# Manual for:

# ZICS: a Windows and Matlab application for Zero-Information Closure Scheme

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This document presents the main features of ZICS application. The application employees the ZI-closure scheme [1, 2], a method to calculate the stationary probability distribution for stochastic reaction networks. The application has also the ability to present the moment equations of stochastic networks.

The application is designed through Matlab's <sup>®</sup> app designer. It is a standalone Windows program. In order to run it, the user can double click the application (ZICS) icon; the application can be installed through the ZICS\_installer.exe file. Non-Windows users can use the application through Matlab <sup>®</sup> 2016b or later by running the zi\_closure\_scheme.mlapp file.

In order to demonstrate the application's aspects and capabilities, we'll use Wilhelm's stochastic reaction network [3] as an example. Wilhelm's network is a two-component non-linear model presented in table 1.

Table 1: The table shows the reactions for Wilhelm's bistable model and its kinetic constants. The network is used as an example to explain the application components.

Wilhelm's Reaction Network	Kinetic constants
$Y \xrightarrow{k_1} 2X$	$k_1 = 35$
$2X \xrightarrow{k_2} X + Y$	$k_2 = 1$
$X + Y \xrightarrow{k_3} Y$	$k_3 = 1$
$X \xrightarrow{k_4} \emptyset$	$k_4 = 9.74$
$\emptyset \xrightarrow{k_5} X$	$k_5 = 30$

# 1 Input the network

In order to start solving the system, the user needs to input the reaction network and the kinetic constants into the application. The network is represented by the stoichiometric matrices for the reactants and products. Each reaction should be an irreversible reaction. Figure 1 presents the starting tab ("Input for Reaction Network") of the application.

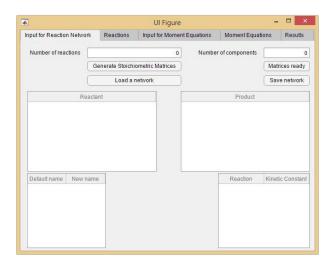


Figure 1: First tab of the ZICS app.

The number of reactions and components are the first options to be defined. Each reaction represents an irreversible reaction, thus a reversible reaction is represented as two separate ones. The number of components includes both the reactants and products. For the network at table 1, the number of reactions is 5 and components 2 (X and Y). The user can insert the number of reaction in the top left box and the number of components in the top right (figure 2).

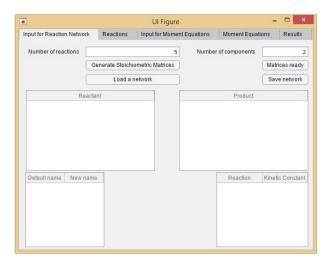


Figure 2: The number of reactions (5) denoted at top left box and the number of components (2) at the top right box.

After the number of components and reactions have been specialized, the user can create the

reaction network. The user should press the "Generate Stoichiometric Matrices" button and the application creates blank matrices for the reactants, products, name of components and kinetic constants (figure 3).

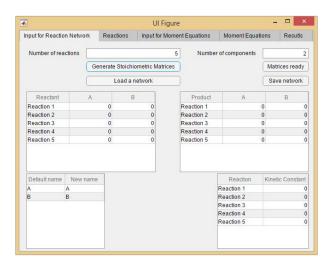


Figure 3: The application creates blank matrices for the network after the "Generate Stoichiometric Matrices" button is pressed.

The user can now start inputing the reaction network. The user can first denote the stoichiometric matrix for the reactants in the top left table with the "Reactant" indicator. The columns of the table denote the different components and the row the reaction of the network. In this case, we have two columns for the two components and five rows for the five reactions. We'll use column A for component X and column B for component Y. From table 1, it is easy to see that there are no molecules of X and 1 molecule of Y involved in the left side of the reaction. Thus, the first row-first column box has 0 and the first row-second column has 1. At the second reaction, 2 molecules of X and none of Y react. So the second row-first column box has 2. Following a similar procedure the user can fill the rest of the reactants table (figure 4).

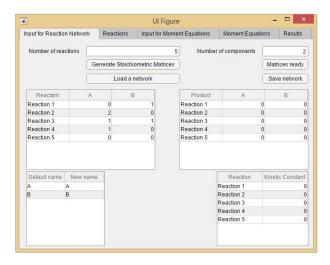


Figure 4: The reactants stoichiometric table (top left) is filled. Each row represents a reaction and each column a component. The table is filled according the reactions of table 1. Column A is used for component X and column B for component Y.

