



## Day 2. Fitness in clonal plants

Mario Vallejo-Marín  
University of Stirling

---

---

---

---

---

---

---

---

### Combining sex and clonality

- Most perennial plants combine sex and asexual reproduction
- Diversity of reproductive strategies
- Measuring life-time fitness in perennial, clonal organisms is complicated



---

---

---

---

---

---

---

---

### Road Map

- Plant clonality
- Effect of clonality on plant sexual strategies
- What is fitness in clonal plants?
- Units of selection
- Demographic approaches to measure fitness
- Primer of population projection matrixes
- Calculating population growth rate
- Case study using clonal monkeyflowers
- Using R: *popbio* package

---

---

---

---

---

---

---

---

## Asexual reproduction



- Clonal (vegetative) growth
- Apomixis (production of seeds without sex)

---

---

---

---

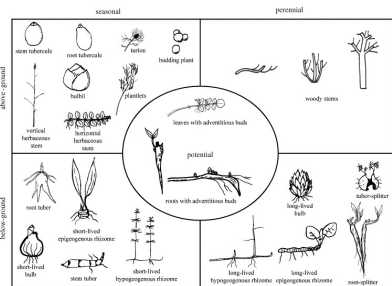
---

---

---

---

## Clonal propagation involves diverse structures




---

---

---

---

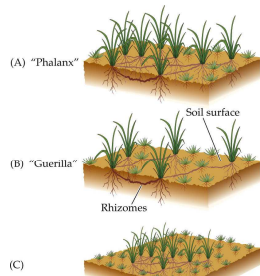
---

---

---

---

## Clonal architecture




---

---

---

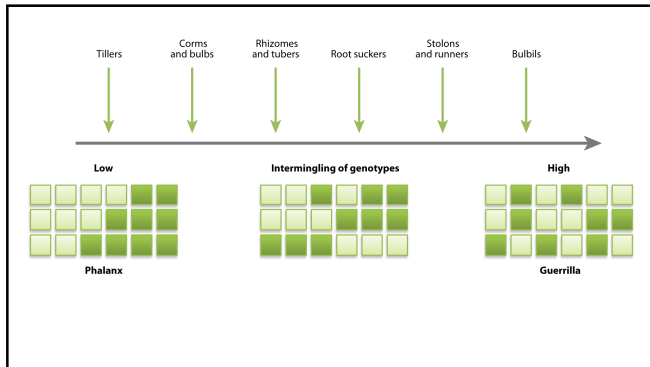
---

---

---

---

---




---

---

---

---

---

---

---

---

## Consequences for Plant Mating

Plant Mating: Who mates with whom and how often?

Barrett (2002)

1. Number of genotypes in the population
2. Spatial distribution of genotypes
3. Persistence of genotypes

### Consequences for plant mating:

- Probability of mating with relatives (including itself).
- Dynamics of deleterious mutations (inbreeding depression), e.g. via accumulation of somatic mutations.
- Benefits of other uniparental modes of reproduction.

---

---

---

---

---

---

---

---

## Ecological Consequences of Clonality

### 1. Reduction in Genotypic Diversity:

- Number of plants does not represent the number of unique genotypes

Number of genotypes (G)

Number of plants sampled (N)

$G/N = \text{"Proportion Distinguishable"}$

(Ellstrand and Rose, 1987)

Study	Number of taxa	Mean G/N (range)
Ellstrand and Rose (1987)	21	0.17 (0.002-1.0)
Widen et al. (1994)	45	0.27 (0.002-1.0)
Arnaud-Haond et al (2007)	220 studies	0.47 (0-1)
Honnay and Jacquemyn (2008)	77	0.44 (0-1)
Silvertown (2008)	218	0.40 (0-1)

---

---

---

---

---

---

---

---

## Pollination dynamics in clonal patches

Pollen transfer:

- Between genetic individuals (**outcross pollen**)
- Within the same genetic individual (**self pollen**)

Self-pollination can be of three types:

- Within the same flowers
  - Between flowers of the same plant (ramet)
  - Between flowers of different ramets of the same genet \*\*
- } geitonogamy

\*\* Exclusive of clonal plants

---

---

---

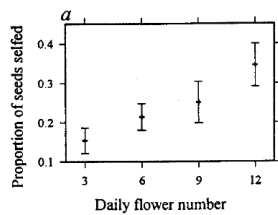
---

---

---

---

---



*Echthornia paniculata*  
(Harder and Barrett, 1995)

- Clonality by increasing geitonogamy among ramets increases transfer of self-pollen

---

---

---

---

---

---

---

---

## Selfing in clonal plants



*Decodon verticillatus* (Lythraceae)

Total self-fertilization (0.3)

- Within flowers = 18%
- Between flowers = 57%
- Between clones = 25%

Eckert (2000)

---

---

---

---

---

---

---

---

Does clonality disfavour the evolution of selfing?

