

Notes

26 March 2024 07:40

Lecture Outline:

Lecture Plan

1. RNN Language Models (25 mins)
2. Other uses of RNNs (8 mins)
3. Exploding and vanishing gradients (15 mins)
4. LSTMs (20 mins)
5. Bidirectional and multi-layer RNNs (12 mins)

- Final Projects
 - Next Thursday: a lecture about choosing final projects
 - It's fine to delay thinking about projects until next week
 - But if you're already thinking about projects, you can view some info/inspiration on the website. It's still last year's information at present!
 - It's great if you can line up your own mentor; we also lining up some mentors

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Simple RNN-based Language Model: Recap

1. The Simple RNN Language Model

output distribution
 $\hat{y}^{(t)} = \text{softmax}(U h^{(t)} + b_y) \in \mathbb{R}^{|\mathcal{V}|}$

hidden states
 $h^{(t)} = \sigma(W_h h^{(t-1)} + W_e e^{(t)} + b_h)$
 $h^{(0)}$ is the initial hidden state

word embeddings
 $e^{(t)} = E x^{(t)}$

words / one-hot vectors
 $x^{(t)} \in \mathbb{R}^{|\mathcal{V}|}$

Note: This input sequence could be much longer

Training an RNN-based LM:

- Dataset: A big corpus of words
- Model: RNN
 - Feed a set of words (sentence if you will) to the model
 - Model predicts probability distribution (of next word) over the corpus
- Loss function:
 - Cross entropy between GT prob of next word and Pred prob at each time step
 - Total loss in one iteration: Avg. Of loss at each time step

Training an RNN Language Model

Loss $\rightarrow J^{(1)}(\theta) + J^{(2)}(\theta) + J^{(3)}(\theta) + J^{(4)}(\theta) + \dots = J(\theta) = \frac{1}{T} \sum_{t=1}^T J^{(t)}(\theta)$

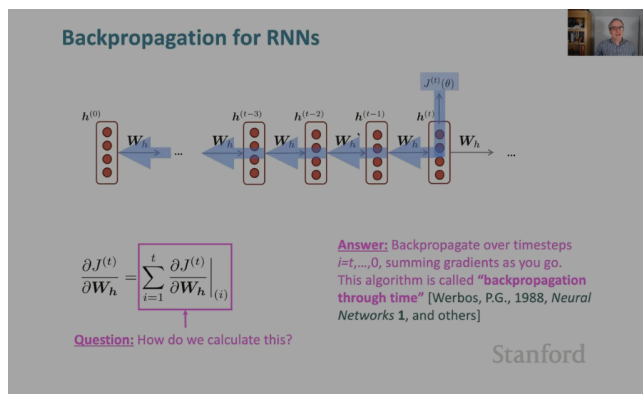
Predicted prob dists $\hat{y}^{(1)}, \hat{y}^{(2)}, \hat{y}^{(3)}, \hat{y}^{(4)}$

Corpus \rightarrow the students opened their exams

Teacher forcing

- Teacher Forcing:
 - Calculating loss at each time step allows model to predict only the next word.

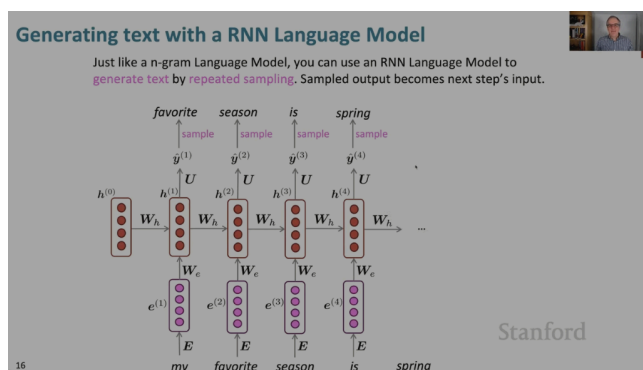
- Another way could be: Give model couple of words as input e.g. "the students" and let the model finish the sentence. The loss can be calculated over the sentence vs only one word.
- Backpropagation and Gradient for RNNs:
 - (if it is not clear until now) There is only one/shared weight matrix W_h .
 - However (downstream) gradient at each timestep t will be different as upstream (gradient) is different.
 - What to do? Sum all the gradients at all timesteps and apply all of them at once (Do not chain the updates as during forward pass each W_h was used as a separate matrix)



