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Introduction

In computer science, a disjoint-set data structure, also called a union-find data structure or merge-find set, is a data structure representing a dynamic collection of sets $S = \{S_1, \dots, S_r\}$. Given an element u , we denote by S_u the set containing u . Each set is identified by a representative, which is some member of the set. It supports three useful operations:

- MAKE-SET(x): creates a new set whose only member (and thus representative) is x . Since the sets are disjoint, we require that x not already be in some other set.
- UNION(x, y): unites the dynamic sets that contain x and y , say S_x and S_y , into a new set that is the union of these two sets. The representative of the resulting set is any member of this new set.
- FIND-SET(x): returns a pointer to the representative of the set containing x .

Implementation

This C implementation of Disjoint Set operations are based on trees for a faster implementation of disjoint sets. Here, we represent sets by rooted trees, with each node containing one member and each tree representing one set. In a disjoint-set forest, each member points only to its parent. The root of each tree contains the representative and is its own parent. Methodology used is union-by-rank heuristics.

Methodology

To implement a disjoint-set forest with the union-by-rank heuristic, we must keep track of ranks.

- With each node x , we maintain the integer value $\text{rank}[x]$, which is an upper bound on the height of x (the number of edges in the longest path between x and a descendant leaf).
- When a singleton set is created by MAKE-SET, the initial rank of the single node in the corresponding tree is 0.
- Each FIND-SET operation leaves all ranks unchanged.
- When applying UNION to two trees, we make the root of higher rank the parent of the root of lower rank.
- In case of a tie, we arbitrarily choose one of the roots as the parent and increment its rank, we assign the parent of node x by $p[x]$.
- The LINK procedure, a subroutine called by UNION, takes pointers to two roots as inputs.

Program

This program is implemented to accept only integer type of data as dynamic set elements. The maximum number of singleton set is limited to 7.

Variables (Global)

- > parent - an integer array to store the parent of each node x .
> rank - an integer array to store the rank of each node x .

Functions

- > makeSet(x) - Creates a tree with just one node with only one member x (and thus the representative).
> findSet(x) - This is a recursive function. We perform a findSet operation by chasing parent pointers until we find the root of the tree and returns its pointer, which is the representative.
> unionSet(x, y) - A unionSet operation causes the root of one tree to point to the root of the other.

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*****/
#include <stdio.h>

int parent[7];
int rank[7];

void makeSet(int x)
{
    parent[x] = x;
    rank[x] = 0;
}
int findSet(int x)
{
    if(x != parent[x])
        parent[x] = findSet(parent[x]);
    return(parent[x]);
}
void link(int x, int y)
{
    if(rank[x] > rank[y])
        parent[y] = x;
    else
    {
        parent[x] = y;
        if(rank[x] == rank[y])
            rank[y] = rank[y] + 1;
    }
}
void unionSet(int x, int y)
{
    x = findSet(x);
    y = findSet(y);
    link(x, y);
}
int main()
{
    int i;
    makeSet(0);
    makeSet(1);
    makeSet(2);
    makeSet(3);
    makeSet(4);
    makeSet(5);
    makeSet(6);
    //printf("%d", findSet(1));
    unionSet(0, 1);
    //printf("%d", findSet(0));
    unionSet(1, 2);
    //printf("%d", findSet(2));
    unionSet(3, 4);
    //printf("%d", findSet(3));
    unionSet(5, 6);
    //printf("%d", findSet(5));
    unionSet(4, 5);
    //printf("%d", findSet(3));
    unionSet(2, 6);
    //printf("%d", findSet(5));
    for(i=0;i<7;i++)
    {
        printf("Parent of %d is %d.",i,parent[i]);
        printf("Rank of %d is %d.\n",i,rank[i]);
    }
    return 0;
}

```

