



Unraveling Neural Complexity: Exploring the Separation of Oscillations and $1/f$ Noise in Neuroscience

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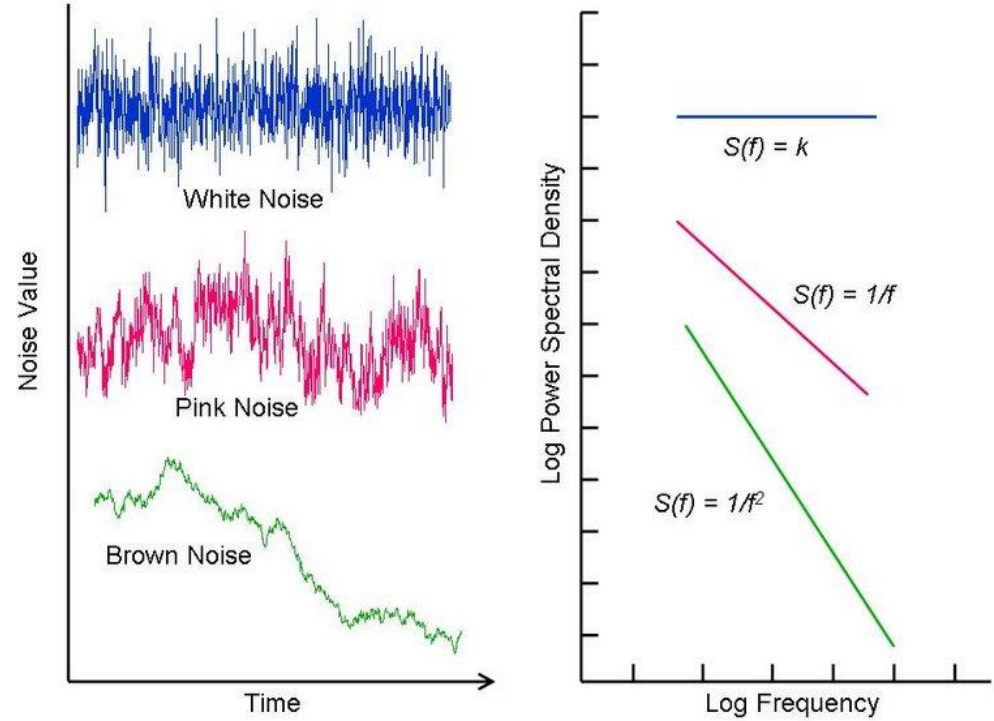
Outline

- Definition & History
- Examples in Neuroscience
- Hypotheses in Neuroscience
- How do we model aperiodic activity
- Tools and frameworks - IRASA vs. FOOOF
- Interactive demonstration with GUI
- Limitations and challenges of current methods
- Example with Sleep EEG data
- Tips & Recommendations



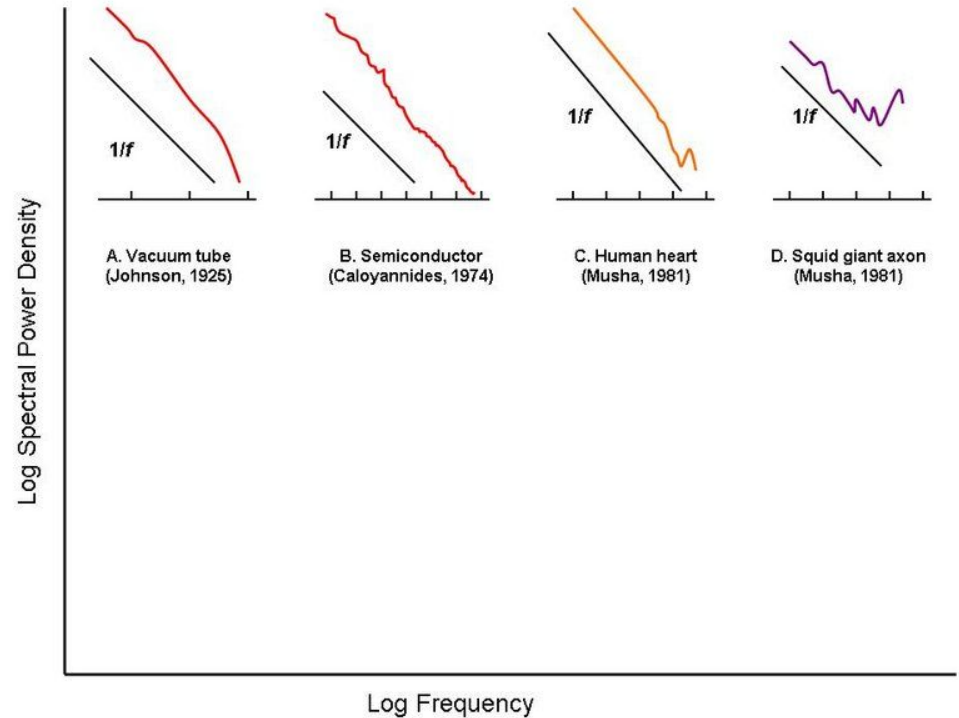
Definition & History

- Power spectral density (PSD) is inversely proportional to frequency, as the frequency increase, the PSD decays linearly in log-log space.



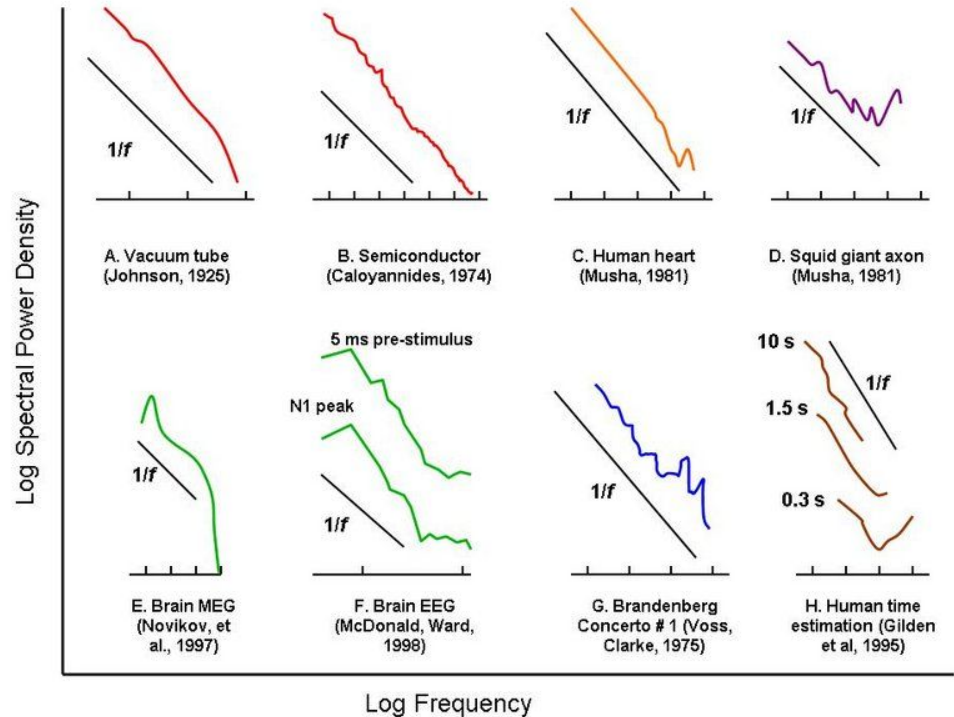
Definition & History

- $1/f$ noise was first observed discovered by Johnson [1] in 1925 in data from an experiment designed to test theory of shot noise in vacuum tubes.



