

HOMEWORK 9: LEARNING PARADIGMS

10-301/10-601 Introduction to Machine Learning (Fall 2022)

<http://www.cs.cmu.edu/~mgormley/courses/10601/>

OUT: 2022-12-02

DUE: 2022-12-09

TAs: Alex, Lavanya, Markov, Neural, Qiuyi, Tara, Yuchen

This is the final homework assignment. This assignment covers **Graphical Models**, **Ensemble Methods**, **k-Means**, **PCA**, and **Recommender Systems**.

START HERE: Instructions

- **Collaboration Policy:** Please read the collaboration policy here: <https://www.cs.cmu.edu/~mgormley/courses/10601/syllabus.html>
- **Late Submission Policy:** See the late submission policy here: <https://www.cs.cmu.edu/~mgormley/courses/10601/syllabus.html>
- **Submitting your work:** You will use Gradescope to submit your answers to all questions.
 - **Written:** For written problems such as short answer, multiple choice, derivations, proofs, or plots, please use the provided template. We strongly encourage you to typeset your submission using L^AT_EX. Submissions can also be handwritten onto the template, but should be labeled and clearly legible. If your writing is not legible, you will not be awarded marks. If your submission is misaligned with the template, there will be a **5% penalty** (e.g., if the homework is out of 100 points, 5 points will be deducted from your final score). Each derivation/proof should be completed in the boxes provided. Do not move or resize any of the answer boxes. If you do not follow the template, your assignment may not be graded correctly by our AI assisted grader.

Instructions for Specific Problem Types

For “Select One” questions, please fill in the appropriate bubble completely:

Select One: Who taught this course?

- Matt Gormley
- Marie Curie
- Noam Chomsky

If you need to change your answer, you may cross out the previous answer and bubble in the new answer:

Select One: Who taught this course?

- Henry Chai
- Marie Curie
- Noam Chomsky

For “Select all that apply” questions, please fill in all appropriate squares completely:

Select all that apply: Which are scientists?

- Stephen Hawking
- Albert Einstein
- Isaac Newton
- I don't know

Again, if you need to change your answer, you may cross out the previous answer(s) and bubble in the new answer(s):

Select all that apply: Which are scientists?

- Stephen Hawking
- Albert Einstein
- Isaac Newton
- I don't know

For questions where you must fill in a blank, please make sure your final answer is fully included in the given space. You may cross out answers or parts of answers, but the final answer must still be within the given space.

Fill in the blank: What is the course number?

10-601

10-~~6~~301

Written Questions (48 points)

1 L^AT_EX Bonus Point (1 points)

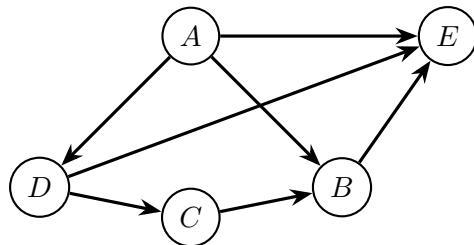
1. (1 point) **Select one:** Did you use L^AT_EX for the entire written portion of this homework?

Yes

No

2 Graphical Models (6 points)

Consider the joint distribution over the binary random variables A, B, C, D, E represented by the Bayesian Network shown in the figure.



1. (1 point) Write the joint probability distribution for $P(A, B, C, D, E)$ factorized as much as possible according to the standard definition of a Bayesian Network using the conditional independence assumptions expressed by the above network.

Your Answer

$$P(A, B, C, D, E) = P(E|A, B, D)P(D|A)P(C|D)P(B|A, C)P(A)$$

2. (1 point) Which nodes are in the Markov boundary of B ? Note that the Markov boundary is the smallest possible Markov blanket.

Your Answer

A, C, D, E

3. (1 point) Which nodes are in the Markov boundary of C ? Note that the Markov boundary is the smallest possible Markov blanket.

Your Answer

A, B, D

4. (1 point) **True or False:** E is conditionally independent of C given $\{A, B, D\}$. That is, $E \perp C | \{A, B, D\}$.

True

False

5. (1 point) How many parameters would we need to represent the joint distribution $P(A, B, C, D, E)$ **without** the conditional independence assumptions expressed by the Bayesian Network?

