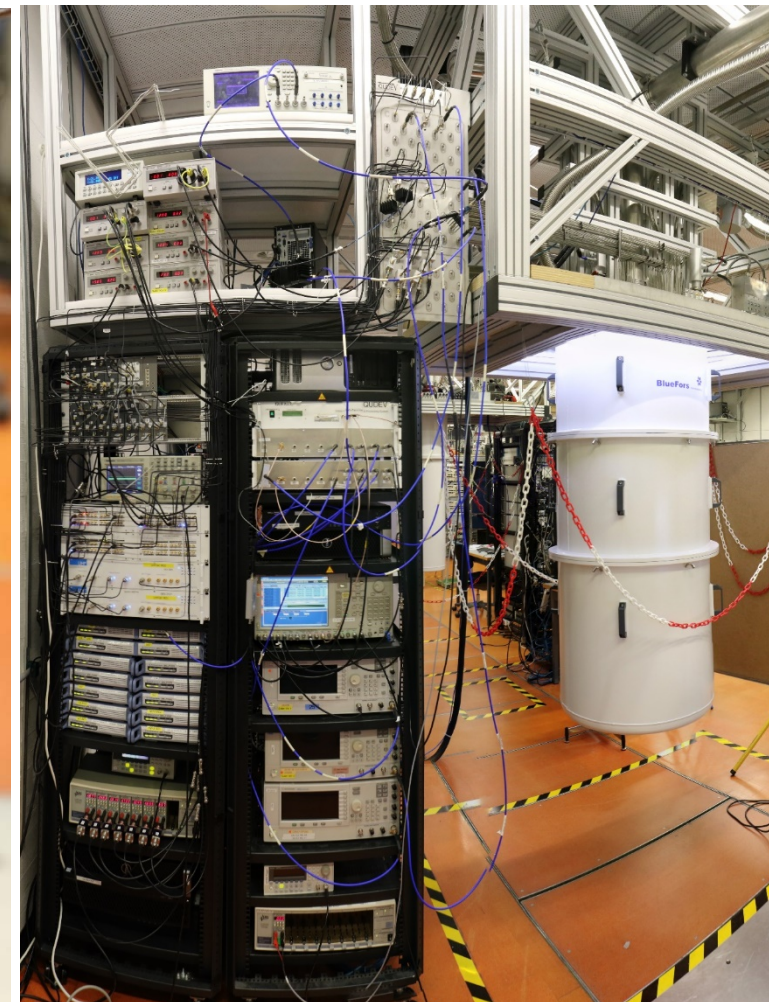
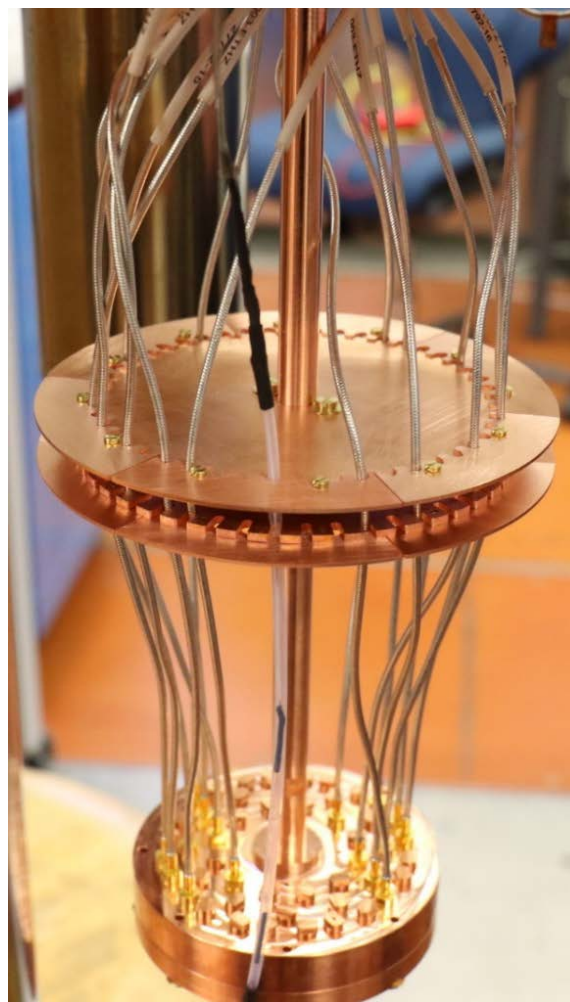
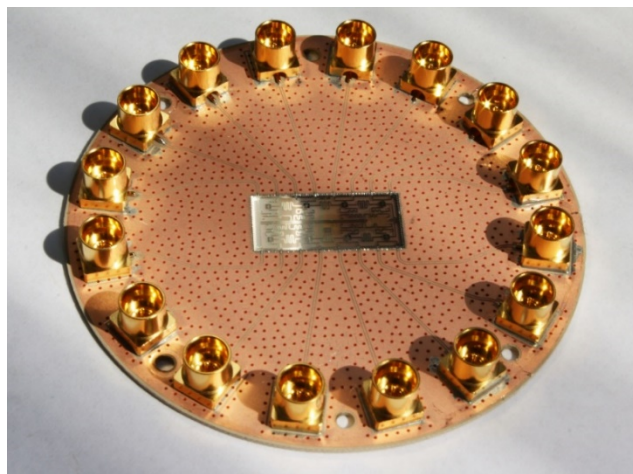
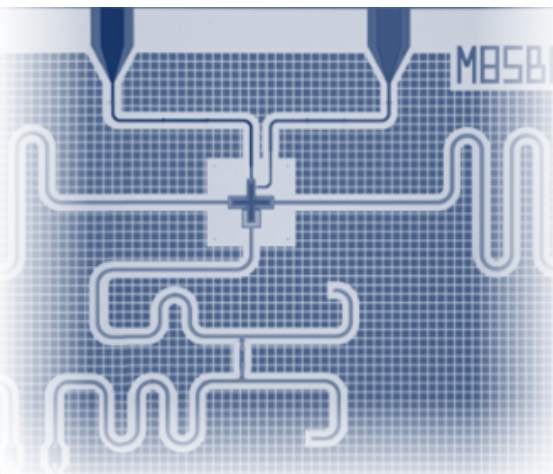
Frequency (Z) control



