

# Design and Implementation of Flight Dynamics Control Strategies for a Quadrotor Based On a Smartphone

Thesis for obtaining the degree of

MASTER OF SCIENCE IN ENGINEERING  
with emphasis in automation

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# Abstract

The field of autonomous systems control is young, but operational experience is rapidly growing, making research on collaborative systems of great importance. Improving aerial robots in particular could be key in facing future environmental challenges.....

In this work, two main problems are addressed: the cooperative source seeking problem and the cooperative level curve tracking problem by a group of agents under undirected constrained communications. ....



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# Chapter 1

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#### 1.1.2 Smartphone as a Controller

#### 1.1.3 Smartphone-based Quadrotors

### 1.2 Outline



# Chapter 2

## Quadrotor Helicopter Model

### 2.1 Nonlinear Model

### 2.2 Linearized Model

The linearised model of the quad-rotor helicopter written as a state space model is given by

$$\begin{aligned}\dot{x}(t) &= Ax(t) + Bu(t), \\ r(t) &= Cx(t),\end{aligned}$$

where

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -g & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & g & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & \frac{1}{m} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix}^T$$

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}^T$$

with the parameters

$$m = 0.64 \text{ kg},$$

$$g = 9.81 \text{ m/s}.$$

The state vector is defined as

$$x(t) = [r_x \quad \dot{r}_x \quad r_y \quad \dot{r}_y \quad r \quad \dot{r}_z]^T,$$

and the control inputs as

$$u(t) = [u_1 \quad u_2 \quad u_3 \quad u_4]^T,$$

and the output vector is defined as

$$r(t) = [r_x \quad r_y \quad r_z]^T.$$

# Chapter 3

## Smartphone-based Quadrotor Prototype

### 3.1 Description of the Components

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## Chapter 4

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### 4.3 State Estimation Through Kalman Filter





# Chapter 5

## Implementation and Results

### 5.1 Kalman Filter for States Estimation

### 5.2 Linear Quadratic Regulator Results

#### 5.2.1 Simple Translational Movements (LQR)

#### 5.2.2 Trajectory Tracking (LQR)

### 5.3 $H_\infty$ Regulator Results

#### 5.3.1 Simple Translational Movements ( $H_\infty$ )

#### 5.3.2 Trajectory Tracking ( $H_\infty$ )



# Conclusions and Outlook

In this thesis distributed algorithms



# Bibliography



# Publications

Rosero Esteban, and Werner Herbert. Modified distributed consensus filter for sensor networks. *2014 European Control Conference (ECC)*. June, 2014.