Your Answer

80

6. (1 point) How many parameters would we need to represent the joint distribution $P(A, B, C, D, E)$ **with** the conditional independence assumptions expressed by the Bayesian Network?

Your Answer

17

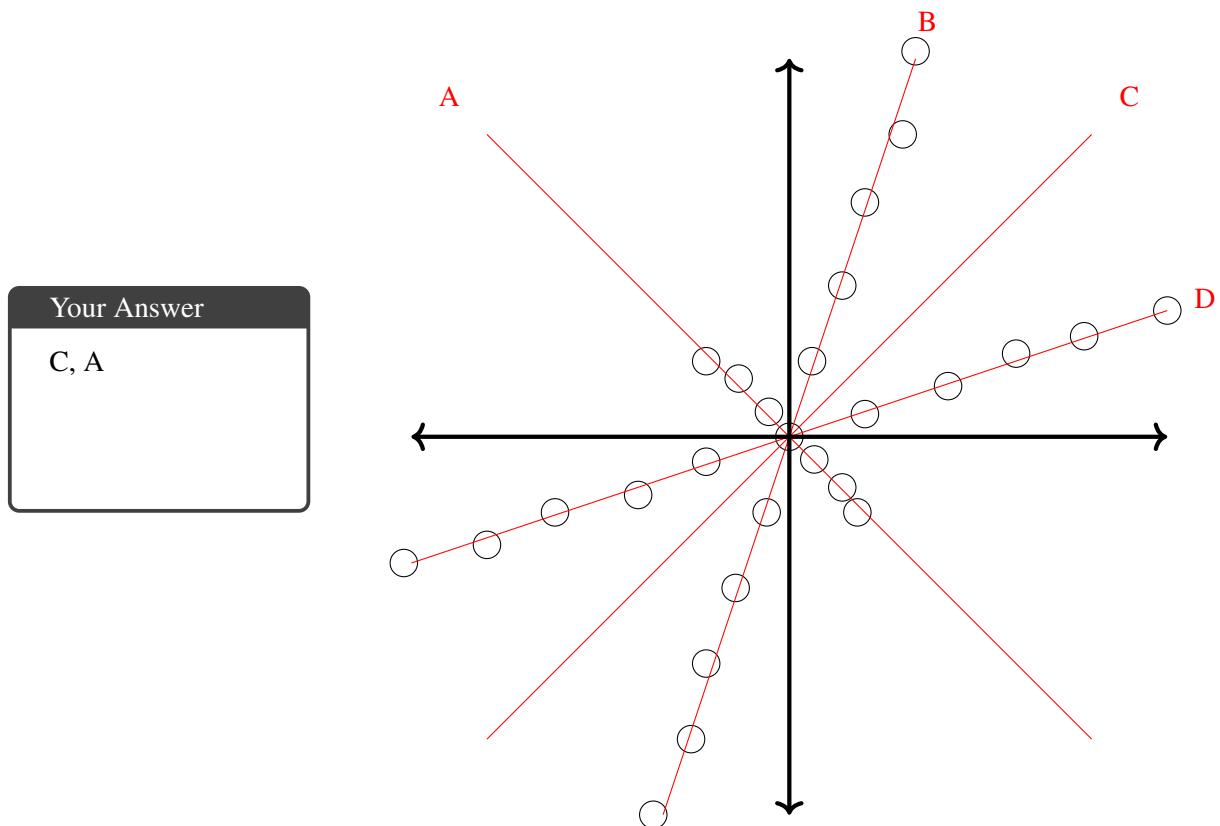
3 PCA (8 points)

Some PCA Theory

1. (1 point) **Select one:** Assume we apply PCA to a matrix $\mathbf{X} \in \mathbb{R}^{n \times 2}$ and obtain two sets of PCA feature scores, $\mathbf{z}_1, \mathbf{z}_2 \in \mathbb{R}^n$, where \mathbf{z}_1 corresponds to the first principal component and \mathbf{z}_2 corresponds to the second principal component. Which is more common in the training data:

- a point with small feature values in \mathbf{z}_2 and large feature values in \mathbf{z}_1
- a point with large feature values in \mathbf{z}_2 and small feature values in \mathbf{z}_1
- a point with large feature values in \mathbf{z}_2 and large feature values in \mathbf{z}_1
- a point with small feature values in \mathbf{z}_2 and small feature values in \mathbf{z}_1

2. (2 points) For the data set shown below, list the principal components from first to last.



