model

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1 Extended Network Model

1.0.1 States

$S_s, S, E, I_n, I_a, I_s, I_d, R_d, R_u, D_d, D_u$

1.0.2 Transitions

$S \to S_s$

$S \to E$

$S_s \to S$

$S_s \to E$

$E \to I_n$

$E \to I_a$

$I_n \to R_u$

$I_a \to I_s$

$I_s \to R_u$

$I_s \to D_u$

$I_s \to I_d$

$I_d \to R_d$

$I_d \to D_d$

$I_a \to I_d$

$E \to I_d$

1.0.3 Seirsplus propensity

$$P[X_i = S \to E] = \left[p\frac{\beta I}{N} + (1-p)\frac{\beta \sum_{j \in C_{G(i)}} \delta_{X_j = I}}{|C_{G(i)}|} \right] \delta_{\{} X_t = S\}$$

where I is a number of infected, N total number of living individuals, β rate of transmission (may be individual for each node), $\delta_{X_j=I}$ is 1 if $X_j = I$, 0 otherwise, X_i state of individual i, $C_{G(i)}$ is a set of close contacts (nodes j, that edge (i, j) is in the given graph G).

1.0.4 Extended propensity

We use the same formula for $P[X_i = S- > E]$ with these modifications:

- I is the total number of I-states, i.e. sum of I_n, I_a, I_s, I_d
- $\delta_{X=I} = 1$ if and only if $X \in \{I_n, I_a, I_s, I_d\}$
- edges has weights
- $|C_{G(i)}|$ is not the number of edges from i, but the sum of their weights (!there is only one edge between (i,j) in G)
- $\sum_{j \in C_{G(i)}} \delta_{X_j=I}$ is replaced by $\sum_{j \in C_{G(i)}} w_{(i,j)} \delta_{X_j=I}$

1.0.5 Constraction G from G_multi

Graph G_{multi} may contain more edges between i, j. Each edge has type t and subtype s and weight $w_{i,j,t,s}$ (intensity).

Graph G has max one edge (i, j) between nodes i, j. Edge as weight $w_{i,j}$.

$w_{i,j,t} = \sum_s w_{i,j,t,s}$ (sum over intensities of sublayers)

Weight $w_{i,j} = 1 - \prod_t (1 - w_{i,j,t})$ (weights on layers t are taking as probabilities of contact on that layer and are the final weight is probabily of contact on any layer) !!!! **this is probably the problem, that this is not correct**

1.0.6 SEIRS + testing

in fact, we use the variant with testing, where I_d states has their own probs, TODO rewrite formulas

```
propensities[("S", "S_s")] = model.false_symptoms_rate*(model.X == "S")

#  "S" -> "E"
numI = model.current_state_count(
    "I_n") + model.current_state_count("I_a") + model.current_state_count("I_s")

S_to_E_koef = (
    model.p * (
        model.beta * numI +
        model.q * model.beta_D * model.current_state_count("I_d")
    ) / model.current_N()
    +
    (1 - model.p) * np.divide(
```

```
        model.beta * numContacts_I +
        model.beta_D * numContacts_Id, model.degree, out=np.zeros_like(model.degree), where=
    )
)
propensities[("S", "E")] = S_to_E_koef * (model.X == "S")

propensities[("S_s", "S")
            ] = model.false_symptoms_recovery_rate*(model.X == "S_s")

# becoming exposed does not depend on unrelated symptoms
propensities[("S_s", "E")] = S_to_E_koef * (model.X == "S_s")

exposed = model.X == "E"
propensities[("E", "I_n")] = model.asymptomatic_rate * \
    model.sigma * exposed
propensities[("E", "I_a")] = (
    1-model.asymptomatic_rate) * model.sigma * exposed

propensities[("I_n", "R_u")] = model.gamma * (model.X == "I_n")

asymptomatic = model.X == "I_a"
propensities[("I_a", "I_s")
            ] = model.symptoms_manifest_rate * asymptomatic

symptomatic = model.X == "I_s"
propensities[("I_s", "R_u")] = model.gamma * symptomatic
propensities[("I_s", "D_u")] = model.mu_I * symptomatic

detected = model.X == "I_d"
propensities[("I_d", "R_d")] = model.gamma_D * detected
propensities[("I_d", "D_d")] = model.mu_D * detected

# testing  TODO
propensities[("I_a", "I_d")] = (
    model.theta_Ia + model.phi_Ia * numContacts_Id) * model.psi_Ia * asymptomatic

propensities[("I_s", "I_d")] = (
    model.theta_Is + model.phi_Is * numContacts_Id) * model.psi_Is * symptomatic

propensities[("E", "I_d")] = (
    model.theta_E + model.phi_E * numContacts_Id) * model.psi_E * exposed
```