

# Model Selection

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```
library(dplyr)

##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##   filter, lag
## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union

library(tidyr)
library(ggplot2)
library(ggthemes)
library(viridis)

## Loading required package: viridisLite

library(nlme)

##
## Attaching package: 'nlme'
## The following object is masked from 'package:dplyr':
##
##   collapse

library(lme4)

## Loading required package: Matrix
##
## Attaching package: 'Matrix'
## The following object is masked from 'package:tidyr':
##
##   expand
##
## Attaching package: 'lme4'
## The following object is masked from 'package:nlme':
##
##   lmList

library(MuMIn)
# install.packages("R2admb")
# install.packages("glmmADMB",
#   repos=c("http://glmmadmb.r-forge.r-project.org/repos",
#     getOption("repos")),
#   type="source")
library(glmmADMB)
```

```

## Loading required package: MASS

##
## Attaching package: 'MASS'

## The following object is masked from 'package:dplyr':
##
##     select

##
## Attaching package: 'glmmADMB'

## The following object is masked from 'package:MASS':
##
##     stepAIC

## The following object is masked from 'package:stats':
##
##     step

library(pscl)

## Warning: package 'pscl' was built under R version 3.4.2

## Classes and Methods for R developed in the
## Political Science Computational Laboratory
## Department of Political Science
## Stanford University
## Simon Jackman
## hurdle and zeroinfl functions by Achim Zeileis

library(cowplot)

##
## Attaching package: 'cowplot'

## The following object is masked from 'package:ggplot2':
##
##     ggsave

emergenceData <- readRDS("data/emergence.RData")
survival <- readRDS("data/survival.RData")
fecundity <- readRDS("data/fecundity.RData")
AedesAll <- readRDS("data/AedesIndividualSurvival.RData")

```

This document goes through model selection for each analysis section of the ms.

## Survival

### Aedes

Survival (or prob. of emergence) is a binary variable per individual mosquito. I use a generalized linear mixed model to explore the effect of Aedes density, Stephensi density, and temperature on emergence, with replicate as a random intercept. The data is subset to that of females (this can differ as males tend to develop more quickly and will emerge first). Predictor variables are normalized/scaled.

Reformat data into successes and failures per jar.

```

aeSurvival <- emergenceData %>%
  filter(Species == "Aedes" & AeDens != 0 & Sex == "Female") %>%
  group_by(Replicate, Temp, TempNum, AeDens, StDens, Ratio) %>%
  summarise(success = sum(Number, na.rm = T)) %>%
  mutate(failure = (AeDens/2) - success) %>%
  ungroup() %>%
  #rescale predictor variables
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T))) %>%
  #drop jar that was all male
  filter(!(Replicate == "A" & Temp == "24" & Ratio == "8:24"))

#for when more than 50% were female
aeSurvival$failure[aeSurvival$failure<0] <- 0

```

Aedes model selection

```

m0 <- glmer(cbind(success, failure) ~ 1 + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))
m1 <- glmer(cbind(success, failure) ~ AeDensScale + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))
m2 <- glmer(cbind(success, failure) ~ AeDensScale + TempNum + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))
m3 <- glmer(cbind(success, failure) ~ AeDensScale + poly(TempNum,2) + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))
m4 <- glmer(cbind(success, failure) ~ AeDensScale*poly(TempNum,2) + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))

m5 <- glmer(cbind(success, failure) ~ AeDensScale + poly(TempNum,2) + StDensScale + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))

m6 <- glmer(cbind(success, failure) ~ AeDensScale + poly(TempNum,2) * StDensScale + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))

m7 <- glmer(cbind(success, failure) ~ AeDensScale + poly(TempNum,2) + StDensScale + TempNum:StDensScale
            data = aeSurvival,
            family = binomial(link = "logit"))

m8 <- glmer(cbind(success, failure) ~ AeDensScale*poly(TempNum,2) + StDensScale*poly(TempNum,2) + (1|Replicate),
            data = aeSurvival,
            family = binomial(link = "logit"))

## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control
## $checkConv, : Model failed to converge with max|grad| = 0.00227615 (tol =
## 0.001, component 1)

```

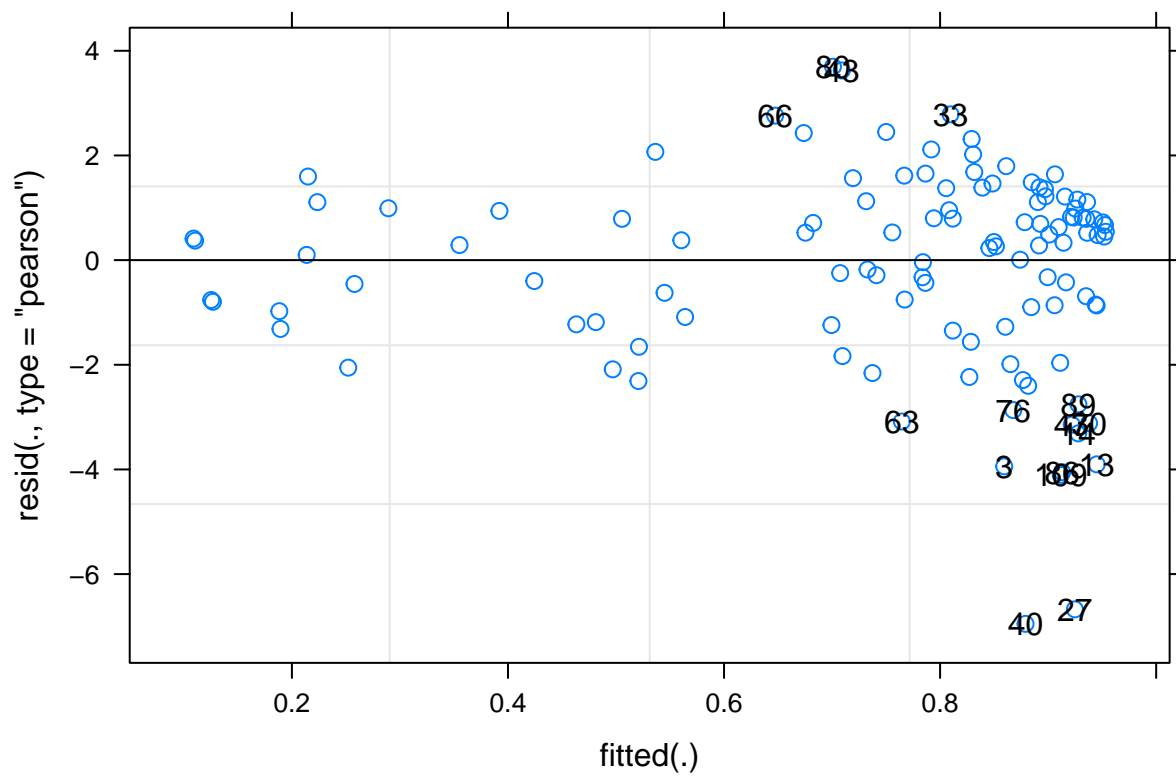
```
modelSummary <- cbind(model = c("m0", "m1", "m2", "m3", "m4", "m5", "m6", "m7", "m8"),
  do.call(rbind, lapply(list(m0, m1, m2, m3, m4, m5, m6, m7, m8), broom::glance)),
  AICc = AICc(m0, m1, m2, m3, m4, m5, m6, m7, m8),
  AICweights = Weights(AIC(m0, m1, m2, m3, m4, m5, m6, m7, m8)))
modelSummary
```

##	model	sigma	logLik	AIC	BIC	deviance	df.residual	AICc.df	
##	m0	m0	1	-815.5837	1635.1674	1640.6917	1365.5858	115	2
##	m1	m1	1	-362.9521	731.9043	740.1908	459.1218	114	3
##	m2	m2	1	-358.0774	724.1549	735.2036	449.5037	113	4
##	m3	m3	1	-330.0400	670.0799	683.8908	393.0043	112	5
##	m4	m4	1	-329.2971	672.5942	691.9294	391.5311	110	7
##	m5	m5	1	-326.8907	665.7815	682.3545	386.5432	111	6
##	m6	m6	1	-323.0674	662.1347	684.2321	378.7112	109	8
##	m7	m7	1	-323.0756	660.1512	679.4864	378.7333	110	7
##	m8	m8	1	-322.9522	665.9045	693.5262	378.4954	107	10
##	AICc	AICc		AICweights					
##	m0	1635.2726		1.267549e-212					
##	m1	732.1167		1.754096e-16					
##	m2	724.5120		8.449045e-15					
##	m3	670.6205		4.667015e-03					
##	m4	673.6217		1.327635e-03					
##	m5	666.5451		4.003427e-02					
##	m6	663.4681		2.479221e-01					
##	m7	661.1787		6.684025e-01					
##	m8	667.9800		3.764646e-02					

```
AedesSurvivalModel <- m7
```

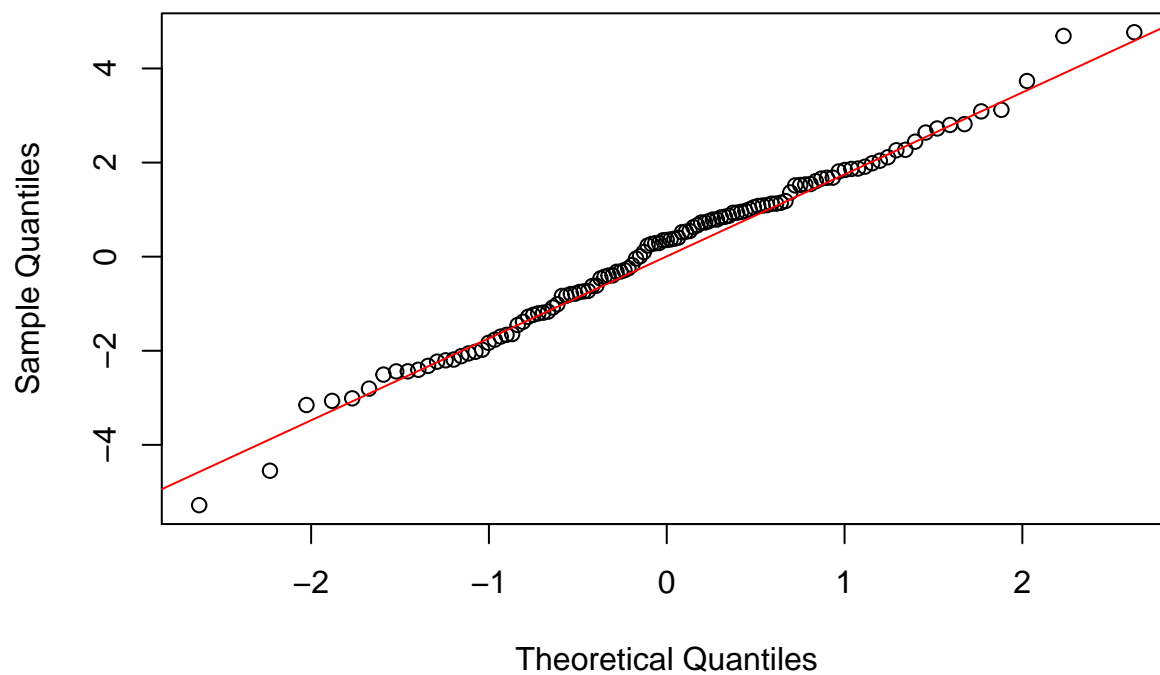
Based on the above, model 7 (survival ~ AeDens + StDens + Temp<sup>2</sup> + StDens:Temp) fits best. Model 6 fits similarly, but has an additional term of an interaction between polynomial temperature and stephensi density, and so the more parsimonious model is chosen. Now we explore model residuals.

```
plot(AedesSurvivalModel, id = 0.01, idLabels=~.obs)
```



```
qqnorm(resid(AedesSurvivalModel))
qqline(resid(AedesSurvivalModel), col = "red")
```

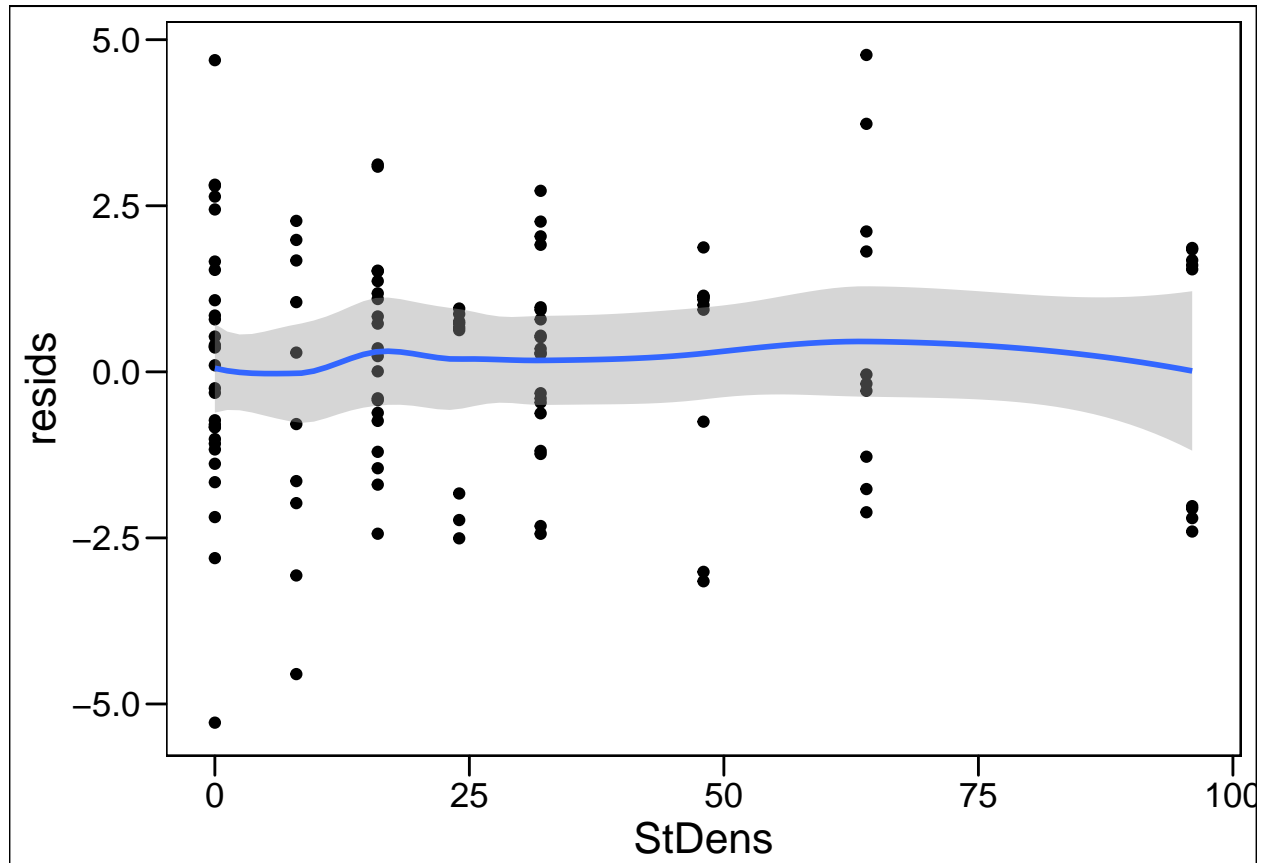
### Normal Q–Q Plot



```
aeSurvival$preds <- predict(AedesSurvivalModel)
aeSurvival$resids <- resid(AedesSurvivalModel)
```

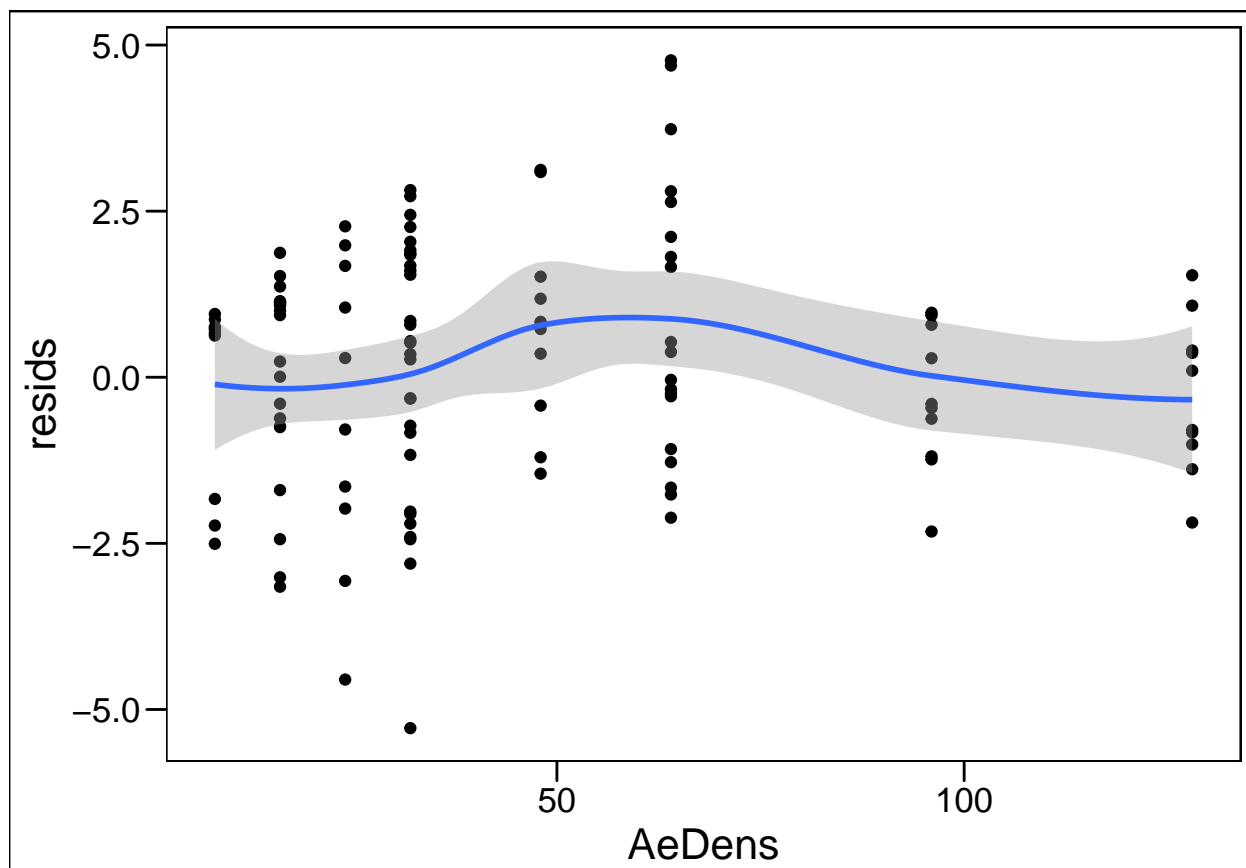
```
ggplot(data = aeSurvival, aes(x=StDens, y = resid)) +
  geom_point() +
  geom_smooth(se=T) +
  theme_base()
```

```
## `geom_smooth()` using method = 'loess'
```



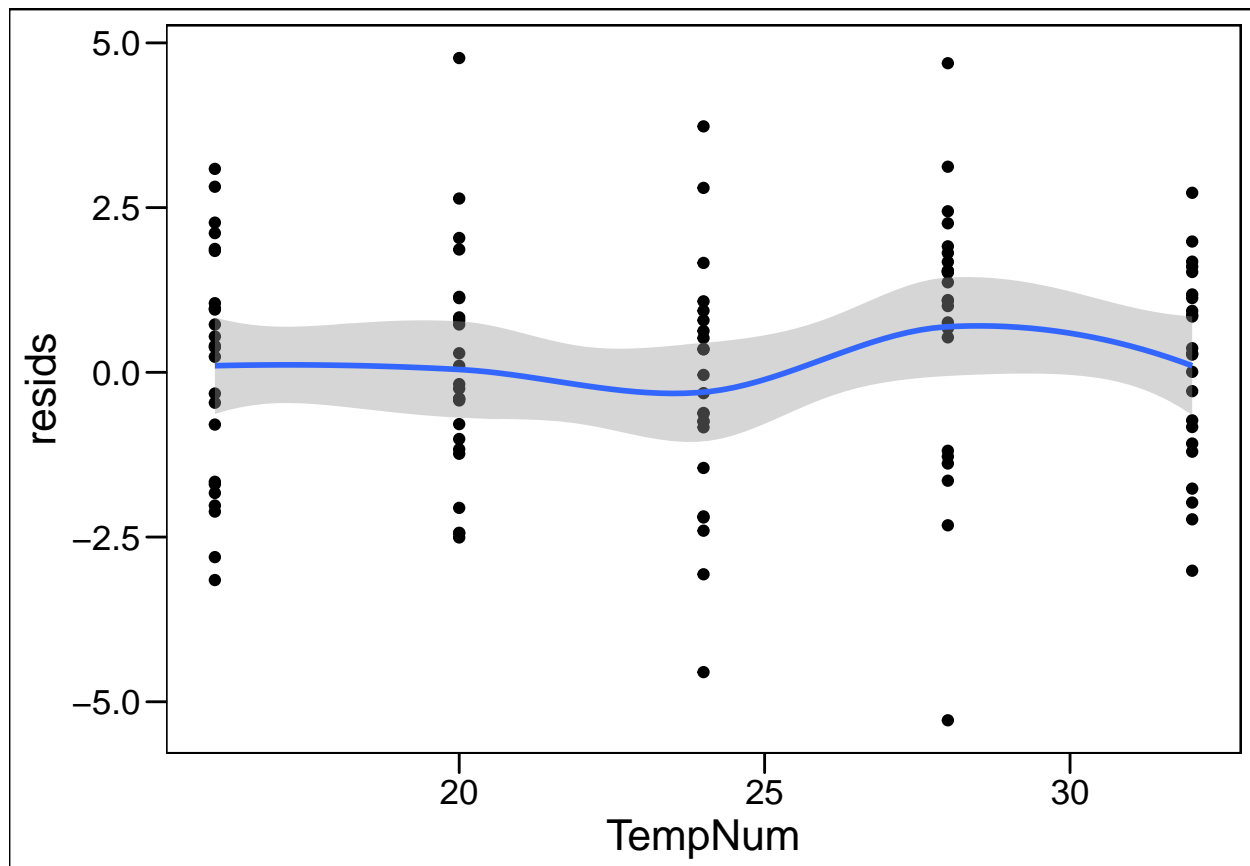
```
ggplot(data = aeSurvival, aes(x=AeDens, y = resid)) +
  geom_point() +
  geom_smooth(se=T) +
  theme_base()
```

```
## `geom_smooth()` using method = 'loess'
```



```
ggplot(data = aeSurvival, aes(x=TempNum, y = resids))+
  geom_point() +
  geom_smooth(se=T)+
  theme_base()
```

```
## `geom_smooth()` using method = 'loess'
```



The residuals for this model are slightly heteroskedastic, but I think are fine in general.