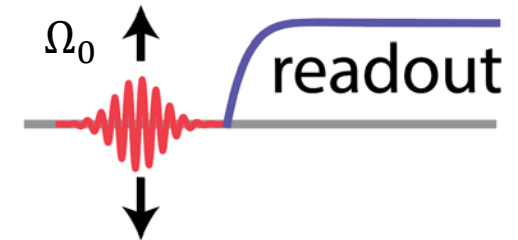
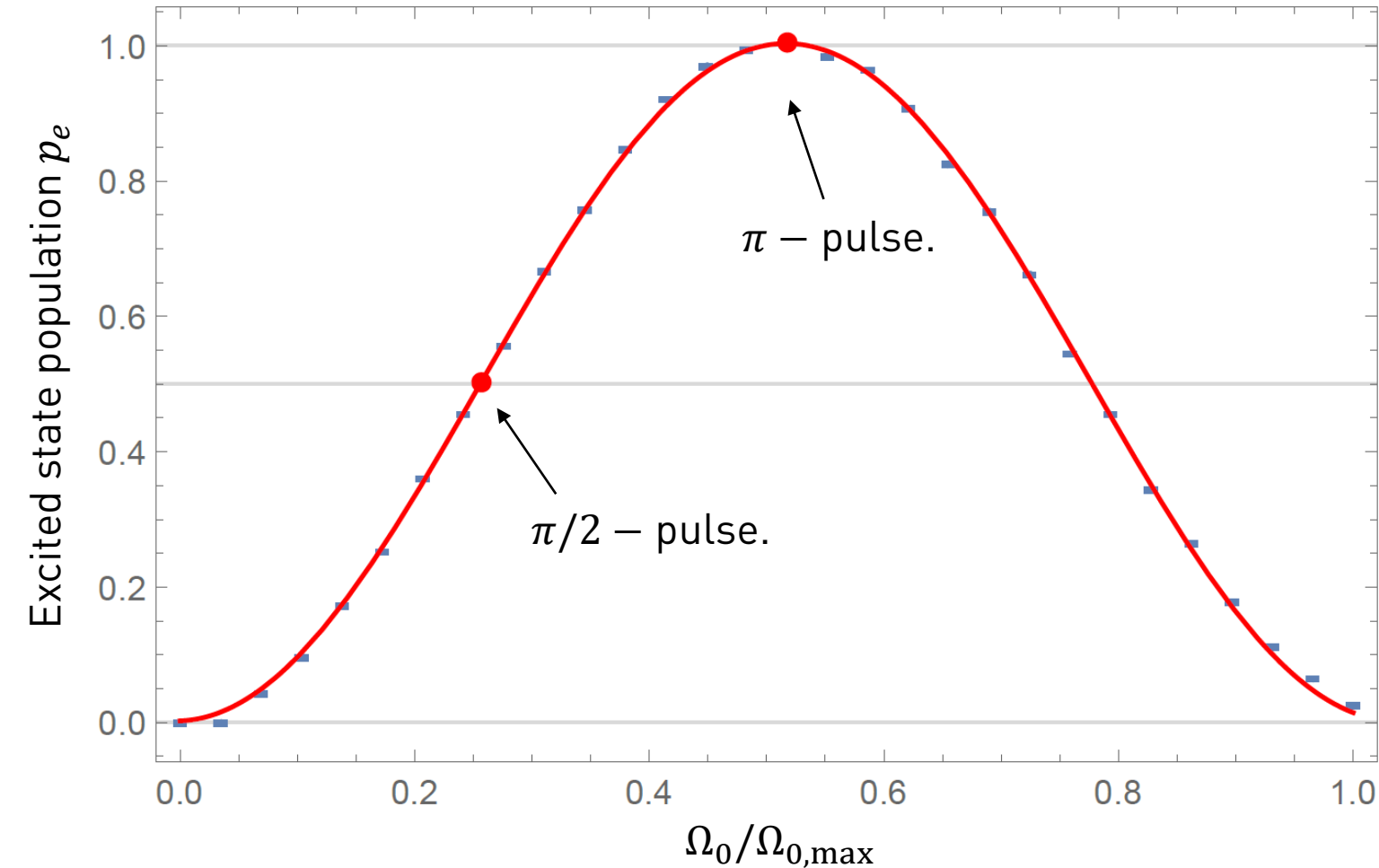
On-chip control