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- Subsequently observed in semiconductors [2], human heart rhythm [3], squid axons [3], M/EEG [4, 5], musical pieces [6], time perception [7], among others.
- Primacy of neural oscillations [8]



Examples in Neuroscience

- Aperiodic exponent (β) for human voltage spectra: Mean = -3.1 (IQR: -4 to -2.5) for freqs >20 Hz [9]

β	Ref	Year	Recording modality	Frequency	Experimental condition
-0.08	[53]	2019	Scalp EEG (n=5)	20-40 Hz	Anesthesia (Ketamine)
-1.12	[19]	2022	Scalp EEG (n=16, control subjects)	1-40 Hz	Eyes closed
-1.3	[59]	2021	Scalp EEG (n=74, Tourette syndrome)	2-40 Hz	Behavioral experiments
-1.44	[59]	2021	Scalp EEG (n=74, control)	2-40 Hz	Behavioral experiments
-1.48	[19]	2022	Scalp EEG (n=18, stroke patients)	1-40 Hz	Stroke patients
-1.51	[18]	2019	Scalp EEG (n=78, control subjects)	4-50 Hz	Resting state
-1.67	[18]	2019	Scalp EEG (n=76, ADHD subjects)	4-50 Hz	Resting state
-1.84	[10]	2020	Scalp EEG (n=9)	30-45 Hz	Wakefulness
-1.86	[60]	2013	Scalp EEG (n=7, adults)	0.2-30 Hz	Sleep
-1.87	[10]	2020	Scalp EEG (n=14)	30-45 Hz	Resting state
-2.03	[53]	2019	Scalp EEG (n=5)	20-40 Hz	Wakefulness
-2.07	[60]	2013	Scalp EEG (n=15, newborns)	0.2-30 Hz	Sleep
-2.32	[61]	2000	Intracranial EEG (n=5)	0.5-150 Hz	Resting state
-2.33	[12]	2021	Scalp EEG (n=175, T5)	2-48 Hz	NREM sleep
-2.44	[31]	2010	Intracranial EEG (n=5)	1-100 Hz	Wakefulness
-2.48	[53]	2019	Scalp EEG (n=5)	20-40 Hz	Wakefulness
-2.71	[11]	2022	Scalp EEG (n=251)	2-48 Hz	NREM sleep
-2.73	[12]	2021	Scalp EEG (n=175, Fz)	2-48 Hz	NREM sleep
-2.75	[10]	2020	Intracranial EEG (n=12)	30-45 Hz	Wakefulness
-2.87	[31]	2010	Intracranial EEG (n=5)	1-100 Hz	Slow wave sleep
-2.99	[10]	2020	Intracranial EEG (n=10)	30-45 Hz	Wakefulness
-3.1	[10]	2020	Scalp EEG (n=9)	30-45 Hz	Anesthesia
-3.13	[53]	2019	Scalp EEG (n=5)	20-40 Hz	Wakefulness
-3.46	[10]	2020	Scalp EEG (n=14)	30-45 Hz	N3 Sleep
-3.59	[53]	2019	Scalp EEG (n=5)	20-40 Hz	Anesthesia (Xenon)
-3.67	[10]	2020	Scalp EEG (n=14)	30-45 Hz	N2 Sleep
-3.69	[10]	2020	Intracranial EEG (n=10)	30-45 Hz	N3 Sleep
-4	[27]	2009	Intracranial EEG (n=20)	80-500 Hz	Behavioral experiments
-4.15	[10]	2020	Intracranial EEG (n=10)	30-45 Hz	REM sleep
-4.34	[10]	2020	Intracranial EEG (n=12)	30-45 Hz	Anesthesia
-4.36	[53]	2019	Scalp EEG (n=5)	20-40 Hz	Anesthesia (Propofol)
-4.73	[10]	2020	Scalp EEG (n=14)	30-45 Hz	REM sleep



Examples in Neuroscience

*Derived from [8]

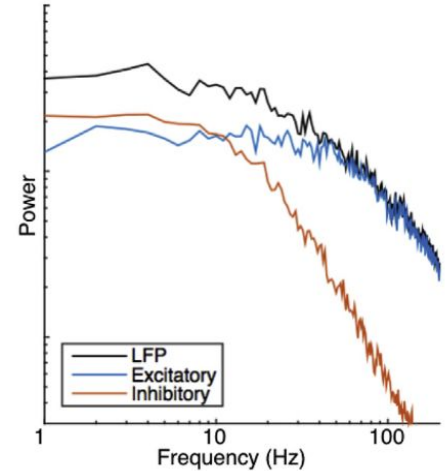
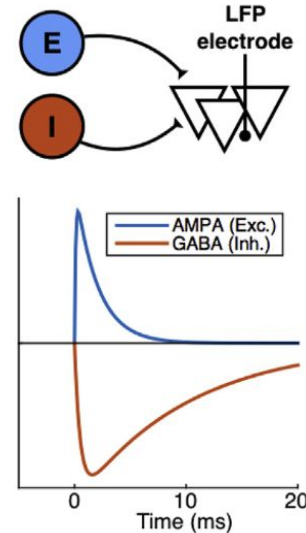
Study (year)	Domain Examined	Key Finding
He (2014), Kello et al. (2010)	Aperiodic component	Introduction and interest in the aperiodic component of $1/f$.
Ouyang et al. (2020), Podvalny et al. (2015), Waschke et al. (2021)	Task	Changes in the $1/f$ exponent with tasks.
Bódizs et al. (2021), Dave et al. (2018), Waschke et al. (2017), Cellier et al. (2021), He et al. (2019), Schaworonkow & Voytek (2021), Voytek et al. (2015)	Age	$1/f$ exponent changes with age.
Muthukumaraswamy & Liley (2018), Stock et al. (2020), Timmermann et al. (2019)	Psychoactive drug administration	$1/f$ changes with drug administration.
Molina et al. (2020), Robertson et al. (2019), Veerakumar et al. (2019), van Heumen et al. (2021), Ostlund et al. (2021), Karalunas et al. (2022)	Disease	$1/f$ exponent correlation with diseases.
Halgren et al. (2021)	Cortical Depth	$1/f$ decreases with cortical depth.
Gao et al. (2017)	Computational modeling	$1/f$ exponent β as estimator of excitation–inhibition balance.
Lendner et al. (2020), Miskovic et al. (2019), Colombo et al. (2019), Muthukumaraswamy & Liley (2018), Waschke et al. (2021), Zhou et al. (2021)	Consciousness States	Differences in $1/f$ exponent in NREM sleep, anesthesia vs. awake states.



