model

April 16, 2020

1 Extended Network Model

1.0.1 States

$$S_s, S, E, I_n, I_a, I_s, I_d, R_d, R_u, D_d, D_u$$

1.0.2 Transitions

$$S \to S_s$$

$$S \to E$$

$$S_s \to S$$

$$S_s \to E$$

$$E \to I_n$$

$$E \to I_a$$

$$I_n \to R_u$$

$$I_a \to I_s$$

$$I_s \to R_u$$

$$I_s \to D_u$$

$$I_s \rightarrow I_d$$

$$I_d \rightarrow R_d$$

$$I_d \rightarrow D_d$$

$$I_a \rightarrow I_d$$

$$E \rightarrow I_d$$

1.0.3 Seirsplus propensity

$$P[X_i = S \rightarrow E] = \left[p\frac{\beta I}{N} + (1-p)\frac{\beta \sum_{j \in C_{G(i)}} \delta_{X_j=I}}{|C_{G(i)}|} \right] \delta_{X_t=S}$$

where I is a number of infected, N total number of living individuals, β rate of transmission (may be individual for each node), $\delta_{X_j=I}$ is 1 if $X_j = I$, 0 otherwise, X_i state of individual i, $C_{G(i)}$ is a set of close contacts (nodes j, that edge (i,j) is in the given graph G).

1.0.4 Extended propensity

We use the same formula for $P[X_i = S-> E]$ with these modifications:

- I is the total number of I-states, i.e. sum of I_n, I_a, I_s, I_d

- $\delta_{X=I} = 1$ if and only if $X \in \{I_n, I_a, I_s, I_d\}$

- edges has weights

- $|C_{G(i)}|$ is not the number of edges from i, but the sum of their weights (!there is only one edge between (i,j) in G)

- $\sum_{j \in C_{G(i)}} \delta_{X_j=I}$ is replaced by $\sum_{j \in C_{G(i)}} w_{(i,j)} \delta_{X_j=I}$

1.0.5 Constraction G from G_multi

Graph G_{multi} may contain more edges between i, j. Each edge has type t and subtype s and weight $w_{i,j,t,s}$ (intensity).

Graph G has max one edge (i, j) between nodes i, j. Edge as weight $w_{i,j}$.

$w_{i,j,t} = \sum_s w_{i,j,t,s}$ (sum over intensities of sublayers)

Weight $w_{i,j} = 1 - \prod_t (1 - w_{i,j,t})$ (weights on layers t are taking as probabilities of contact on that layer and are the final weight is probabily of contact on any layer) !!!! **this is probably the problem, that this is not correct**

1.0.6 SEIRS + testing

in fact, we use the variant with testing, where I_d states has their own probs, TODO rewrite formulas

```python
propensities[("S", "S_s")] = model.false_symptoms_rate*(model.X == "S")

#   "S" -> "E"
numI = model.current_state_count(
    "I_n") + model.current_state_count("I_a") + model.current_state_count("I_s")

S_to_E_koef = (
    model.p * (
        model.beta * numI +
        model.q * model.beta_D * model.current_state_count("I_d")
    ) / model.current_N()
    +
    (1 - model.p) * np.divide(
        model.beta * numContacts_I +
        model.beta_D * numContacts_Id, model.degree, out=np.zeros_like(model.degree), where
    )
)
propensities[("S", "E")] = S_to_E_koef * (model.X == "S")

propensities[("S_s", "S")
            ] = model.false_symptoms_recovery_rate*(model.X == "S_s")

# becoming exposed does not depend on unrelated symptoms
propensities[("S_s", "E")] = S_to_E_koef * (model.X == "S_s")

exposed = model.X == "E"
propensities[("E", "I_n")] = model.asymptomatic_rate * \
    model.sigma * exposed
propensities[("E", "I_a")] = (
    1-model.asymptomatic_rate) * model.sigma * exposed

propensities[("I_n", "R_u")] = model.gamma * (model.X == "I_n")

asymptomatic = model.X == "I_a"
propensities[("I_a", "I_s")
            ] = model.symptoms_manifest_rate * asymptomatic

symptomatic = model.X == "I_s"
propensities[("I_s", "R_u")] = model.gamma * symptomatic
propensities[("I_s", "D_u")] = model.mu_I * symptomatic

detected = model.X == "I_d"
propensities[("I_d", "R_d")] = model.gamma_D * detected
propensities[("I_d", "D_d")] = model.mu_D * detected
```

```python
# testing  TODO
propensities[("I_a", "I_d")] = (
    model.theta_Ia + model.phi_Ia * numContacts_Id) * model.psi_Ia * asymptomatic

propensities[("I_s", "I_d")] = (
    model.theta_Is + model.phi_Is * numContacts_Id) * model.psi_Is * symptomatic

propensities[("E", "I_d")] = (
    model.theta_E + model.phi_E * numContacts_Id) * model.psi_E * exposed
```