PCA in Practice

For this section, refer to the PCA demo linked [here](#). In this demonstration, we have performed PCA for you on a [simple four-feature dataset](#). The questions below have also been added to the colab notebook linked for ease of access. Run the code in the notebook, then answer the questions based on the results.

3. (1 point) **Select one:** Do you see any special relationships between any of the features? In particular, take a look at the `petal_length` feature. How would you describe its association with each of the **other features**? Select the correct statement with appropriate justification.

- The features are highly correlated: we observe linearly proportional relationships where increases in `petal_length` often correspond to increases in another feature
- The features are highly correlated: we observe that the color classes can be separated with decision boundaries along the `petal_length` axis.
- The features are uncorrelated: we observe random noise as if the features were generated from independent distributions
- The features are uncorrelated: we observe the “default $y = x$ ” relationship between features

4. (2 points) **Select all that apply:** To get the principal components of the features, we calculate the eigenvectors of the covariance matrix, which are orthogonal, along with their corresponding eigenvalues. Which of the following are consequences of the principal components being orthogonal to each other?

- The variance of the data is maximized.
- The reconstruction error is minimized.
- The dot product of any two principal components will be 1.0.
- We can attribute certain variations in the data to unique principal components.
- In the dimensionality-reduced space, the covariance of the first and second dimensions will always be zero.
- It ensures that our lower-dimensional data will be linearly separable.
- None of the above.

5. (1 point) If we wanted to find k principal components such that we preserve **at least** 95% of the variance in the data, what would be the value of k ? Hint: it is helpful here to look at the cumulative variance in the first k components, which we have calculated for you.

k
2

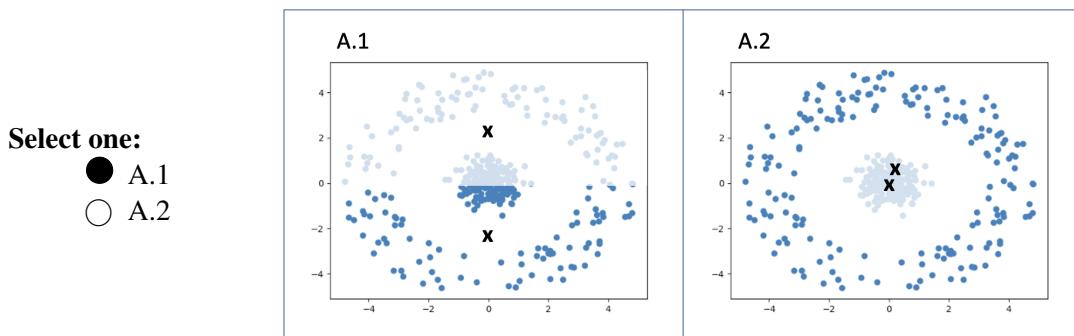
6. (1 point) **Select all that apply:** If we wanted to perform dimensionality reduction to have just two features and train a classifier on them, we could represent our data by EITHER (a) picking any two features from the dataset, OR (b) using the first 2 principal components we obtained from PCA. Which one should we prefer and why?

- We prefer (a), because it ensures randomness in the selection and have a better chance of representing the data well.
- We prefer (a), because PCA introduces artificial bias and does not reflect the original features.
- We prefer (b), because PCA preserves higher variance of the data than two raw features.
- We prefer (b), because PCA ensures that variance is evenly distributed across the features.
- We prefer neither, because it is impossible to train such a classifier.
- Either is fine, because there are only two features in this dataset.
- None of the above.