Hypotheses in Neuroscience

What could it mean?

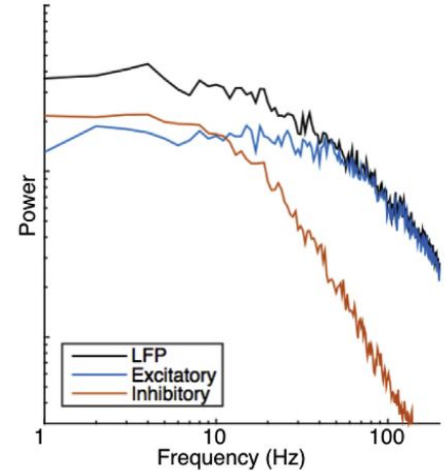
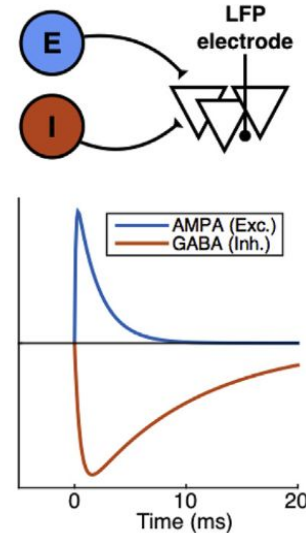
- Neurophysiological interpretation
 - Several computational models indicate that desynchronized non-oscillatory brain activity correlates with population excitation-to-inhibition balance (E-I Ratio) [10-11]



Hypotheses in Neuroscience

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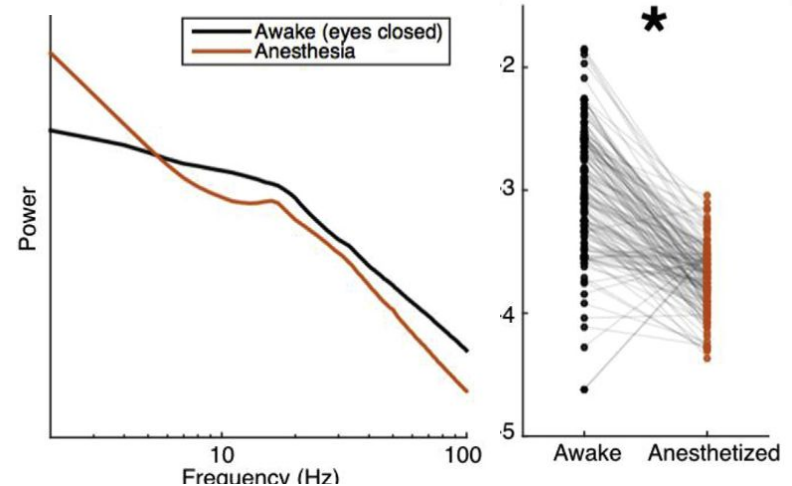
- Neurophysiological interpretation
 - Several computational models indicate that desynchronized non-oscillatory brain activity correlates with population excitation-to-inhibition balance (E-I Ratio) [10-11]
 - *Offset* reflects neuronal population spiking, whereas *exponent* relates to the integration of synaptic currents [14]



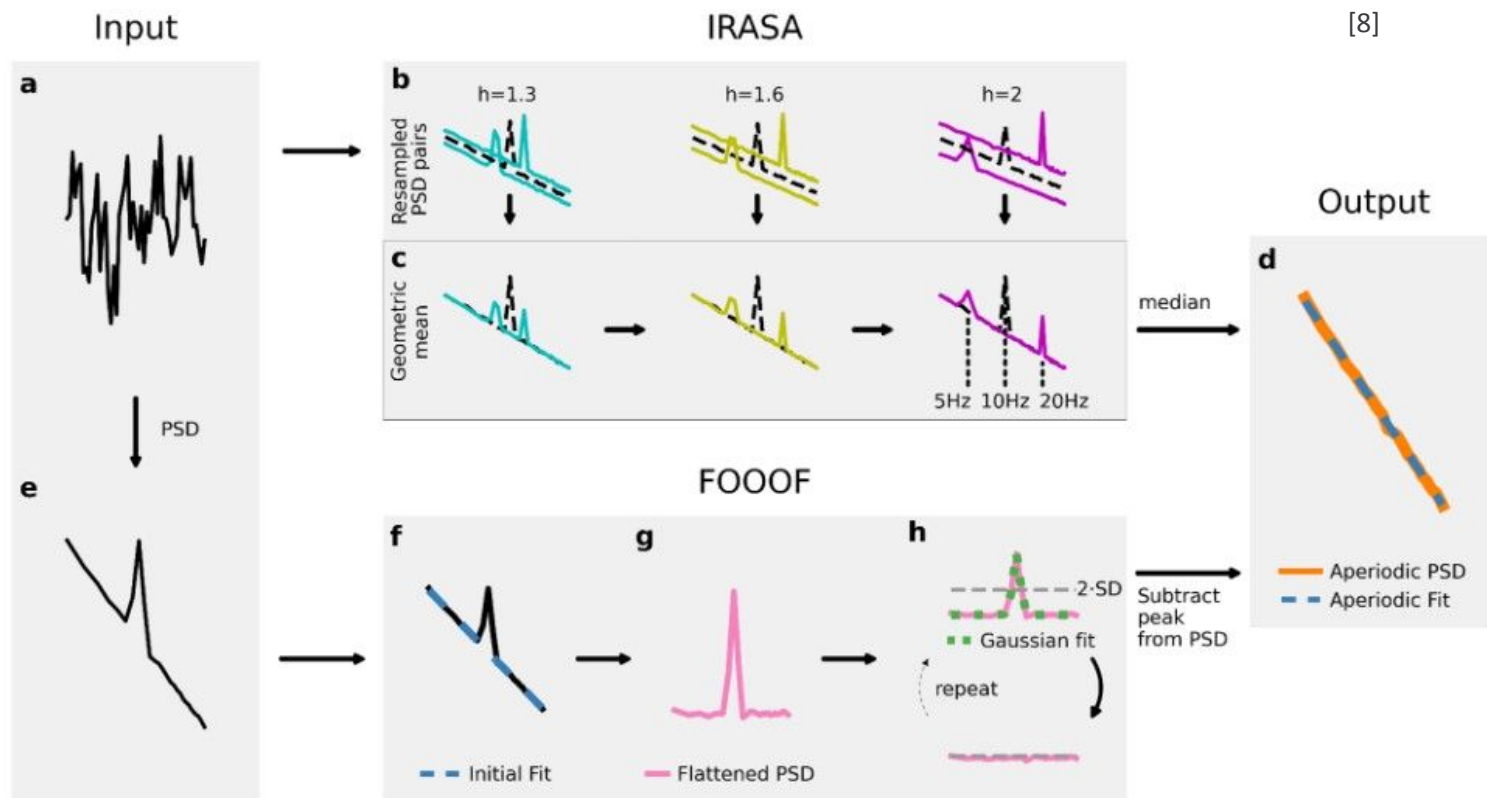
Hypotheses in Neuroscience

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- Neurophysiological interpretation
 - Several computational models indicate that desynchronized non-oscillatory brain activity correlates with population excitation-to-inhibition balance (E-I Ratio) [10-11]
 - Conscious states (increased excitation) vs unconscious states (increased inhibition) [8]
 - (i.e., larger $1/f$ exponents observed for NREM sleep and anesthesia compared to wakefulness)