2 Engine

2.1 Seirsplus implementation

```python
t = 0
while True:
    propensities = calculate_propensties()
    alpha = propensities.sum()
    r = rand()
    # Compute the time until the next event takes place
    tau = (1/alpha) * log(float(1/r))
    t += tau
    # Compute which event takes place
    transition_node, transition_type = select(propensities)
    # Update node states and data series
    update_states(transition_node, transition_type)
```

On Hodonin there are 4500 events per day on average. So propensities are recalculated 4500 times every day.

2.2 Experimental *"daily"* implementation

```python
t = 0
todo_list = []
while True:
    propensities = calculate_propensties()
    alpha = propensities.sum()
    r = rand()

    # Compute the time until the next event takes place
    tau = (1/alpha) * log(float(1/r))
    t += tau

    # Compute which event takes place
    transition_node, transition_type = select(propensities)
```

```
    todo_list.append((transition_node, transition_type))

if day_changed:
    # Update node states and data series
    for transition_node, transition_type in todo_list:
        update_states(transition_node, transition_type)
```

The second implementation is much faster, now waiting for results on Hodonin to be able to compare the two implementations.

Implementation hack: Append to todo_list is done only if node is not yet in todo list (node can change state only once per day). I.e. if (node_5, (S->E)) and (node_5, (S->S_s)) are selected during the day, only the first one is considered. It is not possible to do both, because node_5 is no more in state S, the second transition is not applicable.

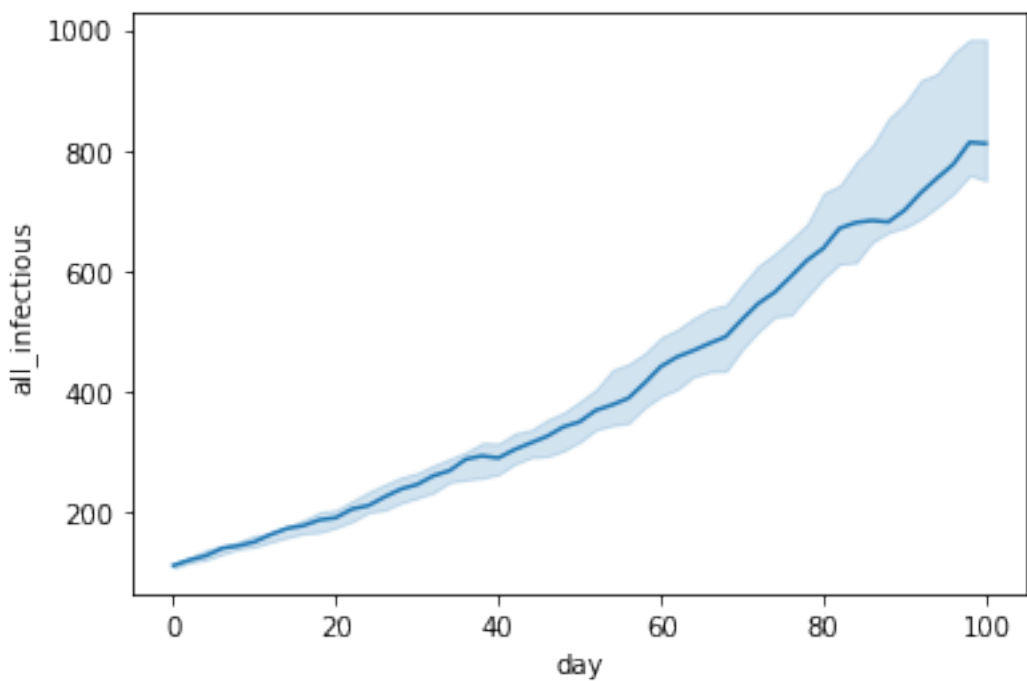### 2.2.1 Difference between original implementation and daily implementation