```
summary(AedesSurvivalModel)
```

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
##   Approximation) [glmerMod]
## Family: binomial ( logit )
## Formula:
## cbind(success, failure) ~ AeDensScale + poly(TempNum, 2) + StDensScale +
##   TempNum:StDensScale + (1 | Replicate)
## Data: aeSurvival
##
##      AIC      BIC   logLik deviance df.resid
##    660.2    679.5   -323.1    646.2     110
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -6.9507 -1.1850  0.3458  1.1078  3.6962
##
## Random effects:
##  Groups      Name      Variance Std.Dev.
## Replicate (Intercept) 0.009197 0.0959
## Number of obs: 117, groups: Replicate, 2
##
## Fixed effects:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)      2.78017    0.15444  18.001  < 2e-16 ***
```



```
## AeDensScale      -1.99257    0.08363 -23.825 < 2e-16 ***
## poly(TempNum, 2)1    0.09639    0.70680    0.136  0.89153
## poly(TempNum, 2)2   -3.83763    0.51334   -7.476  7.67e-14 ***
## StDensScale       -0.60399    0.29535   -2.045  0.04086 *
## StDensScale:TempNum 0.03404    0.01240    2.745  0.00605 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##      (Intr) ADnsSc p(TN,2)1 p(TN,2)2 StDnsS
## AeDensScale -0.796
## ply(TmN,2)1  0.044 -0.026
## ply(TmN,2)2 -0.096  0.147  0.025
## StDensScale -0.100  0.078  0.681  -0.006
## StDensScl:TN -0.030 -0.003 -0.701  -0.004  -0.967
```

```
confint(AedesSurvivalModel)
```

```
## Computing profile confidence intervals ...
```

```
##              2.5 %      97.5 %
## .sig01          0.000000000  0.48341491
## (Intercept)     2.445441095  3.12095464
## AeDensScale     -2.158699523 -1.83075883
## poly(TempNum, 2)1 -1.289426029  1.48235724
## poly(TempNum, 2)2 -4.848420407 -2.83549324
## StDensScale     -1.182425199 -0.02379168
## StDensScale:TempNum 0.009849299  0.05849671
```

Plot predicted values in a heatmap.

```
#heatmap plots
```

```
newData <- expand.grid(AeDens=seq(0,128, by=2), StDens=seq(0,128, by=2), TempNum=c(16,20,24,28,32), Rep=1:3)
newData <- newData %>%
```

```
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T)))
```

```
newData$preds <- predict(AedesSurvivalModel, type = "response", newdata = newData)
```

```
#remove extrapolation outside of measured range
```

```
newData$preds[newData$AeDens+newData$StDens>128] <- NA
```

```
#get means over replicates to plot
```

```
predicted <- newData %>%
```

```
  group_by(TempNum, AeDens, StDens) %>%
  summarise(preds = mean(preds, na.rm = T))
```

```
#plot it
```

```
aeSurvPlot <- ggplot(predicted, aes(x=StDens, y=AeDens, z=preds))+
```

```
  geom_raster(aes(fill=preds))+
```

```
  geom_contour(color="black", binwidth = 0.1)+
```

```
  theme_minimal()+
```

```
  scale_fill_viridis(name="Prop. Emerged", na.value = "gray90",
    begin = 0, end = 1)+
```

```
  #geom_contour(color="white")+
```

```
  #scale_fill_gradient(low = "gray90", high = "gray10", na.value = "white")+
```

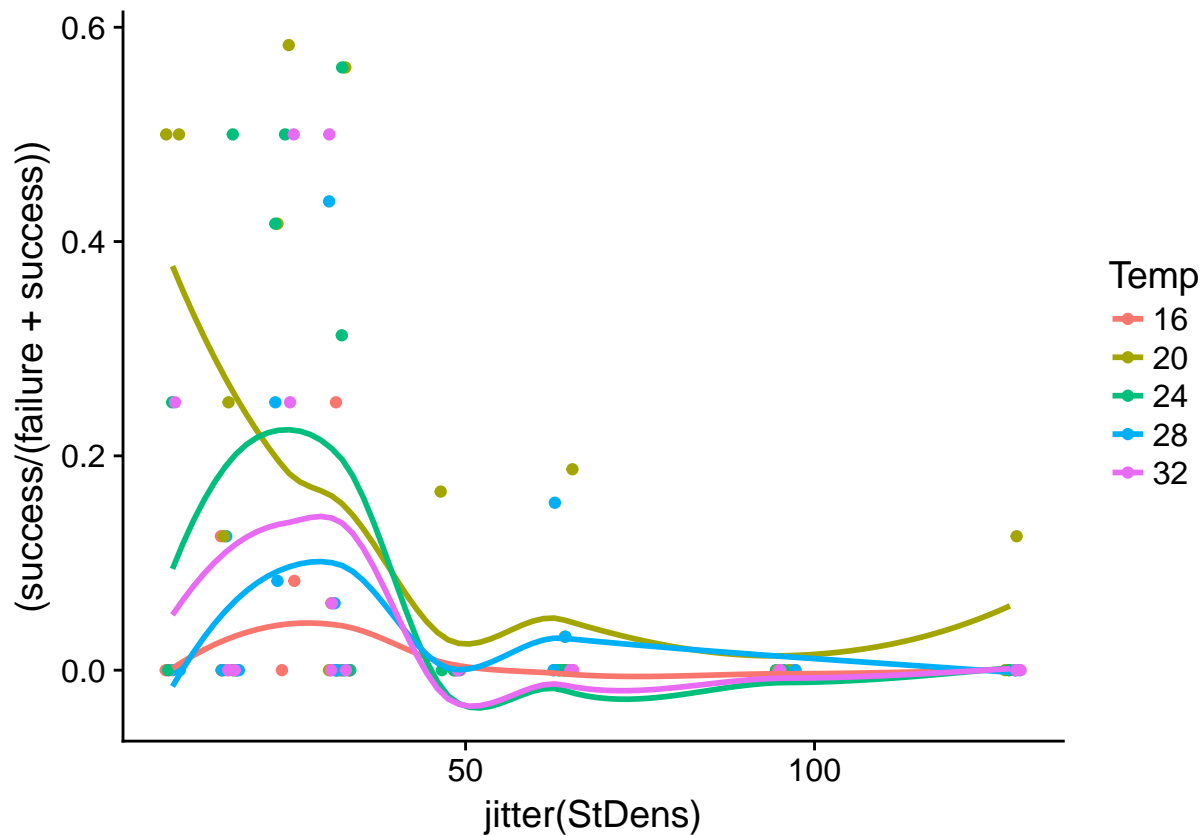
```
  facet_wrap(~TempNum, ncol = 5) +
```

```
xlab("Stephensi Density") +
ylab("Aegypti Density")
```

## Stephensi

```
#stephensi
stSurvival <- emergenceData %>%
  filter(Species == "Stephensi" & StDens != 0 & Sex == "Female") %>%
  group_by(Replicate, Temp, TempNum, AeDens, StDens, Ratio) %>%
  summarise(success = sum(Number, na.rm = T)) %>%
  mutate(failure = (StDens/2) - success) %>%
  ungroup() %>%
  #rescale predictor variables
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T)))
#for when more than 50% were female
stSurvival$failure[stSurvival$failure<0] <- 0

ggplot(data = stSurvival, aes(y = (success/(failure+success))))+
  geom_point(aes(x = jitter(StDens), color = Temp))+
  geom_smooth(method="loess", aes(color = Temp, x = StDens), se = F)
```



Stephensi model selection

```

m0 <- glmer(cbind(success, failure) ~ 1 + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m1 <- glmer(cbind(success, failure) ~ StDensScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m2 <- glmer(cbind(success, failure) ~ AeDensScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m3 <- glmer(cbind(success, failure) ~ AeDensScale + StDensScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m4 <- glmer(cbind(success, failure) ~ StDensScale + TempScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m5 <- glmer(cbind(success, failure) ~ AeDensScale + StDensScale + TempScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m6 <- glmer(cbind(success, failure) ~ poly(AeDensScale,2) + TempScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m7 <- glmer(cbind(success, failure) ~ AeDensScale + TempScale + poly(StDensScale,2) + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

m8 <- glmer(cbind(success, failure) ~ poly(StDensScale,2) + AeDensScale + (1|Replicate),
            data = stSurvival,
            family = binomial(link = "logit"))

modelSummary <- cbind(model = c("m0", "m1", "m2", "m3", "m4", "m5", "m6", "m7", "m8"),
                      do.call(rbind, lapply(list(m0, m1, m2, m3, m4, m5, m6, m7, m8), broom::glance)),
                      AICc = AICc(m0, m1, m2, m3, m4, m5, m6, m7, m8),
                      AICweights = Weights(AIC(m0, m1, m2, m3, m4, m5, m6, m7, m8)))

modelSummary

```

##	model	sigma	logLik	AIC	BIC	deviance	df.residual	AICc.df	
##	m0	m0	1	-297.6846	599.3692	604.9274	504.6813	117	2
##	m1	m1	1	-237.9006	481.8011	490.1385	385.1724	116	3
##	m2	m2	1	-256.1250	518.2499	526.5873	421.6337	116	3
##	m3	m3	1	-149.5923	307.1846	318.3011	208.3711	115	4
##	m4	m4	1	-237.8882	483.7763	494.8928	385.1481	115	4
##	m5	m5	1	-149.5698	309.1396	323.0352	208.3260	114	5
##	m6	m6	1	-225.8552	461.7105	475.6061	361.1321	114	5
##	m7	m7	1	-138.5947	289.1894	305.8641	186.3157	113	6
##	m8	m8	1	-138.6183	287.2366	301.1323	186.3631	114	5
##	AICc.AICc			AICweights					
##	m0			599.4726	1.208987e-68				

```
## m1 482.0098 4.092674e-43
## m2 518.4586 4.980202e-51
## m3 307.5354 3.384615e-05
## m4 484.1272 1.524372e-43
## m5 309.6705 1.273459e-05
## m6 462.2415 9.432540e-39
## m7 289.9394 2.736021e-01
## m8 287.7676 7.263513e-01
```

```
StephSurvivalModel <- m8
```

For stephensi, model m8 is the best fit (survival ~ AeDens + StDens^2). Temperature is not significant in m7, which has a similar AIC as m8.

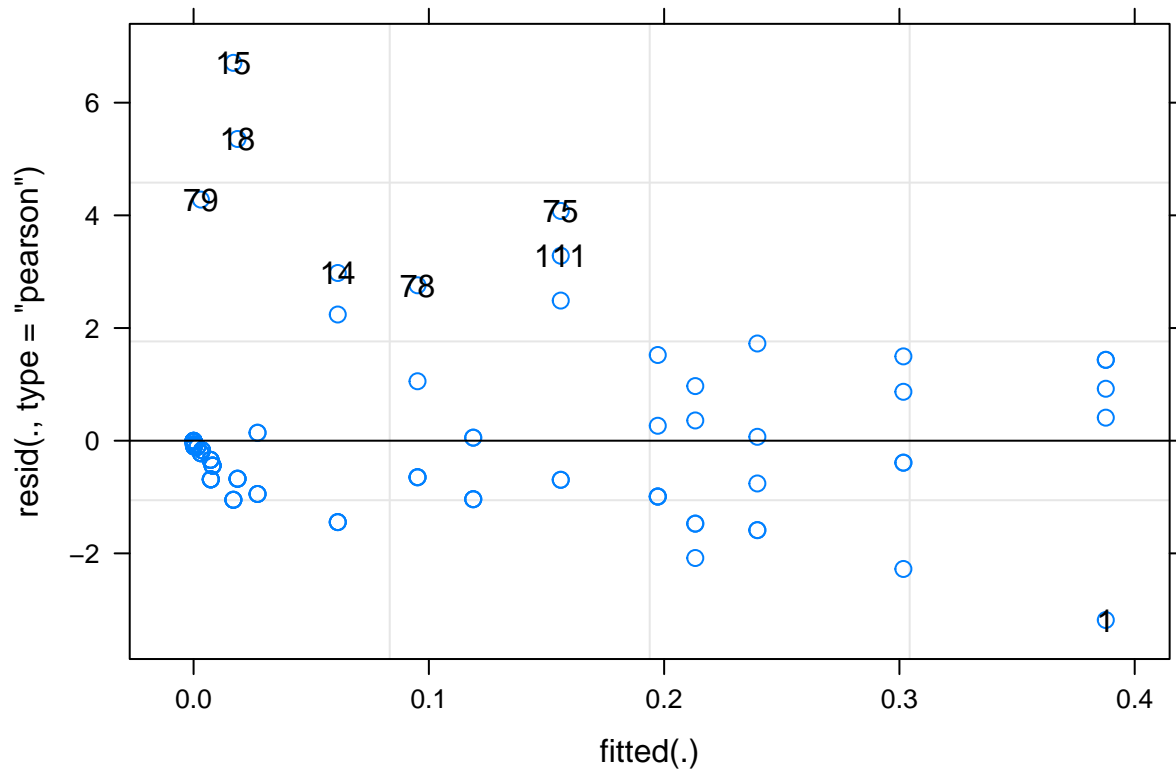
```
summary(StephSurvivalModel)
```

```
## Generalized linear mixed model fit by maximum likelihood (Laplace
## Approximation) [glmerMod]
## Family: binomial ( logit )
## Formula: cbind(success, failure) ~ poly(StDensScale, 2) + AeDensScale +
## (1 | Replicate)
## Data: stSurvival
##
##      AIC      BIC    logLik deviance df.resid
##    287.2    301.1   -138.6    277.2     114
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.1830 -0.6864 -0.1111 -0.0026  6.7071
##
## Random effects:
##  Groups      Name      Variance Std.Dev.
## Replicate (Intercept) 0.202    0.4494
## Number of obs: 119, groups: Replicate, 2
##
## Fixed effects:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)      -1.4190     0.3462  -4.098 4.16e-05 ***
## poly(StDensScale, 2)1 -19.6742     1.6183 -12.157 < 2e-16 ***
## poly(StDensScale, 2)2  6.9151     1.5378  4.497 6.90e-06 ***
## AeDensScale       -5.5629     0.6991 -7.957 1.76e-15 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) p(SDS,2)1 p(SDS,2)2
## ply(SDS,2)1 -0.090
## ply(SDS,2)2  0.118 -0.460
## AeDensScale -0.239  0.603  -0.557
```

```
confint(StephSurvivalModel)
```

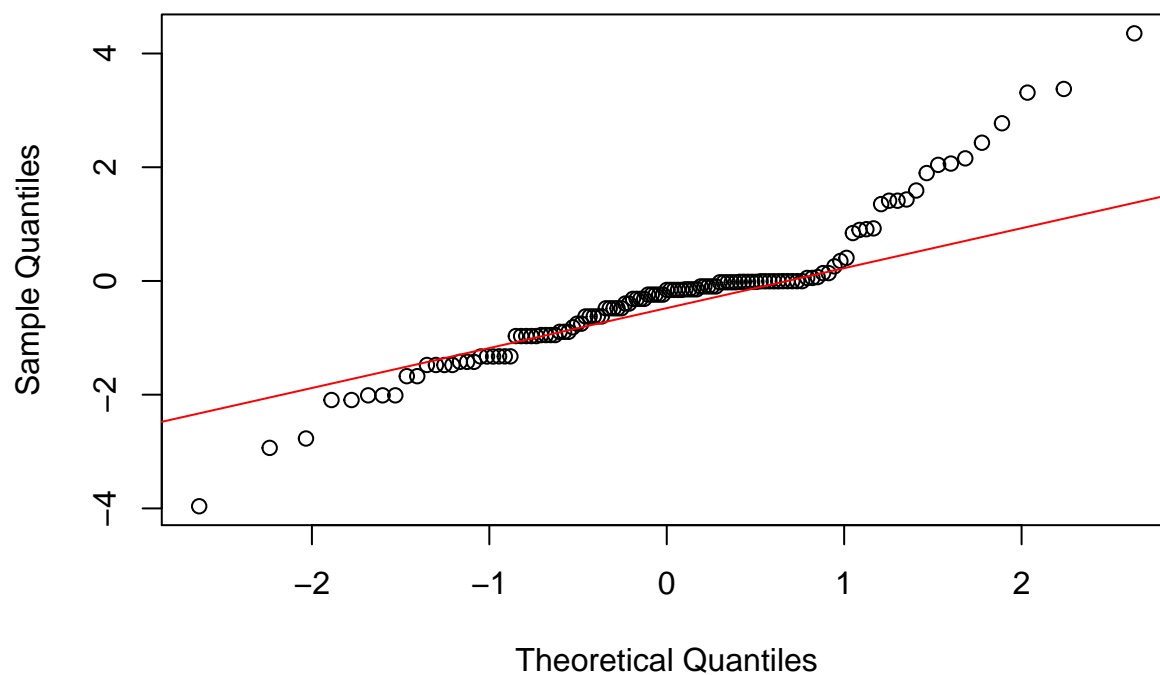
```
## Computing profile confidence intervals ...
##
##              2.5 %      97.5 %
## .sig01          0.1681237  1.9825641
## (Intercept)     -2.5813812 -0.2776183
```

```
## poly(StDensScale, 2)1 -23.0023494 -16.6240987
## poly(StDensScale, 2)2  3.9850359  10.0771246
## AeDensScale          -7.0354834  -4.2887939
plot(StephSurvivalModel, id = 0.01, idLabels=~.obs)
```



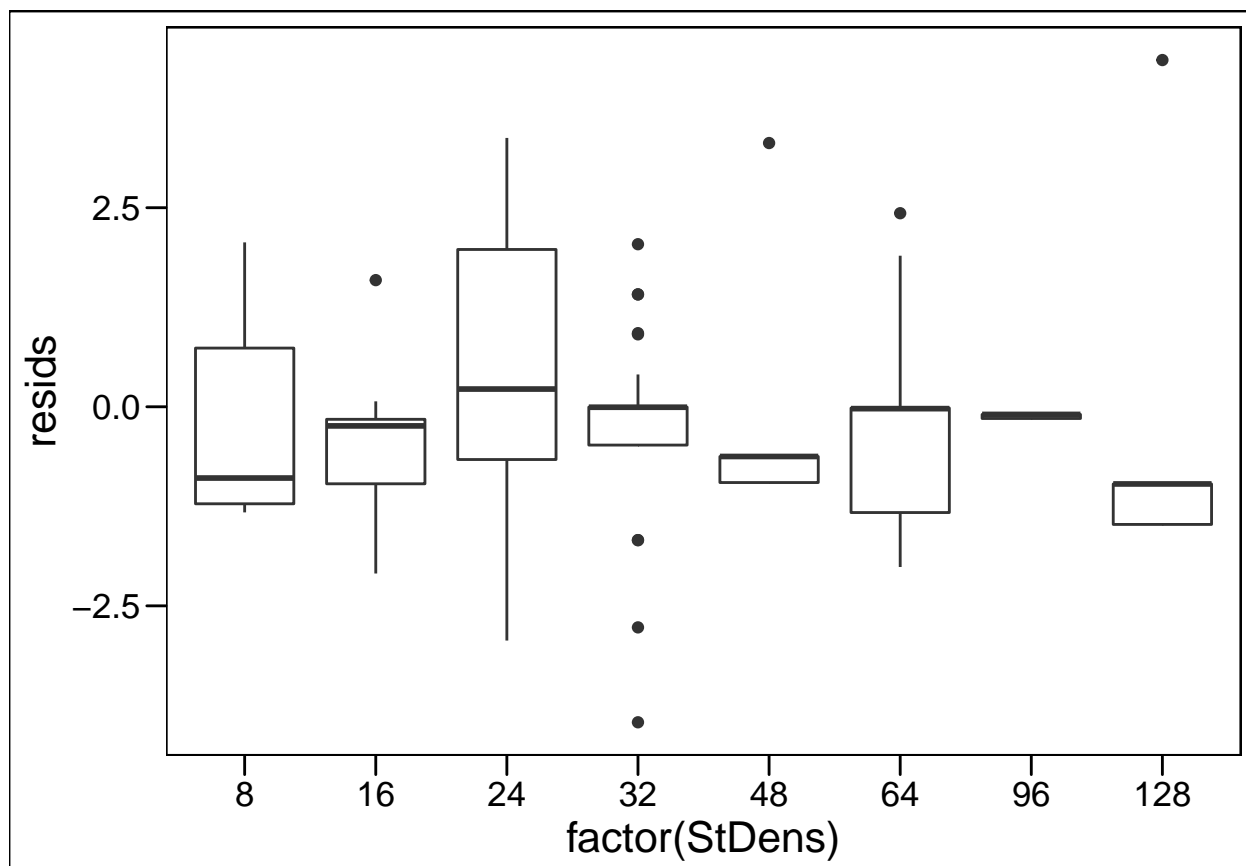
```
qqnorm(resid(StephSurvivalModel))
qqline(resid(StephSurvivalModel), col = "red")
```

## Normal Q-Q Plot

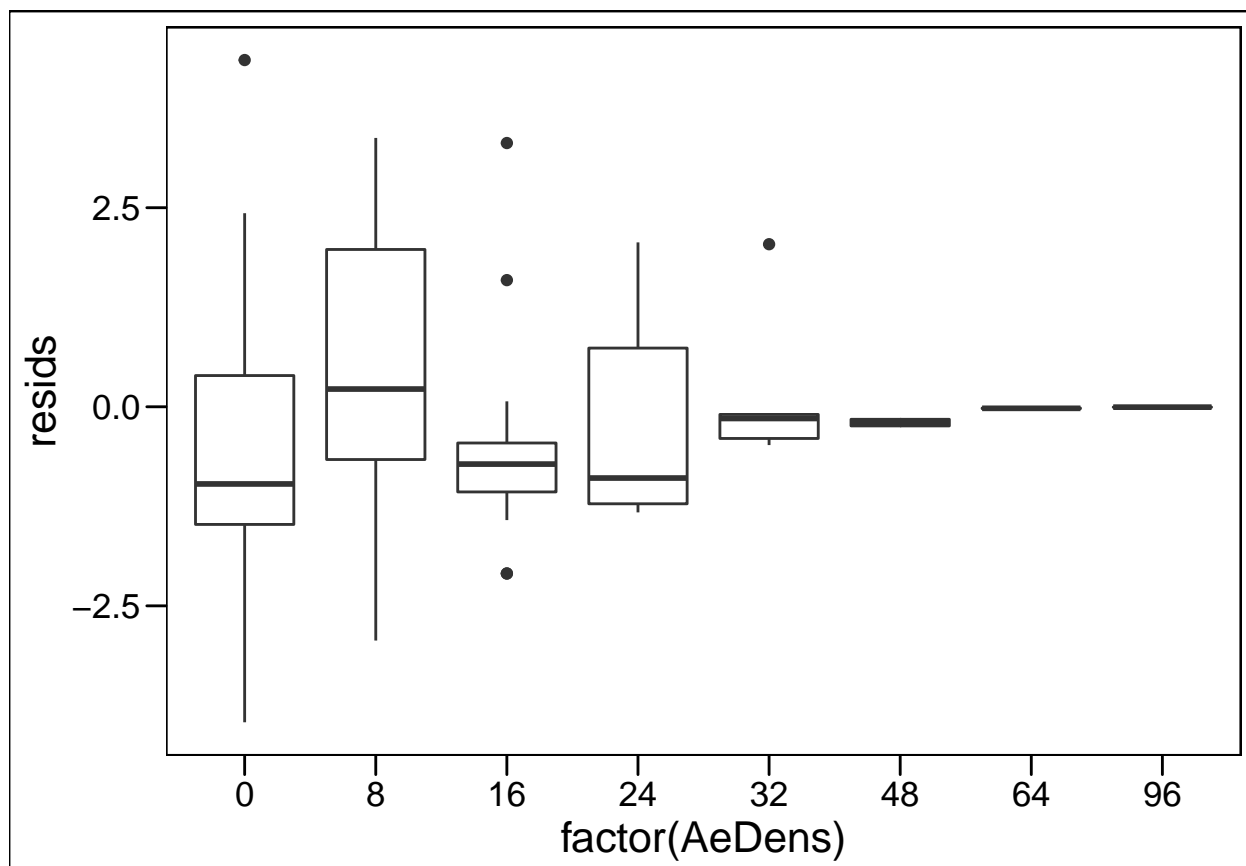


```
stSurvival$preds <- predict(StephSurvivalModel)
stSurvival$resids <- resid(StephSurvivalModel)

ggplot(data = stSurvival, aes(x=factor(StDens), y = resids))+
  geom_boxplot() +
  geom_line(aes(y=0), color="red") +
  theme_base()
```

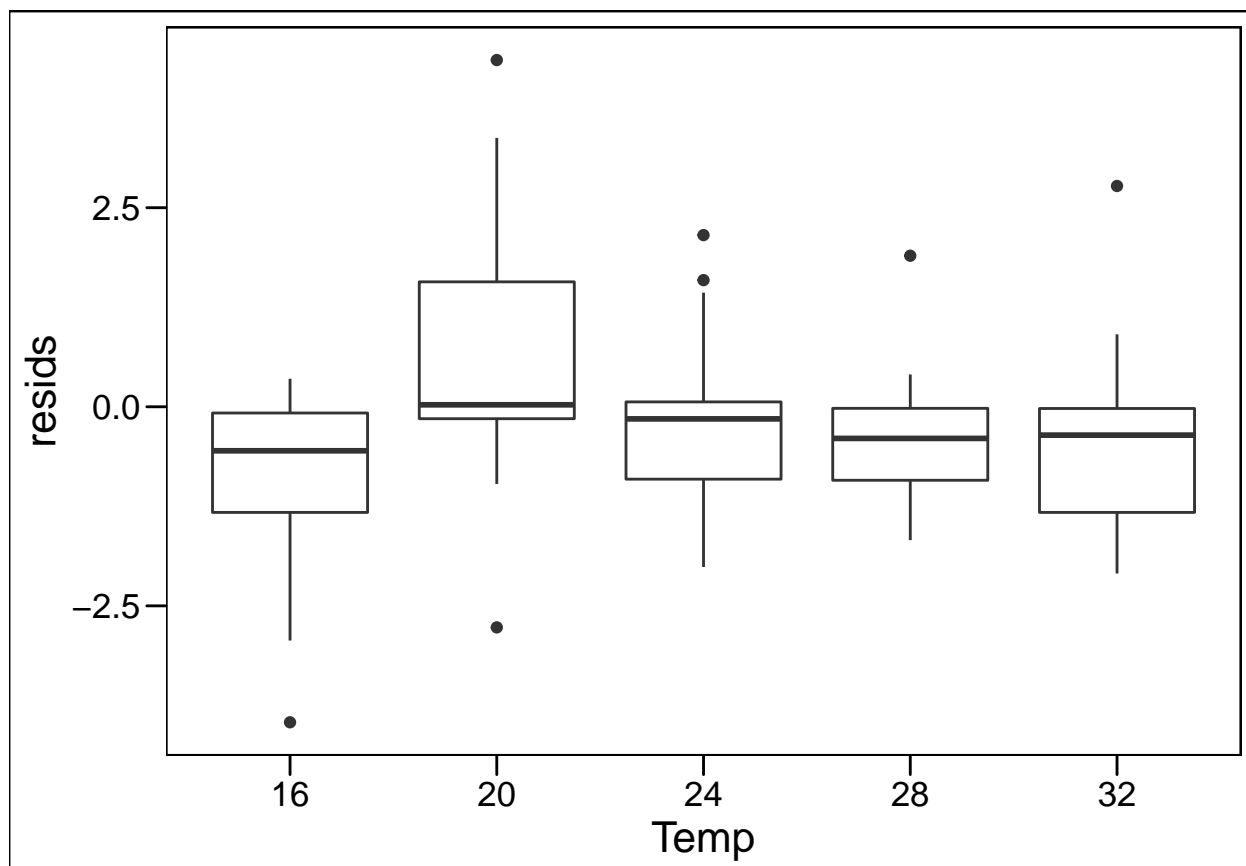


```
ggplot(data = stSurvival, aes(x=factor(AeDens), y = resids))+
  geom_boxplot() +
  theme_base()
```

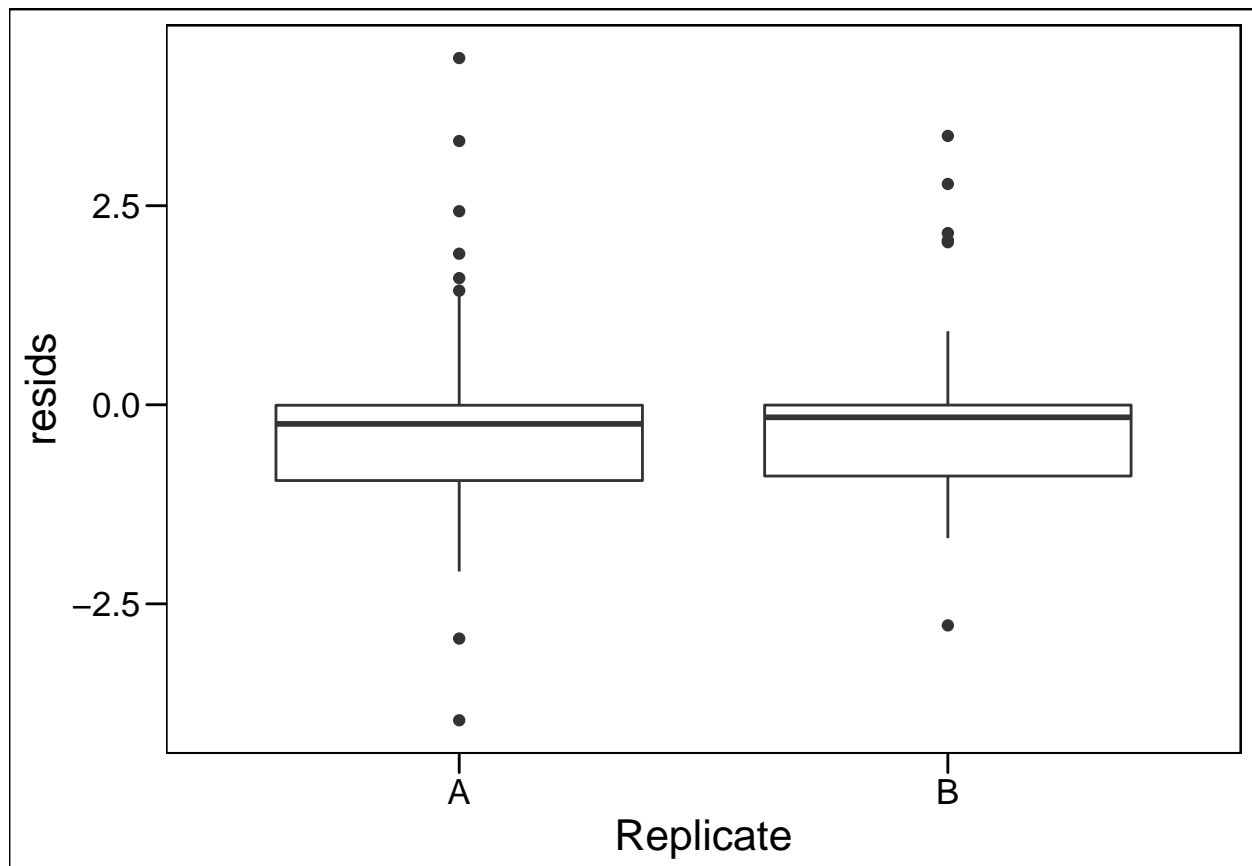


```
ggplot(data = stSurvival, aes(x=Temp, y = resids))+  
  geom_boxplot() +  
  theme_base()
```





```
ggplot(data = stSurvival, aes(x=Replicate, y = resids))+  
  geom_boxplot() +  
  theme_base()
```



The residuals on this model look very bad.