How to model aperiodic activity

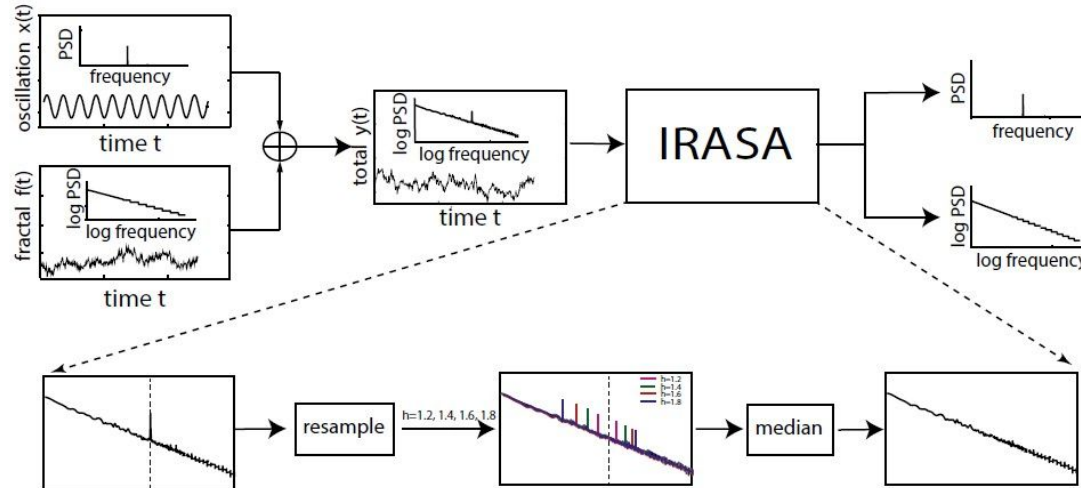


Tools and frameworks - IRASA

Step 1: Compute the original power spectral density (PSD).

[12]

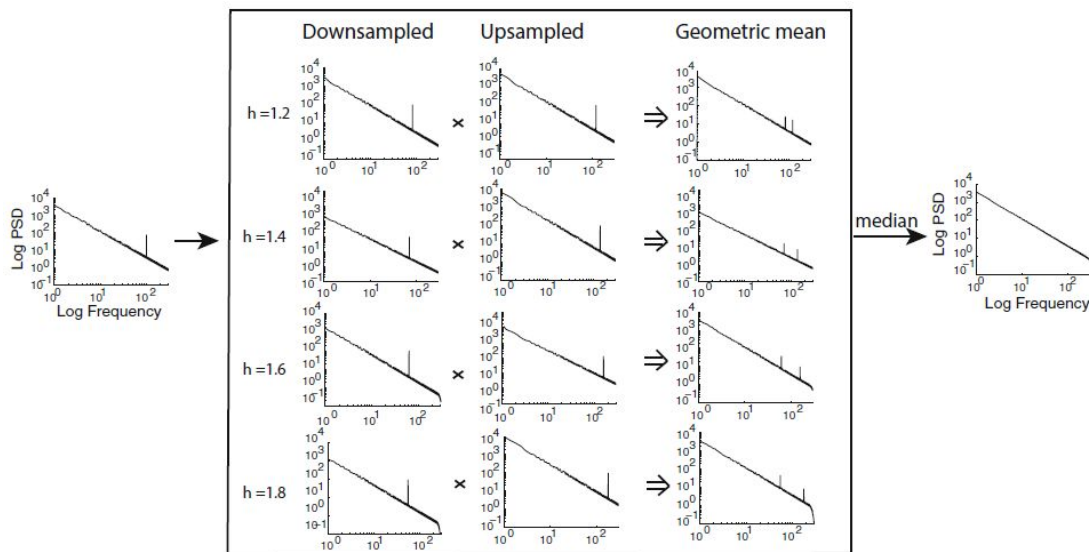
Step 2: Resample the EEG data by multiple non-integer factors and their reciprocals (h and $1/h$)



Tools and frameworks - IRASA

Step 3: For each resampled signal pair, compute the PSD and then determine their geometric mean; this process shifts oscillatory component power by a varying frequency offset while keeping the fractal component's power consistent.

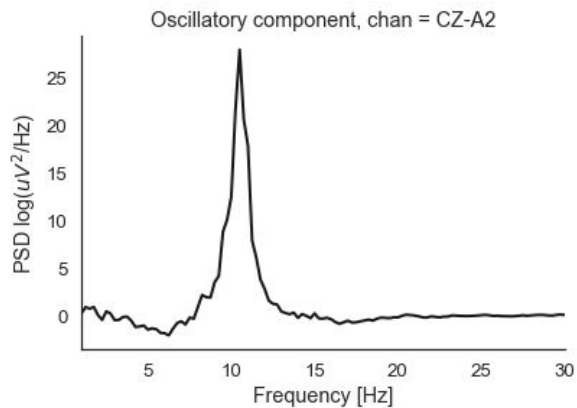
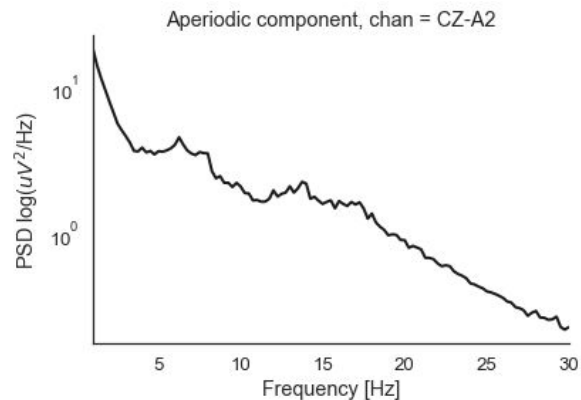
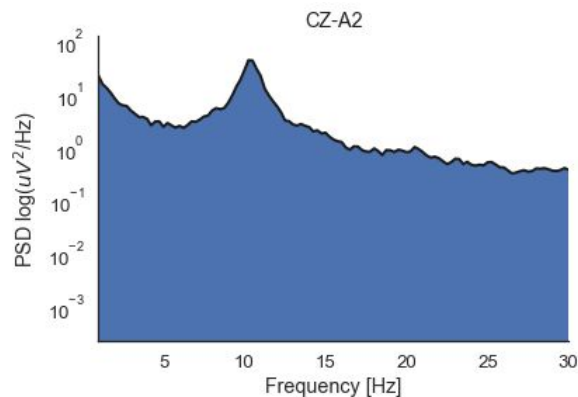
Step 4: Extract the fractal component's power spectrum by finding the median PSD of the resampled signals, and subtract this from the original to estimate the oscillatory component's power spectrum.



