Achievable virtual system.
Looking at force as input and disp. as satput
relative degree 4 (or more)
Have Hzw + (HzwHuw) (highest possible for causality) Listen to belocity
L'relative degree 2 (Newton's laur)
Li. relative degree 2.
From fora to belocity
From fora to velocity 8 HAVS: relative degree 1 - OK for passivity
: 3=0 is a zero-needed so that
constant fire does
not produce a velocity.
Other requirements on H":
1. Has factor (S+25WS+W2) in the close to HDVS
To H.
denominator
denominator 2. $H^{AVB}(\delta) = \frac{1}{V^S}$
$2. H^{AVB}(\delta) = \frac{1}{14Ve}$
2. $H^{Avg}(\delta) = \frac{1}{K^{Vg}}$ 3. Relative degree of $(H^{AVS} - H_{ZW})$
2. $H^{Avg}(\delta) = \frac{1}{K^{VS}}$ 3. Relative degree of $(H^{AVS} - H_{zw})$ > relative degree H_{zu} , so that
2. $H^{Avg}(\delta) = \frac{1}{K^{Vg}}$ 3. Relative degree of $(H^{AVS} - H_{ZW})$

ST model

$$\dot{X} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & \frac{1}{m} \\ 0 & 0 & -k_{a} & -k_{a} \end{bmatrix} \times + \begin{bmatrix} 0 \\ 0 \\ 0 & 0 \end{bmatrix} \times + \begin{bmatrix} 0 \\ k_{a} \\ 0 & 0$$

The highest (deg(DV)+1) a terms of (const. N, - ND1) must be zero Ar Huw to be causal const = 1 for the highest power term to be o · let Dy = 3+0018 + ··· + 00 Ny = 8,300 + 8,-1,300-1+...+8 with a = yo $= (3^{n} + \alpha_{m-1} 3^{n-1} + \dots + \alpha_{0}) - (3+\beta) (3^{n-3} + \alpha_{n-4} 3^{n-4} + \dots + \alpha_{0})$ + 9Kh (2"-+2,-++ ... +2) (3+2(Ws+W) $= (3^n + \alpha_{n-1} S^{n-1} + \cdots + \alpha_0)$ Let the conditions be met for the highest (degree (Ov)+1)=(n-2) order terms to be zero What remains? (a28+ a, s+ a0)-

Going off on a different path

Want to see if actuator can have

force -> displacement causality.

$$\dot{F} = -\beta F + dx_v - ka\dot{x}$$

$$\dot{x}_v = -\alpha x_v + \alpha u_v$$

$$(S+\beta)F = \frac{dx}{8+\alpha}u_{v} - k_{\alpha}8x$$

$$\mathbb{O}\left[F = \frac{d\alpha}{(8+\alpha)(3+\beta)}u_{\nu} - \frac{k_{\alpha}s}{(8+\beta)}x\right]$$

alternatively,
$$2[X = \frac{d\alpha}{K_a s(s+\alpha)}u_v - \frac{s+\beta}{k_a s}F$$

Thun 1 becomes

$$F = \frac{d\alpha}{(3+\alpha)(s+\beta)} \frac{K_e u - \frac{d\alpha}{(3+\alpha)(s+\beta)}}{(3+\alpha)(s+\beta)} \frac{K_p F - \frac{k_{\alpha} S}{s+\beta} x}{\frac{c_{\beta} + \alpha}{(s+\alpha)(s+\beta)}} \frac{(1+\frac{d\alpha}{(s+\alpha)(s+\beta)}) F = \frac{d\alpha}{(s+\alpha)(s+\beta)} \frac{K_e S}{(s+\alpha)(s+\beta)} \frac{(k_{\alpha} S(s+\alpha) + d\alpha K_e)}{(s+\alpha)(s+\beta) + d\alpha K_e} \frac{K_{\alpha} S(s+\alpha) + d\alpha K_e}{(s+\alpha)(s+\beta) + d\alpha K_e}$$

$$X = \frac{(s+\alpha)(s+p) + d\alpha Kp}{K_{\alpha}s(s+\alpha) + d\alpha Ke} \omega + \frac{d\alpha Ke}{K_{\alpha}s(s+\alpha) + d\alpha Ke} \omega.$$

mHil control design with force -> displacement causality for the actuator

$$\dot{F} = -\beta F - k_{\alpha} \dot{x} + dx_{\nu}$$

$$\dot{x}_{\nu} = -\alpha x_{\nu} + \alpha u_{\nu}$$

Feedback: Uy = U-Kxx-KFF

$$\dot{F} = -\beta F - k_{\alpha}\dot{x} + dx_{\nu}$$

$$\dot{x}_{\nu} = -\alpha x_{\nu} + \alpha u - \alpha k_{x} x - \alpha k_{F} F$$

State transformation.

$$Z = F + kax$$
; then. $X = \frac{Z - F}{ka}$

$$\dot{z} = dx_y - \beta F$$

$$\dot{x}_y = -dx_y + \alpha u - \alpha \frac{K_x}{k_a} + \alpha \frac{K_x}{k_a} - K_F F$$