- Microwave drive $b_{in}(t)$ resonant with qubit frequency rotates Bloch vector about X and Y axis. Drive power $P_{in} = \hbar\omega b_{in}^+ b_{in}$.
- Arbitrary waveform generators (AWG) used to generate pulses, up-converted to the MW frequency band by mixing with a local oscillator field.
- Coupling rate to charge line $\gamma = \frac{C_c^2 Z_0 \omega^2}{C_\Sigma}$ imposes decay and therefore needs to be $\gamma \ll 1/T_1$.
- Tunability of the qubit achieved by sending a current $I(t)$ to a separate control line generating a magnetic flux $\Phi(t)$ in the SQUID loop.
- Used for both static (DC) control of the qubit frequency and for applying pulses on nanosecond timescales.

2.1 Control and Characterization of superconducting qubits

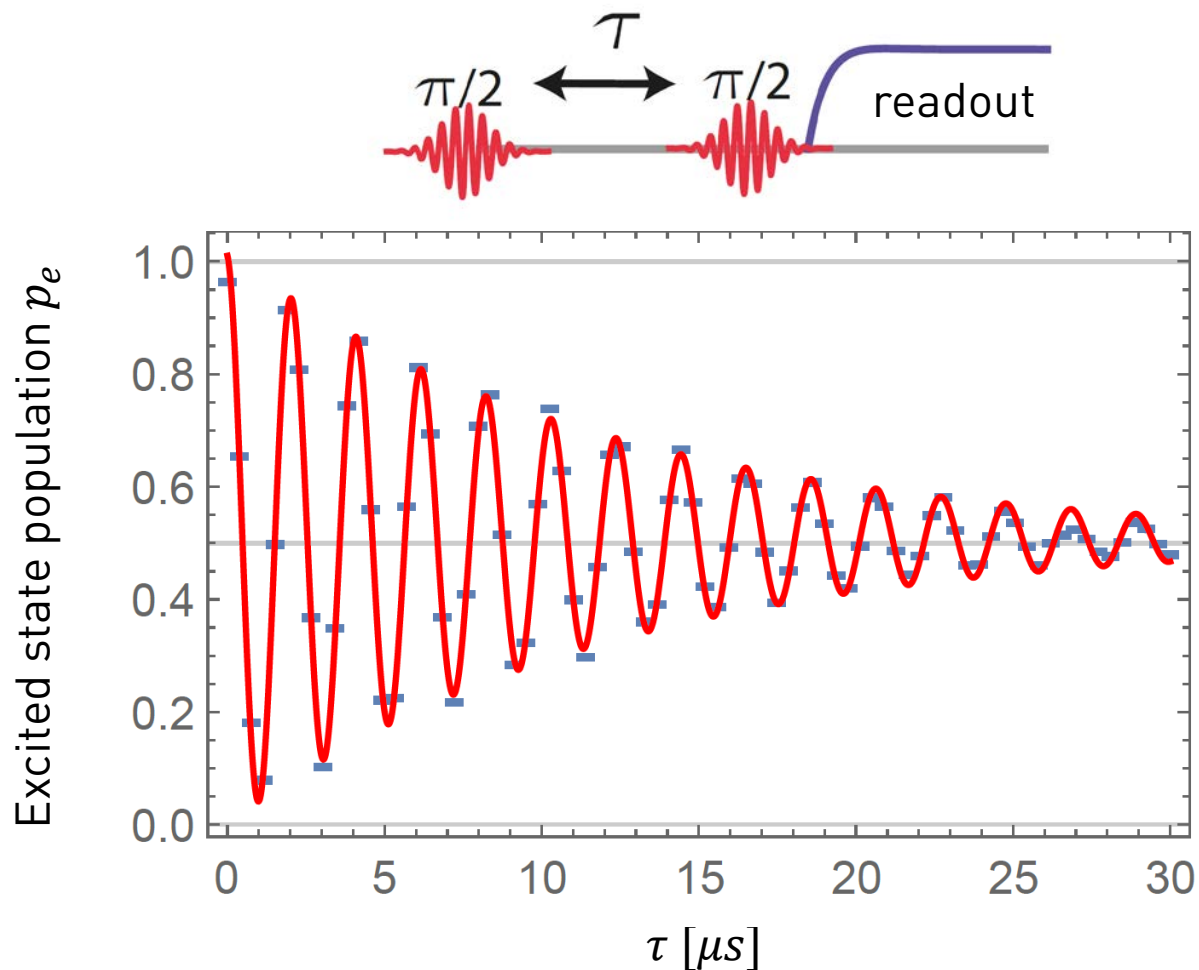


2.2 Measurement of Rabi oscillations



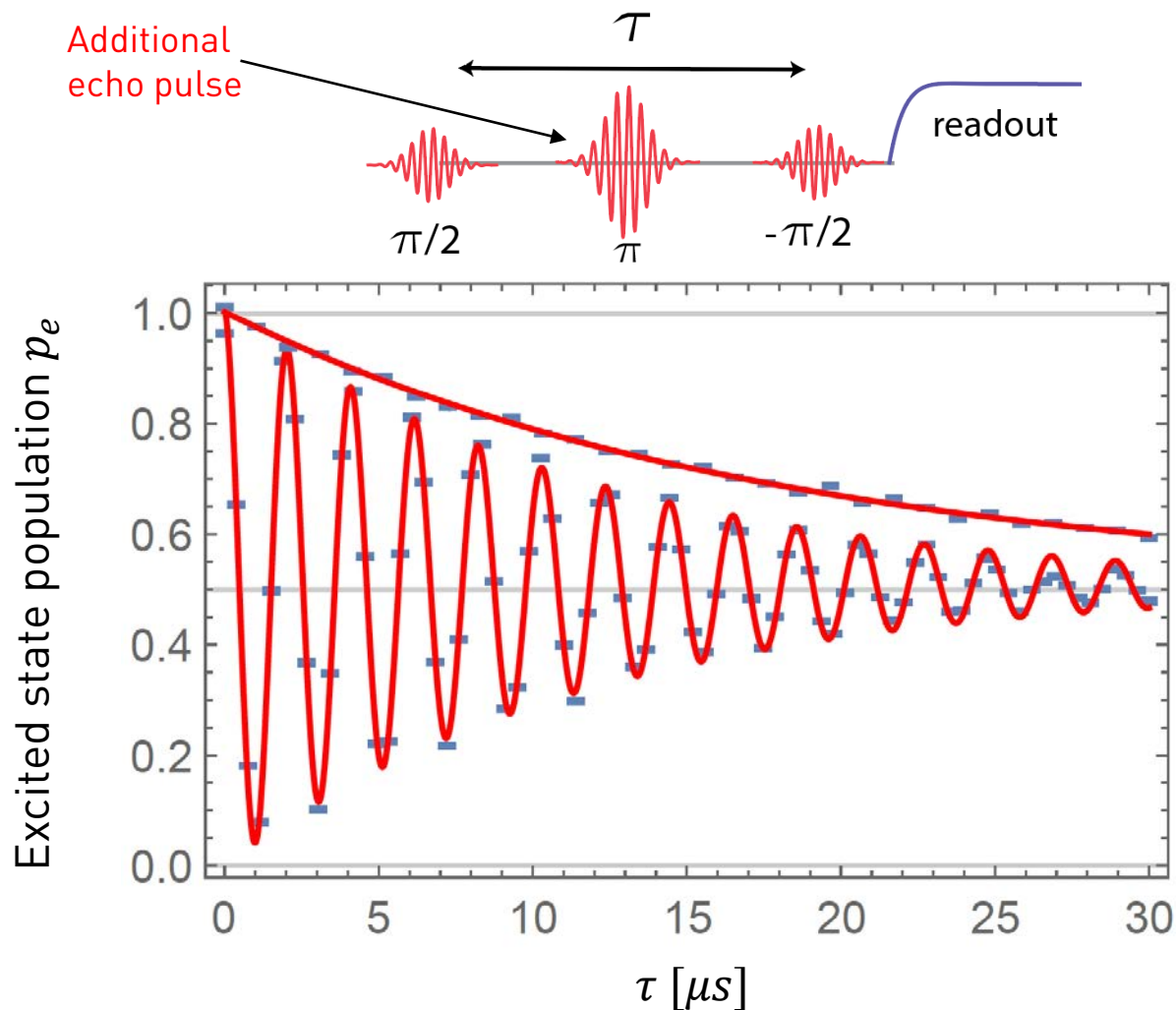