Now we can predict over the response surface.

```
#heatmap plots
newData <- expand.grid(AeDens=seq(0,128, by=2), StDens=seq(0,128, by=2), TempNum=c(16,20,24,28,32), Rep=1:2)
newData <- newData %>%
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T)))

newData$preds <- predict(StephSurvivalModel, type = "response", newdata = newData)
#remove extrapolation outside of measured range
newData$preds[newData$AeDens+newData$StDens>128] <- NA
#get means over replicates to plot
predicted <- newData %>%
  group_by(AeDens, StDens, TempNum) %>%
  summarise(preds = mean(preds))

#plot it
stSurvPlot <- ggplot(predicted, aes(x=StDens, y=AeDens, z=preds))+
  geom_raster(aes(fill=preds))+
  geom_contour(color="gray90", binwidth=0.1)+
  theme_minimal()+
  scale_fill_viridis(name="Prop. Emerged", na.value = "gray90",
    begin = 0, end = 1)+
  facet_wrap(~TempNum, ncol = 5) +
```

```
xlab("Stephensi Density") +
ylab("Aegypti Density")
```

## Fecundity

Split into Two Dataframes. Change the NAs of those that didn't lay to 0.

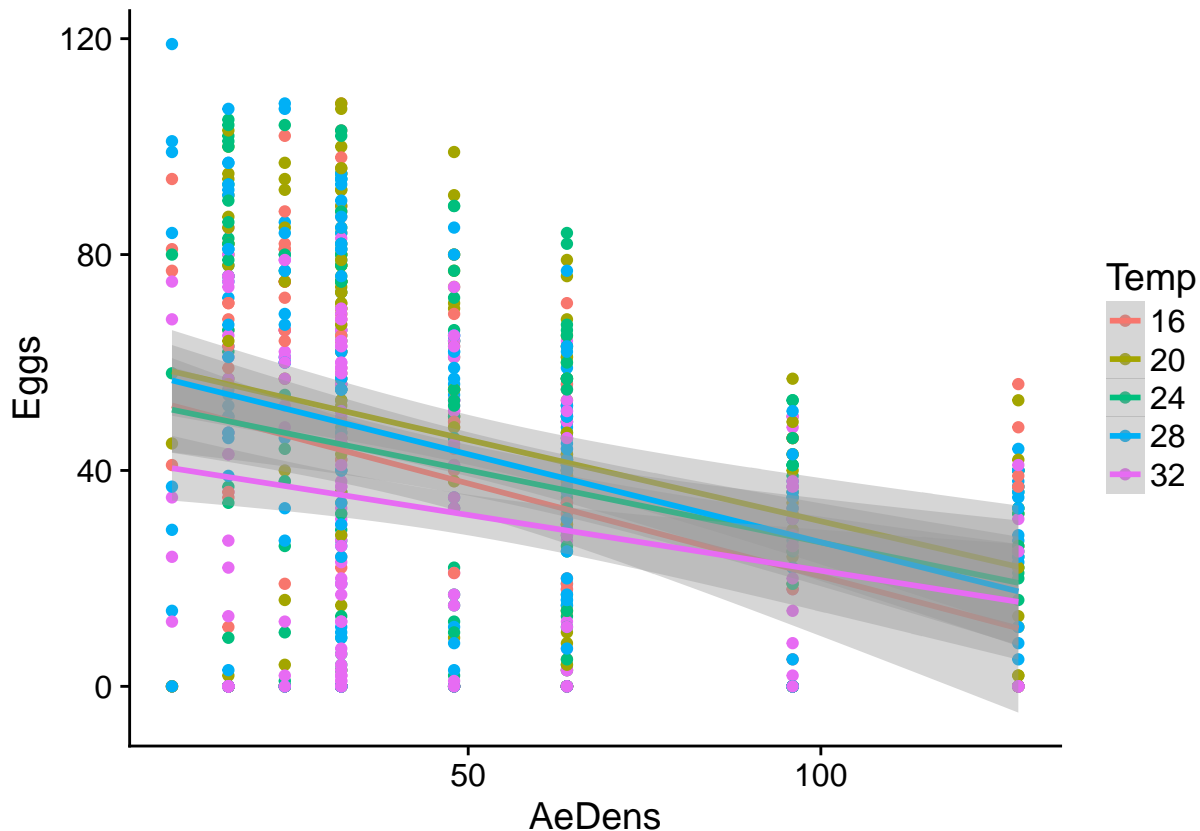
```
aeFec <- dplyr::filter(fecundity, Species == "Aedes")
aeFec$Eggs[is.na(aeFec$Eggs)] <- 0
stFec <- dplyr::filter(fecundity, Species == "Stephensi")
stFec$Eggs[is.na(stFec$Eggs)] <- 0
```

We will use a zero-inflated mixed model here from the `glmmADMB` package because we have many zeros, and this drastically improved model fit during preliminary explorations. Note that these models take a long time to run.

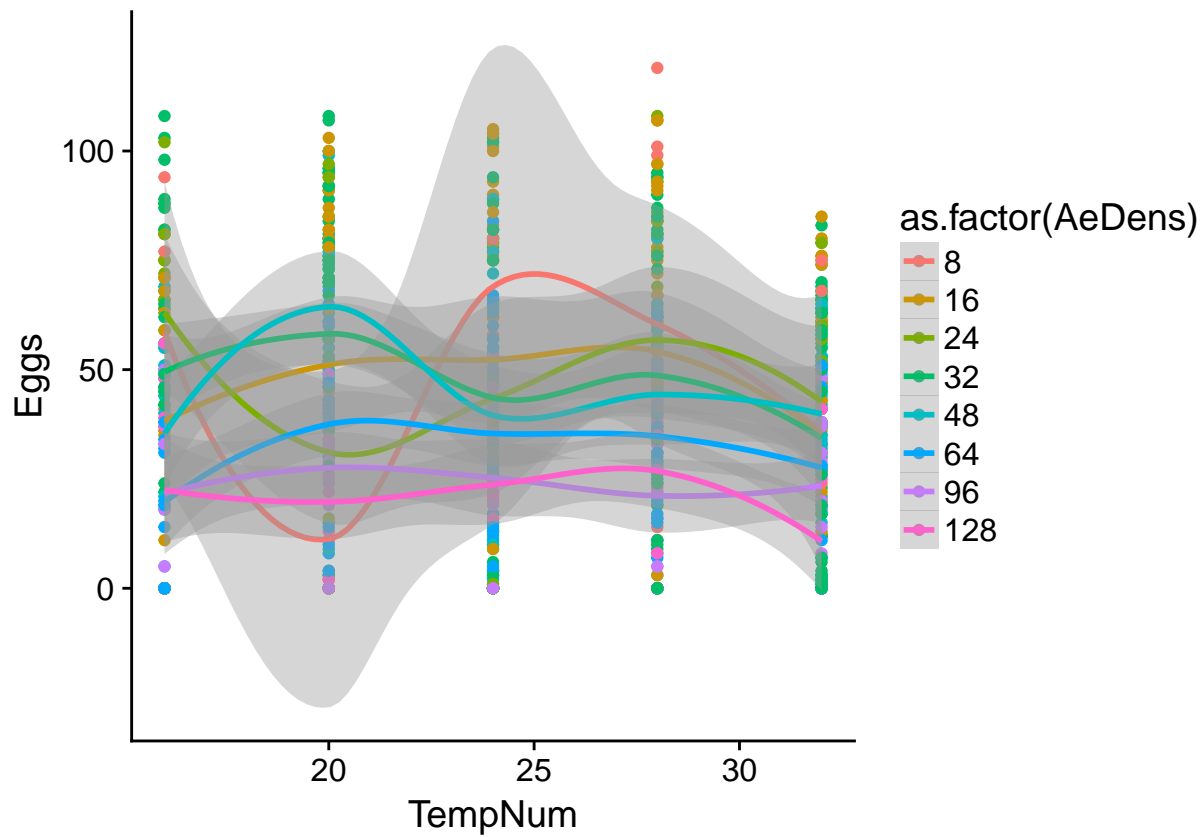
## Aedes

Model Selection

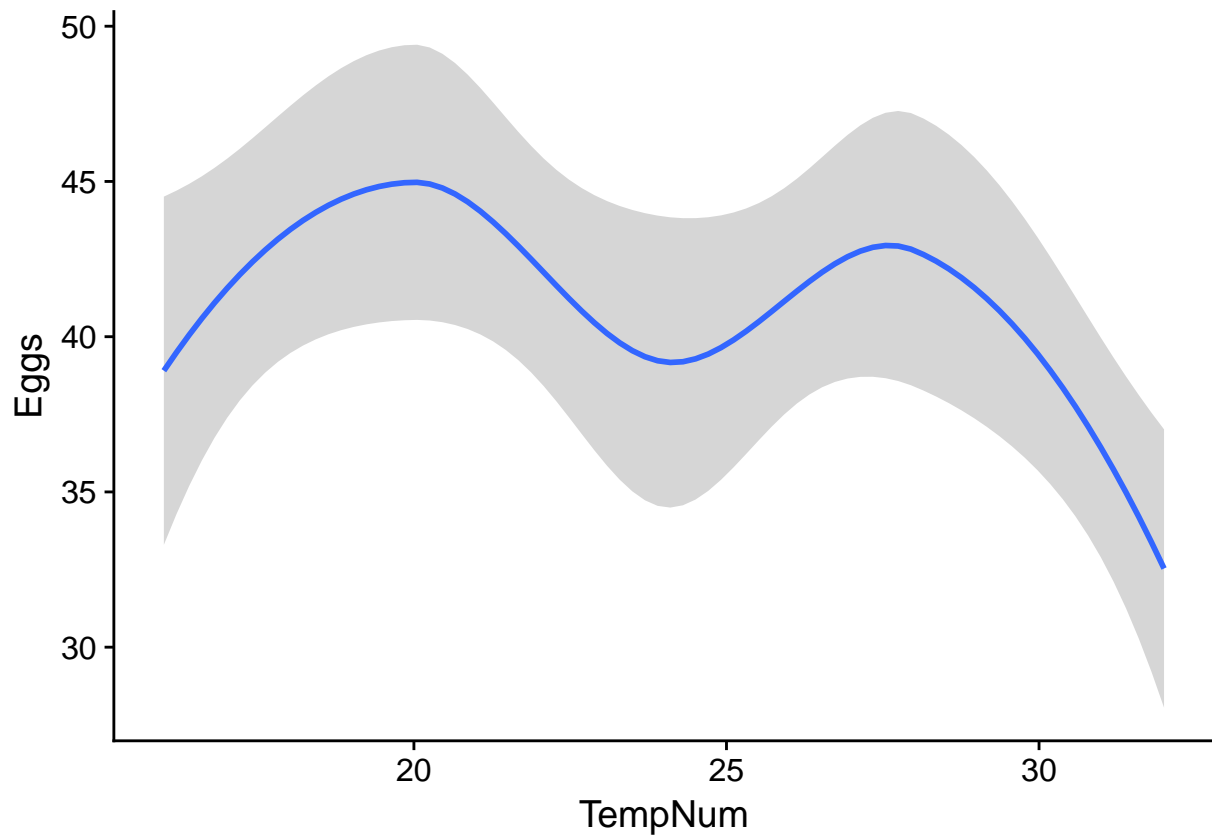
```
ggplot(data = aeFec, aes(y = Eggs, x = AeDens)) +
  geom_point(aes(color = Temp)) +
  geom_smooth(method = "lm", aes(color = Temp))
```



```
ggplot(data = aeFec, aes(y = Eggs, x = TempNum))+
  geom_point(aes(color = as.factor(AeDens)))+
  geom_smooth(method = "loess", aes(color = as.factor(AeDens)))
```



```
ggplot(data = aeFec, aes(y = Eggs, x = TempNum))+
  geom_smooth(method = "loess")
```



```
m0 <- glmmadmb(Eggs ~ 1 + (1|Replicate),
               data = aeFec,
               zeroInflation=TRUE,
               family="nbinom")

m1 <- glmmadmb(Eggs ~ TempNum + (1|Replicate),
               data = aeFec,
               zeroInflation=TRUE,
               family="nbinom")

m2 <- glmmadmb(Eggs ~ AeDens + (1|Replicate),
               data = aeFec,
               zeroInflation=TRUE,
               family="nbinom")

m3 <- glmmadmb(Eggs ~ AeDens + StDens + (1|Replicate),
               data = aeFec,
               zeroInflation=TRUE,
               family="nbinom")

m4 <- glmmadmb(Eggs ~ AeDens + TempNum + (1|Replicate),
               data = aeFec,
               zeroInflation=TRUE,
               family="nbinom")

m5 <- glmmadmb(Eggs ~ AeDens + poly(TempNum,2) + (1|Replicate),
               data = aeFec,
```

```

      zeroInflation=TRUE,
      family="nbinom")

m6 <- glmmadmb(Eggs ~ AeDens*poly(TempNum,2) + (1|Replicate),
  data = aeFec,
  zeroInflation=TRUE,
  family="nbinom")

m7 <- glmmadmb(Eggs ~ AeDens*TempNum + (1|Replicate),
  data = aeFec,
  zeroInflation=TRUE,
  family="nbinom")

modelSummary <- cbind(model = c("m0","m1","m2","m3", "m4", "m5", "m6", "m7"),
  logLik = logLik(m0, m1, m2, m3, m4, m5, m6, m7),
  AIC = AIC(m0, m1, m2, m3, m4, m5, m6, m7),
  AICc = AICc(m0, m1, m2, m3, m4, m5, m6, m7),
  AICweights = Weights(AIC(m0, m1, m2, m3, m4, m5, m6, m7)))

modelSummary

```

##	model	logLik	AIC.df	AIC.AIC	AICc.df	AICc.AICc	AICweights
##	m0	m0 -3559.7	4	7127.40	4	7127.448	1.626996e-28
##	m1	m1 -3559.7	5	7112.68	5	7112.753	2.557371e-25
##	m2	m2 -3559.7	5	7024.64	5	7024.713	3.353026e-06
##	m3	m3 -3559.7	6	7024.24	6	7024.342	4.095395e-06
##	m4	m4 -3559.7	6	7006.02	6	7006.122	3.704406e-02
##	m5	m5 -3559.7	7	7000.52	7	7000.656	5.794665e-01
##	m6	m6 -3559.7	9	7001.44	9	7001.659	3.658077e-01
##	m7	m7 -3559.7	7	7007.50	7	7007.636	1.767423e-02

```
AedesFecundityModel <- m5
```

The best fitting model is m5 (AeDens + TempNum<sup>2</sup>).

```
summary(AedesFecundityModel)
```

```

##
## Call:
## glmmadmb(formula = Eggs ~ AeDens + poly(TempNum, 2) + (1 | Replicate),
##   data = aeFec, family = "nbinom", zeroInflation = TRUE)
##
## AIC: 7000.5
##
## Coefficients:
##               Estimate Std. Error z value Pr(>|z|)
## (Intercept)    4.274073   0.071869   59.47 < 2e-16 ***
## AeDens        -0.008073   0.000699  -11.56 < 2e-16 ***
## poly(TempNum, 2)1 -3.040470   0.653640   -4.65 3.3e-06 ***
## poly(TempNum, 2)2 -1.810872   0.656650   -2.76 0.0058 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Number of observations: total=832, Replicate=2
## Random effect variance(s):
## Warning in .local(x, sigma, ...): 'sigma' and 'rdig' arguments are present

```

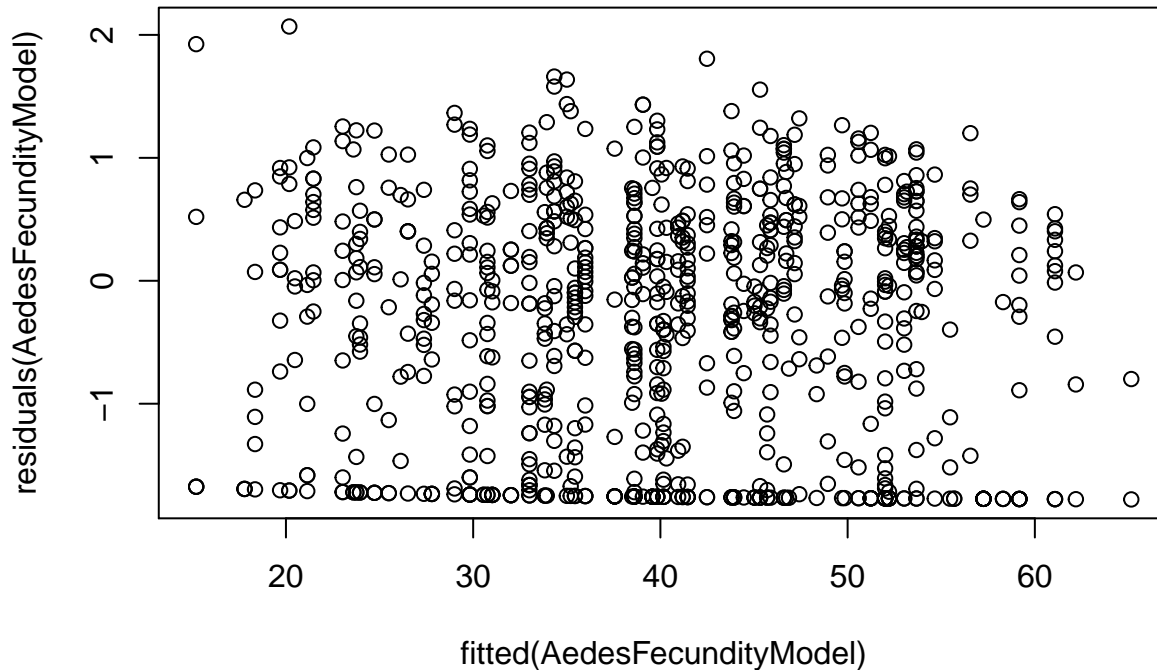
```
## for compatibility only: ignored
## Group=Replicate
##          Variance StdDev
## (Intercept) 0.007013 0.08374
##
## Negative binomial dispersion parameter: 3.2897 (std. err.: 0.19832)
## Zero-inflation: 0.20296 (std. err.: 0.013951 )
##
## Log-likelihood: -3493.26
```

```
confint(AedesFecundityModel)
```

```
##              2.5 %      97.5 %
## (Intercept)   4.13321201  4.414933313
## AeDens        -0.00944218 -0.006703836
## poly(TempNum, 2)1 -4.32158105 -1.759359330
## poly(TempNum, 2)2 -3.09788248 -0.523861782
```

```
#plot(AedesFecundityModel, id = 0.01, idLabels=~.obs)
```

```
plot(fitted(AedesFecundityModel), residuals(AedesFecundityModel))
```



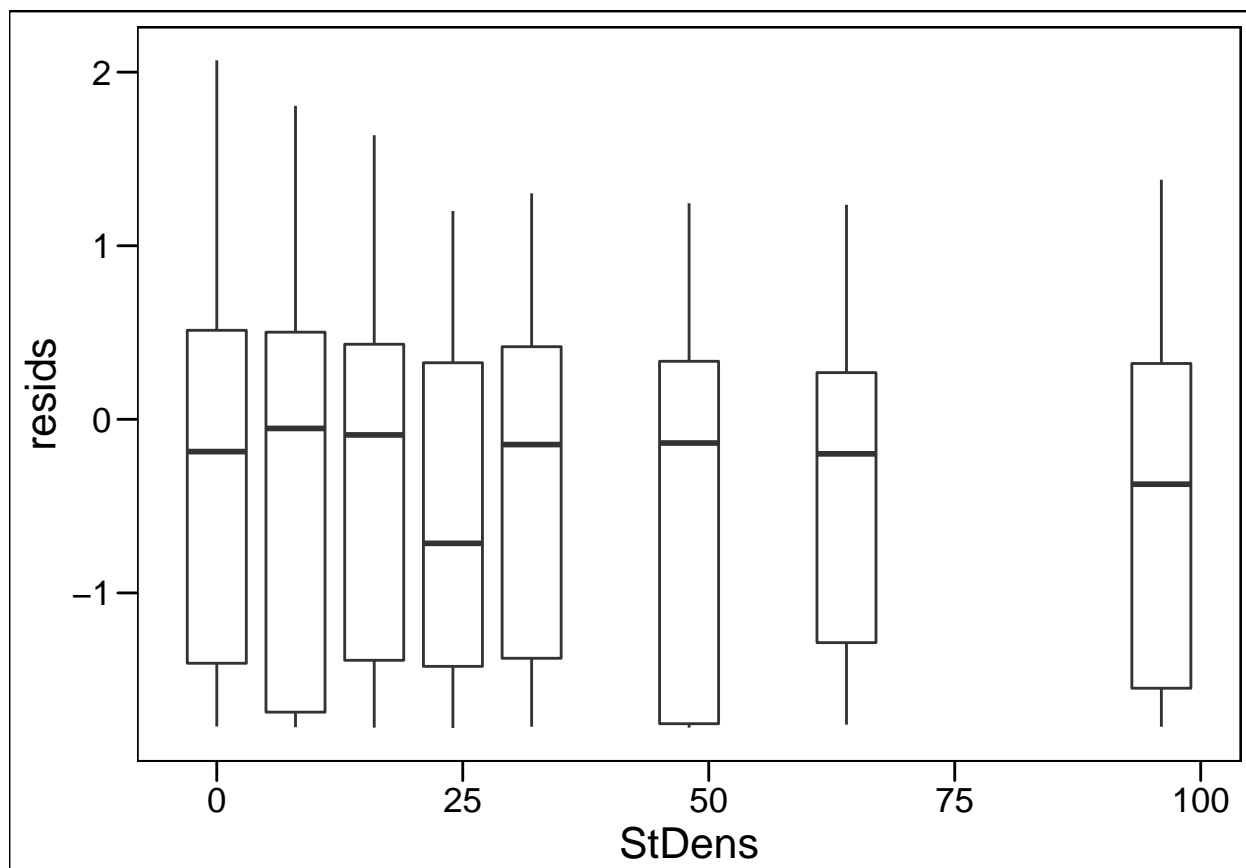
```
# qqnorm(resid(AedesFecundityModel))
```

```
# qqline(resid(AedesFecundityModel), col = "red")
```

```
aeFec$preds <- predict(AedesFecundityModel)
```