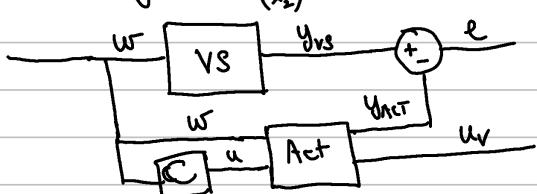
$$\left(\frac{\dot{z}}{\dot{x}_{v}}\right)^{2} = \left[-\alpha \frac{K_{x}}{k_{a}} - \alpha\right]\left(\frac{z}{x_{v}}\right) + \left[\alpha \left(K_{f} - \frac{K_{x}}{K_{a}}\right) \omega + \alpha\right] \omega$$

$$y = x = \frac{Z - F}{k_n} = \frac{Z}{k_n} + \frac{w}{k_n}.$$

$$y = \left[\frac{1}{K_{x}} \cdot O\right] \left(\frac{2}{X_{y}}\right) + \frac{1}{K_{x}} w^{-1}$$

$$y = \left[\frac{1}{K_{x}} \cdot O\right] \left(\frac{2}{X_{y}}\right) + \frac{1}{K_{x}} w^{-1}$$

VS model:



PASSIVITY OF THE ACTUATOR.

$$\dot{x} = U$$
 $\dot{x} = U$
 $\dot{x} = -\beta F - k_{\alpha}U + dx_{\gamma}$
 $\dot{x} = -\alpha x_{\gamma} + \alpha U_{\gamma}$
 $\dot{x}_{\gamma} = -\alpha x_{\gamma} + \alpha U_{\gamma}$
 $\dot{x}_{\gamma} = -\alpha x_{\gamma} + \alpha U_{\gamma} - k_{\alpha}U$
 $\dot{x}_{\gamma} = -\alpha x_{\gamma} + \alpha U_{\gamma} - \alpha K_{\gamma} - \alpha K_{\gamma}F$
 $\dot{x}_{\gamma} = -\alpha x_{\gamma} + \alpha U_{\gamma} - \alpha K_{\gamma} - \alpha K_{\gamma}F$
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 $\dot{x}_{\gamma} = -\alpha x_{\gamma} + \alpha U_{\gamma}$
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 $\dot{x}_{\gamma} = -\alpha U_{\gamma}$
 \dot{x}_{γ}

Not clear what I work before. Start from scratch.

$$SX = -\frac{(8+\beta)}{k_a}F + \frac{d}{k_a}X_V = -\frac{(3+\beta)}{k_a}F + \frac{dK}{k_a(3+\kappa)}U_V$$

$$\int X = -\frac{(s+\beta)}{k_a s} F + \frac{d\alpha}{k_a s(s+\alpha)} U_V$$

$$U_V = U - K_X X - K_F F$$

$$X = -\frac{(3+\beta)}{k_a s} + \frac{dx}{k_a s(s+\alpha)} - \frac{K_x dx}{K_a s(s+\alpha)} \times \frac{1}{k_a s(s+\alpha)}$$

$$\left[1 + \frac{K_{x} d\alpha}{k_{a} s(s+\alpha)}\right] \times = -\left[\frac{(s+\alpha)(s+\beta) + K_{x} d\alpha}{k_{a} (s+\alpha)}\right] + \frac{d\alpha}{k_{a} s(s+\alpha)}$$

$$X = -\frac{(3+\alpha)(3+\beta) + K_F d\alpha}{K_a 3(3+\alpha) + K_X d\alpha} + \frac{d\alpha}{K_a 3(3+\alpha) + K_X d\alpha}$$

NOTE: F=-w from equilibrium.

$$X = \frac{S^2 + (\alpha + \beta)S + \alpha(\beta + K_F d)}{K_A(S^2 + \alpha S + \frac{K_X d\alpha}{K_A})}w + \frac{d\alpha}{w}u$$

$$\chi = \frac{dx}{dx} u + \frac{N(s)}{k_x D(s)} w$$

$$= \frac{dx}{k_x D(s)} u + \frac{N(s)}{k_x D(s)} w$$

Try HXW of the form

① Want
$$H^{Avs}(o) = \frac{1}{Kvs}$$
 $\Rightarrow \frac{a_0 b_0}{K_x d \kappa \omega^2} = \frac{1}{Kvs}$
 $\Rightarrow \frac{a_0 b_0}{m_{vs}} = \frac{1}{m_{vs}}$

2) Want HAVS - Hxw to have relative degree 2. Neumerator of HAVS - Hxw

=
$$(s^2 + a_1 s + a_0)(s^2 + b_1 s + b_0) - (s^2 + (x + \beta) s + a(\beta + K + d))$$