Similarly, the user can input the stoichiometric matrix for the products in the top right table with the "Product" indicator. Each row of the table represents a reaction. The order of the reactions does not affect the solution, however each row of the reactants and products matrices should represent the same reaction. The columns of the table represent the components. In this case, column A refers to component X and column B to component Y. Again, the pairing of columns and components does not influence the final result, however each column of the reactants and products matrices should represent the same component. For the reaction network presented at table 1, the first reaction produces two molecules of X and zero molecules of Y. Thus, the first row-first column box is filled with 2 and the first row-second column with 0. The second reaction produces one molecule of X and Y, hence the second row-first column box is filled with 1 (for X) and the second row-second column box has also 1 (for Y). With the same strategy, the rest of the products stoichiometric matrix can be filled (figure 5). At this point the reaction network has been fully defined and the user can input the reaction kinetic constants.

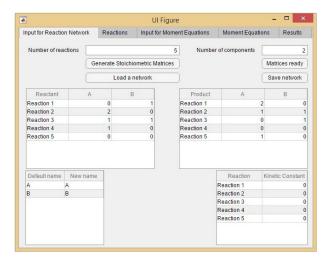


Figure 5: The products stoichiometric table (top right) is filled. Each row represents the same reaction and each column the same component as in the reactants stoichiometric matrix. The table is filled according the reactions of table 1.

The reaction constants can be inputted in the bottom right table indicated with "Kinetic Constant". The table has one row representing the value of the kinetic constants and multiple rows, one for each reaction. Each row should represent the same reaction as in the stoichiometric matrices for products and reactants. Based on table 1, the first element of the table should 35 (for the kinetic constant of the first reaction), the second 1, the third 1 etc. (figure 6).

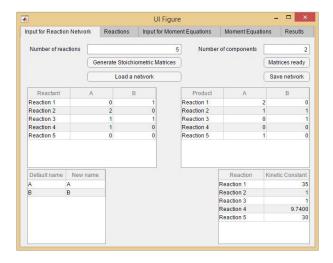


Figure 6: The kinetic constants table (bottom right) has been filled. Each row represents the same reaction as in the stoichiometric tables for the reactants and products. The value of the kinetic constants is based on table 1.

Finally, the application gives the ability to the user to rename the reactions components. The default option is the letters of the alphabet. The user can rename the components at the bottom left table. In this example, component A represents X so it is renamed as X and component B as Y, as shown in figure 7.

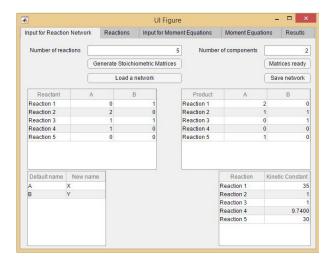


Figure 7: At the bottom left table, the user can rename the components. A and B represent X and Y, respectively.

The user has also the ability to save the network. The "Save network" button saves the network in a matlab .mat format. The application can load the previously saved networks with the "Load a network" button. This function allows to load sbml files (.xml) as a .tsv format. In order to first transform the .xml files to .tsv the user is directed to free available website https://rumo.biologie.hu-berlin.de/SBtab/default/converter.

After, the network, the kinetic constants and the name of the reactants have been inputted the user can move on by pressing "Matrices Ready" button. The user has the ability to check the form of the network at the second tab ("Reactions"), as shown figure 8. If there is an error in the network, the user can go back to the previous tab ("Input for Reaction Network") and make the appropriate changes as described above. If changes in the "Input for Reaction Network" tab has been made, the user should press the "Matrices Ready" button to make them final and apply them for the rest of the application.

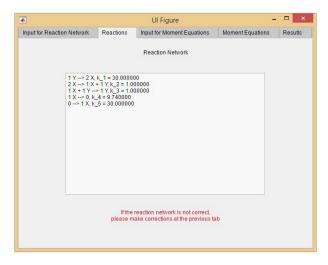


Figure 8: At the second tab named "Reactions" the user can check the form of the network. In case, an error has occurred the user can go back to the previous tab "Input for Reaction Network" and make the appropriate changes.

# 2 Simulation parameters

After the input of the reaction network and pressing the "Matrices ready" button, the user can enter the simulation parameters in order to solve the system. Simulation parameters can be entered at the third tab (named "Input for Moment Equations" as shown in figure 9). More details about the code of the application can be found in the supplementary material of the article and the book chapter [4]. The code of the application can be found at (zi\_closure\_scheme.mlapp) and be opened through Matlab <sup>®</sup>, version 2016b or later.

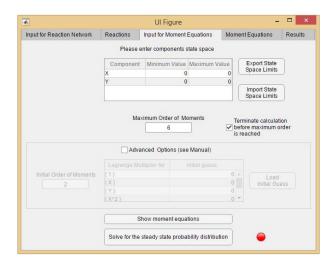


Figure 9: The simulation parameters can be entered at the "Input for Moment Equations" tab.