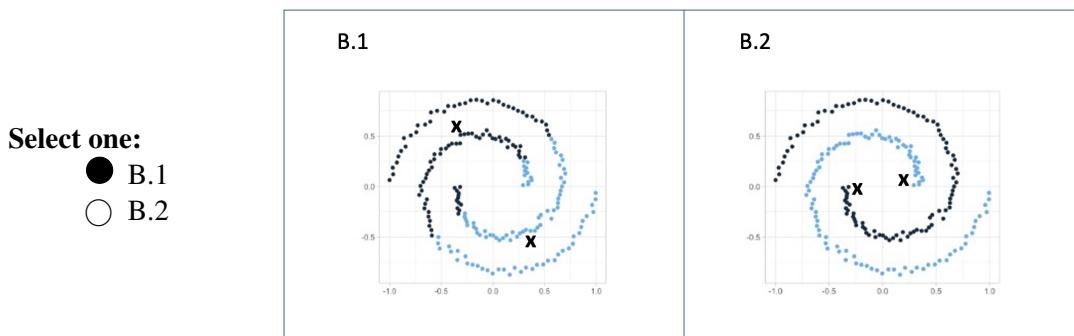
4 k -Means (12 points)

1. Consider the 3 datasets A, B and C. Each dataset is classified into k clusters, with centers marked X and cluster membership represented by different colors in the figure. For each dataset, exactly one clustering was generated by k -means with Euclidean distance. Select the image with clusters generated by k -means.

(a) (1 point) Dataset A



(b) (1 point) Dataset B



2. Consider a dataset \mathcal{D} with 5 points as shown below. Perform a k -means clustering on this dataset with $k = 2$ using the Euclidean distance as the distance function. Remember that in the k -means algorithm, one iteration consists of following two steps: first, we assign each data point to its nearest cluster center; second, we recompute each center as the average of the data points assigned to it. Initially, the 2 cluster centers are chosen randomly as $\mu_0 = (5.3, 3.5)$, $\mu_1 = (5.1, 4.2)$. Parts (a) through (d) refer only to the first iteration of k -means clustering performed on \mathcal{D} .

$$\mathcal{D} = \begin{bmatrix} 5.5 & 3.1 \\ 5.1 & 4.8 \\ 6.6 & 3.0 \\ 5.5 & 4.6 \\ 6.8 & 3.8 \end{bmatrix}$$

(a) (1 point) **Select one:** Which of the following points will be the new center for cluster 0?

- (5.7 , 4.1)
- (5.6 , 4.8)
- (6.3 , 3.3)
- (6.7 , 3.4)

(b) (1 point) **Select one:** Which of the following points will be the new center for cluster 1?

- (6.1 , 3.8)
- (5.5 , 4.6)
- (5.4 , 4.7)
- (5.3 , 4.7)

(c) (1 point) How many points will belong to cluster 0, using the new centers?

Answer
3

(d) (1 point) How many points will belong to cluster 1, using the new centers?

Answer
2

3. Recall that in k -means clustering we attempt to find k cluster centers $\mathbf{c}_1, \dots, \mathbf{c}_k$ such that the total distance between each point and the nearest cluster center is minimized. We thus solve

$$\operatorname{argmin}_{\mathbf{c}_1, \dots, \mathbf{c}_k} \sum_{i=1}^N \min_{j \in \{1, \dots, k\}} \|\mathbf{x}^{(i)} - \mathbf{c}_j\|_2^2$$

where n is the number of data points. Instead of holding the number of clusters k fixed, your friend John tries to also minimize the objective over k , solving

$$\operatorname{argmin}_k \operatorname{argmin}_{\mathbf{c}_1, \dots, \mathbf{c}_k} \sum_{i=1}^N \min_{j \in \{1, \dots, k\}} \|\mathbf{x}^{(i)} - \mathbf{c}_j\|_2^2$$

You found this idea to be a bad one.

- (a) (1 point) What is the minimum possible value of the objective function when minimizing over k ?

Answer
0

- (b) (1 point) What is a value of k for which we achieve the minimum possible value of the objective function when $N = 100$?