 $(s^2 + 2 + 2 + a + b) - (s^2 + (x + \beta) + a(\beta + K + d))$

$$= \left[(a_1+b_1) - (25\omega + \alpha + \beta) \right]^3 + \cdots$$

$$\boxed{a_1+b_1 = 25\omega + \alpha + \beta}$$

3 Want 8.4 Ms to be positive real. Do m, m, -n, n, in Mathematica.
Do m, m, -n, n, in Mathematica.

Now go the other way. Inverting & F=- kas(sta) + Kxda x + da (sta)(stb)+Kxda v. Set w=-x (these signs must be considered/ justified more carefully based on what is input and what is autiful) Try HAVS to be of the form. $H^{AV3} = k_a \frac{(s^2 + 2j\omega s + \omega^2)(s^2 + a_1 s + a_0)}{[s^2 + (\alpha + \beta)s + \alpha(\beta + d + k_f)](s^2 + b_3 + b_0)}$ 1) Want HAVS(0)= kys => ka · cosa. = kys =) bo = ka (B+dK) ao

2) Want HAVS - HFW to have relative degree 2

Numerator =
$$(s^2 + 2y\omega + 3w^2)(s^2 + a_1s + a_0)$$

 $-(s^2 + \alpha + 3 + \frac{dk_x\alpha}{k_\alpha})(s^2 + b_1s + b_0)$
 $= s^3 [a_1 + 2y\omega - b_1 - \alpha] + \cdots$
 $\Rightarrow [b_1 = a_1 + 2y\omega - \alpha]$

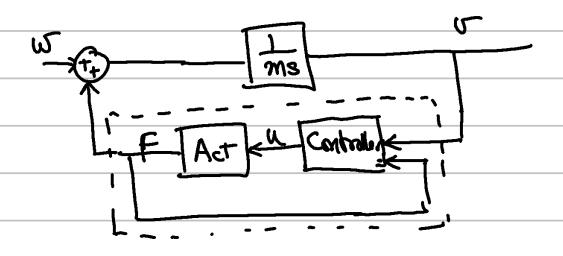
Want	I H'	vs to	be	positiv	e real.		
Compo	te m	mm	1172 U	ising	Mathem	atræa.	
•							

FOURTH ORDER CONTROLLER FOR Fin Dout case. $X = \frac{S^2 + (\alpha + \beta)S + \alpha(\beta + K_F d)}{K_{\alpha}(S^2 + \alpha S + \frac{K_{\alpha} d\alpha}{K_{\alpha}})} w + \frac{d\alpha}{k_{\alpha}(S^2 + \alpha S + \frac{K_{\alpha} d\alpha}{K_{\alpha}})}$ X = Hxu u+ Hxw w = dx u + N(s) w K, D(s) K, D(s) Try $H_{xw}^{M8} = \frac{(s^2 + a_1 s + a_0)(s^2 + b_1 s + b_0)(s^2 + c_1 s + c_0)}{k_a(s^2 + \alpha s + \frac{K_x d_w}{k_o})(s^2 + 2j\omega s + c_0)}$ 1) Want How (0) = Ivs = aoboco = Ivs =) aoboco = Kxda/ 2 Want Hxw-Hxw to be relative degree 2. Numerator of HAVS - HXW = (5+0,9+00)(5+b,9+b0)(5+c,5+c0) - (32+ (x+B)3+x(B+KFd))(52+2100+02)(52+d15+d0)

= [a, +b,+c,] 85 - [a+B+24w+d] 85+... 19,+b,+C, = x+B+250+d,

3) Want SHAVS to be PR. Do mine - nine in Mathematica

ACTUATOR-LEVEL SUBSTRUCTURING WITH FEEDBACK AND FEEDFORWARD



How is PR iff - Hope is PR. (act+cont)

Let Controller act on x instead of on v.

[basic idea is to act on x so that DC

force produces DC x (not DC v) and.

vice versa; in fact, if acting on v, to match

w-> x response of VS, Controller will have

an -s in it leading to internal stability problems

$$F = -\beta F - ka \dot{x} + d u_{V} \quad (ignoring trained dynamics)$$

$$F = -\frac{k_{u}s}{s+\beta} \times + \frac{d}{s+\beta} \quad u_{V}$$

$$U_{V} = -\frac{k_{u}s}{s+\beta} \times - \frac{k_{v}d}{s+\beta} \quad N_{v} \times - \frac{K_{F}d}{s+\beta} \frac{N_{F}}{D} F$$

$$F = -\frac{k_{u}s}{s+\beta} \times - \frac{k_{v}d}{s+\beta} \frac{N_{v}}{D} \times - \frac{K_{F}d}{s+\beta} \frac{N_{F}}{D} F$$

$$[1 + \frac{K_{F}d}{s+\beta} \cdot \frac{N_{F}}{D}]F = -\frac{k_{u}s}{s+\beta} + \frac{k_{v}d}{s+\beta} \cdot \frac{N_{v}}{D} \times$$

$$F = -\frac{k_{u}s}{s+\beta} \cdot \frac{N_{F}}{D} + \frac{k_{v}d}{s+\beta} \cdot \frac{N_{v}}{S+\beta} \times \frac{N_{v}}{D} \times \frac{N_{v}}{D} \times \frac{N_{v}}{S+\beta} \times \frac{N_{v}}{S+\beta}$$

mg(stb)D +mgKfdNf + kasD+ KxdNx