The user can first specify the state space of the system. The state space of the system indicates the minimum and maximum number of molecules for each component. ZICS application solves stochastic reaction networks numerically and thus the state space of system should be indicated by the user and cannot be infinite. In the application, the state space is represented as a table (figure 9). Each row represents each of the components. There are two columns, one for the minimum value of the state space and one for the maximum value.

It is suggested that the minimum value of each component is 0. The maximum value can vary per system and component. If the maximum value is less than the actual value, the application will produce inaccurate results, since it was not allowed to perform calculation in the whole necessary space. It is suggested that the maximum value is slightly higher than the actual value so that the application can perform calculations at the whole state space. There are two common approaches in case the user does not have a good educated guess about the maximum value. The first is to input an arbitrarily high numerical value. This can ensure accurate results, however the computational time required to produce results increases with the values of the state space. Thus, this solution can be computationally costly. An alternative way is to solve the system with a relatively average numerical value and then solve the the system with a higher maximum value and compare the two solutions. The final correct solution of the network should be independent of the state space values. For this example, we chose to use 50 molecules as the maximum value for component X and 40 for component Y as shown in figure 10. The user is the ability to save the state in a Matlab .mat format by pressing the "Export State Space Limits" button and load them again by pressing the "Import State Space Limits" button.

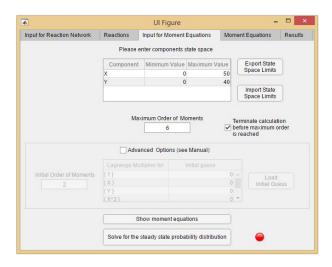


Figure 10: The state space for component X is between 0 and 50 and for component Y is from 0 to 40.

After the state space is specified, the user can enter the maximum order of moments. The application solves moment equations and the number of moments can change the size of the equations solved and thus the accuracy of the method. The maximum order of moments can be entered at the homonymous box (figure 9). For the majority of networks tested, an order of 6 moments is enough. The application has the ability to dynamically change the number of moments and test the accuracy of the results. Thus, the application can terminate the calculations before the maximum number of moments is reached if the solution meets the desired accuracy. This mode is automatically enabled. If desired, the user can disable this feature and force the application to perform calculations until the maximum number of moments is reached, by unselecting the box indicated as "Terminate calculation before maximum order is reached". It is suggested that the user inputs a high number of maximum moments and keeps the feature enabled. For this example, we chose that 8 order of moments is large enough (figure 11).

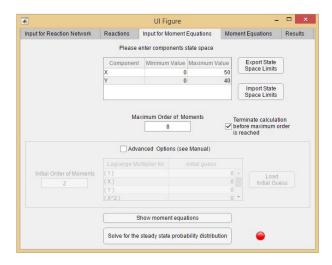


Figure 11: The maximum order of moments can be modified. The application has the ability to terminate calculations before this number is reached. In this case, the maximum order of moments was changed to 8.

With the order of moments and state space specified, the application is ready to produce results. The application calculates the stationary probability distribution for each component and their stationary probability moments. In order to start the calculations, the user should press the "Solve for the steady state probability distribution" button. Every time changes are performed in the "Input for Moment Equations" tab, the "Solve for the steady state probability distribution" button should be pressed to apply those changes. There is a lamp next to this button that indicates the status of the calculations. Before or during the calculations, the light of the lamp is red (figure 11). The light becomes green when the program has finished running and the stationary probability distribution for all the components of the network have been calculated (figure 12).

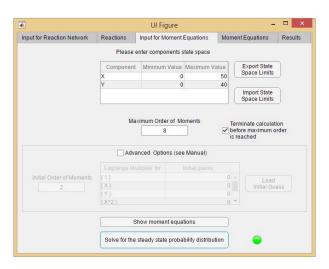


Figure 12: Calculations start when the "Solve for the steady state probability distribution" button is pressed. When the lamp next to the button is green, the calculations have finished.

#### 2.1 Advanced options

ZICS application is using Zi-closure scheme's Newton-Raphson algorithm. As such, the program requires an initial guess; the initial guess comes in the from of the initial number of moments and their associated lagrange multipliers. For more information about how the lagrange multipliers affect the algorithm of the application, the reader is directed to supplementary material of the article and the book chapter [4]. The default initial condition is a uniform distribution with second order of moments and zero lagrange multipliers. The user has the ability to change the initial guess of the program by checking the "Advanced options (see Manual)" box. In the advanced options section, the user can modify the initial order of moments, the initial guess for lagrange multipliers and also load an initial guess (by pressing the "Load Initial Guess" button). It is encouraged this section to mainly be used by experienced users.

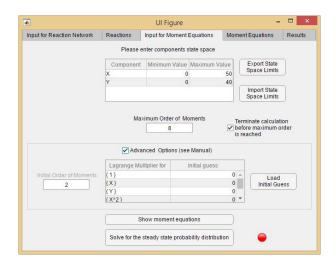


Figure 13: The user can input an initial guess for the algorithm by checking the "Advanced options (see Manual)" box.