With policy function (detected nodes go to quarrantine): (top original, bottom
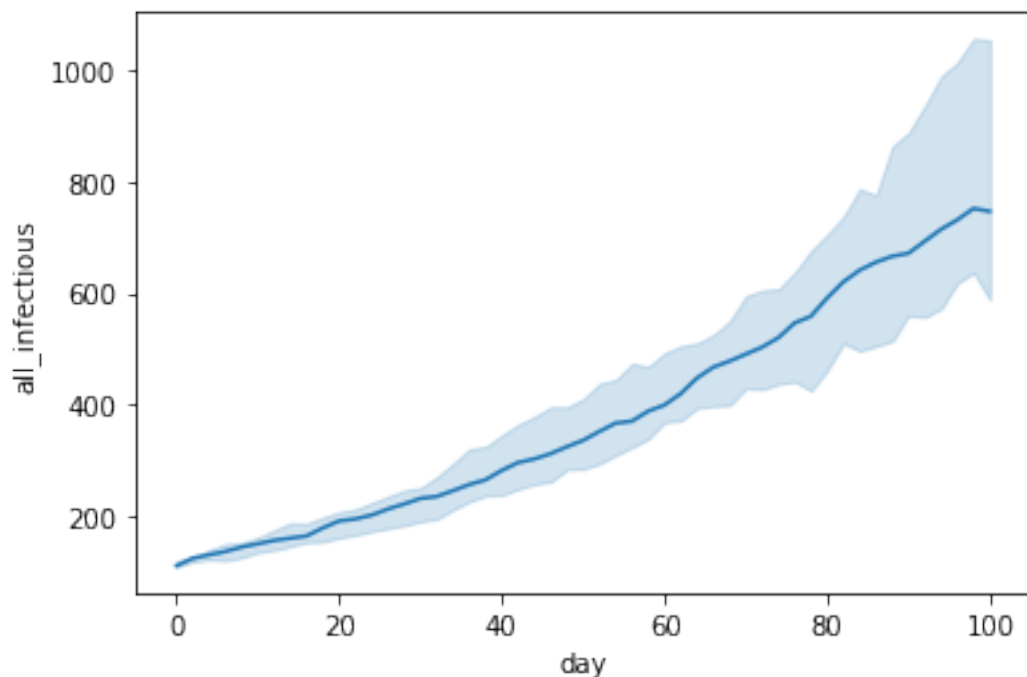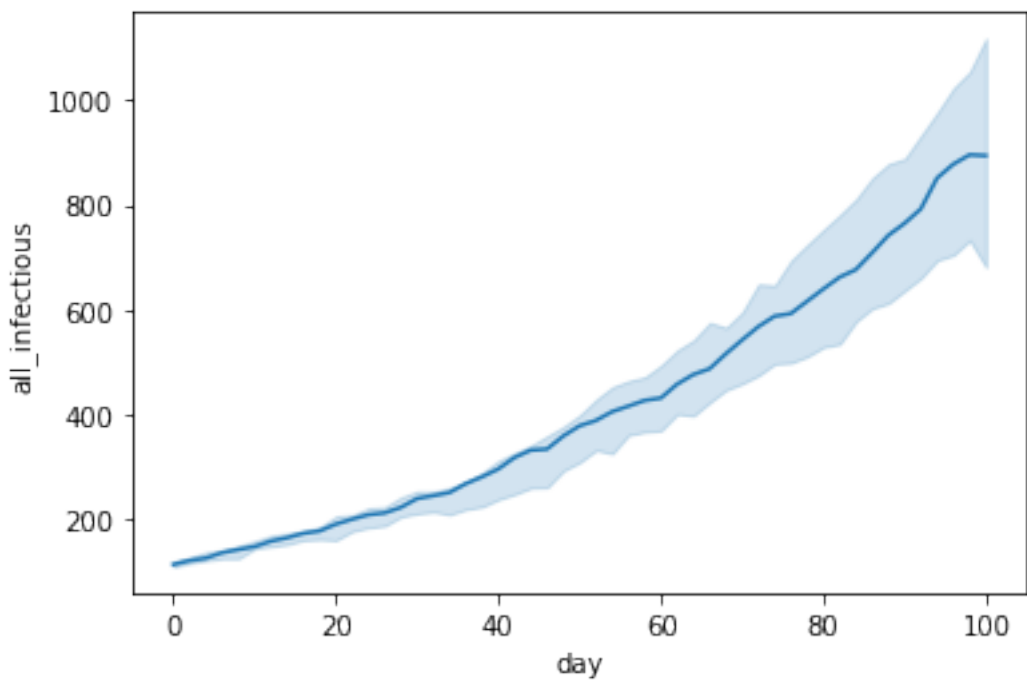