Answer
100

4. Consider the following brute-force algorithm for minimizing the k -means objective: Iterate through each possible assignment of the points to k clusters, $\mathbf{z} = [z^{(1)}, \dots, z^{(N)}]$. For each assignment $\mathbf{z} \in \{1, \dots, k\}^N$, you evaluate the following objective function:

$$J(\mathbf{z}) = \underset{\mathbf{c}_1, \dots, \mathbf{c}_k}{\operatorname{argmin}} \sum_{i=1}^N \|\mathbf{x}^{(i)} - \mathbf{c}_{z^{(i)}}\|_2^2$$

At the end, you pick the assignment \mathbf{z} that had lowest $J(\mathbf{z})$.

- (a) (1 point) Suppose we have N points and k clusters. For how many possible assignments \mathbf{z} does the brute force algorithm have to evaluate $J(\mathbf{z})$?

Answer
k^N

- (b) (1 point) Suppose $N = 1000$, $k = 10$, and it takes us 0.01 seconds to evaluate $J(\mathbf{z})$ for a single assignment \mathbf{z} . How many seconds will the brute force algorithm take to check all assignments?

Answer
10^{998}

5. Initializing the centers has a big impact on the performance of the k -means clustering algorithm. Usually, we randomly initialize k cluster centers. However, there are other methods, namely, furthest point initialization and k -means++ initialization.

(a) (1 point) **Select all that apply:** Clustering at convergence generated by furthest point initialization is sensitive to outliers. Which of the following statements is correct about this phenomenon?

- Although outliers will not be selected in the first several iterations, they will temporarily be chosen as centers during training and slow convergence.
- Outliers will be cluster centers in the final result.
- Outliers will slow convergence, but they will not be centers at convergence time.
- Outliers are selected as centers in the first few iterations.
- This phenomenon does not exist.
- None of the above.

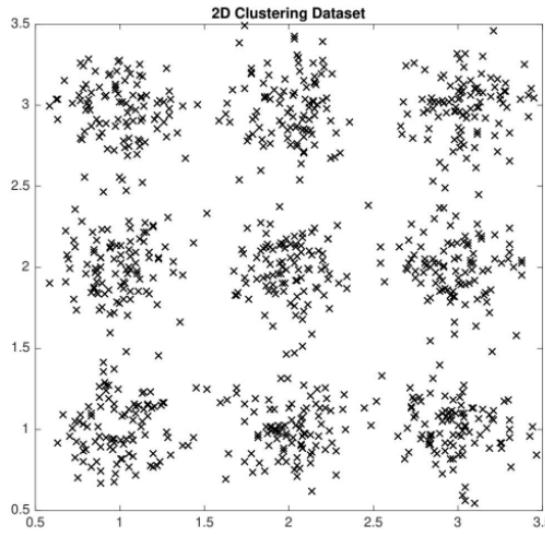


Figure 1: 2D Dataset

(b) (1 point) **Select one:** Using the dataset in Figure 1 above, compared to random initialization, using k -means++ initialization is _____.

- more likely to choose one sample from each cluster because centers are chosen with probability proportional to squared distance from existing centers.
- less likely to choose one sample from each cluster because the formula does not account for the number of clusters which may be found and thus won't be calibrated to correctly choose one point from each cluster.
- equally likely to choose one sample from each cluster because as the number of points grows large, k -means++ asymptotically approaches random initialization.

5 Ensemble Methods (11 points)

1. In the following question, we will explore two different kinds of ensemble methods: the halving algorithm and the doubling algorithm.

Consider the **halving algorithm**:

We first maintain a list of n weak classifiers h_1, \dots, h_n . The training labels and classifier predictions are in $\{-1, 1\}$. For each training sample (x, y) , we make prediction based on the majority vote of weak classifiers $\hat{y} = \text{sign}(\sum_{i=1}^n h_i(x))$. If the majority vote prediction does not equal to the label, we will eliminate all the h_i such that $h_i(x) \neq y$. The final aggregated classifier will be the ensemble of all the remaining classifiers.

- (1 point) Assume there are a total of n classifiers initially, and at least one classifier left in the end. What would be the big-O bound of the total number of mistakes made in terms of n ?

Your Answer
$O(\log(n))$

- (1 point) **Fill in the blank:** We can set the multiplicative penalty $\beta = \underline{\hspace{2cm}}$ in the weighted majority algorithm to have the weighted majority algorithm be equivalent to the halving algorithm.