[12]

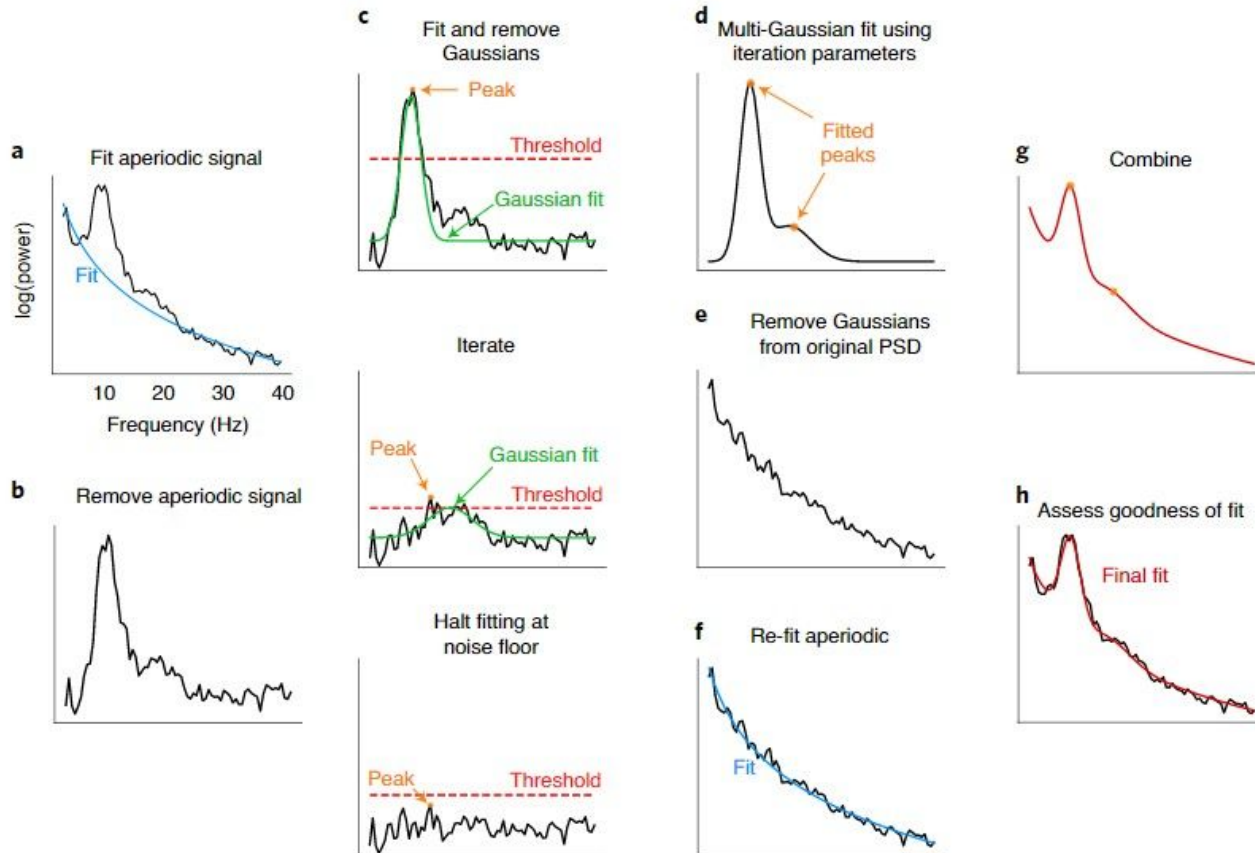


Tools and frameworks - IRASA



Tools and frameworks - FOOOF

[13]



Tools and frameworks - FOOOF

Resulting goodness of fit metrics (i.e., fit error & R^2)

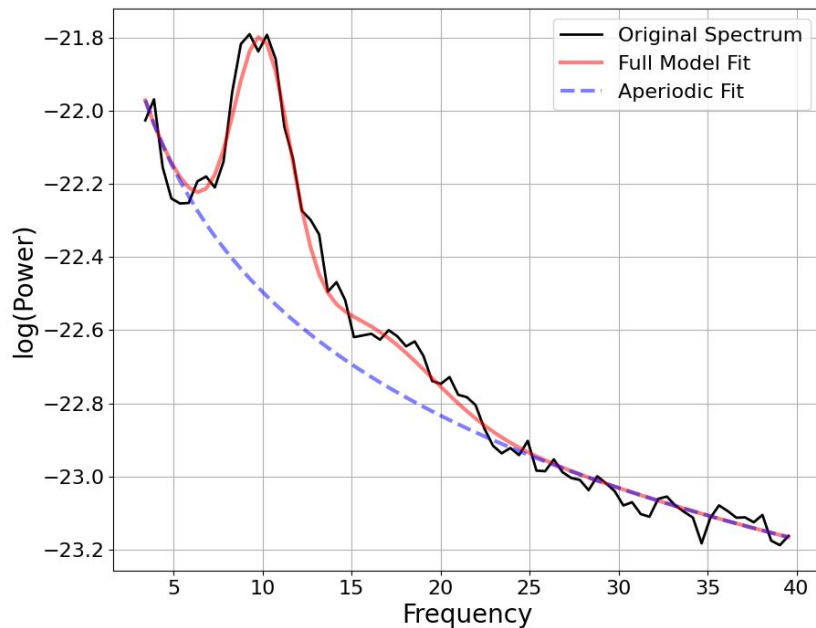
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FOOOF - POWER SPECTRUM MODEL

The model was run on the frequency range 3 - 40 Hz
Frequency Resolution is 0.49 Hz

Aperiodic Parameters (offset, exponent):
-21.3713, 1.1239

2 peaks were found:
CF: 10.00, PW: 0.685, BW: 3.18
CF: 16.32, PW: 0.138, BW: 7.03