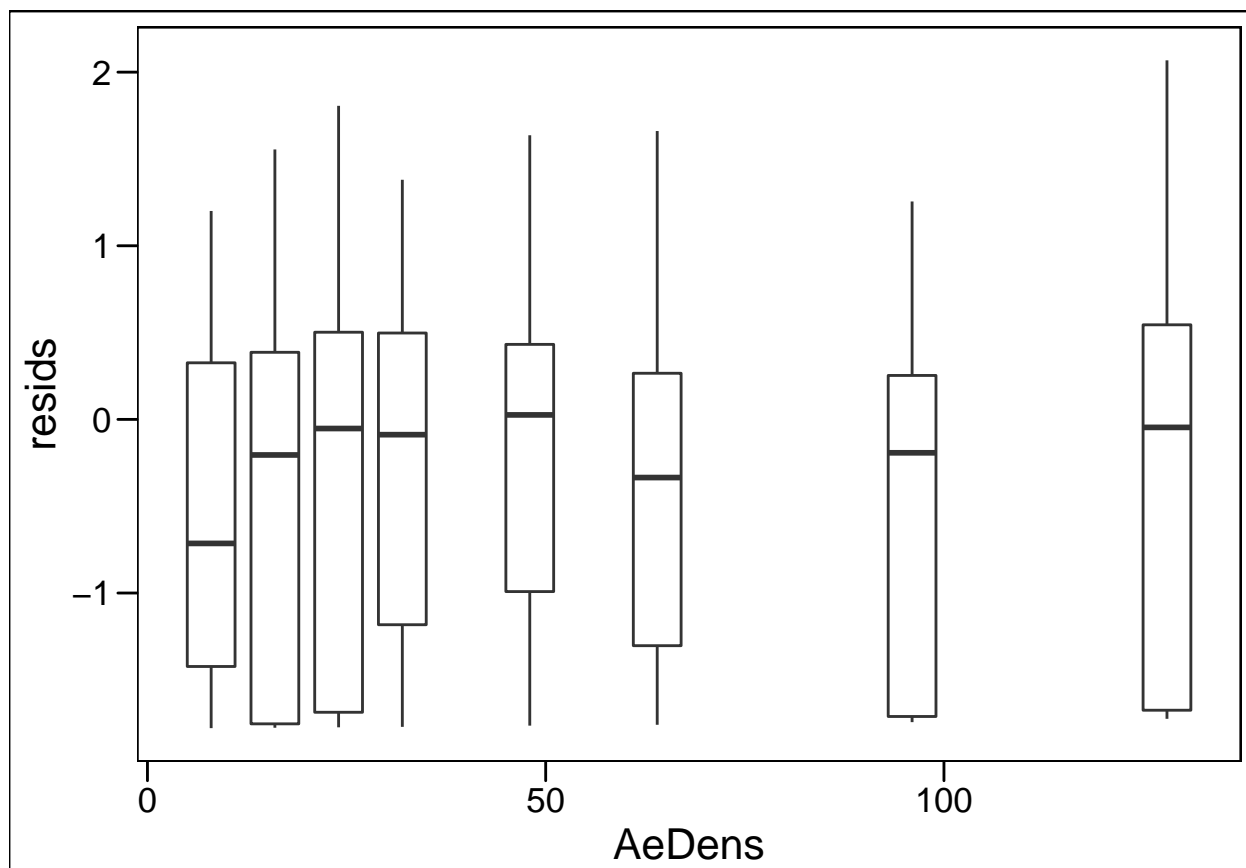
```
aeFec$resids <- resid(AedesFecundityModel)
```

```
ggplot(data = aeFec, aes(x = StDens, y = resids, group=StDens))+
  geom_boxplot() +
  theme_base()
```

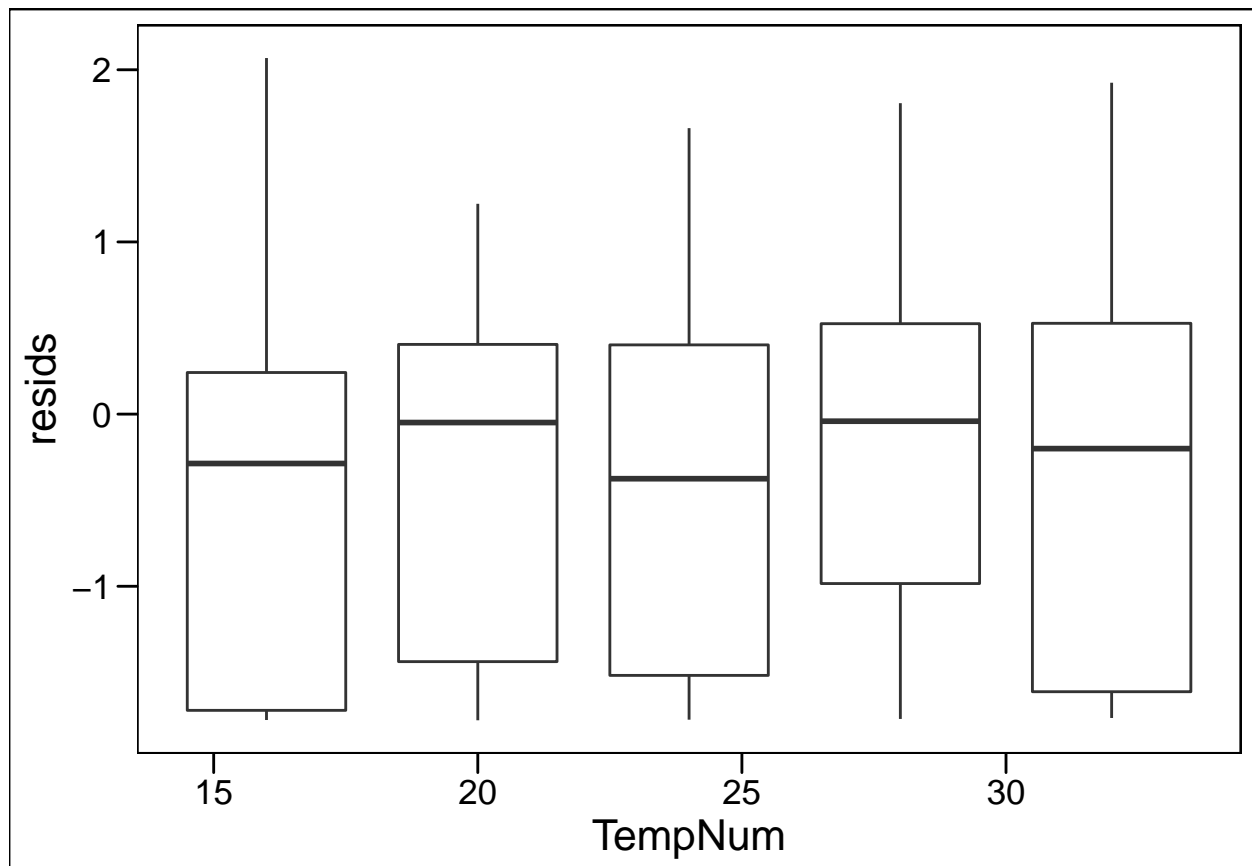


```
ggplot(data = aeFec, aes(x = AeDens, y = resids, group = AeDens))+  
  geom_boxplot() +  
  theme_base()
```





```
ggplot(data = aeFec, aes(x = TempNum, y = resids, group = TempNum))+  
  geom_boxplot() +  
  theme_base()
```



Create heatmaps of the eggs. If there are only two covariates, can do a 3D surface plot.

```
#heatmap plots
newData <- expand.grid(AeDens=seq(0,128, by=2), StDens=seq(0,128, by=2), TempNum=c(16,20,24,28,32), Rep=1:3)
newData <- newData %>%
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T)))

newData$preds <- predict(AedesFecundityModel, type = "response", newdata = newData)
#remove extrapolation outside of measured range
newData$preds[newData$AeDens+newData$StDens>128] <- NA
#get means over replicates to plot
predicted <- newData %>%
  group_by(TempNum, AeDens) %>%
  summarise(preds = mean(preds, na.rm = T)) %>%
  ungroup()

aeFecPlot<- ggplot(predicted, aes(x=TempNum, y=AeDens, z=preds))+
  geom_raster(aes(fill=preds))+
  geom_contour(color="gray90", binwidth = 10)+
  theme_minimal()+
  scale_fill_viridis(name="Number of Eggs Laid")+
  #facet_wrap(~TempNum, ncol = 5) +
  xlab("Temperature(C)") +
  ylab("Aegypti Density") +
  coord_cartesian(xlim = c(16, 32))
```

## Stephensi

There are too many zeros in this for the zero-inflated model to work, so we try a hurdle. We end up dropping the random effect of replicate because the variance was so low.

Model Selection

```
m0 <- pscl::hurdle(Eggs ~ 1,
                  data = stFec,
                  dist = "negbin")

m1 <- hurdle(Eggs ~ poly(TempNum,2),
            data = stFec,
            dist = "negbin")

m2 <- hurdle(Eggs ~ AeDens,
            data = stFec,
            dist = "negbin")

m3 <- hurdle(Eggs ~ StDens,
            data = stFec,
            dist = "negbin")

m4 <- hurdle(Eggs ~ TempNum,
            data = stFec,
            dist = "negbin")

modelSummary <- cbind(model = c("m0", "m1", "m2", "m3", "m4"),
                      AICc = AICc(m0, m1, m2, m3, m4),
                      AICweights = Weights(AIC(m0, m1, m2, m3, m4)))

modelSummary
```

```
##      model AICc.df AICc.AICc AICweights
## m0      m0        3  329.4214 0.40656754
## m1      m1        7  331.9014 0.20123954
## m2      m2        5  333.4822 0.06617691
## m3      m3        5  330.7322 0.26173239
## m4      m4        5  333.5403 0.06428362
```

```
StephensiFecundityModel <- m0
```

The best fitting model is the null model. None of these factors affect *Stephensi* fecundity.

```
summary(StephensiFecundityModel)
```

```
##
## Call:
## pscl::hurdle(formula = Eggs ~ 1, data = stFec, dist = "negbin")
##
## Pearson residuals:
##      Min      1Q  Median      3Q      Max
## -0.5131 -0.5131 -0.5131 -0.3769  3.1208
##
## Count model coefficients (truncated negbin with log link):
```

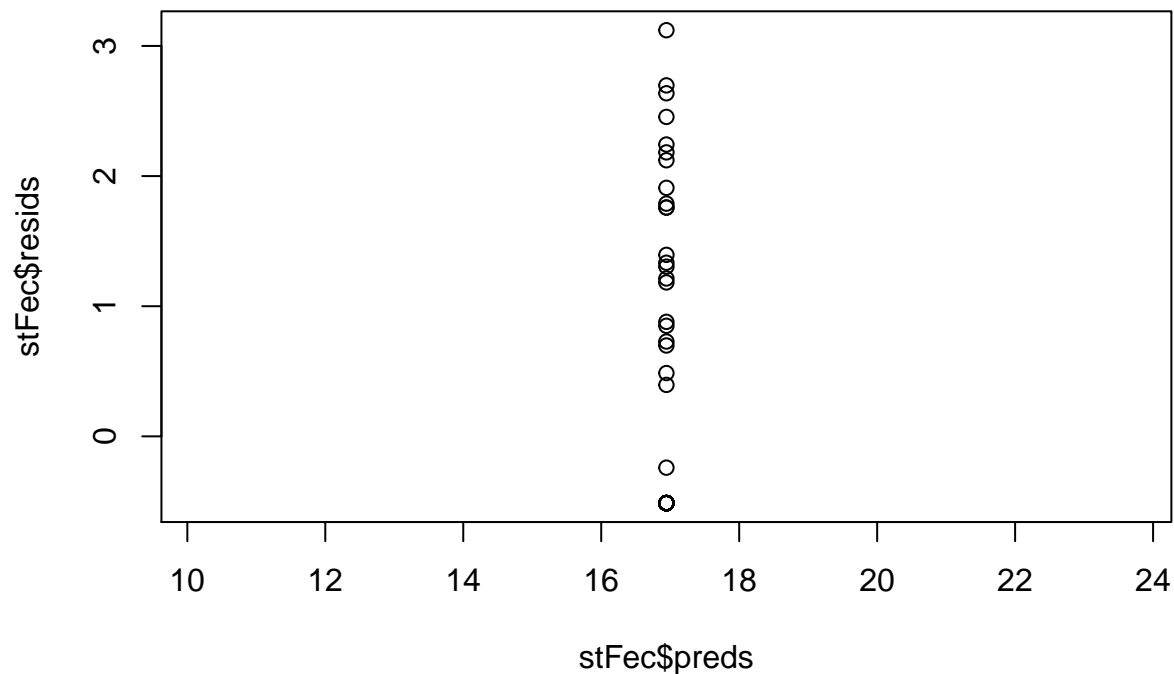
```
##           Estimate Std. Error z value Pr(>|z|)
## (Intercept)  4.20534    0.09614   43.74 < 2e-16 ***
## Log(theta)   1.62111    0.31725    5.11 3.22e-07 ***
## Zero hurdle model coefficients (binomial with logit link):
##           Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -1.0840     0.2412  -4.494 6.99e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Theta: count = 5.0587
## Number of iterations in BFGS optimization: 18
## Log-likelihood: -161.6 on 3 Df
```

```
confint(StephensiFecundityModel)
```

```
##           2.5 %      97.5 %
## count_(Intercept)  4.016905  4.3937752
## zero_(Intercept)  -1.556784 -0.6112429
```

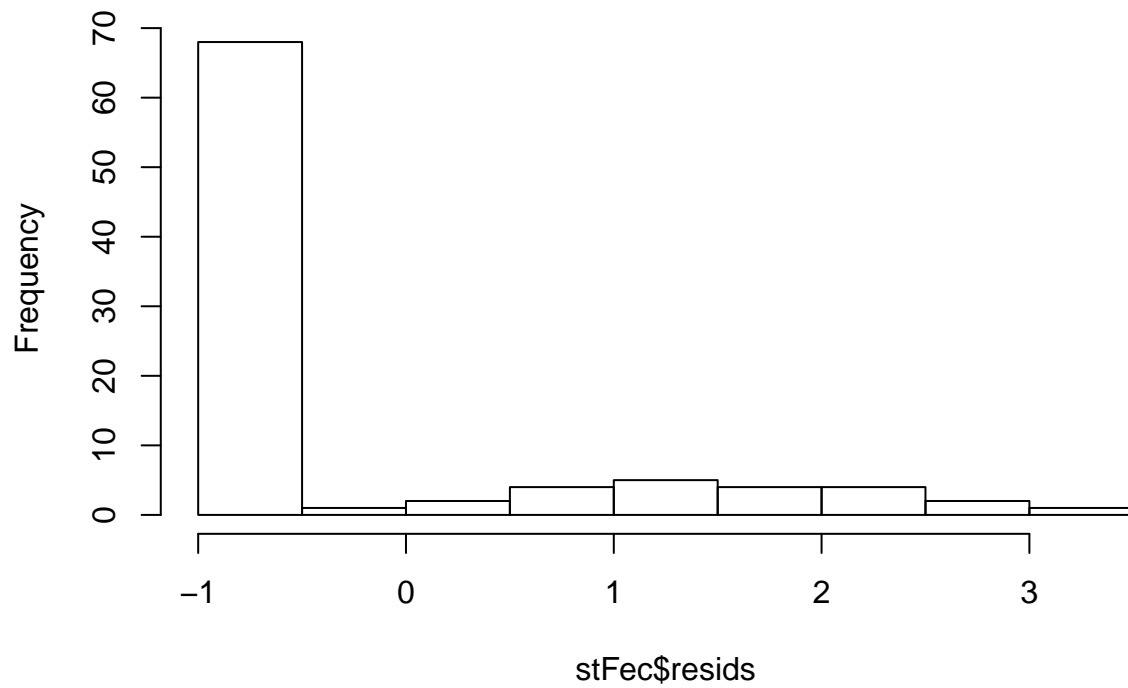
```
stFec$preds <- fitted(StephensiFecundityModel)
stFec$resids <- resid(StephensiFecundityModel)
```

```
plot(stFec$preds, stFec$resids)
```

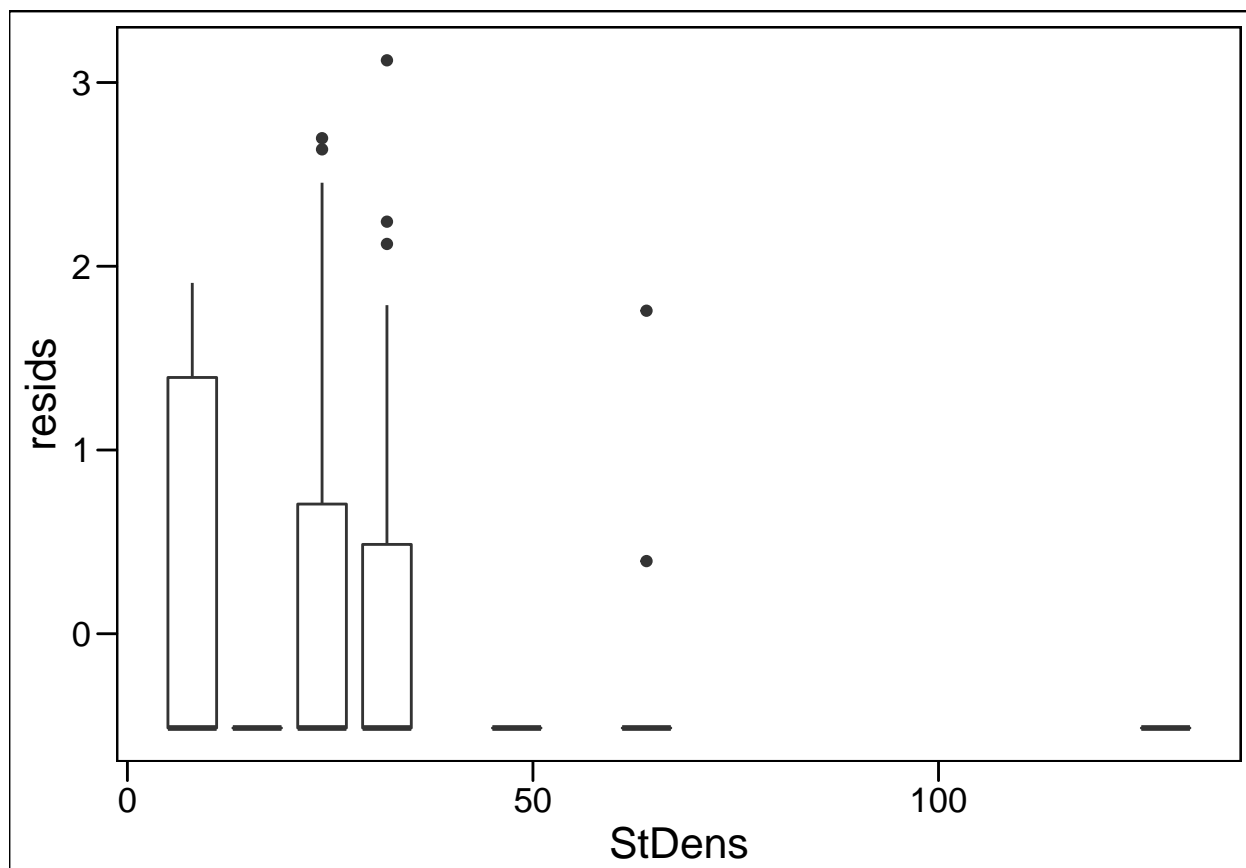


```
hist(stFec$resids)
```

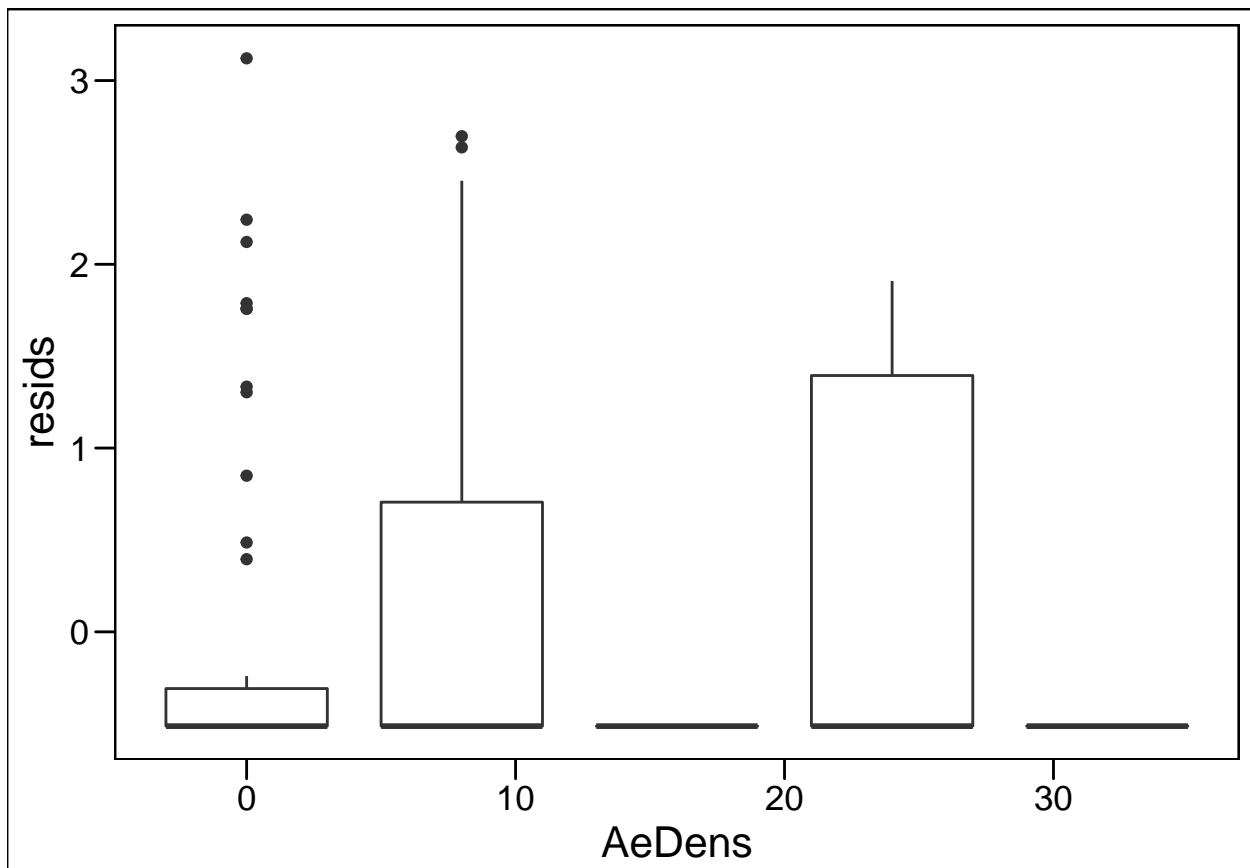
**Histogram of stFec\$resids**



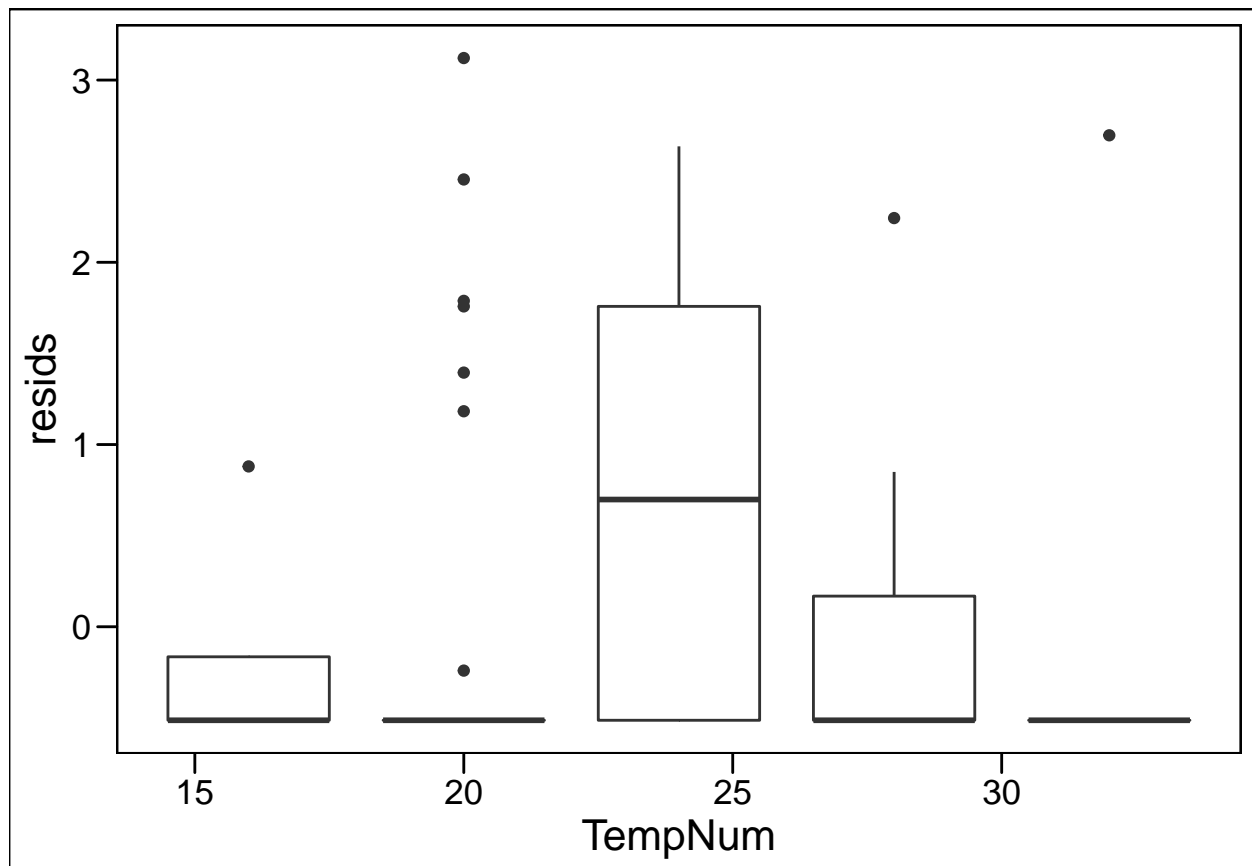
```
ggplot(data = stFec, aes(x = StDens, y = resids, group = StDens))+  
  geom_boxplot() +  
  theme_base()
```



```
ggplot(data = stFec, aes(x = AeDens, y = resids, group = AeDens))+
  geom_boxplot() +
  theme_base()
```



```
ggplot(data = stFec, aes(x=TempNum, y = resids, group = TempNum))+  
  geom_boxplot() +  
  theme_base()
```



## Growth Rate

Growth rate calculated via Sugihara based on raw data.