- Qubit frequency $\omega_{ge}/2\pi = 5.758$ GHz determined spectroscopically.
- Initialize qubit in ground state.
- Apply pulse at ω_{ge} with variable amplitude Ω_0 .
- Gaussian pulse envelop with characteristic $\sigma \sim 5 - 10$ ns.
- Readout qubit state and average over $\sim 10^3$ repetitions.
- Sinusoidal fit to extract π - and $\pi/2$ -pulse amplitude.

2.3 Measurement of dephasing time



- Initial $\frac{\pi}{2}$ -pulse prepares $|g\rangle + |e\rangle$.
- Map remaining coherence after time τ to excited state using a second $\frac{\pi}{2}$ -pulse, and measure.
- Detune pulse by $f_{\text{IF}} = 0.5$ MHz from qubit frequency to obtain oscillating pattern. → Higher accuracy in estimating the qubit frequency.
- Fit Characteristic decay time $T_2^* = 13 \mu\text{s}$
- In this case, decay reasonably well described by exponential function $e^{-\tau/T_2^*}$
- Depending on spectral properties of the dominant noise source, decay better described by different functional form, e.g. Gaussian decay for $1/f$ – noise.
- If relaxation is only source of decoherence: $T_2 = 2 T_1$ (“T1 limit of dephasing time”).

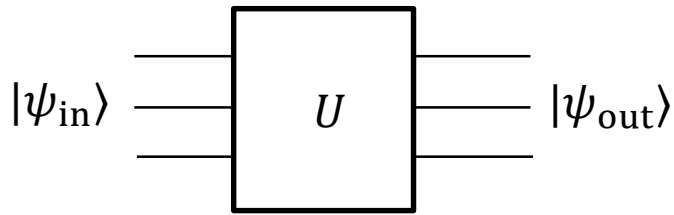
2.3 Measurement of dephasing time



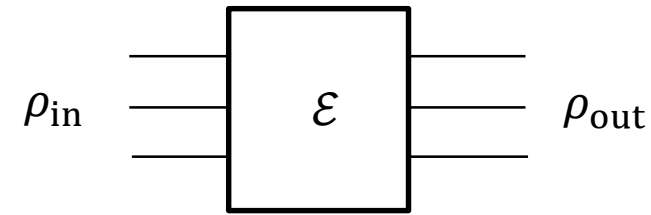
- Low frequency noise can be partly compensated for by applying an echo π -pulse after $\tau/2$ to reverse the direction of the Larmor precession.
- The resulting decay time $T_2^{echo} = 18 \mu s$ is longer than T_2^* .
- Explanation: Low frequency noise which causes the qubit frequency to change on timescales longer than τ_{max} will cancel out.
- Variants of such dynamical decoupling sequences can be used to do noise spectroscopy → See e.g. *Bylander et al., Nat. Phys. (2011)*