### 3 Results

## 3.1 Stationary probability distribution

The results of the application are displayed at the last tab named "Results" (figure 14). The stationary probability distribution for the first component is automatically plotted at the top center. The x-axis represents the number of molecules of the component and the y-axis the probability. The plot can be exported by pressing the "Save plot" Button in multiple formats (.fig, .jpg, .png, .eps). Below the plot, the stationary values of the moments as well as their Lagrange multipliers are presented. The results can be saved in a Matlab (.mat) or spreadsheet (.xlsx) format by clicking the "Export Results" button. There is also the option to save the stationary lagrange multipliers in a matlab (.mat) format. Their values can be used at the advanced options section (Section 2.1) for future runs.

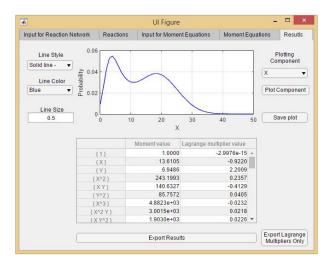


Figure 14: At the last tab named "Results" the user can find the solution of the network. The stationary probability distribution of the first component is automatically plotted. Additionally, the stationary moments and Lagrange multipliers are reported.

The user has the ability to plot the stationary probability distribution for all the components of the system. By clicking the "Plotting Component" drop-down menu, the user can select the desired component. In order to plot the new component, the "Plot Component" button should be pressed (figure 15). The user can also choose between four different line styles, seven colors and change the line size of the plot from the respective options at the left-hand side of the plot (figure 16). Again, to apply any changes the user should press the "Plot Component" button. Any plots can be saved in four different formats (.fig, .jpg, .png or .eps) by pressing the "Save plot" Button.

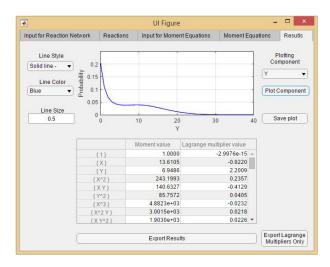


Figure 15: The "Plotting Component" drop-down menu gives the ability to plot different components. Here, the stationary probability distribution for component Y is plotted after the press of "Plot Component" button.

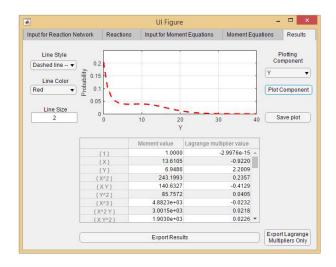


Figure 16: The user can modify the plot with the options of the left upper side and press the "Plot Component" button. Here, the "Line Style" is chosen to be dashed, the "Line Color" red and the "Line Size" 2.

#### 3.2 Moment equations

Aside from calculating the stationary probability distribution of stochastic networks, the application also calculates the moment equations and its associated matrices. The moment equations are displayed at the "Moment Equations" tab, as shown in figure 17. In order for the matrices to appear, the "Show moment equations" button should be pressed at the "Input Moment Equations" tab (figure 12). This function is independent of the function that calculates the stationary probability distributions. The user can calculate the moment equation without solving the system. The moment equations can be exported in a matlab (.mat) or spreadsheet (.xlsx) format by clicking the "Export Matrices" button.

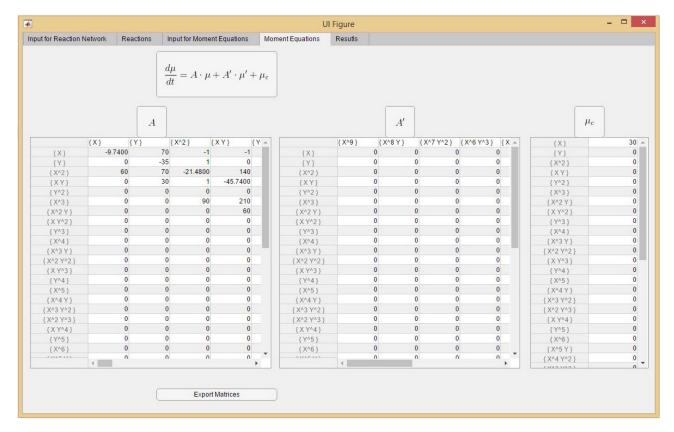


Figure 17: Moment equations matrices are displayed at the "Moment Equations" tab. This function is possible by pressing the "Show moment equations" button at the "Input Moment Equations" tab and independent of the function that calculated the stationary probability distribution.

# Bibliography

- [1] Patrick Smadbeck and Yiannis N Kaznessis. A closure scheme for chemical master equations. *Proceedings of the National Academy of Sciences of the United States of America*, 110(35):14261–5, aug 2013.
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