### Aedes

Calculate growth rate. Using raw data except for fecundity (since this was only estimated from a subset). Fecundity is estimated using models above. In the case of *stephensi*, it is just the mean across all treatments, since none of our covariates were significant.

```
# only need female emergence
GrowthAedes <- emergenceData %>%
  filter(Species == "Aedes" & Sex == "Female") %>%
  #assume 50% female
  mutate(NO = AeDens/2) %>%
  rename(x = Day, Ax = Number) %>%
  #don't calculate for ones that had no aedes to begin with
  filter(AeDens>0)

#add in predicted fecundity
GrowthAedes$fwx <- predict(AedesFecundityModel, type = "response", newdata = GrowthAedes)

#calculate overall per capita growth rate
GrowthAedes <- GrowthAedes %>%
```



```

mutate(Axfwx = Ax*fwx, xAxfwx = x*Ax*fwx) %>%
group_by(Replicate, Temp, Ratio, TempNum, AeDens, StDens) %>%
mutate_at(c("Axfwx", "xAxfwx"), sum, na.rm=T) %>%
mutate(D=14) %>%
ungroup() %>%
mutate(r=(log((1/NO)*Axfwx))/(D+(xAxfwx/Axfwx))) %>%
group_by(Replicate, Temp, TempNum, Ratio, AeDens, StDens, Species) %>%
#each row is now a duplicate of the same thing so only need the first one
slice(1) %>%
mutate(lambda=exp(r)) %>%
ungroup() %>%
#rescale predictor variables
mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T))) %>%
#drop jar that was all male
filter(!(Replicate == "A" & Temp == "24" & Ratio == "8:24")) %>%
#drop unnecessary columns
dplyr::select(-x, -Ax, -Sex, -NO, -fwx, -Axfwx, -xAxfwx, -D)

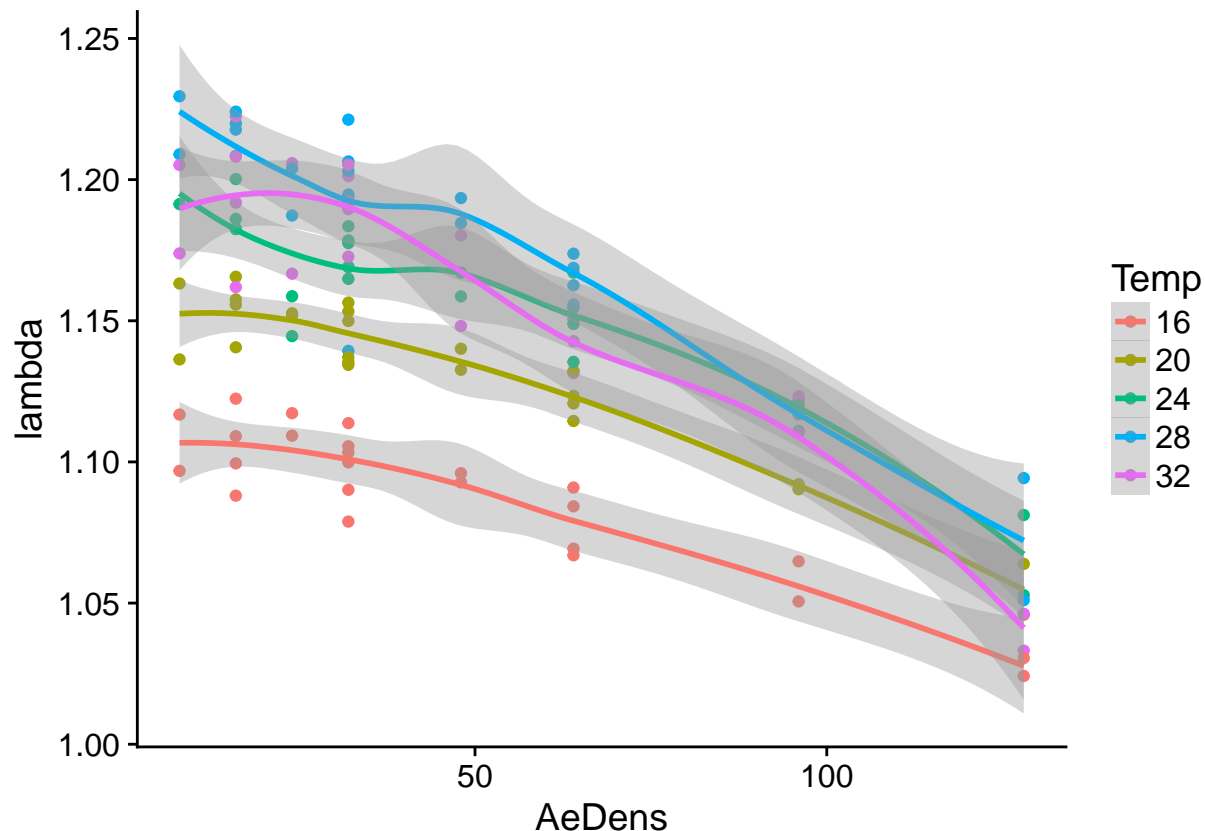
```

```

ggplot(data = GrowthAedes, aes(x = AeDens, y = lambda, color = Temp)) +
  geom_point() +
  geom_smooth()

```

## `geom\_smooth()` using method = 'loess'



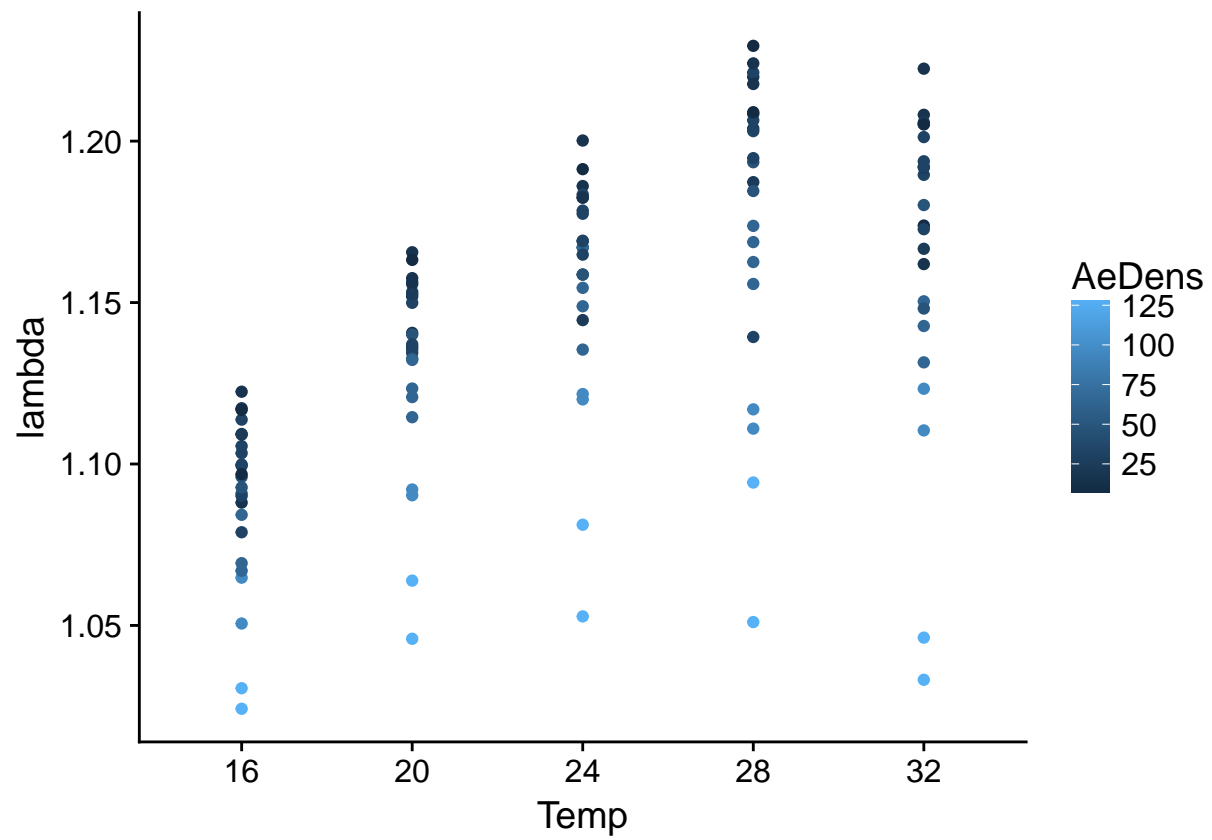
```

ggplot(data = GrowthAedes, aes(x = Temp, y = lambda, color = AeDens)) +
  geom_point() +

```

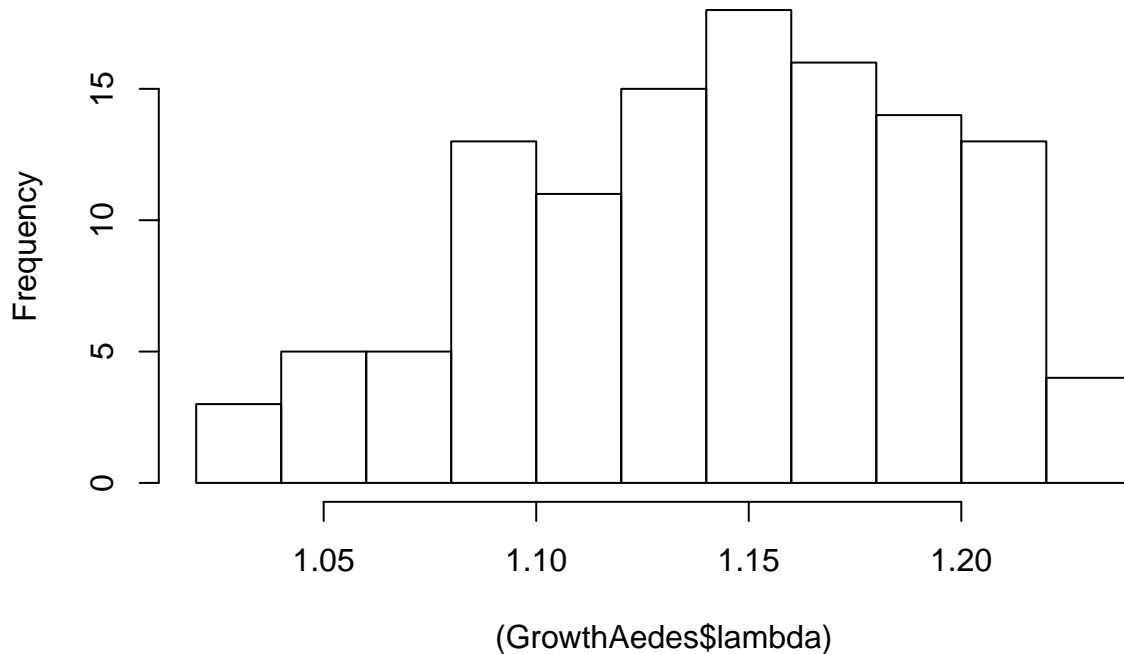
```
geom_smooth()
```

```
## `geom_smooth()` using method = 'loess'
```



```
hist((GrowthAedes$lambda))
```

## Histogram of (GrowthAedes\$lambda)



### Model Selection

```
#model selection
```

```
m0 <- glmer(lambda ~ 1 + (1|Replicate),  
             data = GrowthAedes,  
             family = gaussian)
```

```
## Warning in glmer(lambda ~ 1 + (1 | Replicate), data = GrowthAedes, family  
## = gaussian): calling glmer() with family=gaussian (identity link) as a  
## shortcut to lmer() is deprecated; please call lmer() directly
```

```
m1 <- glmer(lambda ~ poly(TempScale,2) + (1|Replicate),  
             data = GrowthAedes,  
             family = gaussian)
```

```
## Warning in glmer(lambda ~ poly(TempScale, 2) + (1 | Replicate), data =  
## GrowthAedes, : calling glmer() with family=gaussian (identity link) as a  
## shortcut to lmer() is deprecated; please call lmer() directly
```

```
m2 <- glmer(lambda ~ AeDensScale + (1|Replicate),  
             data = GrowthAedes,  
             family = gaussian)
```

```
## Warning in glmer(lambda ~ AeDensScale + (1 | Replicate), data =  
## GrowthAedes, : calling glmer() with family=gaussian (identity link) as a  
## shortcut to lmer() is deprecated; please call lmer() directly
```

```
m3 <- glmer(lambda ~ poly(AeDensScale,2)+ (1|Replicate),  
             data = GrowthAedes,  
             family = gaussian)
```

```
## Warning in glmer(lambda ~ poly(AeDensScale, 2) + (1 | Replicate), data =
```

```

## GrowthAedes, : calling glmer() with family=gaussian (identity link) as a
## shortcut to lmer() is deprecated; please call lmer() directly
m4 <- glmer(lambda ~ AeDensScale + poly(TempScale,2) + (1|Replicate),
            data = GrowthAedes)

## Warning in glmer(lambda ~ AeDensScale + poly(TempScale, 2) + (1 |
## Replicate), : calling glmer() with family=gaussian (identity link) as a
## shortcut to lmer() is deprecated; please call lmer() directly
m5 <- glmer(lambda ~ AeDensScale + poly(TempScale,2) + StDensScale + (1|Replicate),
            data = GrowthAedes,
            family = gaussian)

## Warning in glmer(lambda ~ AeDensScale + poly(TempScale, 2) + StDensScale
## + : calling glmer() with family=gaussian (identity link) as a shortcut to
## lmer() is deprecated; please call lmer() directly
m6 <- glmer(lambda ~ AeDensScale*TempScale+ (1|Replicate),
            data = GrowthAedes,
            family = gaussian)

## Warning in glmer(lambda ~ AeDensScale * TempScale + (1 | Replicate), data
## = GrowthAedes, : calling glmer() with family=gaussian (identity link) as a
## shortcut to lmer() is deprecated; please call lmer() directly
modelSummary <- cbind(model = c("m0","m1","m2","m3", "m4", "m5", "m6"),
                      do.call(rbind, lapply(list(m0, m1, m2, m3, m4, m5, m6), broom::glance)),
                      AICc = AICc(m0, m1, m2, m3, m4, m5, m6),
                      AICweights = Weights(AIC(m0, m1, m2, m3, m4, m5, m6)))
modelSummary

##      model      sigma  logLik      AIC      BIC  deviance df.residual
## m0      m0 0.04923772 182.3091 -358.6182 -350.3317 -373.5690          114
## m1      m1 0.03827006 207.8519 -405.7037 -391.8929 -434.5699          112
## m2      m2 0.03588733 215.2306 -422.4613 -411.4126 -448.5905          113
## m3      m3 0.03560982 216.0652 -422.1303 -408.3195 -451.4288          112
## m4      m4 0.01686122 296.3931 -580.7862 -564.2131 -625.8884          111
## m5      m5 0.01674383 292.4653 -570.9306 -551.5954 -628.4225          110
## m6      m6 0.02122358 269.4684 -526.9367 -510.3637 -573.5566          111
##      AICc.df AICc.AICc  AICweights
## m0          3 -358.4058 5.671444e-49
## m1          5 -405.1632 9.510331e-39
## m2          4 -422.1041 4.140410e-35
## m3          5 -421.5898 3.509018e-35
## m4          6 -580.0226 9.928096e-01
## m5          7 -569.9031 7.190382e-03
## m6          6 -526.1731 2.011861e-12

AedesGrowthModel <- m4

The final model is Aedes + Temp^2.

summary(AedesGrowthModel)

## Linear mixed model fit by REML ['lmerMod']
## Formula: lambda ~ AeDensScale + poly(TempScale, 2) + (1 | Replicate)
##      Data: GrowthAedes
##

```

```

## REML criterion at convergence: -592.8
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -3.1571 -0.4454  0.1016  0.5721  2.0021
##
## Random effects:
##   Groups      Name      Variance Std.Dev.
## Replicate (Intercept) 5.485e-06 0.002342
## Residual              2.843e-04 0.016861
## Number of obs: 117, groups: Replicate, 2
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept)      1.188818   0.003108   382.5
## AeDensScale      -0.057255   0.002631   -21.8
## poly(TempScale, 2)1  0.300785   0.016861    17.8
## poly(TempScale, 2)2 -0.158920   0.016867    -9.4
##
## Correlation of Fixed Effects:
##              (Intr) ADnsSc p(TS,2)1
## AeDensScale -0.682
## ply(TmS,2)1 -0.002  0.003
## ply(TmS,2)2 -0.013  0.019  0.000

```

```

confint(AedesGrowthModel)

```

```

## Computing profile confidence intervals ...

## Warning in optwrap(optimizer, par = start, fn = function(x)
## dd(mkpar(npar1, : convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, 0L), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, 0L), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, 0L), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, 0L), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, 0L), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

```

```

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, OL), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, OL), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

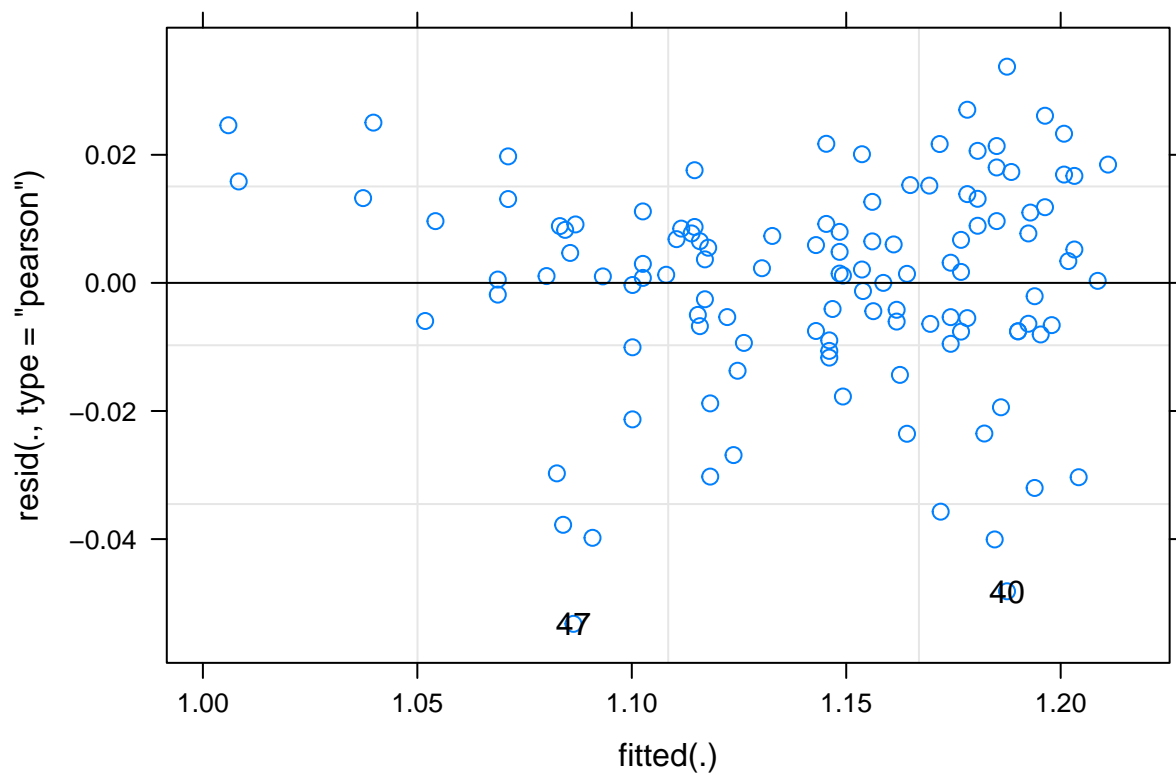
## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, OL), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, OL), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

## Warning in optwrap(optimizer, par = thopt, fn = mkdevfun(rho, OL), lower
## = fitted@lower): convergence code 3 from bobyqa: bobyqa -- a trust region
## step failed to reduce q

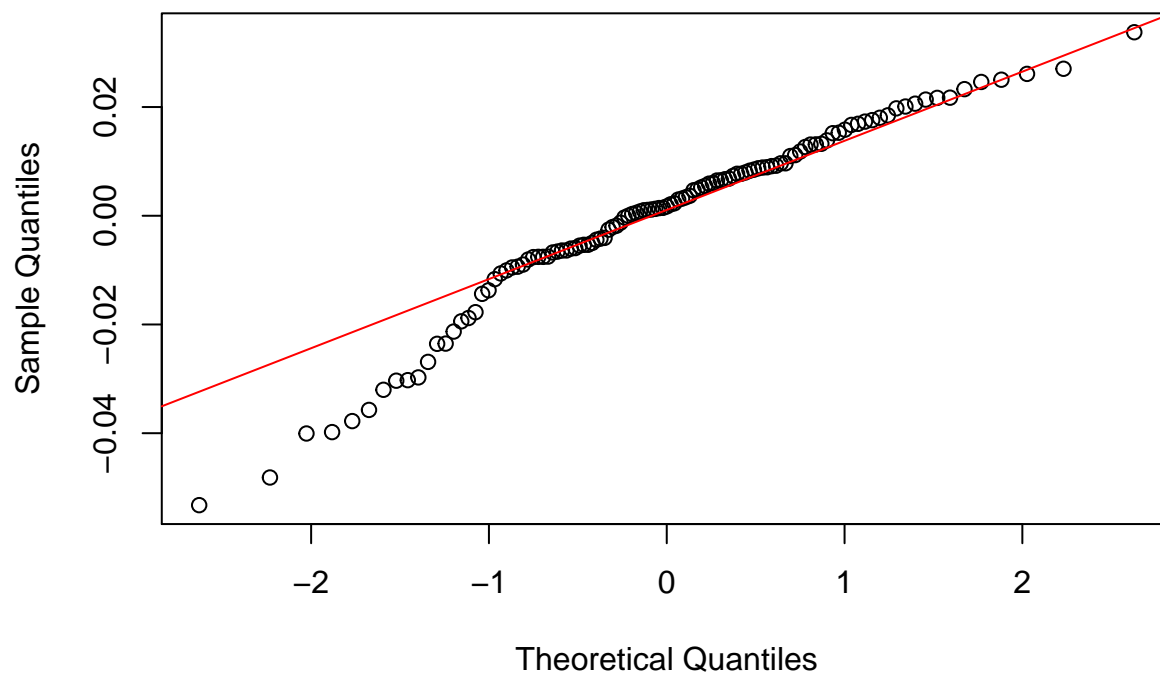
##              2.5 %      97.5 %
## .sig01          0.00000000 0.009266837
## .sigma          0.01470086 0.019035151
## (Intercept)     1.18264086 1.195039674
## AeDensScale    -0.06234742 -0.052089784
## poly(TempScale, 2)1 0.26798708 0.333737367
## poly(TempScale, 2)2 -0.19146150 -0.125699949
plot(AedesGrowthModel, id = 0.01, idLabels=~.obs)

```



```
qqnorm(resid(AedesGrowthModel))
qqline(resid(AedesGrowthModel), col = "red")
```

