

# Chapter 1

## MOTs

<https://journals.aps.org/prl/pdf/10.1103/PhysRevA.70.063413> narrow line cooling and momentum space crystals

<https://journals.aps.org/prl/pdf/10.1103/PhysRevLett.93.073003> previous paper narrow line cooling finite photon recoil dynamics For the 689 line in strontium, the ratio of the recoil frequency  $\omega_r = \frac{\hbar k^2}{2m} = 2\pi \times 4.8$  kHz to the natural linewidth  $\Gamma = 2\pi \times 7.4$  kHz the transition is on the order of unity. this is what defines a narrow line MOT.

### 1.1 Finite photon recoil dynamics

The 1s0-3p1 transition has its single photon recoil is of comparable size to the natural linewidth. When an atom of mass  $m$  emits or absorbs a photon  $\gamma$  of frequency  $\omega$ , then momentum of the photon  $p_\gamma = h/\lambda = \hbar k$  is transferred to the atom giving it some velocity  $v_{rec} = \hbar k/m$

### 1.2 Regimes of red-detuned MOT

Three regimes of behavior depend on the relative magnitudes of  $|\Delta|$ ,  $\Gamma$ , and  $\Gamma_E = \Gamma\sqrt{1+s}$  where  $\Gamma$  is the natural linewidth  $s = I/I_{sat}$  is the saturation intensity which may broaden the line. The three regimes are (I)  $\Gamma \ll \Gamma_E \ll |\Delta|$ , (II),  $|\Delta| < \Gamma_E$  and  $\Gamma \ll \Gamma_E$  so  $\Gamma < |\Delta| < \Gamma_E$  (but perhaps  $\Gamma \not\ll |\Delta|$ ?), and (III), when  $s \simeq 1$ . and so  $\Gamma \not\ll \Gamma_E$ .

#### 1.2.1 Red-detuned MOT Regime (I)

In the first regime,  $\Gamma \ll \Gamma_E \ll |\Delta|$ . For the 689 line in strontium, the ratio of the recoil frequency  $\omega_r = \frac{\hbar k^2}{2m} = 2\pi \times 4.8$  kHz to the natural linewidth  $\Gamma = 2\pi \times 7.4$  kHz the transition is on the order of unity. In this regime,

#### 1.2.2 regime 2

$|\Delta| \lesssim \Gamma_E$  and  $\Gamma \ll \Gamma_E$

this is more typical and thermodynamics reminiscent of ordinary doppler cooling.  $\delta$  and  $s$  dependent temperature minima

#### 1.2.3 regime 3

$s$  approaches unit, photon-recoil-driven impulsive force dominates and temperature below photon-recoil limit  $T_r = 2\hbar\omega_r/k_b$

$$\Gamma \simeq \Gamma_E$$

### 1.2.4 other regimes?

sing  $\Gamma \sim \omega_r$  you get momentum packets. explained by analytic solution to the 1D semiclassical radiative force equation. for  $\delta > 0$ , and  $\Gamma \sim \omega_r$  allow direct visualization of positive feedback acceleration that effeciently bunches the atoms into discrete, well-defined momentum packets. the gravity ratio  $R$  directly influences the blue detuned thermodynamics, enabling cooling around a velocy where radiation pressure and gravity balance. aparently the underlying physics here is the same as regime I but manifest bvery differently.

### 1.2.5 method

uses frequency modulate redMOT, start at 3G/cm and go to 10 G/cm. Then transition to singlefrequency