- 1. Clonality increases self-pollination rates, producing more unfit offspring
- 2. Clonality provides reproductive assurance
- 3. Clonality increases inbreeding depression via accumulation of somatic mutations
- 4. Clonality reduces the genetic advantage of uniparental reproduction gained by selfing

Selection should rarely favour the joint evolution of clonality and selfing

---

---

---

---

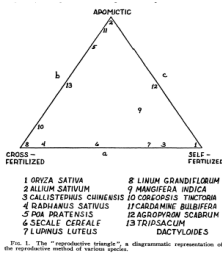
---

---

---

---

Fryxell's Reproductive Triangle (1957)



---

---

---

---

---

---

---

---

Building the Reproductive Triangle

Total Reproduction = Outcrossing + Selfing + Clonal

• **Clonal Reproduction:**  
Approximated as the proportion of adults produced via clonality

Clonal Fraction =  $1 - \text{Genets} / \text{Ramets} = 1 - G/N$

• **Reproduction via Outcrossing:**  
Adults produced sexually \* Outcrossing rate (estimated via genetic markers)  
 $= (G/N) * t$

• **Reproduction via Selfing:**  
Adults produced sexually \* (1-Outcrossing rate)

Collected estimates of both clonal fraction and outcrossing rates from the literature

---

---

---

---

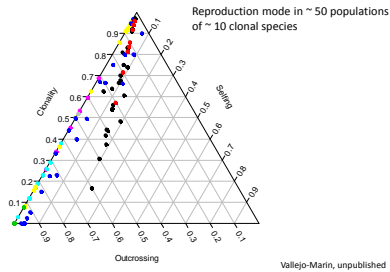
---

---

---

---

### Reproductive Triangle




---

---

---

---

---

---

---

---

### What is fitness in clonal organisms?

#### Fitness

- *The success of an entity in reproducing; hence the average contribution of an allele or genotype to the next generation or succeeding generations.*

Futuyma (2013)

- *The fitness of a trait or allele is... the expected reproductive success of an individual who has that trait or allele relative to other members in the populations.*

Bergstrom and Dugatkin (2016)

---

---

---

---

---

---

---

---

### Fitness in sexual organisms

#### Individual (=genotype) fitness

- Number of offspring contributed to the next generation
- E.g., in a dioecious plant, the fitness of a female individual is the expected number of offspring produced \* offspring quality
- Male plant, number of offspring sired \* quality

#### Allele fitness

- Average number of offspring produced by individuals carrying a **particular allele**

---

---

---

---

---

---

---

---

### Fitness: Survival (viability) and Fertility

Genotype	Viability	Fertility	Fitness
AA	$v_{11}$	$f_{11}$	$W_{11}$
Aa	$v_{12}$	$f_{12}$	$W_{12}$
aa	$v_{22}$	$f_{22}$	$W_{22}$

Viability: Survival to reproductive age  
Fertility: Offspring produced

---

---

---

---

---

---

---

---

### Relative fitness

$$w_{11} = W_{11} / W_{11}$$

$$w_{12} = W_{12} / W_{11}$$

$$w_{22} = W_{22} / W_{11}$$

$W$  = Absolute fitness  
 $w$  = relative fitness

Genotype	Viability	Fertility	Absolute Fitness	Relative Fitness
AA	0.90	3.00	2.70	1.0
Aa	0.90	2.00	1.80	0.67
aa	0.45	2.00	0.90	0.33

---

---

---

---

---

---

---

---

### Two *levels* of individuals: genets and ramets

- Genet: Genetically unique individual
- Ramet: Physiologically independent unit

- Which *individuals* should we count to measure fitness in clonal organisms?