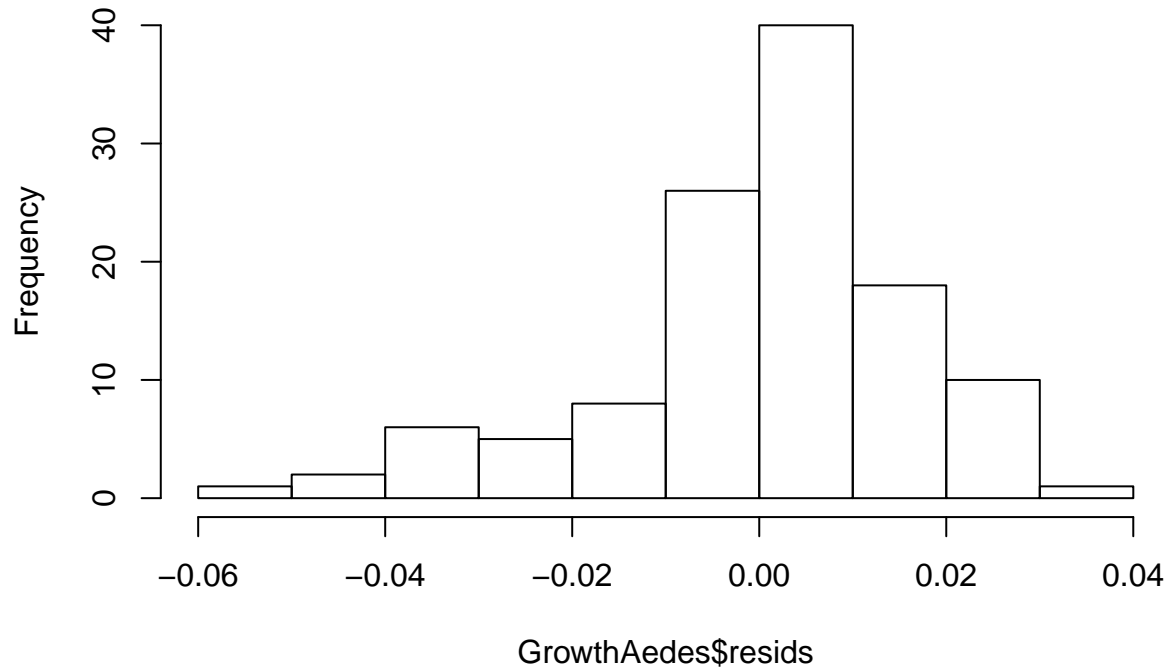
### Normal Q-Q Plot



```
GrowthAedes$preds <- predict(AedesGrowthModel)
GrowthAedes$resids <- resid(AedesGrowthModel)
```

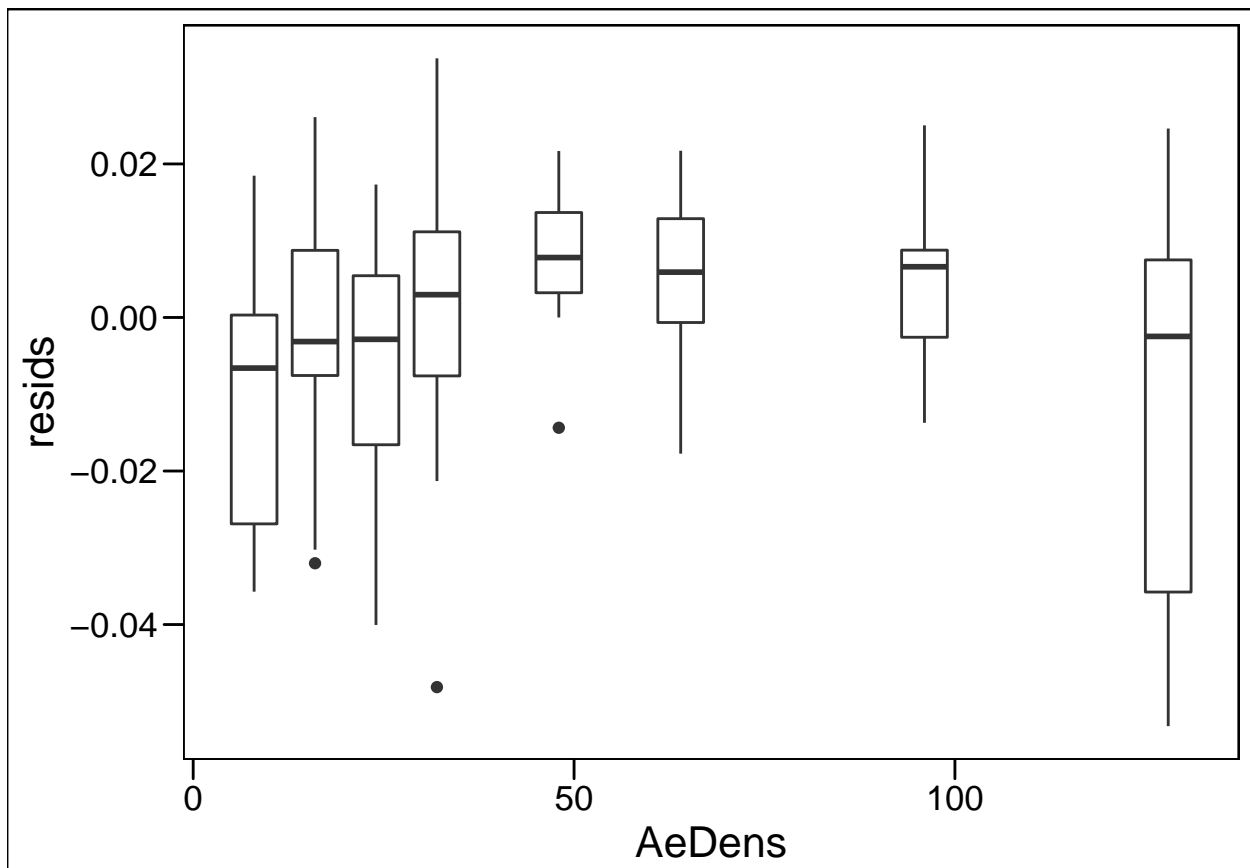
```
hist(GrowthAedes$resids)
```

**Histogram of GrowthAedes\$resids**

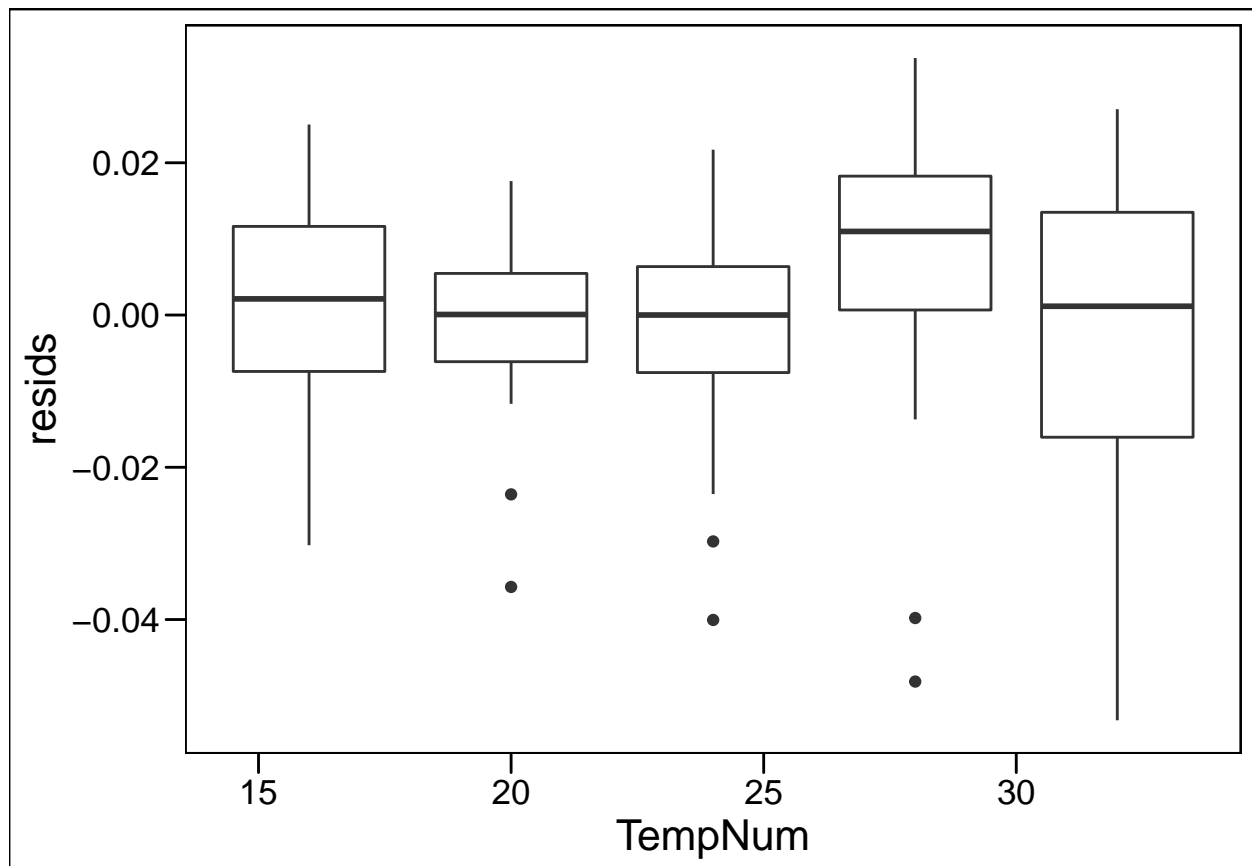


```
ggplot(data = GrowthAedes, aes(x=AeDens, y = resids, group = AeDens))+  
  geom_boxplot() +  
  theme_base()
```





```
ggplot(data = GrowthAedes, aes(x=TempNum, y = resids, group = TempNum))+  
  geom_boxplot() +  
  theme_base()
```



Create heatmaps of the growth. Ditto 3D surface above:

```
#heatmap plots
newData <- expand.grid(AeDens=seq(0,128, by=2), StDens=seq(0,128, by=2), TempNum=c(16,20,24,28,32), Rep=1)
newData <- newData %>%
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T)))

newData$preds <- predict(AedesGrowthModel, type = "response", newdata = newData)
#remove extrapolation outside of measured range
newData$preds[newData$AeDens+newData$StDens>128] <- NA
#get means over replicates to plot
predicted <- newData %>%
  group_by(TempNum, AeDens, StDens) %>%
  summarise(preds = mean(preds, na.rm=T)) %>%
  ungroup()

aeGrowthPreds <- predicted

#plot it
aeGrowthPlot <- ggplot(aeGrowthPreds, aes(x=StDens, y=AeDens, z=preds))+
  geom_raster(aes(fill=preds))+
  geom_contour(color="black", binwidth = 0.1)+
  theme_minimal()+
  scale_fill_viridis(name="Growth Rate", na.value = "gray90",
    limits = c(0,1.25))+
```

```
facet_wrap(~TempNum, ncol = 5) +
xlab("Stephensi Density") +
ylab("Aegypti Density")
```

## Stephensi

```
# only need female emergence
GrowthStephensi <- emergenceData %>%
  filter(Species == "Stephensi" & Sex == "Female") %>%
  #assume 50% female
  mutate(NO = StDens/2) %>%
  rename(x = Day, Ax = Number) %>%
  filter(StDens>0)

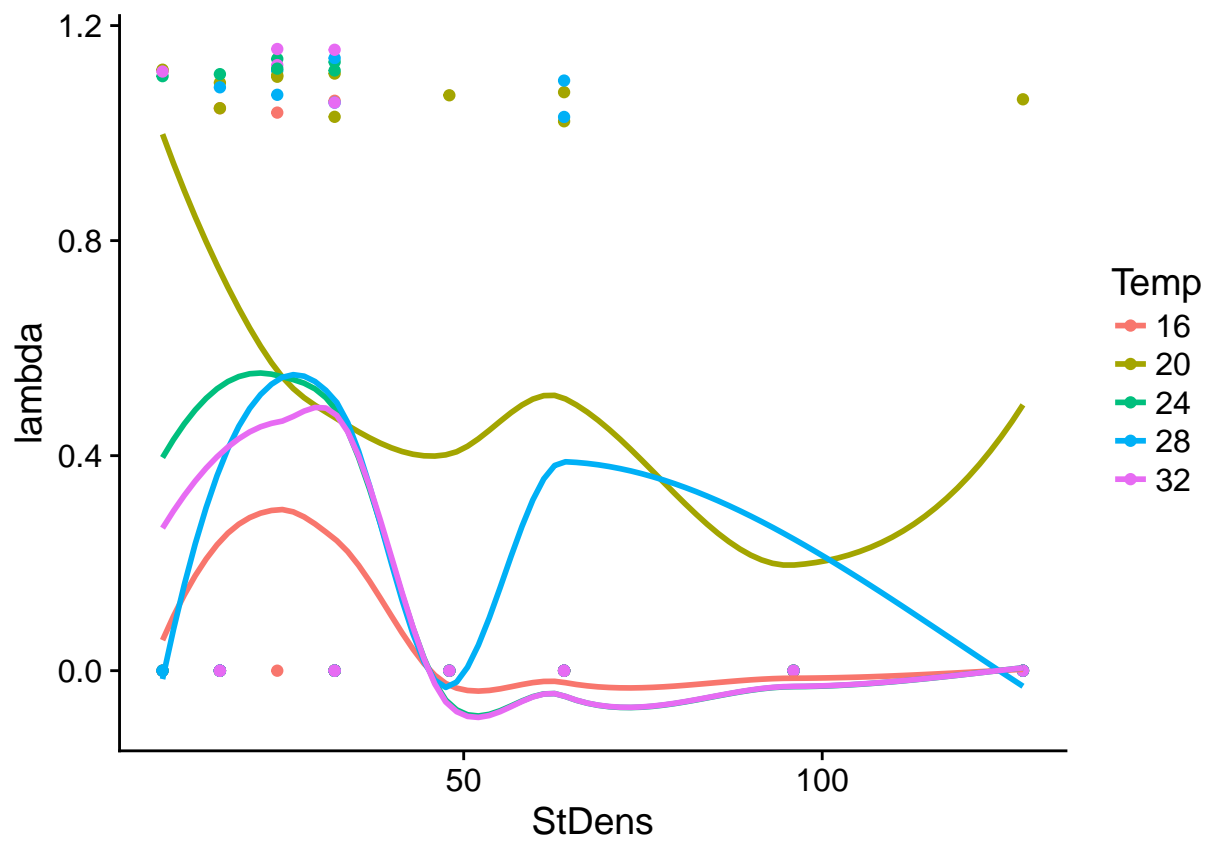
#add in predicted fecundity based on overall mean since model had no significance
GrowthStephensi$fwx <- mean(fecundity$Eggs[fecundity$Species == "Stephensi"],
  na.rm = T)

#calculate overall per capita growth rate
GrowthStephensi <- GrowthStephensi %>%
  mutate(Axfwx = Ax*fwx, xAxfwx = x*Ax*fwx) %>%
  group_by(Replicate, Temp, Ratio, TempNum, AeDens, StDens) %>%
  mutate_at(c("Axfwx", "xAxfwx"), sum, na.rm=T) %>%
  mutate(D=14) %>%
  ungroup() %>%
  mutate(r=(log((1/NO)*Axfwx))/(D+(xAxfwx/Axfwx))) %>%
  group_by(Replicate, Temp, TempNum, Ratio, AeDens, StDens, Species) %>%
  #each row is now a duplicate of the same thing so only need the first one
  slice(1) %>%
  mutate(lambda=exp(r)) %>%
  ungroup() %>%
  #rescale predictor variables
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T))) %>%
  #drop unnecessary columns
  dplyr::select(-x, -Ax, - Sex, - NO, -fwx, - Axfwx, - xAxfwx, -D)

# NAs are truly zeros
GrowthStephensi$lambda[is.na(GrowthStephensi$lambda)] <- 0

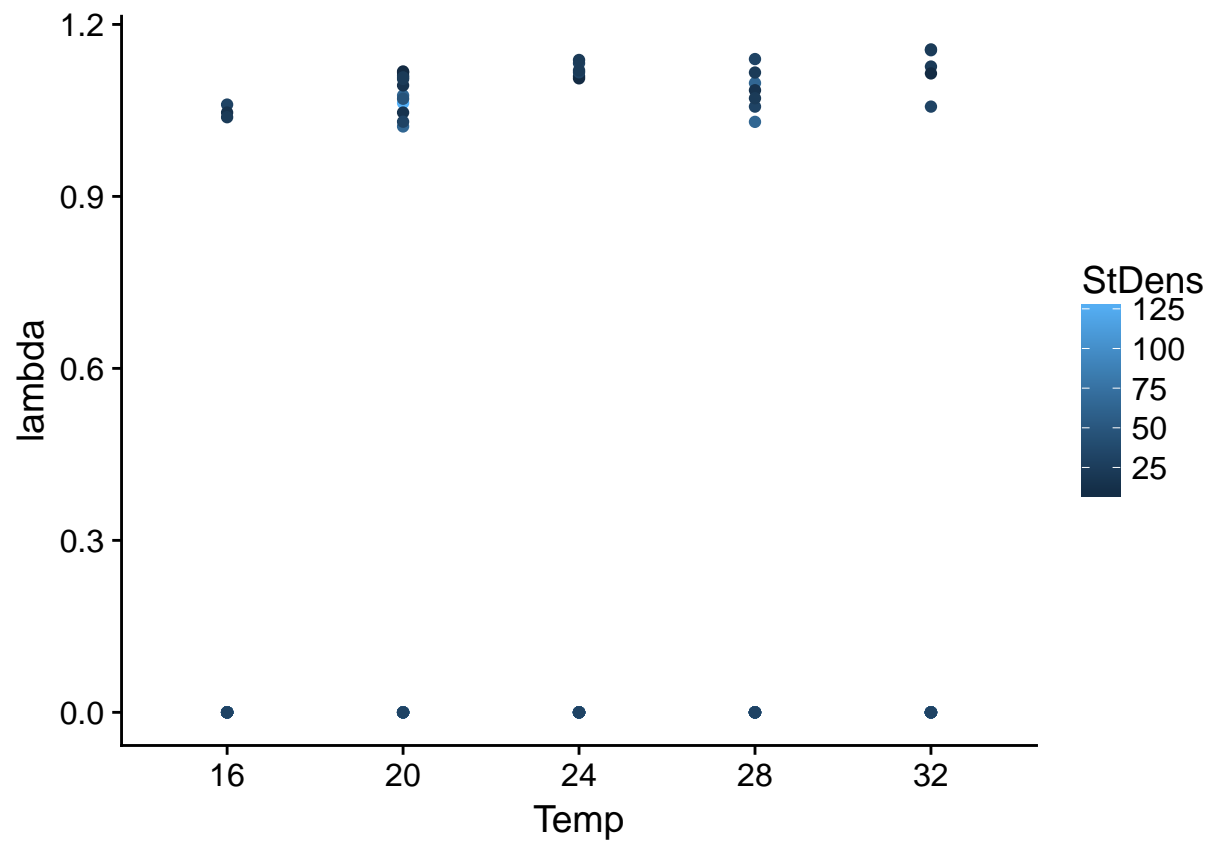
ggplot(data = GrowthStephensi, aes(x = StDens, y = lambda, color = Temp)) +
  geom_point() +
  geom_smooth(se = F)

## `geom_smooth()` using method = 'loess'
```

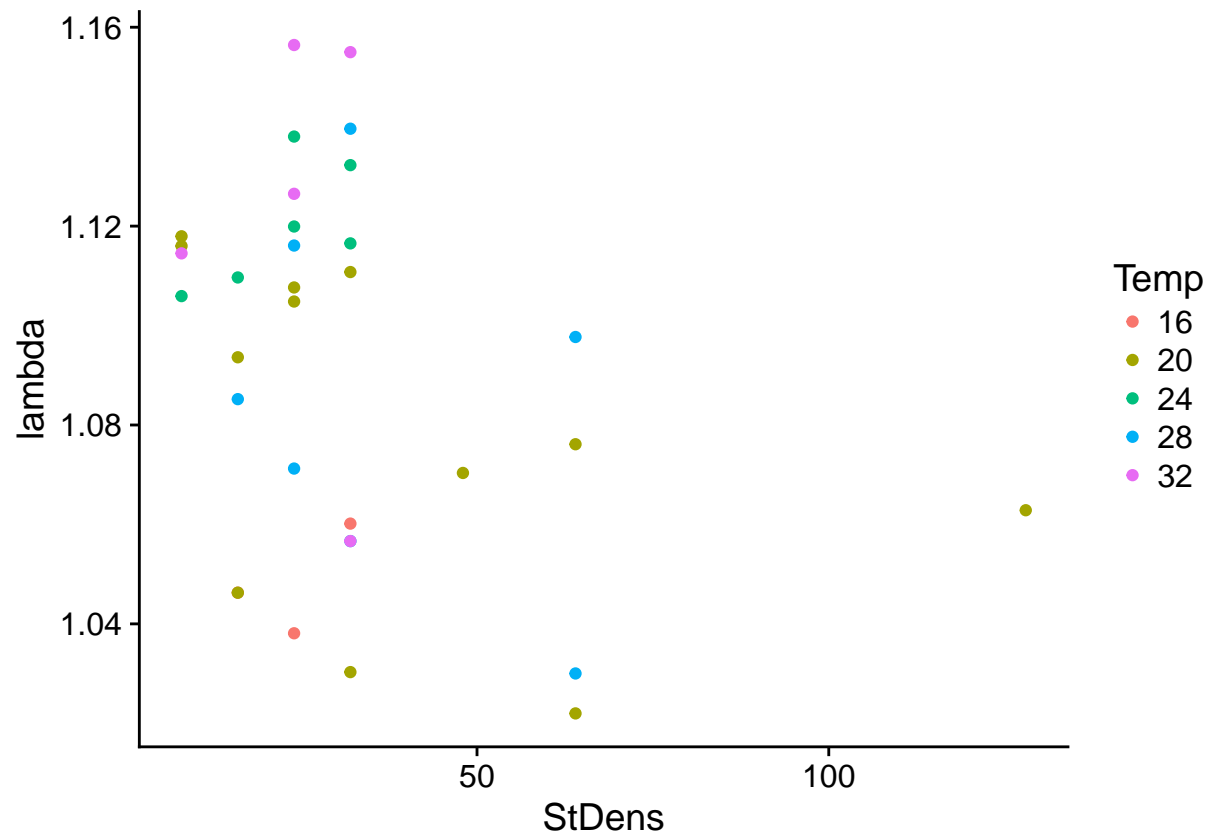


```
ggplot(data = GrowthStephensi, aes(x = Temp, y = lambda, color = StDens)) +
  geom_point() +
  geom_smooth(se = F)
```

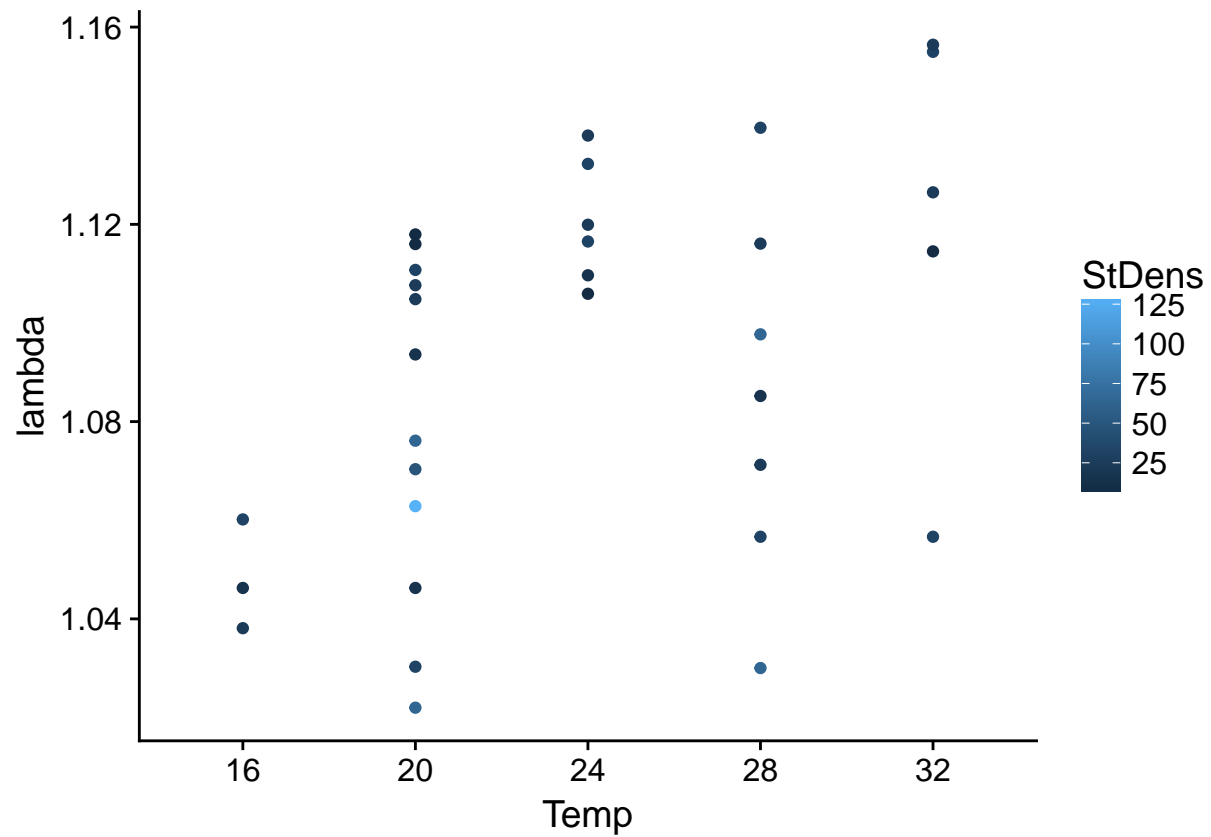
```
## `geom_smooth()` using method = 'loess'
```



```
ggplot(data = GrowthStephensi[GrowthStephensi$lambda>0,],  
  aes(x = StDens, y = lambda, color = Temp)) +  
  geom_point()
```



```
ggplot(data = GrowthStephensi[GrowthStephensi$lambda>0,],
  aes(x = Temp, y = lambda, color = StDens)) +
  geom_point()
```