3.1 Characterization & Benchmarking of Quantum Processes

Ideally



Realistically

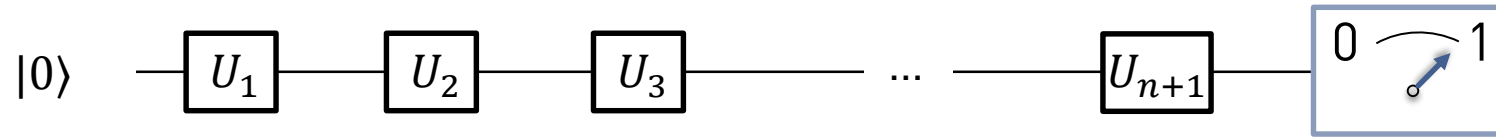


Questions:

- General properties of the map \mathcal{E} ?
- How to measure the map \mathcal{E} ?
 - State and process tomography
- Measure of distance between quantum states and processes: Fidelity
- How to benchmark quantum gates with fidelities close to one?
 - Randomized Benchmarking

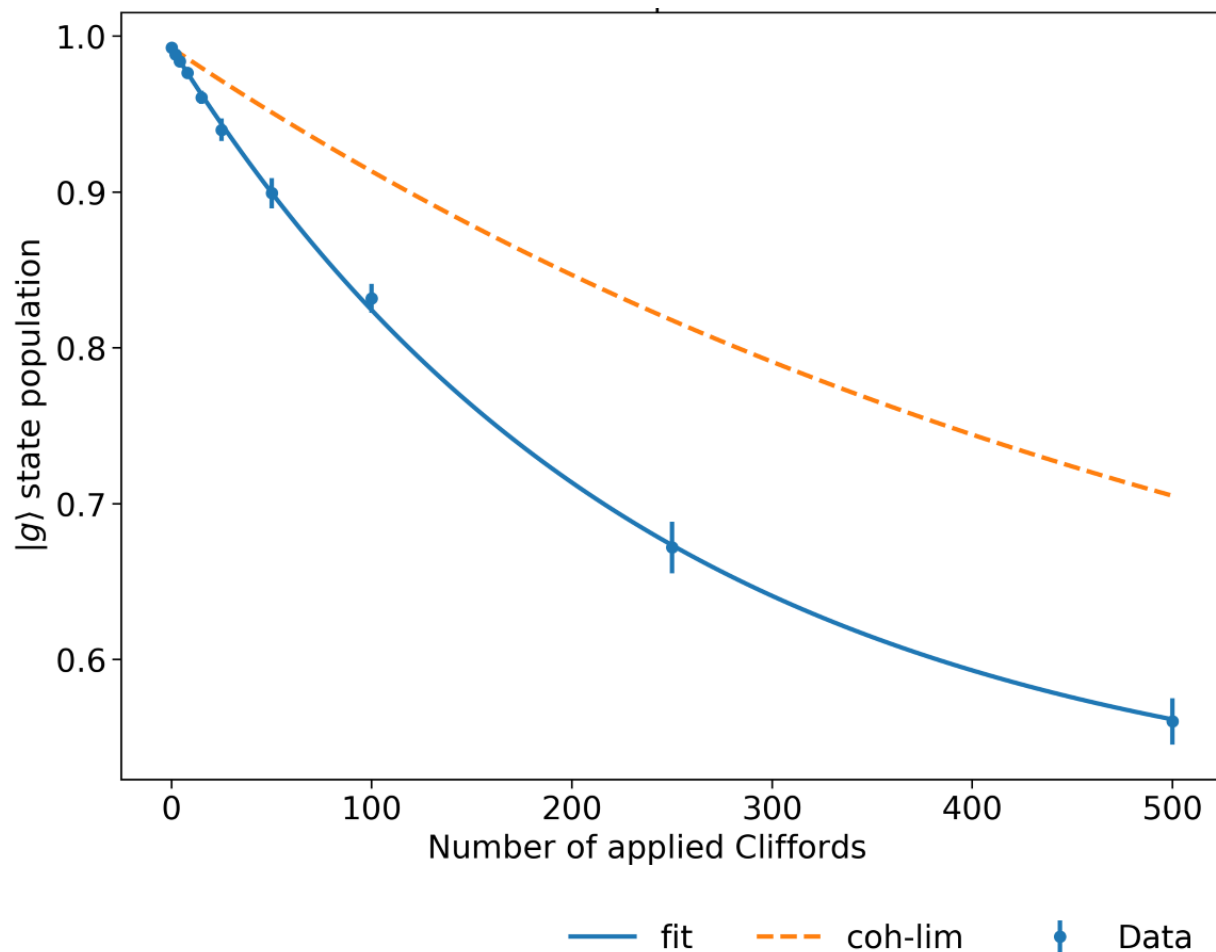
3.2 Randomized benchmarking

- For simplicity, consider single-qubit case.
- Apply sequence of n gate operations U_i before measuring.



- Gates U_i are chosen randomly from the Clifford group, mapping an element of the Pauli group to an element of the Pauli group. For a single qubit there are 24 Clifford gates.
- Last gate U_{n+1} is chosen such that in the absence of errors state is brought back to initial state, i.e. $U_{n+1} \dots U_2 U_1 = I$.
- Average over m different such sequences.
- Success probability p_0 to recover the initial state decays exponentially with # of gates $p_0 \propto \alpha^n$, with depolarization parameter α .
- The error per gate is given by $\epsilon_{RB} = (1 - \alpha) \frac{(d-1)}{d}$ where d is the dimension of Hilbert space ($d=2$ for a single qubit).