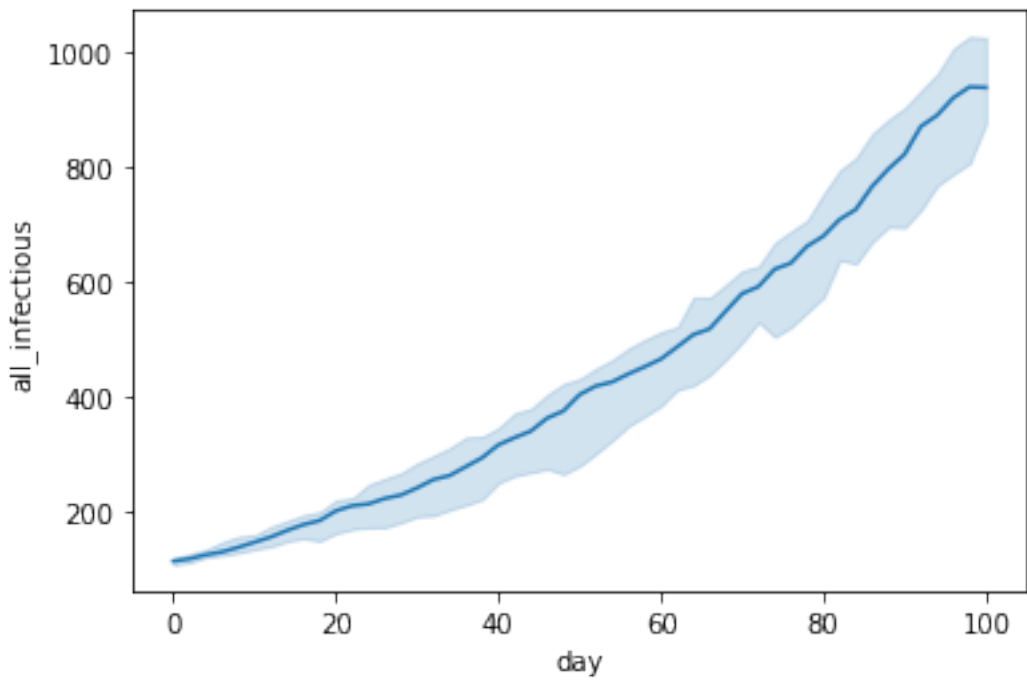

daily)

With no policy function (no quarrantine): (top original, bottom daily)

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