Your Answer
0

- (1 point) **Select all that apply:** What weak classifiers are guaranteed to be kept by the halving algorithm?

- Weak classifiers with zero training error.
- Weak classifiers that only get one training example wrong.
- Weak classifiers that always predict the same as the majority vote.
- Weak classifiers that always predict the opposite of the majority vote.
- None of the above.

Now we consider another algorithm, the **doubling algorithm**, which doubles the count of correct classifiers (by making identical copies of the correct classifiers each iteration) when the majority vote is incorrect.

(d) (1 point) **Select all that apply:** How could we modify the weighted majority algorithm to behave equivalently to the doubling algorithm for every input x and true label y ?

- Set the factor $\beta = 2$, and perform weight update of all classifiers h_i for which $h_i(x) \neq y$ when the majority vote is incorrect.
- Set the factor $\beta = \frac{1}{2}$, and perform weight update of all classifiers h_i for which $h_i(x) \neq y$ when the majority vote is correct.
- Set the factor $\beta = \frac{1}{2}$, and perform weight update of all classifiers h_i for which $h_i(x) \neq y$ when the majority vote is incorrect.
- Set the factor $\beta = 2$, and perform weight update of all classifiers h_i for which $h_i(x) = y$ when the majority vote is correct.
- Set the factor $\beta = 2$, and perform weight update of all classifiers h_i for which $h_i(x) = y$ when the majority vote is incorrect.
- None of the above.

2. (1 point) **Select all that apply:** Which of the following are true?

- In the weighted majority algorithm, the weights associated with the weak learners are learned during training.
- In the AdaBoost algorithm, the weights associated with the weak learners are learned during training.
- In the weighted majority algorithm, the weak learners are learned during training.
- In the AdaBoost algorithm, the weak learners are learned during training.
- None of the above.

3. (1 point) **True or False:** Consider some training point $(x^{(i)}, y^{(i)})$ to the AdaBoost algorithm. If for all t , the weak learner h_t learned during training at time t correctly classifies $h_t(x^{(i)}) = y^{(i)}$, there will eventually be a finite time t such that the weight assigned to $x^{(i)}$ in the training distribution \mathcal{D}_t reaches exactly 0.

- True
- False

4. (1 point) **True or False:** If AdaBoost reaches perfect training accuracy, all weak learners created in subsequent iterations will be identical (i.e., they will produce the same output on any input). Assume we are using deterministically selected weak learners.

- True
- False

5. In the following question, we will examine the generalization error of AdaBoost using a concept known as the *classification margin*.

Throughout the question, use the following definitions:

- N : The number of training samples.
- $S = \{(x^{(1)}, y^{(1)}), \dots, (x^{(N)}, y^{(N)})\}$: The training samples with binary labels ($y^{(i)} \in \{-1, +1\}$).
- $\mathcal{D}_t(i)$: The weight assigned to training example i at time t . Note that $\sum_i \mathcal{D}_t(i) = 1$.
- h_t : The weak learner constructed at time t .
- ϵ_t : The error of h_t on \mathcal{D}_t .
- Z_t : The normalization factor for the distribution update at time t .
- α_t : The weight assigned to the learner h_t in the composite hypothesis.
- $f_t(x) = (\sum_{t'=1}^t \alpha_{t'} h_{t'}(x)) / (\sum_{t'=1}^t \alpha_{t'})$: The aggregated vote of the weak learners, rescaled based on the total weight.

For a binary classification task, assume that we use a probabilistic classifier that provides a probability distribution over the possible labels (i.e. $p(y|x)$ for $y \in \{+1, -1\}$). The classifier output is the label with highest probability. We define the *classification margin* for an input as the signed difference between the probability assigned to the correct label and the incorrect label $p_{\text{correct}} - p_{\text{incorrect}}$, which takes on values in the range $[-1, 1]$. Recall from recitation that $\text{margin}_t(x^{(i)}, y^{(i)}) = y^{(i)} f_t(x^{(i)})$.

Note: Consistency points will not be awarded for this question.