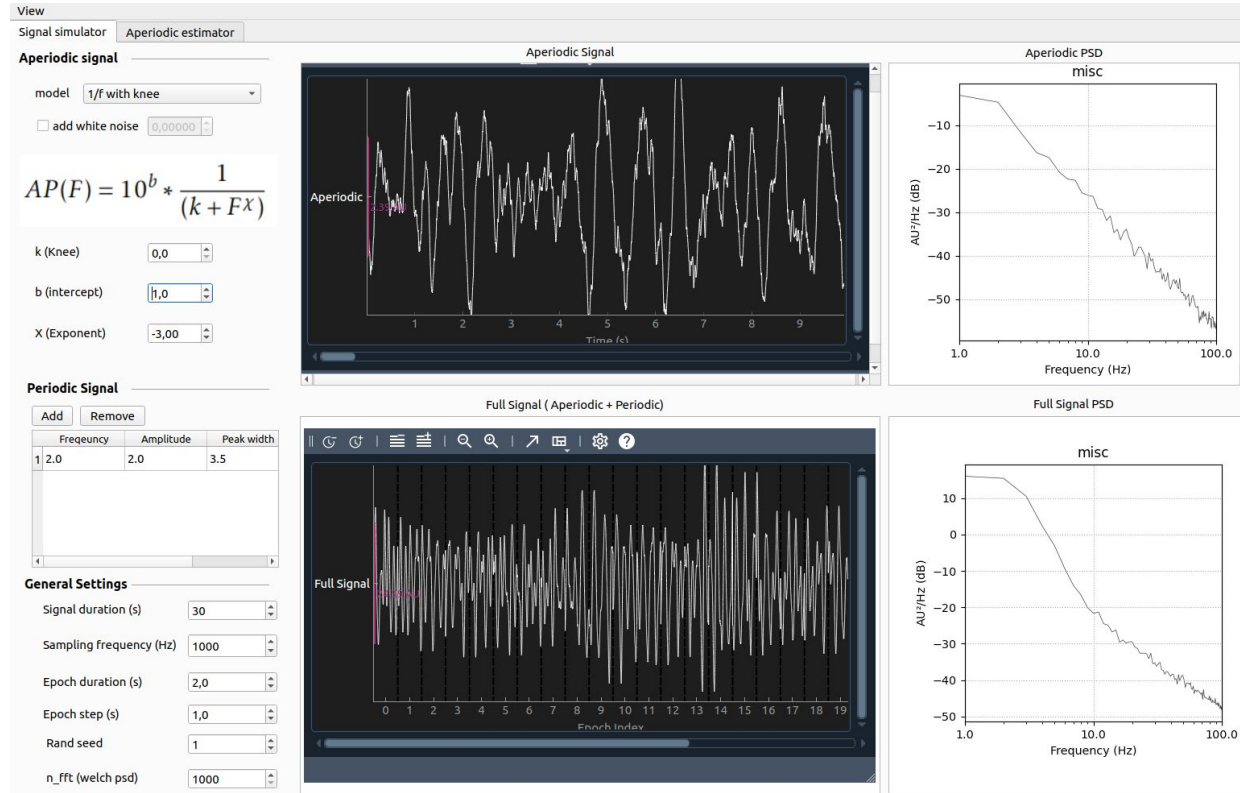
Goodness of fit metrics:
R^2 of model fit is 0.9909
Error of the fit is 0.0332
=====
```



Full model fit of the power spectrum



Interactive demonstration with GUI



Interactive demonstration with GUI

- All workshop materials are available at:
 - https://github.com/Farzin-Negahbani/NeNa_aperiodic_GUI
 - https://github.com/mvaliadis/2023_NENA_Aperiodic_Workshop
- To setup the repository:
 - a. `git clone git@github.com:Farzin-Negahbani/NeNa_aperiodic_GUI.git`
 - b. `cd gui`
 - c. `conda create -n aperiodic python=3.9.7`
 - d. `conda activate aperiodic`
 - e. `pip install -r requirements.txt`
- To run the GUI:
 - a. `python gui.py`



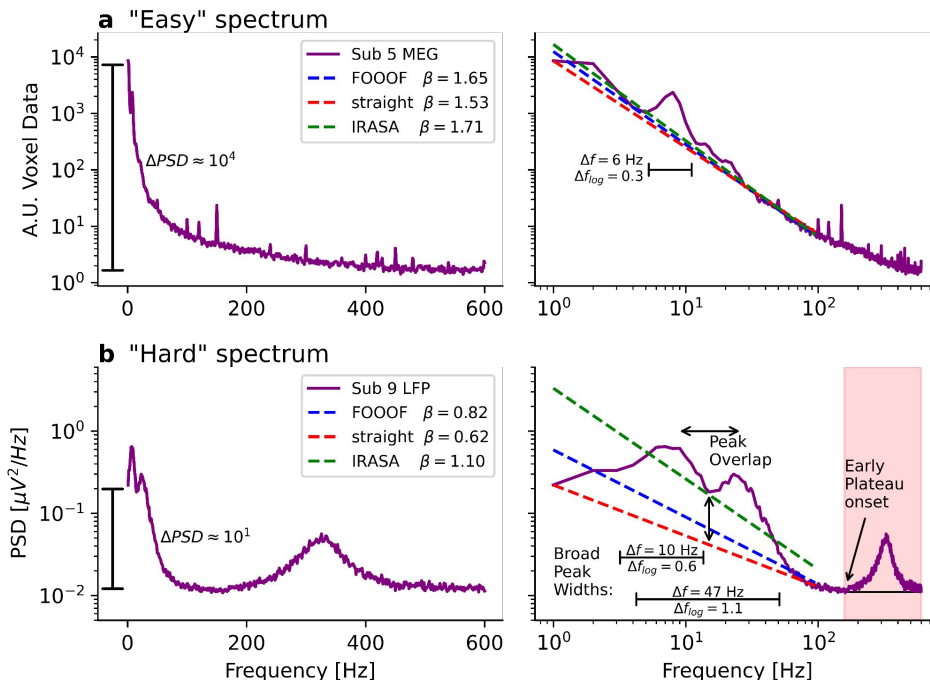
Demonstrations

1. Pick higher freq band for fitting when having low frequency oscillations.
 - a. E.g. CF= 2 hz, amp= 2, width=3, use 1-30 hz and 30-60 hz for fitting
2. Add gaussian noise and increase the noise level and observe the spectral plateau. Try changing fitting range to exclude the plateau.
3. Change h_max parameter and observe change in fit of IRASA.



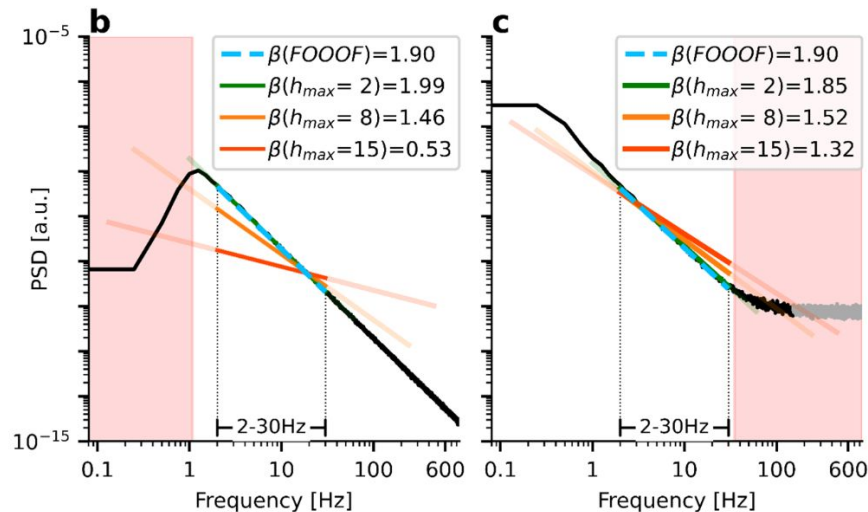
Limitations and challenges of current methods