3.3 Randomized benchmarking: Example single qubit gates



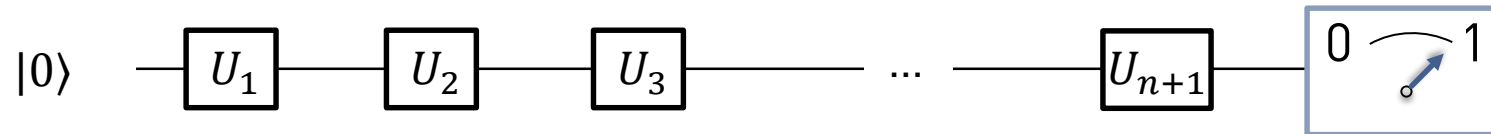
- Pulse duration typically between 15 to 50 ns. Leakage into second excited state avoided by using (DRAG*) pulse parametrization.
- Use Clifford decomposition in terms of X rotations and virtual Z gates (see McKay et al., PRA (2017)).
- Population of ground state decays exponentially.
- Fitted depolarization parameter $\alpha \approx 99.6\%$ and gate error $\epsilon \approx 0.2\%$ in this example.
- Orange dashed line indicates the limit expected when only considering qubit decoherence.
- Deviation from coherence limit hints at finite control errors, e.g. resulting in leakage to the f-level.

*Motzoi et al., PRL 103, 110501 (2009)

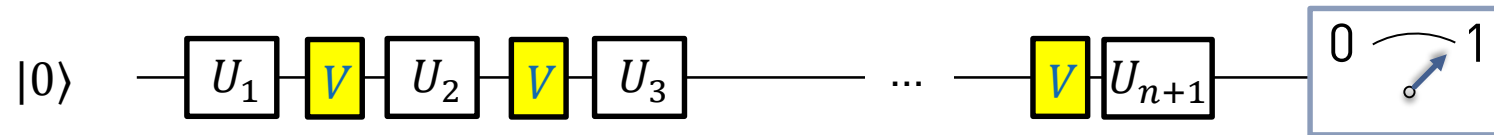
3.4 Interleaved Randomized benchmarking (IRB)

Question how to characterize the fidelity of one particular Clifford gate V ?

- Compare decay of standard RB sequence ...



- ...with result of a 2nd experiment, in which gate V gets interleaved with random Clifford gates.



- Difference between the depolarization parameters α_{RB} and α_{IRB} results in an estimate for the error $\epsilon_V = \frac{d}{d+1} (1 - \frac{\alpha_{IRB}}{\alpha_{RB}})$ per gate V .
- Randomized Benchmarking can be generalized to multi-qubit gates.