- (a) (1 point) Recall the update AdaBoost performs on the distribution of weights:

- $\mathcal{D}_1(i) = 1/N$
- $\mathcal{D}_{t+1}(i) = \mathcal{D}_t(i) \frac{\exp(-y^{(i)} \alpha_t h_t(x^{(i)}))}{Z_t} = \frac{1}{N} \left(\prod_{t'=1}^t \frac{1}{Z_{t'}} \right) \exp(-\sum_{t'=1}^t y^{(i)} \alpha_{t'} h_{t'}(x^{(i)}))$

We define $C_{t+1} = \frac{1}{N} \left(\prod_{t'=1}^t \frac{1}{Z_{t'}} \right)$ and $M_{t+1}(i) = -\sum_{t'=1}^t y^{(i)} \alpha_{t'} h_{t'}(x^{(i)})$. We then have

$$\mathcal{D}_{t+1}(i) = C_{t+1} \exp(M_{t+1}(i))$$

Let $\alpha = \sum_{t'=1}^t \alpha_{t'}$. Rewrite $M_{t+1}(i)$ in terms of $\text{margin}_t(x^{(i)}, y^{(i)})$ and α . (Hint: first rewrite $M_{t+1}(i)$ in terms of $y^{(i)}$, α , f_t , $x^{(i)}$, then apply our given formula for the margin).

Your Answer

$$-\text{margin}_t(x^{(i)}, y^{(i)}) * \alpha$$

- (b) (1 point) **Select one:** Note that C_{t+1}, α are treated as positive constants with respect to the input points. Using the classification margin and the above formulation of the weights assigned by AdaBoost, fill in the blanks to describe which points AdaBoost assigns high weight to at time t .

At time t , AdaBoost assigns higher weight to points $x^{(i)}$ with _____ value of margin on the current ensemble classifier (i.e., $\text{margin}_t(x^{(i)}, y^{(i)})$).

- higher absolute
- higher signed
- lower absolute
- lower signed

- (c) (1 point) **Select one:** This weighting behavior causes the margins of the points you chose in part (b) to _____.

- increase
- decrease
- stay the same

- (d) (1 point) **Select all that apply:** How does this change in the margins explain the empirical result of test error continuing to decrease after training error has converged?

- AdaBoost can continue to increase the confidence of its predictions, particularly on lower confidence training examples, which makes it less likely at test time to misclassify points similar to those it has seen in the training set.
- Adaboost continues to increase confidence of its predictions on high confidence training examples only, leading to a highly accurate classifier which, at test time, will outperform the training error.
- Adaboost lowers the confidence in high confidence areas by continuing to train on low confidence training examples. This averages out the confidence between high and low confidence training examples, overall creating a more generalizable classifier.
- The test error does not continue to decrease after the training error has converged as the model stops updating once we reach convergence.
- None of the above.