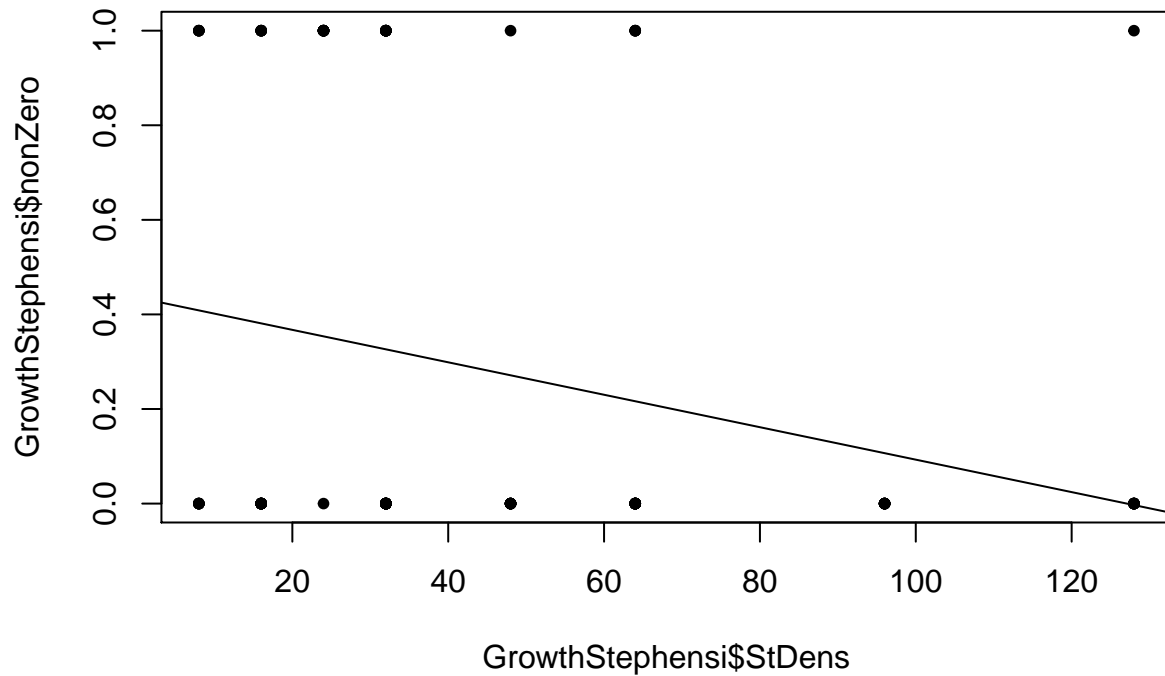


Model Selection

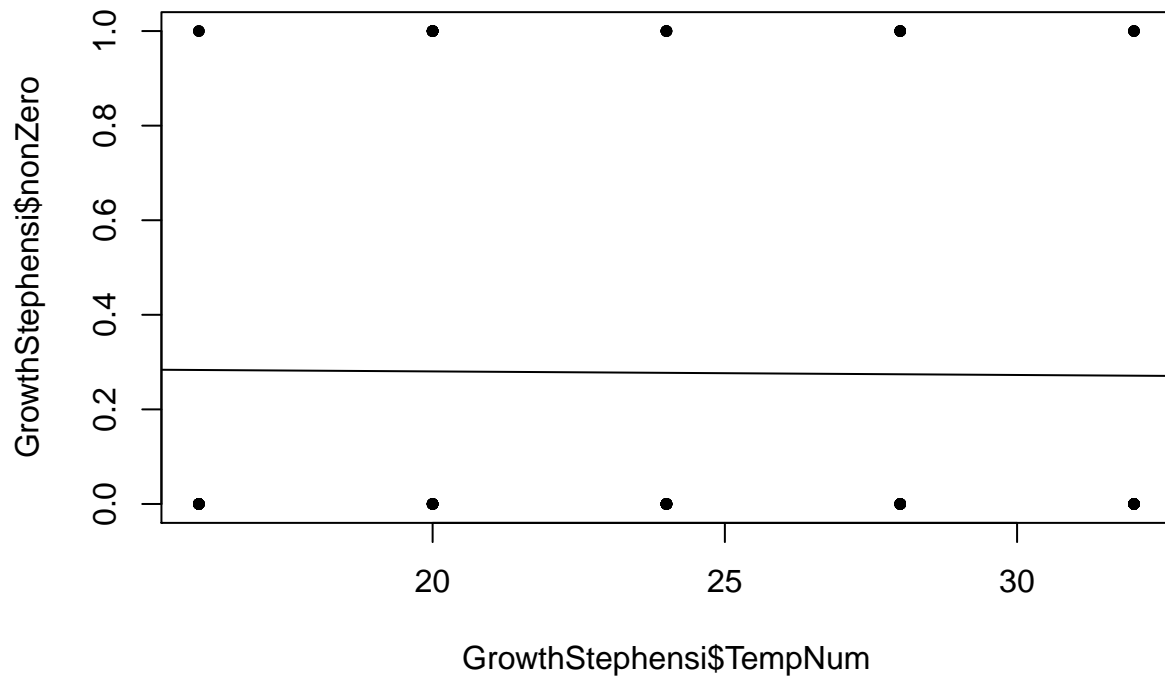
Impliment a hurdle model.

```
#create nonzero variable
GrowthStephensi$nonZero <- ifelse(GrowthStephensi$lambda>0,1,0)

plot(GrowthStephensi$StDens, GrowthStephensi$nonZero, pch=20)
abline(lm(nonZero ~ StDens, data = GrowthStephensi))
```



```
plot(GrowthStephensi$TempNum, GrowthStephensi$nonZero, pch=20)
abline(lm(nonZero ~ TempNum, data = GrowthStephensi)) #temperature has no effect zero
```



Model selection for zero vs. nonzero growth

```
m0 <- glmer(nonZero ~ 1 + (1|Replicate),
            data = GrowthStephensi,
            family = binomial(link = logit))

m1 <- glmer(nonZero ~ TempScale + (1|Replicate),
            data = GrowthStephensi,
```



```

    family = binomial(link = logit))

m2 <- glmer(nonZero ~ AeDensScale + (1|Replicate),
  data = GrowthStephensi,
  family = binomial(link = logit))

m3 <- glmer(nonZero ~ StDensScale + (1|Replicate),
  data = GrowthStephensi,
  family = binomial(link = logit))

m4 <- glmer(nonZero ~ AeDensScale + StDensScale + (1|Replicate),
  data = GrowthStephensi,
  family = binomial(link = logit))

m5 <- glmer(nonZero ~ AeDensScale * StDensScale + (1|Replicate),
  data = GrowthStephensi,
  family = binomial(link = logit))

modelSummary <- cbind(model = c("m0", "m1", "m2", "m3", "m4", "m5"),
  do.call(rbind, lapply(list(m0, m1, m2, m3, m4, m5), broom::glance)),
  AICc = AICc(m0, m1, m2, m3, m4, m5),
  AICweights = Weights(AIC(m0, m1, m2, m3, m4, m5)))

modelSummary

##      model sigma    logLik      AIC      BIC deviance df.residual AICc.df
## m0      m0      1 -70.25708 144.51416 150.0724 140.51416      117      2
## m1      m1      1 -70.25163 146.50325 154.8406 140.50325      116      3
## m2      m2      1 -54.88365 115.76730 124.1047 109.76730      116      3
## m3      m3      1 -65.40196 136.80393 145.1413 130.80393      116      3
## m4      m4      1 -40.76960  89.53920 100.6557  81.53920      115      4
## m5      m5      1 -40.70169  91.40338 105.2990  81.40338      114      5
##      AICc.AICc  AICweights
## m0 144.61761 8.282498e-13
## m1 146.71195 3.063620e-13
## m2 115.97599 1.446982e-06
## m3 137.01262 3.912163e-11
## m4  89.89008 7.174979e-01
## m5  91.93436 2.825007e-01

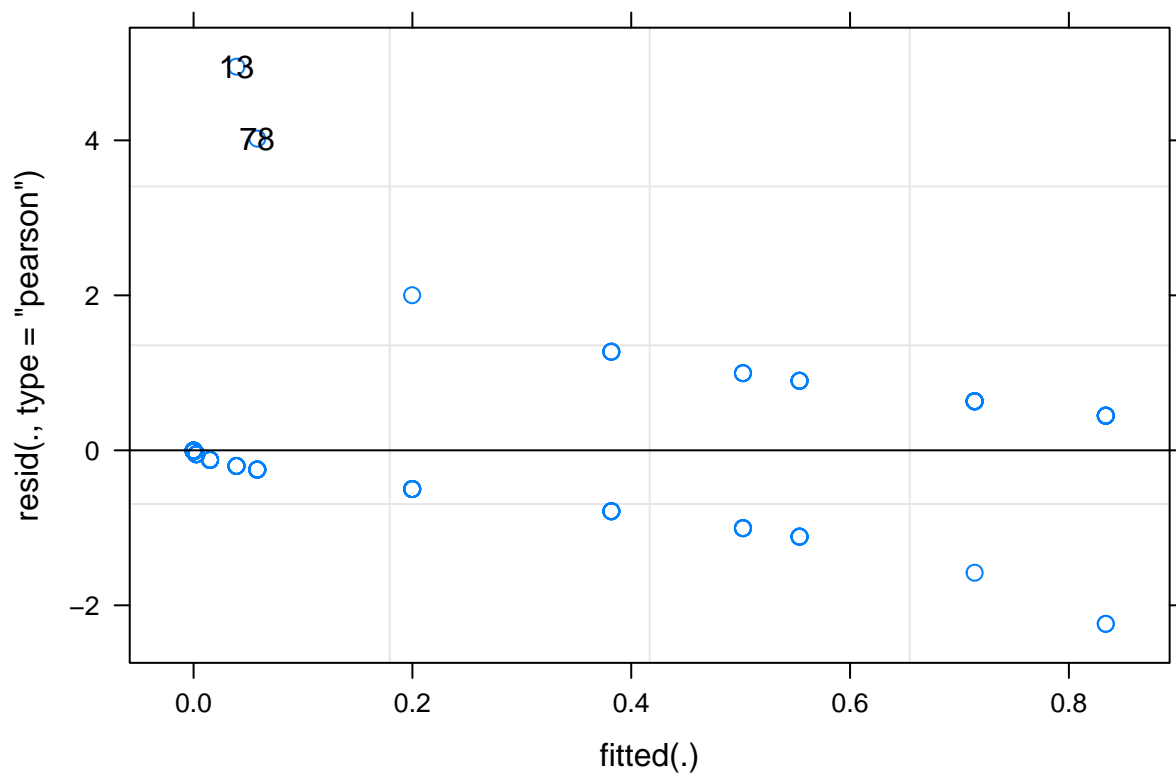
StephensiGrowthModelBin <- m4

```

Whether or not growth is zero (basically mosquitoes emerge), is dependent on density (Aedes and Stephensi), not temperature.

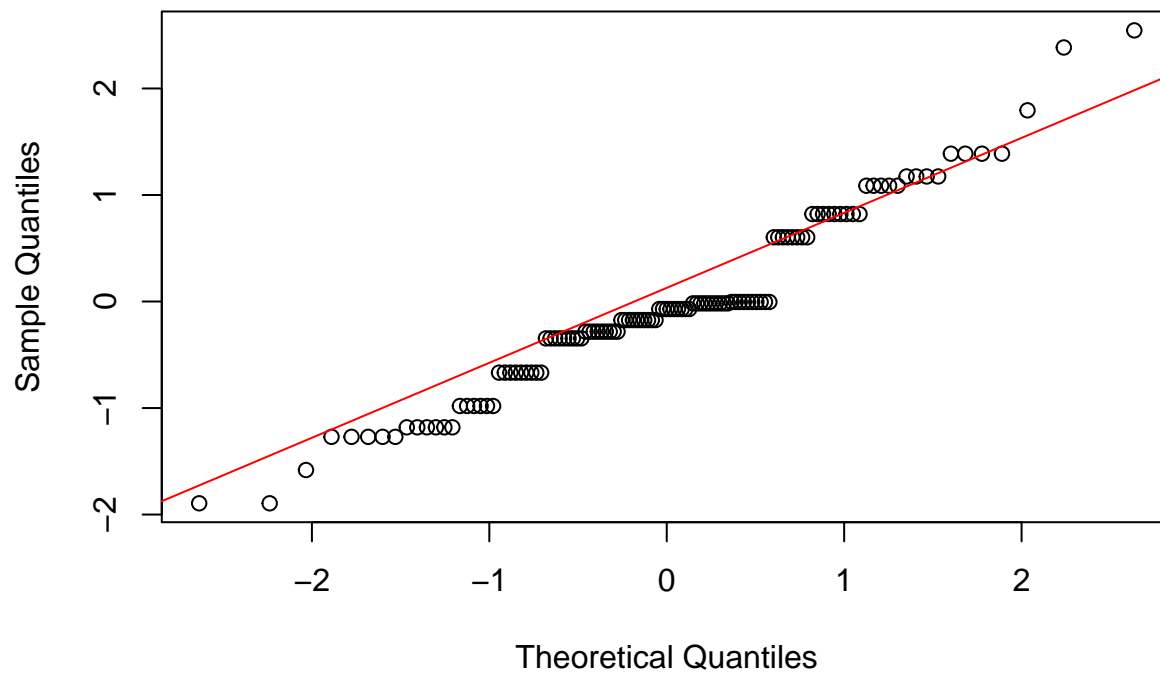
Inspect residuals, although this is more important for final hurdle model.

```
plot(StephensiGrowthModelBin, id = 0.01, idLabels=~.obs)
```



```
qqnorm(resid(StephensiGrowthModelBin))
qqline(resid(StephensiGrowthModelBin), col = "red")
```

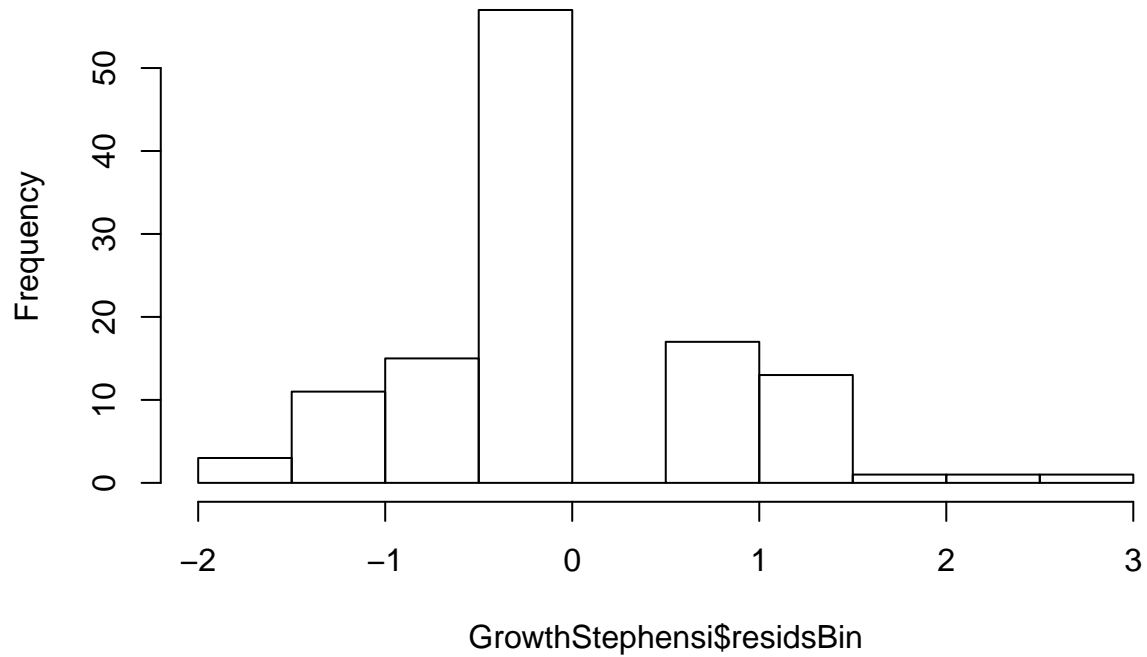
### Normal Q–Q Plot



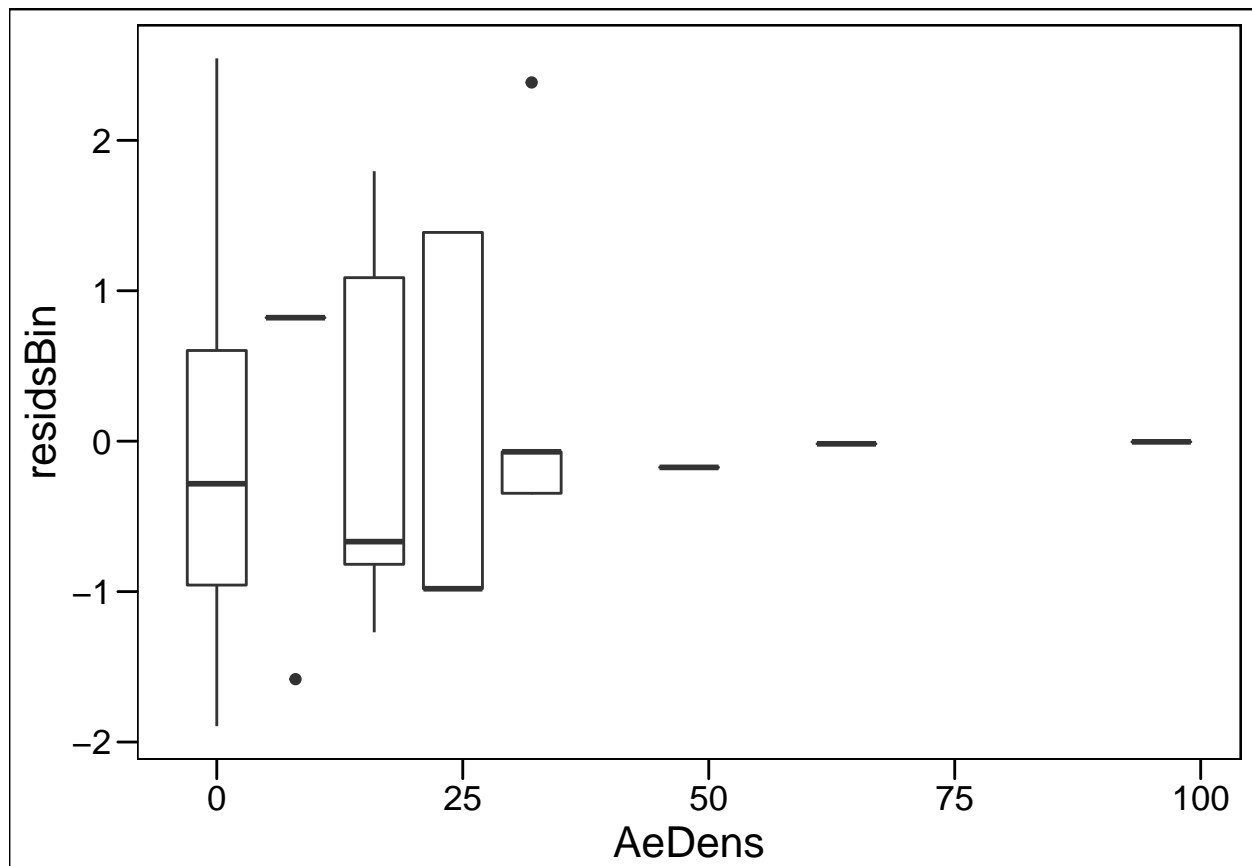
```
GrowthStephensi$predsBin <- predict(StephensiGrowthModelBin)
GrowthStephensi$residsBin <- resid(StephensiGrowthModelBin)
```

```
hist(GrowthStephensi$residsBin)
```

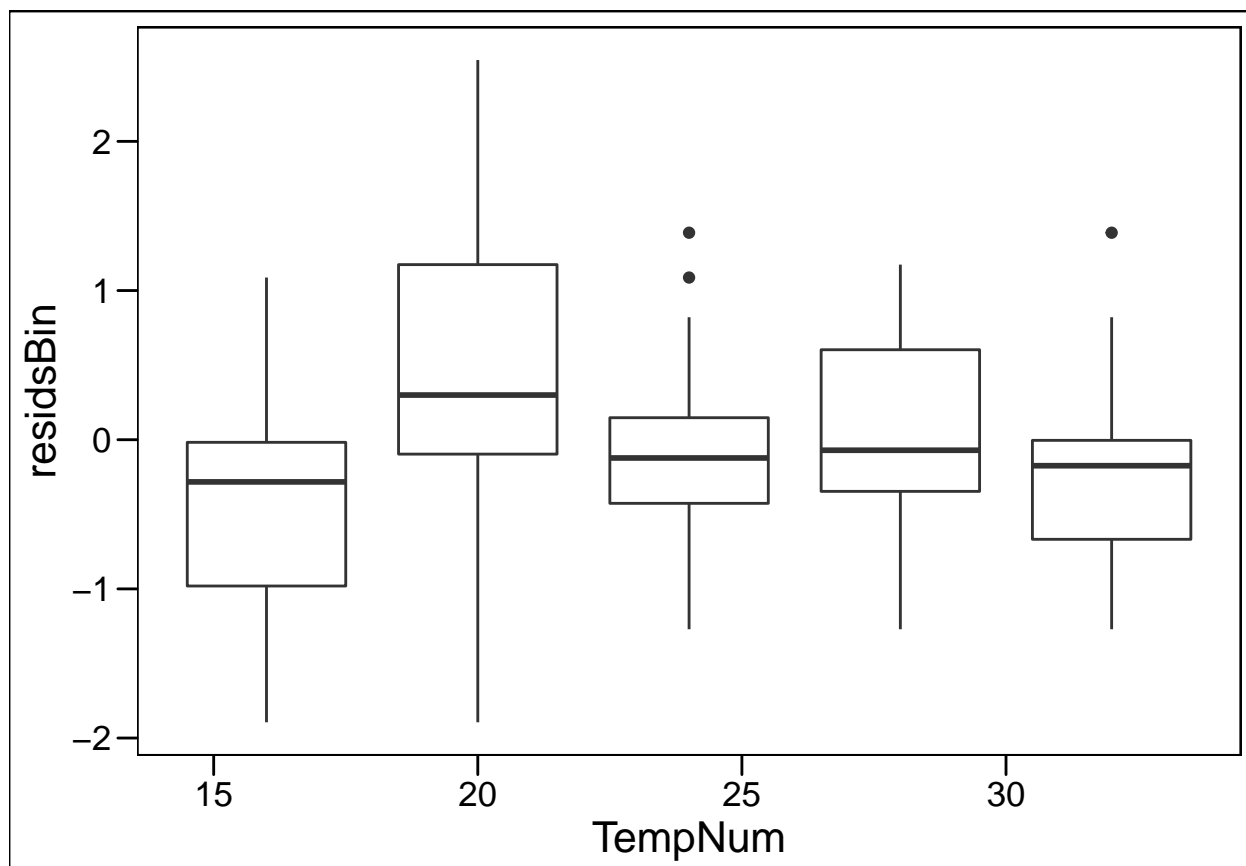
## Histogram of GrowthStephensi\$residsBin



```
ggplot(data = GrowthStephensi, aes(x=AeDens, y = residsBin, group = AeDens))+  
  geom_boxplot() +  
  theme_base()
```



```
ggplot(data = GrowthStephensi, aes(x=TempNum, y = residsBin, group = TempNum))+
  geom_boxplot() +
  theme_base()
```