---

---

---

---

---

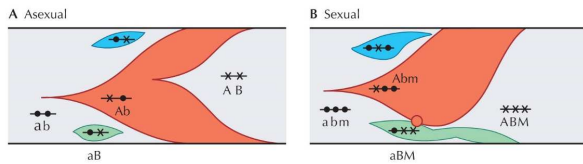
---

---

---

### Asexuality results in linkage disequilibrium

- Recombination breaks associations between loci
- In asexuals, loci are not statistically independent but are transmitted together with other loci




---

---

---

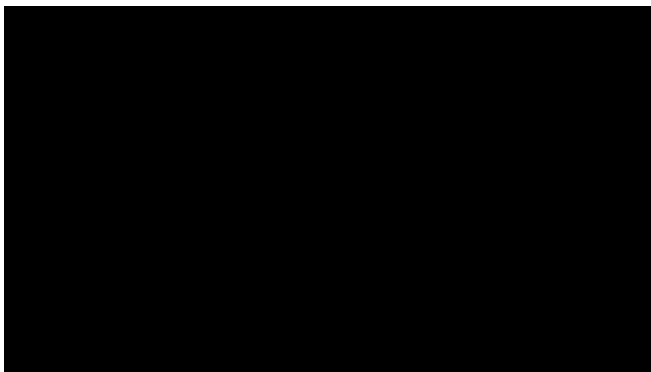
---

---

---

---

---




---

---

---

---

---

---

---

---

### Fitness in asexuals: Number of individuals in genotypic classes

#### Operational definitions

- Number of individuals per lineage (e.g., yeast cells in sexual vs. asexual lineages)
- Clonal plants: seeds + clones




---

---

---

---

---

---

---

---



### How to weight seeds vs. clones?

- Seeds and vegetative propagules often make different contributions to the next generation
- E.g., plants may produce many seeds, but the probability of establishment may be low
- In contrast, clonal propagules may be less numerous but have a higher competitive advantage



---

---

---

---

---

---

---

### A demographic approach

- Measure plant fitness in groups of individuals (populations)

$$n_{t+1} = \lambda * n_t$$

$n$  = number of individuals  
 $\lambda$  = population growth rate

If  $\lambda_1 > \lambda_2$ , then species 1 has higher fitness than species 2 (higher rate of population growth)

---

---

---

---

---

---

---

### Primer in population demography

---

---

---

---

---

---

---

Modelling population demography: Structured populations

- A structured population is simply a population in which there are different classes of individuals
- Age structure: Individuals classified by age
- Stage structure: Individuals classified by stage
- Individuals from different classes make different contributions to population growth

---

---

---

---

---

---

---

Modelling population growth

- How does survival and fertility affect population growth?
- Which stages have the strongest effects on population growth?

Modelling population growth:

- Short- and long term growth
- Population structure
- Reproductive value
- Sensitivity of growth at specific changes in survival and reproduction

---

---

---

---

---

---

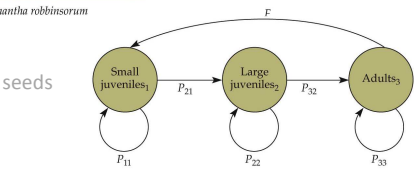
---



*Coryphantha robbinsorum*

Life cycle graphs

$F$  (=effective fertility)= average number of fruits \* average seeds per fruit \* seed survival and germination \* survival to first census



ECOLOGY OF PLANTS, Second Edition, Figure 5.7 © 2005 Sinauer Associates, Inc.

---

---

---

---

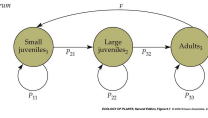
---

---

---



*Conspicillaria rubicundum*



Number of **Juveniles** at time  $t + 1$ :

$$n_1(t+1) = P_{11}n_1(t) + Fn_3(t)$$

Number of **Large Juveniles** at time  $t + 1$ :

$$n_2(t+1) = P_{21}n_1(t) + P_{22}n_2(t)$$

Number of **Adults** at time  $t + 1$ :

$$n_3(t+1) = P_{31}n_1(t) + P_{32}n_2(t) + P_{33}n_3(t)$$

## Matrix Model

Transition Matrix

Population Vector

$$\begin{bmatrix} n_1(t+1) \\ n_2(t+1) \\ n_3(t+1) \end{bmatrix} = \begin{bmatrix} P_{11} & 0 & F \\ P_{21} & P_{22} & 0 \\ 0 & P_{32} & P_{33} \end{bmatrix} \times \begin{bmatrix} n_1(t) \\ n_2(t) \\ n_3(t) \end{bmatrix}$$

$$\mathbf{n}_{t+1} = \mathbf{Mn}_t$$

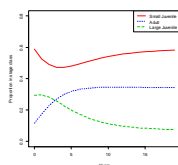
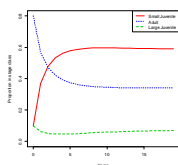
- Multiplying a vector times a matrix

Row  $\times$  column

How to build a matrix:  
Describes the transition probabilities from "column" number stage to "row" number stage.