6 Recommender Systems (10 points)

1. (2 points) **Select all that apply:** In which of the following situations will a collaborative filtering system be a more appropriate learning algorithm than a linear or logistic regression model?
 - You manage an online bookstore, and you have book ratings and sales data from many users. For each user, you want to recommend other books she will enjoy, based on her own ratings and the ratings of other users.
 - You manage an online bookstore, and you have book ratings and sales data from many users. You want to learn to predict the expected sales volume (number of books sold) as a function of the average rating of a book.
 - You run an online news aggregator, and for every user, you know some subset of articles that the user likes and some different subset that the user dislikes. You want to use this to find other articles that the user likes.
 - You've written a piece of software that downloads news articles from many news websites. In your system, you also keep track of which articles you personally like and which ones you dislike, and the system also stores away features of these articles (e.g., word counts, name of author). Using this information, you want to build a system to try to find additional new articles that you personally will like.
 - None of the above
2. (2 points) **Select all that apply:** What is the basic intuition behind matrix factorization?
 - That content filtering and collaborative filtering are just two different factorizations of the same rating matrix.
 - That factoring user and item matrices can partition the users and items into clusters that can be treated identically, reducing the complexity of making recommendations.
 - The user-user and item-item correlations are more efficiently computed by factoring matrices, even when including the cost of factoring matrices.
 - That users and items can be well described in a shared low dimensional space that can be computed from the rating matrices.
 - None of the above
3. Neural the Narwhal decides to set up a friend-recommendation system for all the students in 10-301/601, of which there are $N = 10,301,601$. Ideally, Neural would store the full $N \times N$ matrix M , where M_{ij} is 1 if student i and j are friends and 0 if student i and j are nemeses, or null if students i and j have never met. Assume that these are the only possible relationships between 2 people and that all relationships are symmetric (so it cannot be the case that student i thinks student j is their friend while j thinks i is their nemesis). Unfortunately, storing M in its entirety would take over 10 TB of storage, which Neural cannot afford on a TA salary. Neural instead uses the following procedure to approximate M as UU^T for some low rank $N \times d$ matrix U , where each row of U corresponds to a student.
 - (a) (2 points) One of the lines in the above algorithm is incorrect. State the line number, and provide the correct line.

```

1: Given learning rate  $\eta$ , ground truth relationships  $M$ 
2: Randomly initialize user embedding matrix  $U \in \mathbb{R}^{N \times d}$ 
3: while not converged do
4:   Sample  $i \sim \text{Uniform}(1, N)$ ,  $j \sim \text{Uniform}(1, N)$ 
5:    $\hat{M}_{ij} \leftarrow \sigma(\vec{u}_i^T \vec{u}_j)$  //  $\sigma$  is sigmoid function
6:    $\mathcal{L}(\vec{u}_i, \vec{u}_j) \leftarrow -\hat{M}_{ij} \log(\hat{M}_{ij}) - (1 - \hat{M}_{ij}) \log(1 - \hat{M}_{ij})$  // Compute logistic loss
7:    $\vec{g}_i \leftarrow \nabla_{\vec{u}_i} \mathcal{L}(\vec{u}_i, \vec{u}_j)$  // Compute and perform gradient updates
8:    $\vec{g}_j \leftarrow \nabla_{\vec{u}_j} \mathcal{L}(\vec{u}_i, \vec{u}_j)$ 
9:    $\vec{u}_i \leftarrow \vec{u}_i - \eta \cdot \vec{g}_i$ 
10:   $\vec{u}_j \leftarrow \vec{u}_j - \eta \cdot \vec{g}_j$ 

```

Line #	Fixed line of code
4	Sample $i \sim \text{Uniform}(1, N)$, $j \sim \text{Uniform}(i+1, N)$ where M_{ij} is not null

- (b) (2 points) **Select all that apply:** Based on the loss function given on line 6, derive an expression for $\nabla_{\vec{u}_j} \mathcal{L}(\vec{u}_i, \vec{u}_j)$ in terms of \vec{u}_i , \vec{u}_j , and M_{ij} . Note that σ denotes the sigmoid function and log is natural log.

- $M_{ij}\sigma(\vec{u}_i^T \vec{u}_j)$
- $\vec{u}_i M_{ij}\sigma(\vec{u}_i^T \vec{u}_j)$
- $\vec{u}_i(M_{ij} + \sigma(\vec{u}_i^T \vec{u}_j))$
- $\vec{u}_i(-M_{ij} + \sigma(\vec{u}_i^T \vec{u}_j))$
- None of the above.

Your Work

- (c) (2 points) **Select all that apply:** Why is it appropriate here to factorize M as the product of a

single matrix by itself UU^T rather than as the product of two distinct matrices VW^T ?

- UU^T enforces that our approximation is symmetric, while VW^T is not necessarily symmetric.
- SGD is guaranteed to converge faster and to a better optimum for U because we have fewer parameters to learn.
- We can parallelize training for U , whereas we could not parallelize training for V and W .
- We wish to model relationships between objects of a single type, not between objects of two different types.
- None of the above.

7 Collaboration Questions

After you have completed all other components of this assignment, report your answers to these questions regarding the collaboration policy. Details of the policy can be found [here](#).

1. Did you receive any help whatsoever from anyone in solving this assignment? If so, include full details.
2. Did you give any help whatsoever to anyone in solving this assignment? If so, include full details.
3. Did you find or come across code that implements any part of this assignment? If so, include full details.

Your Answer

1. No
2. No
3. No