Second part of hurdle model for non-zeros

```
m0 <- glmer(lambda ~ 1 + (1|Replicate),
             data = subset(GrowthStephensi, nonZero==1),
             family = gaussian)
```

```
## Warning in glmer(lambda ~ 1 + (1 | Replicate), data =
## subset(GrowthStephensi, : calling glmer() with family=gaussian (identity
## link) as a shortcut to lmer() is deprecated; please call lmer() directly
```

```
m1 <- lmerTest::lmer(lambda ~ TempScale + (1|Replicate),
                     data = subset(GrowthStephensi, nonZero==1))
```

```
m2 <- glmer(lambda ~ AeDensScale + (1|Replicate),
             data = subset(GrowthStephensi, nonZero==1),
             family = gaussian)
```

```
## Warning in glmer(lambda ~ AeDensScale + (1 | Replicate), data =
## subset(GrowthStephensi, : calling glmer() with family=gaussian (identity
## link) as a shortcut to lmer() is deprecated; please call lmer() directly
```

```
m3 <- glmer(lambda ~ StDensScale + (1|Replicate),
             data = subset(GrowthStephensi, nonZero==1),
             family = gaussian)
```

```
## Warning in glmer(lambda ~ StDensScale + (1 | Replicate), data =
## subset(GrowthStephensi, : calling glmer() with family=gaussian (identity
## link) as a shortcut to lmer() is deprecated; please call lmer() directly
```

```

m4 <- glmer(lambda ~ StDensScale + TempScale + (1|Replicate),
             data = subset(GrowthStephensi, nonZero==1),
             family = gaussian)

## Warning in glmer(lambda ~ StDensScale + TempScale + (1 | Replicate), data
## = subset(GrowthStephensi, : calling glmer() with family=gaussian (identity
## link) as a shortcut to lmer() is deprecated; please call lmer() directly

m5 <- glmer(lambda ~ StDensScale * TempScale + (1|Replicate),
             data = subset(GrowthStephensi, nonZero==1),
             family = gaussian)

## Warning in glmer(lambda ~ StDensScale * TempScale + (1 | Replicate), data
## = subset(GrowthStephensi, : calling glmer() with family=gaussian (identity
## link) as a shortcut to lmer() is deprecated; please call lmer() directly

m6 <- glmer(lambda ~ StDensScale + poly(TempScale,2) + (1|Replicate),
             data = subset(GrowthStephensi, nonZero==1),
             family = gaussian)

## Warning in glmer(lambda ~ StDensScale + poly(TempScale, 2) + (1 |
## Replicate), : calling glmer() with family=gaussian (identity link) as a
## shortcut to lmer() is deprecated; please call lmer() directly

modelSummary <- cbind(model = c("m0","m1","m2","m3", "m4", "m5", "m6"),
                      do.call(rbind, lapply(list(m0, m1, m2, m3, m4, m5, m6), broom::glance)),
                      AICc = AICc(m0, m1, m2, m3, m4, m5, m6),
                      AICweights = Weights(AIC(m0, m1, m2, m3, m4, m5, m6)))

## Warning in deviance.merMod(x): deviance() is deprecated for REML fits;
## use REMLcrit for the REML criterion or deviance(.,REML=FALSE) for deviance
## calculated at the REML fit

modelSummary

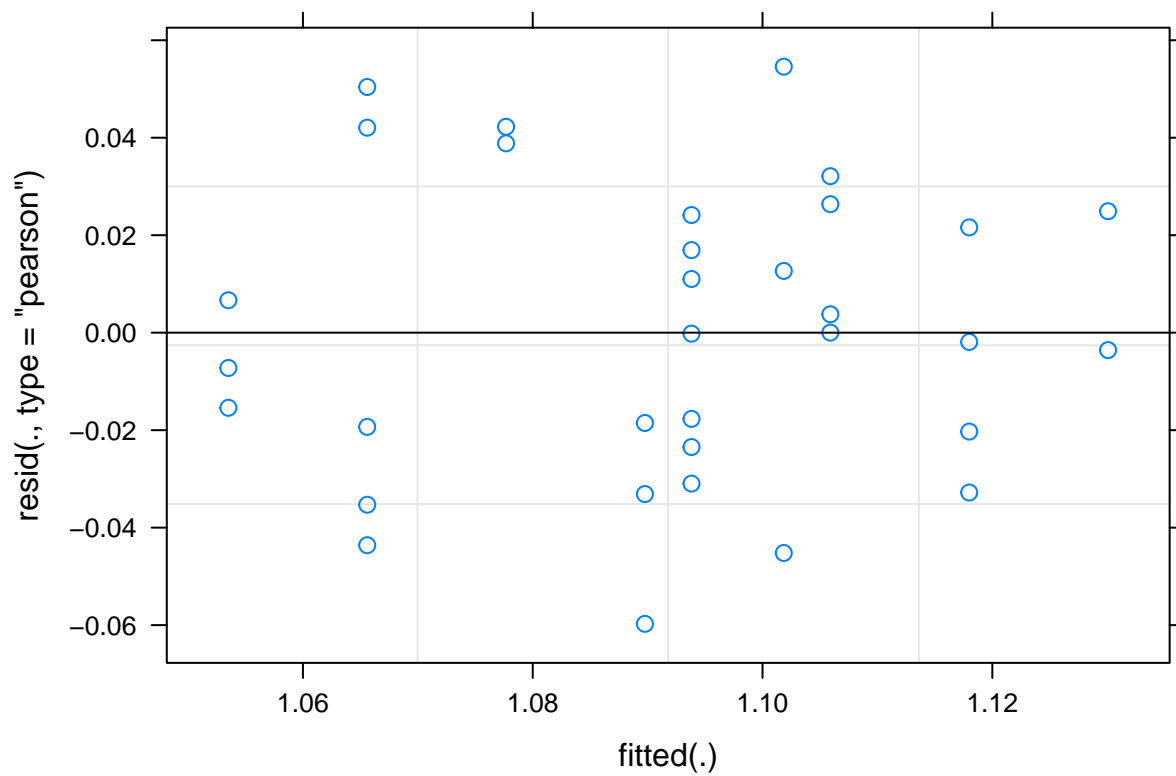
##      model      sigma  logLik      AIC      BIC  deviance df.residual
## m0      m0 0.03405524 59.94293 -113.8859 -109.39634 -126.2077          30
## m1      m1 0.03092073 60.80450 -113.6090 -107.62297 -121.6090          29
## m2      m2 0.03461804 57.21009 -106.4202 -100.43416 -126.2387          29
## m3      m3 0.03075010 60.10393 -112.2079 -106.22184 -133.1257          29
## m4      m4 0.02778850 60.90507 -111.8101 -104.32760 -140.7422          28
## m5      m5 0.02800588 59.68014 -107.3603  -98.38123 -141.4462          27
## m6      m6 0.02822665 58.53774 -105.0755  -96.09643 -141.0352          27
##      AICc.df AICc.AICc  AICweights
## m0          3 -113.0583 0.366100165
## m1          4 -112.1804 0.318771044
## m2          4 -104.9916 0.008758874
## m3          4 -110.7793 0.158207410
## m4          5 -109.5879 0.129676280
## m5          6 -104.1295 0.014014773
## m6          6 -101.8447 0.004471453

StephensiGrowthModel2 <- m1

Best Model is temperature (slightly positive).

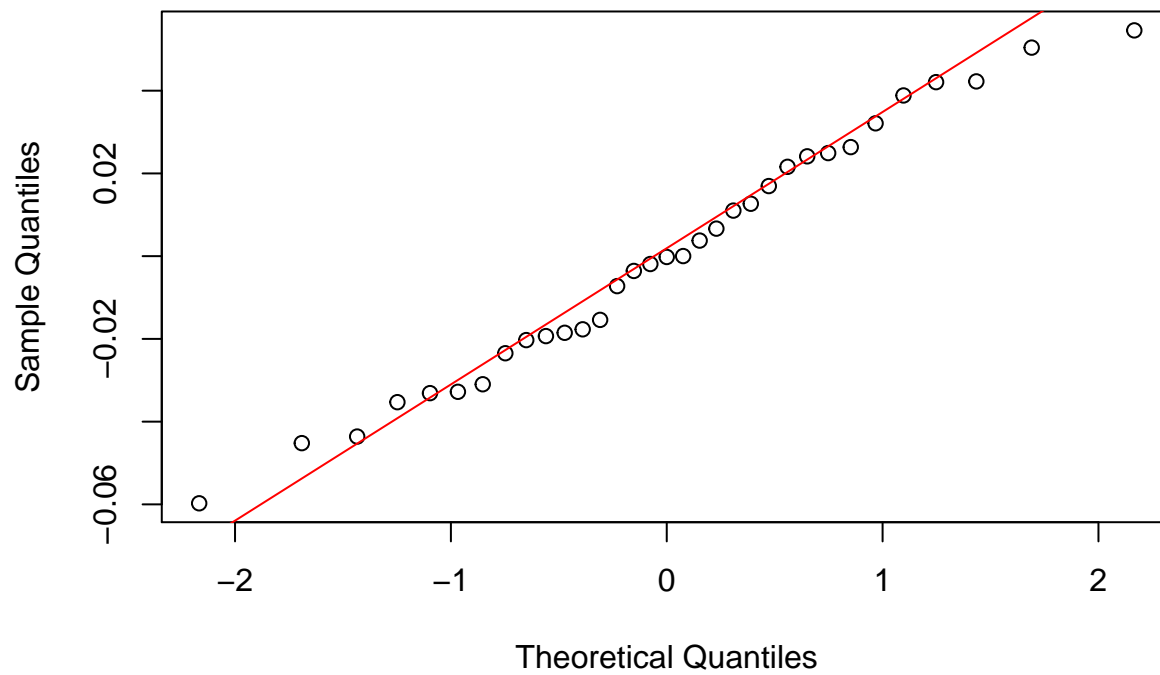
plot(StephensiGrowthModel2, id = 0.01, idLabels=~.obs)

```



```
qqnorm(resid(StephensiGrowthModel12))
qqline(resid(StephensiGrowthModel12), col = "red")
```

### Normal Q-Q Plot



```
GrowthStephensi$predsGam[GrowthStephensi$nonZero==1] <- predict(StephensiGrowthModel2)
```

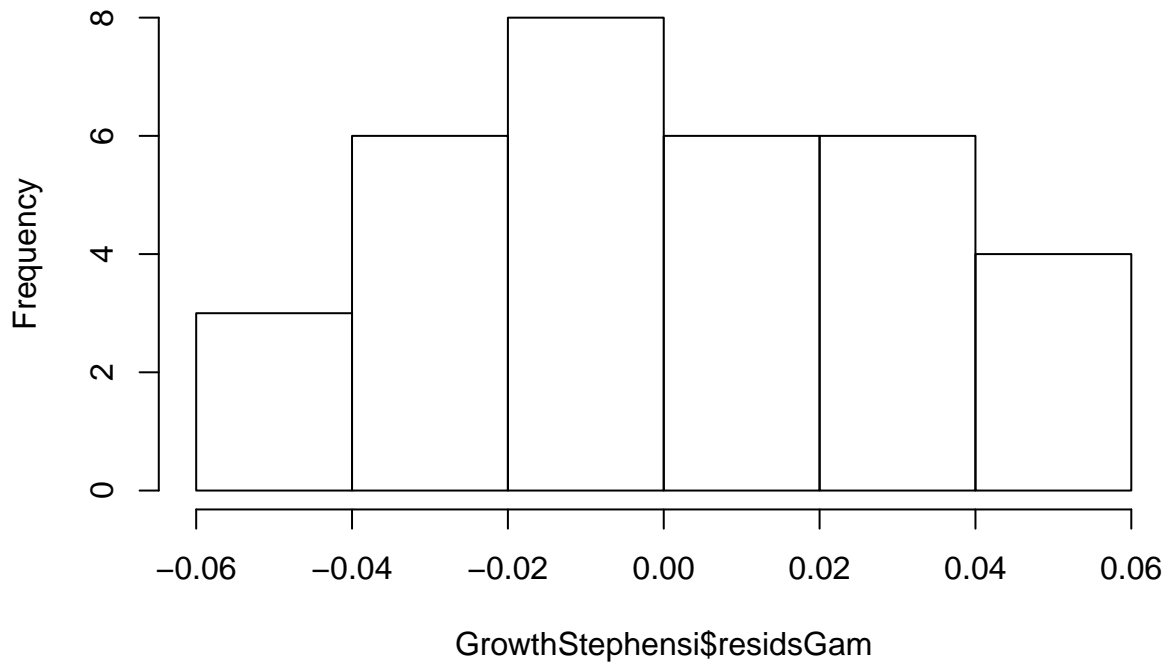
```
## Warning: Unknown or uninitialised column: 'predsGam'.
```

```
GrowthStephensi$residsGam[GrowthStephensi$nonZero==1] <- resid(StephensiGrowthModel2)
```

```
## Warning: Unknown or uninitialised column: 'residsGam'.
```

```
hist(GrowthStephensi$residsGam)
```

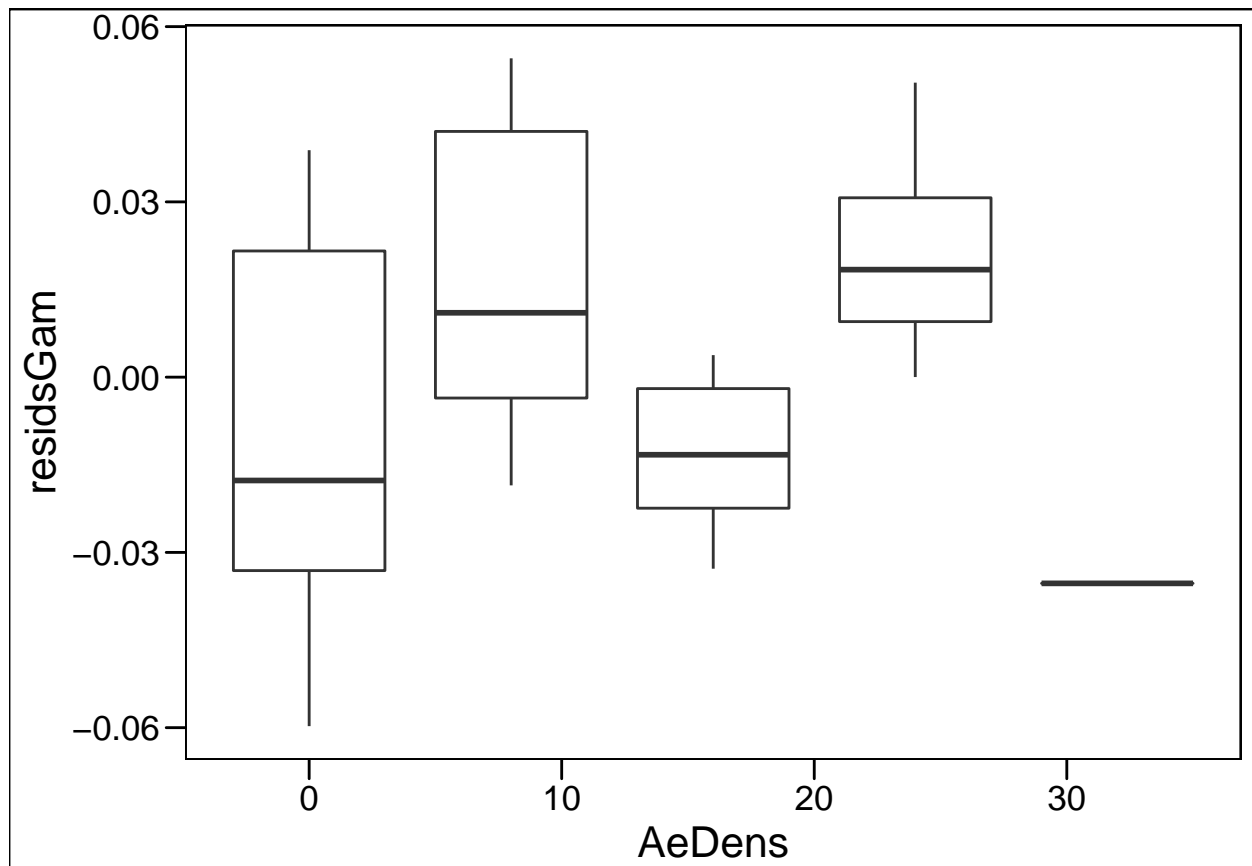
## Histogram of GrowthStephensi\$residsGam



```
ggplot(data = GrowthStephensi, aes(x=AeDens, y = residsGam, group = AeDens))+  
  geom_boxplot() +  
  theme_base()
```

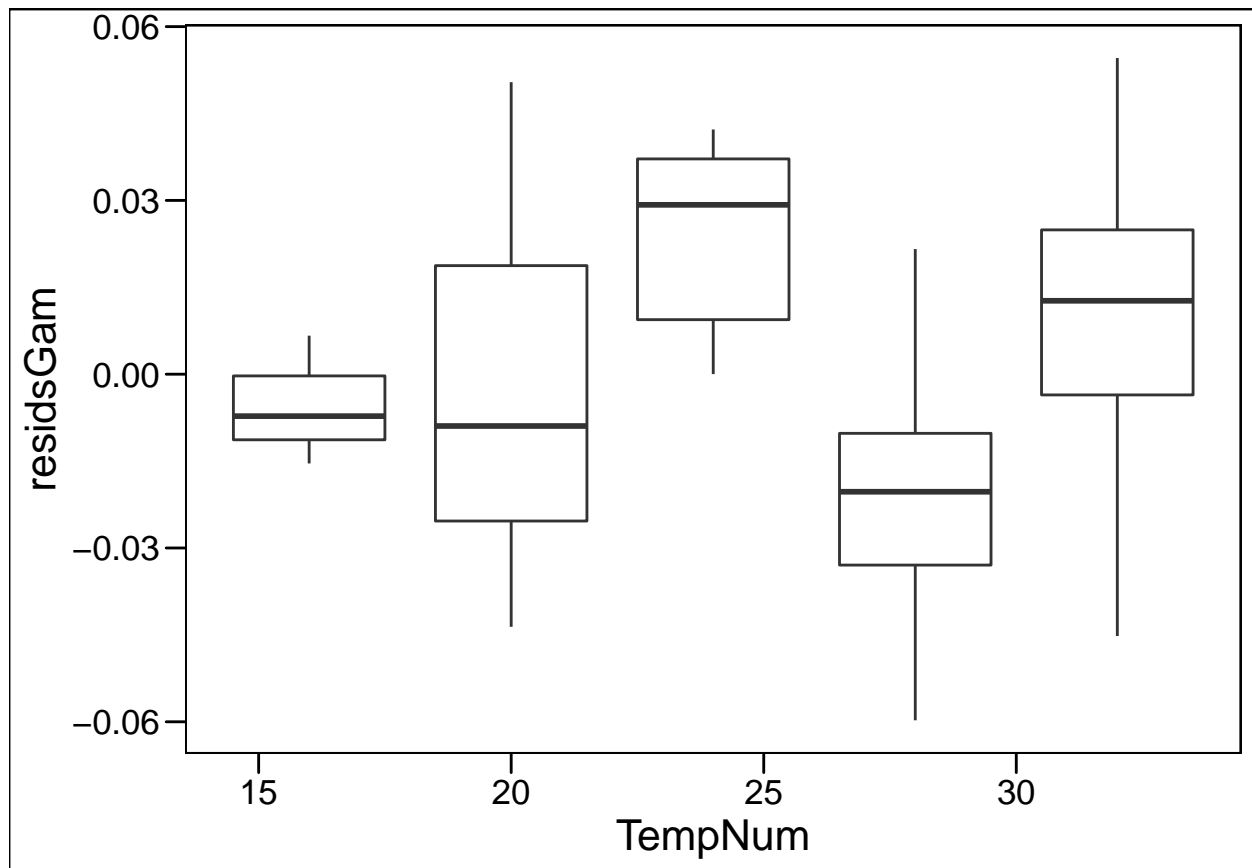
```
## Warning: Removed 86 rows containing non-finite values (stat_boxplot).
```





```
ggplot(data = GrowthStephensi, aes(x=TempNum, y = residGam, group = TempNum))+  
  geom_boxplot() +  
  theme_base()
```

```
## Warning: Removed 86 rows containing non-finite values (stat_boxplot).
```



```
summary(StephensiGrowthModel2)
```

```
## Linear mixed model fit by REML t-tests use Satterthwaite approximations
## to degrees of freedom [lmerMod]
## Formula: lambda ~ TempScale + (1 | Replicate)
## Data: subset(GrowthStephensi, nonZero == 1)
##
## REML criterion at convergence: -121.6
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -1.93201 -0.65619 -0.00646  0.78043  1.76496
##
## Random effects:
##  Groups      Name                Variance Std.Dev.
##  Replicate (Intercept) 0.0004499 0.02121
##  Residual              0.0009561 0.03092
## Number of obs: 33, groups:  Replicate, 2
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)   1.01929    0.03042 10.73300  33.512 3.29e-12 ***
## TempScale     0.07472    0.02684 30.03800   2.783  0.00921 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```

## Correlation of Fixed Effects:
##           (Intr)
## TempScale -0.852
confint(StephensiGrowthModel2)

## Computing profile confidence intervals ...

##           2.5 %    97.5 %
## .sig01      0.00000000 0.06626058
## .sigma      0.02417192 0.03990503
## (Intercept) 0.96259638 1.07576942
## TempScale   0.02205714 0.12898464

unHurdle <- function(mod1, mod2, newDF){
  #' Function that creates predictions based on binomial/gaussian hurdle model

  #' @param mod1 binomial model
  #' @param mod2 second model, gaussian in this case
  #' @param newDF new data frame to predict over, must have same columns as original
  phi_zero <- predict(mod1, newdata = newDF, type = "response")
  mod2Preds <- predict(mod2, newdata = newDF, type = "response")
  #calculate probability of zero in second model to subtract from first
  phi_count <- pnorm(q = 0,
                    mean = mod2Preds,
                    sd = sigma(mod2),
                    log.p = F)
  phi <- phi_zero - phi_count
  predsAll <- phi * mod2Preds
  return(predsAll)
}

predsAll <- unHurdle(mod1 = StephensiGrowthModelBin, mod2 = StephensiGrowthModel2, newDF = GrowthStephen
GrowthStephensi$predsFinal <- predsAll

#heatmap plots
newData <- expand.grid(AeDens=seq(0,128, by=2), StDens=seq(0,128, by=2), TempNum=c(16,20,24,28,32), Rep
newData <- newData %>%
  mutate(TempScale = as.vector(scale(TempNum, center = F, scale = T))) %>%
  mutate(AeDensScale = as.vector(scale(AeDens, center = F, scale = T))) %>%
  mutate(StDensScale = as.vector(scale(StDens, center = F, scale = T)))

newData$preds <- unHurdle(mod1 = StephensiGrowthModelBin, mod2 = StephensiGrowthModel2, newDF = newData)
#get means over replicates to plot
predicted <- newData %>%
  group_by(TempNum, AeDens, StDens) %>%
  summarise(preds = mean(preds))
#remove extrapolation outside of measured range
predicted$preds[predicted$AeDens+predicted$StDens>128] <- NA

stGrowthPreds <- predicted

#plot it
stGrowthPlot <- ggplot(stGrowthPreds, aes(x=StDens, y=AeDens,
                                           z=preds))+

```

```

geom_raster(aes(fill=preds))+
geom_contour(color="gray90", binwidth = 0.1)+
theme_minimal()+
scale_fill_viridis(name="Growth Rate", na.value = "gray90",
                    limits = c(0,1.25))+
facet_wrap(~TempNum, ncol = 5) +
xlab("Stephensi Density") +
ylab("Aegypti Density")

```

## Save All Results

```

#models
save(AedesSurvivalModel, AedesFecundityModel, AedesGrowthModel,
     StephSurvivalModel, StephensiFecundityModel, StephensiGrowthModelBin,
     StephensiGrowthModel2, file = "code/finalModels.RData")

```

```

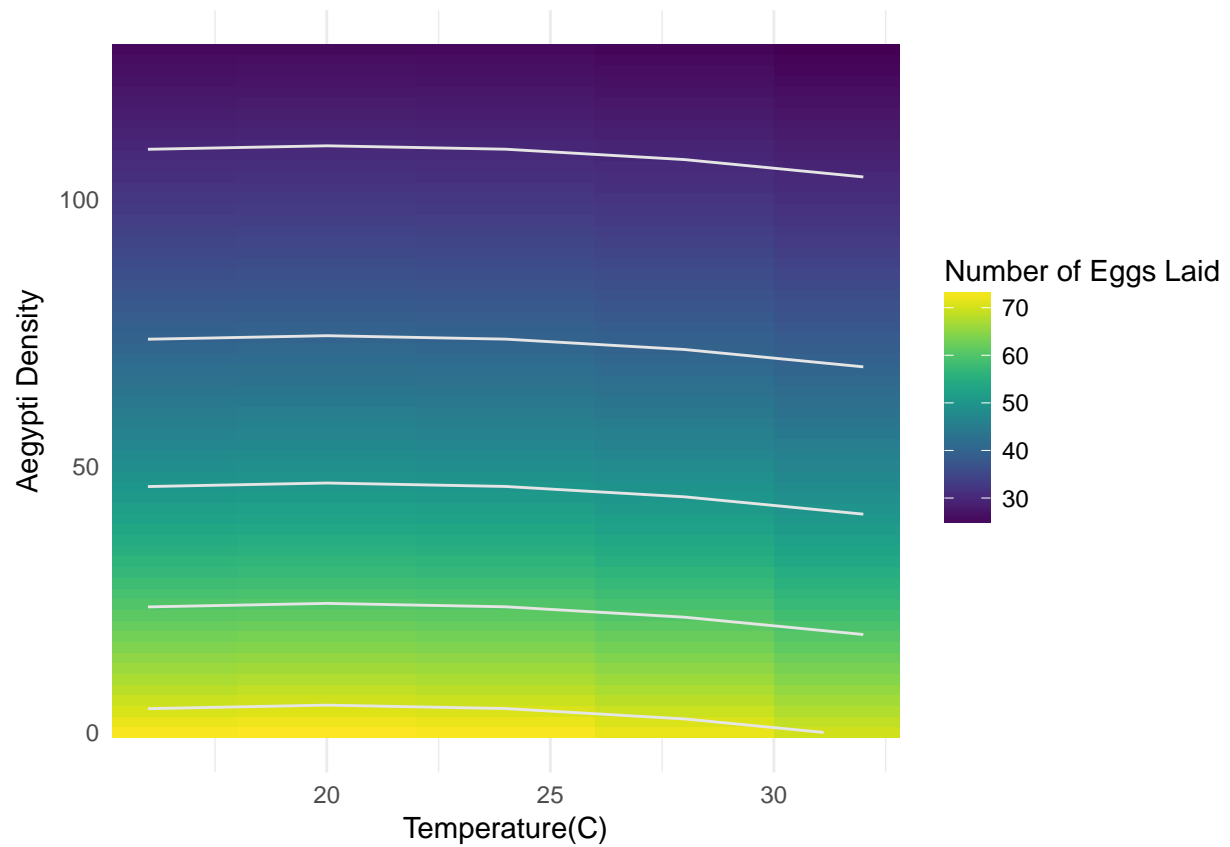
survivalPlot <- plot_grid(aeSurvPlot,
                          stSurvPlot,
                          nrow = 2,
                          labels=c("A", "B"))

```

```
## Warning: Removed 10400 rows containing non-finite values (stat_contour).
```

```
## Warning: Removed 10400 rows containing non-finite values (stat_contour).
```

```
aeFecPlot
```



```
growthPlot <- plot_grid(aeGrowthPlot, stGrowthPlot, nrow = 2, labels = c("A", "B"))
```

```
## Warning: Removed 10400 rows containing non-finite values (stat_contour).
```

```
## Warning: Removed 10400 rows containing non-finite values (stat_contour).
```

```
save(survivalPlot, aeFecPlot, growthPlot, file = "code/figures/finalFigures.RData")
```