Other Uses of RNNs:

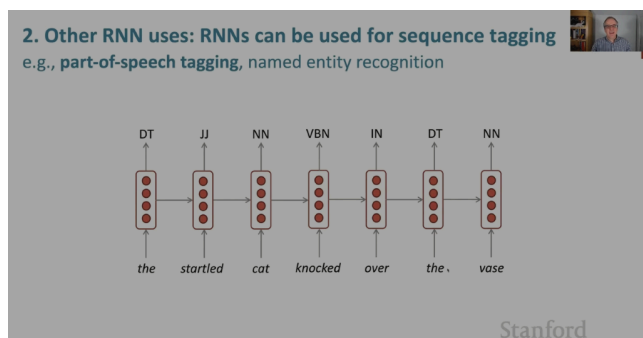
Text Generation:

- Notice how output at time t is being fed back as input of time $t+1$.



Sequence Tagging:

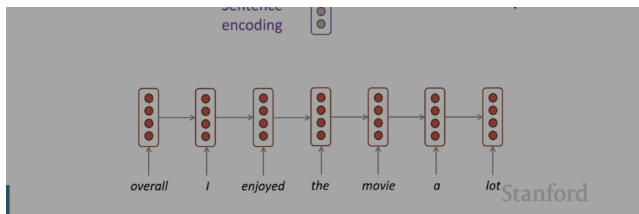
- Assigning Part of speech to each word in the sentence



Sentiment Analysis:

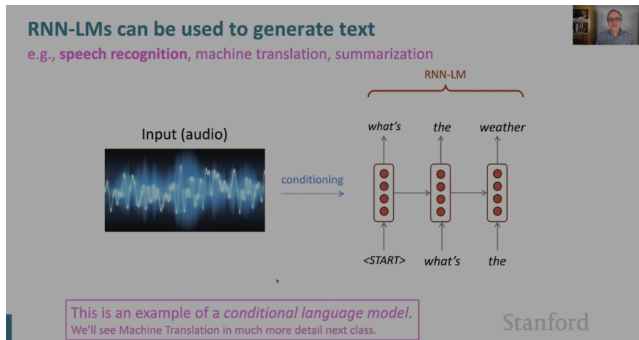
- Using RNN to get encoding of sentence and use a classifier layer to get a score





Speech-to-Text/Text Generation:

- Using a NN as conditioning layer (to transform audio signal into embedding vectors)



Evaluating RNN LM:

Perplexity:

- Standard eval metric.
- Geometric representation of inverse probability.
- Indicates how well the model predicted the next word? In Ideal case, the model should have perplexity of 1.
- It is a unitless measure. Ranging from 1 to positive inf.
- e.g. perplexity value of 53 sort of means that model is choosing the next word from 53 near equiprobable words (out of all output prob. Values 53 values are very close to each other) -- representing model's uncertainty.

Evaluating Language Models

- The standard evaluation metric for Language Models is **perplexity**.

$$\text{perplexity} = \prod_{t=1}^T \left(\frac{1}{P_{\text{LM}}(\mathbf{x}^{(t+1)} | \mathbf{x}^{(1)}, \dots, \mathbf{x}^{(t)})} \right)^{1/T}$$

Normalized by number of words

Inverse probability of corpus, according to Language Model

- This is equal to the exponential of the cross-entropy loss $J(\theta)$:

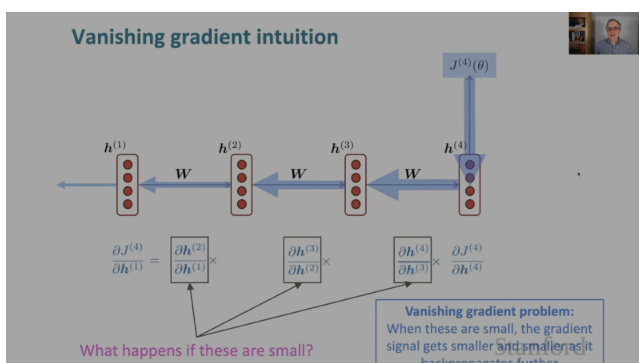
$$= \prod_{t=1}^T \left(\frac{1}{y_{x_{t+1}}^{(t)}} \right)^{1/T} = \exp \left(\frac{1}{T} \sum_{t=1}^T -\log y_{x_{t+1}}^{(t)} \right) = \exp(J(\theta))$$