## Analysing matrix models

- Repeated multiplication of the vector and matrix reaches a stable structure:  
That is, the population size keeps changing, but the proportion of individuals in each class remains constant



## Analysing matrix models

- Repeated multiplication of the vector and matrix reaches a stable structure:  
*That is, the population keeps growing, but the proportion of individuals in each class remains constant*
- The transition matrix can be replaced by a single number:  
 $\lambda$  (eigenvalue)
- Eigenvalues and Eigenvectors  
 $M$  = transition matrix  
 $x$  = vector

$$Mx = \lambda x$$

*(Diagram: An arrow points from  $\lambda$  to the word "eigenvalue" and another arrow points from  $x$  to the word "eigenvector")*

---

---

---

---

---

---

---

## Eigenvalues and eigenvectors

- The eigenvalues tell us about population changes in numbers  
 $\lambda = 1$     Population is stable  
 $\lambda > 1$     Population is growing  
 $\lambda < 1$     Population is declining
- The eigenvectors tell us how many at each stage

---

---

---

---

---

---

---

## Eigenvalues and eigenvectors

- Each matrix has a number of eigenvalues and eigenvectors
- A matrix with  $N$  rows and columns (stages) has  $N$  eigenvalues and eigenvectors
- A 3x3 matrix:  $\lambda_1, \lambda_2, \lambda_3$
- One eigenvalue is always larger than the rest: Dominant or leading eigenvalue
- Overtime, the population growth rate approaches the leading eigenvalue, and the structure its associated eigenvector
- Population growth and structure can be predicted using eigenvalues and eigenvectors

---

---

---

---

---

---

---

## Demography of *Coryphanta*

Site A (northeastern exposure)	Site B (southwestern exposure)	Site C (hilltop) $A_{max}$
$A_{site A} = \begin{bmatrix} 0.672 & 0 & 0.561 \\ 0.018 & 0.849 & 0 \\ 0 & 0.138 & 0.969 \end{bmatrix}$	$A_{site B} = \begin{bmatrix} 0.493 & 0 & 0.561 \\ 0.013 & 0.731 & 0 \\ 0 & 0.234 & 0.985 \end{bmatrix}$	$A_{site C} = \begin{bmatrix} 0.434 & 0 & 0.560 \\ 0.333 & 0.610 & 0 \\ 0 & 0.304 & 0.956 \end{bmatrix}$

$$\lambda = 0.9978 \quad \lambda = 0.9977 \quad \lambda = 1.1187$$

- Long-term prediction of population growth

ECOLOGY OF PLANTS, Second Edition, Box 10 © 1998 Sinauer Associates, Inc.

## Sensitivity and Elasticity

- How does *lambda* change as the individual elements of a transition matrix change?
- Sensitivity: Rate at which *lambda* changes when all other elements in the matrix are held constant

$$\begin{bmatrix} P_{11} & 0 & F \\ P_{21} & P_{22} & 0 \\ 0 & P_{32} & P_{33} \end{bmatrix} \rightarrow a_{ij} \quad \text{Sensitivity} = \frac{\partial \lambda}{\partial a_{ij}}$$

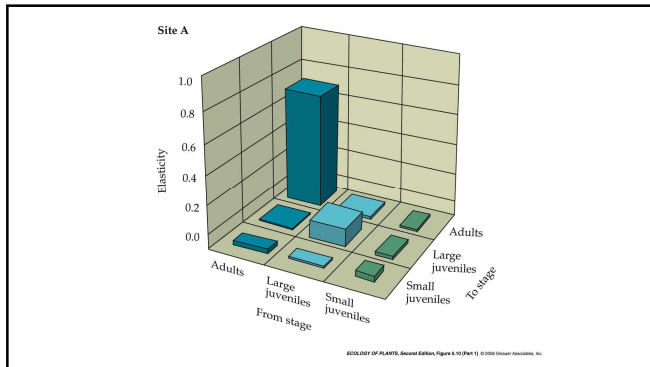
- Partial derivative with respect to  $a_{ij}$

## Sensitivity and Elasticity

- Sensitivities: How to compare among scales and account for matrix elements that are defined as zero?
- Elasticity ( $e_{ij}$ ): The proportional sensitivity of *lambda* with respect to change in an element of the matrix

$$e_{ij} = \frac{a_{ij}}{\lambda} \frac{\partial \lambda}{\partial a_{ij}}$$

- Elasticities are comparable across the matrix
- Elasticities add up to one
- Comparable across matrices based on the same life cycle graph




---

---

---

---

---

---

---

---

## A case study using monkeyflowers

- Handouts for this practical exercise are provided separately

---

---

---

---

---

---

---

---