- Main challenges of FOOOF [8]:
 - 1/f disruption from spectral plateaus
 - Avoiding oscillations that cross fitting range boundaries
 - Not sensitive to oscillatory peaks that are not clearly distinguishable



Limitations and challenges of current methods

- Main challenges of IRASA [8]:
 - Evaluated frequency range is larger than the fitting range
 - Broad peak widths require large resampling factors
 - Not sensitive to oscillatory peaks that are not clearly distinguishable
 - Computational speed



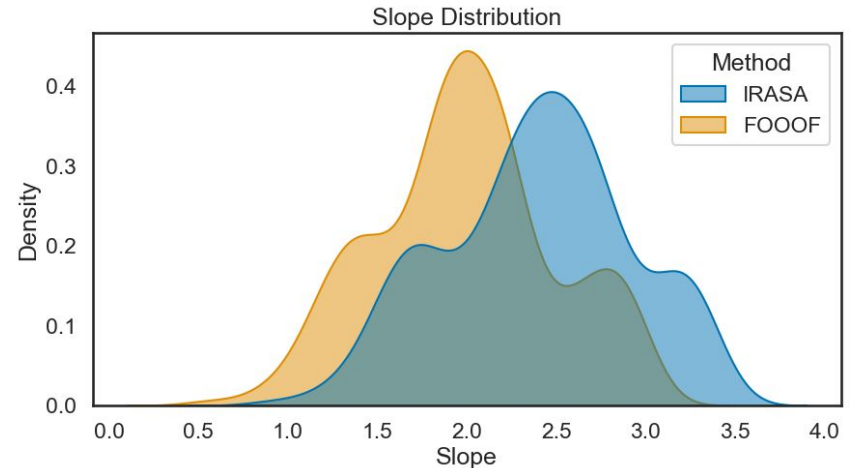
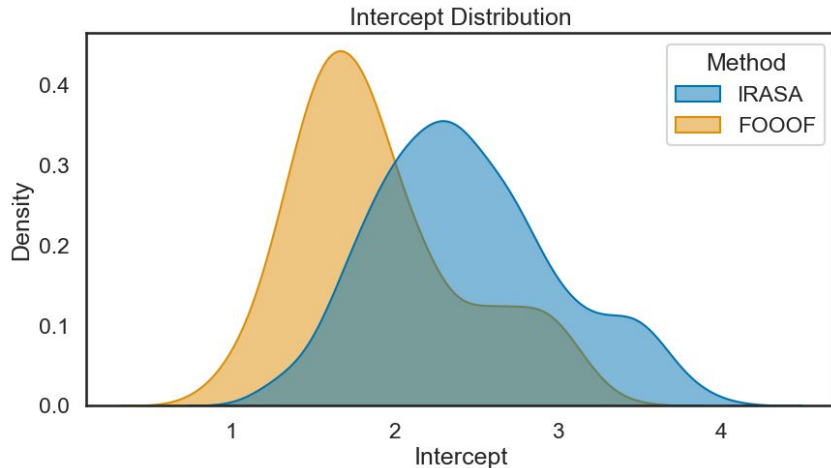
Example with Sleep EEG data

- Cleveland Family Study (Sleep EEG) Data ($n = 50$)



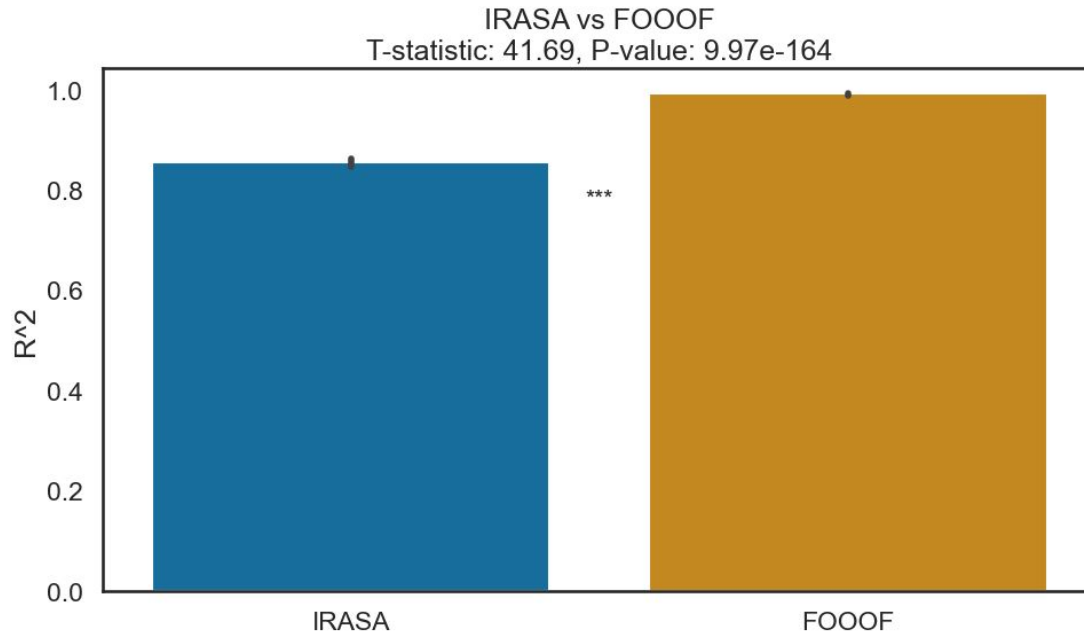
Example with Sleep EEG data

- Cleveland Family Study (Sleep EEG) Data ($n = 50$)
- Correlation between IRASA and FOOOF:
 - Intercept: 0.9707
 - Slope: 0.9893



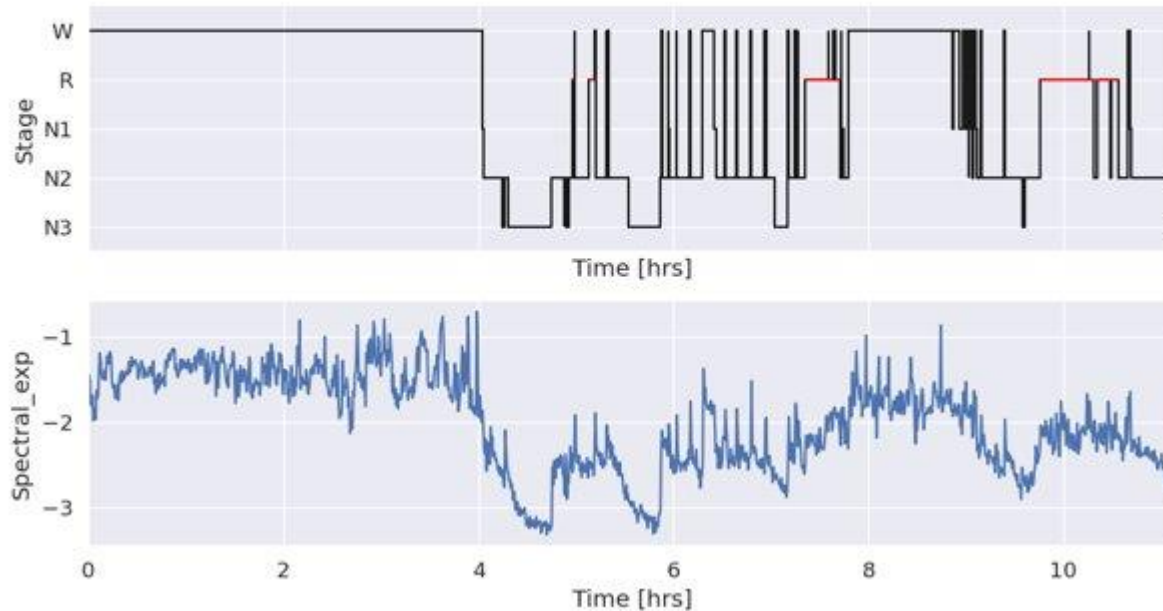
Example with Sleep EEG data

- Goodness of fit comparison



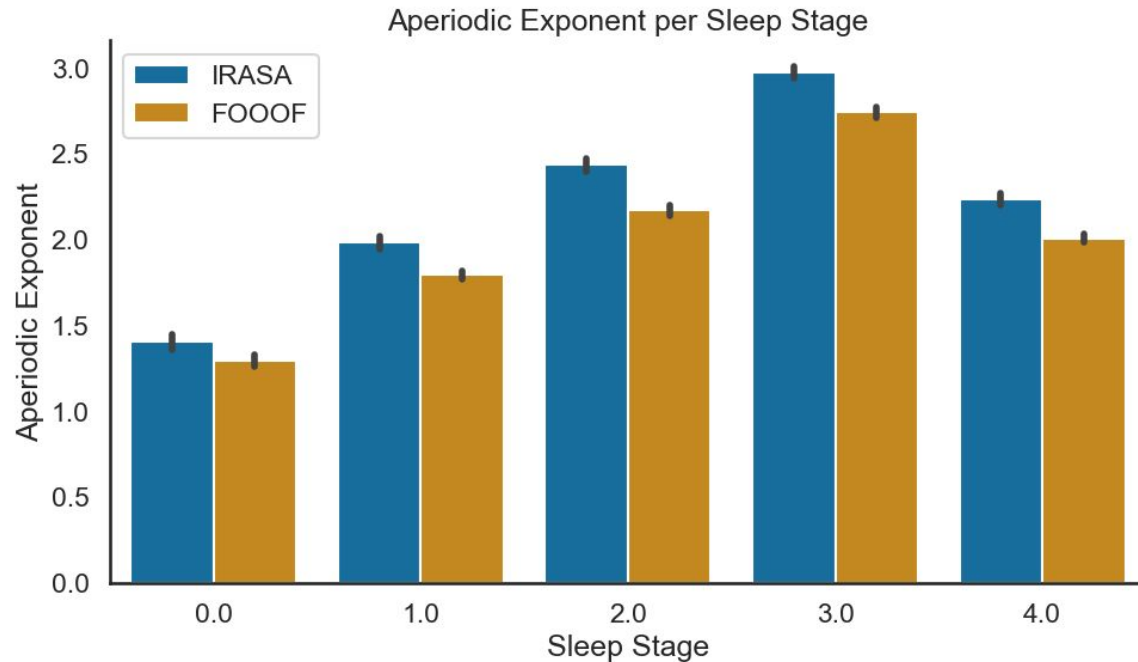
Example with Sleep EEG data

- Sleep Stage Differences (Example Subject with IRASA)



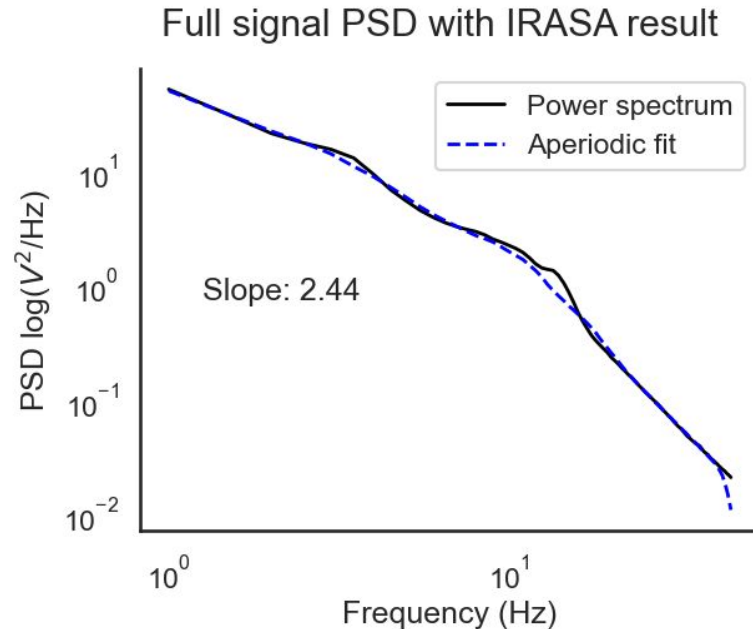
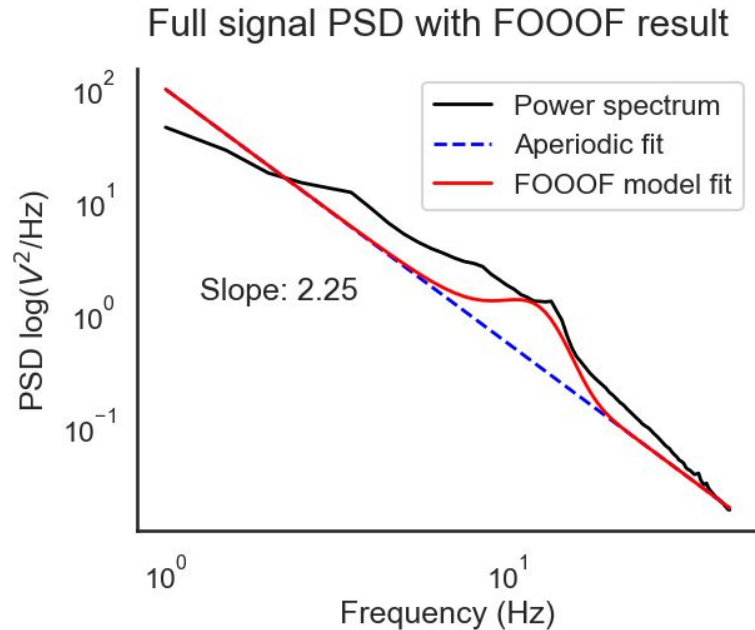
Example with Sleep EEG data

- Sleep Stage Differences (Group level):



Example with Sleep EEG data

- Sleep Stage Comparison (NREM2)



Tips & Recommendations

- Spend time looking at your raw PSDs!
 - If there's too many overlapping peaks, avoid fitting aperiodic component
 - Decide on maximal of number of peaks -> go low
 - You may need to model the knee!
- Use a fitting range at higher frequencies (e.g., 40–60 Hz) to avoid distortion from low-frequency oscillation



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 - If there's too many overlapping peaks, avoid fitting aperiodic component
 - Decide on maximal number of peaks -> go low
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- Use a fitting range at higher frequencies (e.g., 40–60 Hz) to avoid distortion from low-frequency oscillation
- Choose h_{\max} as small as possible but large enough to obtain peak-free estimates of the aperiodic component

$$f_{\text{eval. min}} = f_{\text{fit min}} / h_{\max}$$

$$f_{\text{eval. max}} = f_{\text{fit max}} \cdot h_{\max}$$



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Thank you for your attention!



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