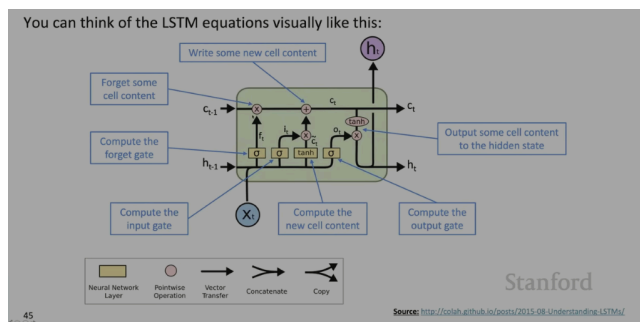
Lower perplexity is better!

Gradient Problems: Vanishing and Exploding

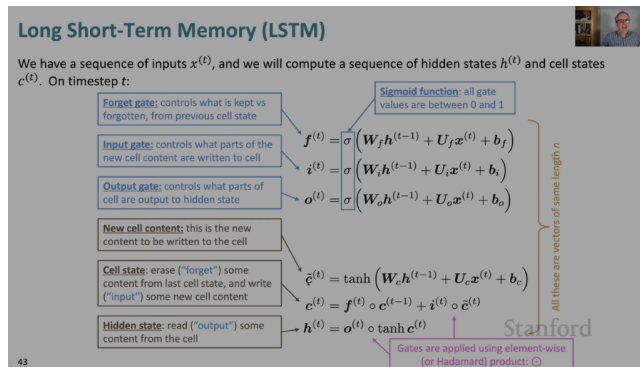
Vanishing Gradients:

- No update at all to the model weights.





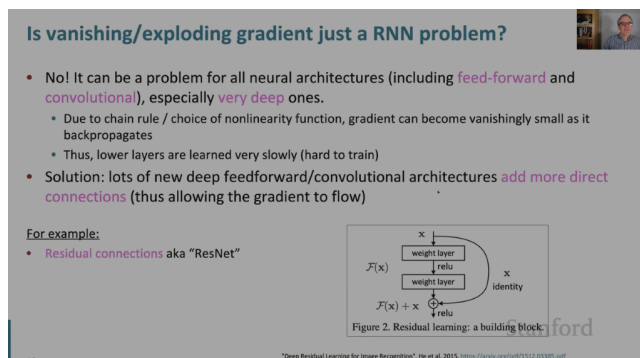
- Mathematical representation of LSTM Block



- Key difference to simple RNNs:
 - In LSTM: Not all is changed (added/forgotten) in each iteration
 - When new information is added to hidden states (in simple RNN) it is added by multiplication vs addition when new information is added to Cell states in (LSTMs)
 - In RNNs – multiplication carries out drastic changes vs in LSTMs addition carries out gradual changes
 - This makes retaining information lot easier for LSTMs
- How LSTMs help to control/reduce vanishing gradients problem?
 - By controlling rate of change of information in cell states, LSTM create a longer term version of short term memory
 - This prevents frequent changes to hidden states allowing upstream gradient to flow for until timestamp 0 for longer duration of time

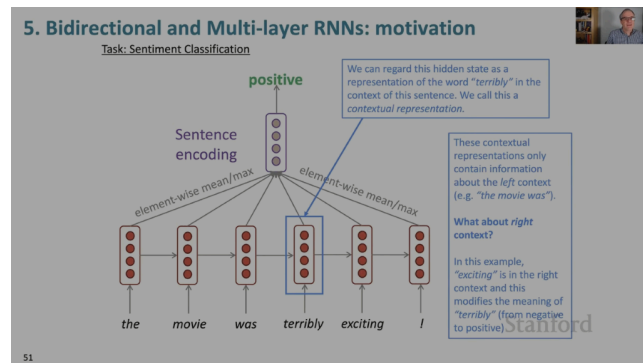
Vanishing/Exploding Gradients in general DNN:

- Not only RNN specific. Every Deep Network suffers from such issues due to chaining the upstream gradient for longer depths
- Solution:



Bi-directional and Multi-layer RNNs:

- Adding bi-directional context to RNNs: not only left context (from words on the left/previous words) but also right context (from words on the right of the current word)
- Only applicable when you have access to entire sentence e.g. when in sentiment analysis. Not applicable in e.g. language



- How?? -- Add a second backward RNN and concatenate both RNN's hidden states

