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# Basics of Neural Network Programming

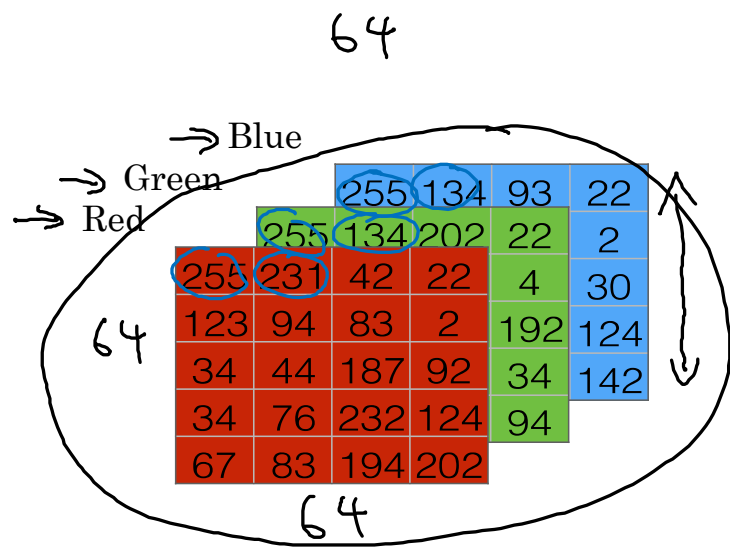
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## Binary Classification

# Binary Classification



1 (cat) vs 0 (non cat)  
 $y$



$$X = \begin{bmatrix} 255 \\ 231 \\ \vdots \\ 255 \\ 134 \\ \vdots \end{bmatrix}$$

$$64 \times 64 \times 3 = 12288$$

$$n = n_x = 12288$$

$X \rightarrow y$

# Notation

$$(x, y) \quad x \in \mathbb{R}^{n_x}, y \in \{0, 1\}$$

$$m \text{ training examples} : \{(\underline{x}^{(1)}, \underline{y}^{(1)}), (\underline{x}^{(2)}, \underline{y}^{(2)}), \dots, (\underline{x}^{(m)}, \underline{y}^{(m)})\}$$

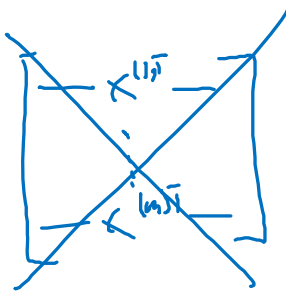
$$M = M_{\text{train}}$$

$$M_{\text{test}} = \# \text{test examples.}$$

$$X = \begin{bmatrix} | & | & & | \\ x^{(1)} & x^{(2)} & \dots & x^{(m)} \\ | & | & & | \end{bmatrix}$$

$X \in \mathbb{R}^{n_x \times m}$

$X.\text{shape} = (n_x, m)$



$$Y = [y^{(1)} \ y^{(2)} \ \dots \ y^{(m)}]$$

$$Y \in \mathbb{R}^{1 \times m}$$

$$Y.\text{shape} = (1, m)$$



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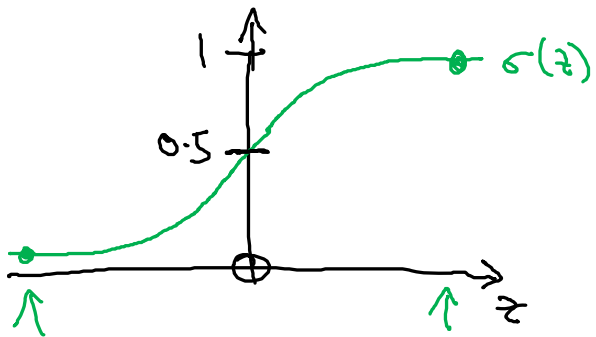
## Logistic Regression

# Logistic Regression

Given  $x$ , want  $\hat{y} = \frac{P(y=1|x)}{0 \leq \hat{y} \leq 1}$   
 $x \in \mathbb{R}^{n_x}$

Parameters:  $\underline{w} \in \mathbb{R}^{n_x}$ ,  $\underline{b} \in \mathbb{R}$ .

Output  $\hat{y} = \sigma(\underbrace{w^T x + b}_z)$



$$x_0 = 1, \quad x \in \mathbb{R}^{n_x+1}$$
$$\hat{y} = \sigma(\theta^T x)$$

$$\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \theta_2 \\ \vdots \\ \theta_{n_x} \end{bmatrix} \begin{matrix} \} b \leftarrow \\ \} w \leftarrow \end{matrix}$$

$$\sigma(z) = \frac{1}{1 + e^{-z}}$$

If  $z$  large  $\sigma(z) \approx \frac{1}{1+0} = 1$

If  $z$  large negative number

$$\sigma(z) = \frac{1}{1 + e^{-z}} \approx \frac{1}{1 + \text{Big num}} \approx 0$$



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## Logistic Regression cost function

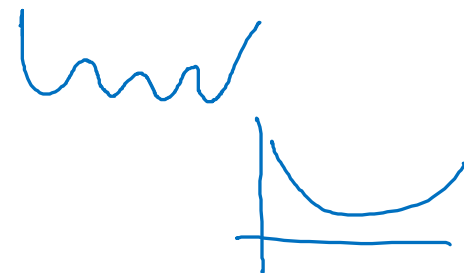
# Logistic Regression cost function

$$\rightarrow \hat{y}^{(i)} = \sigma(w^T \underline{x}^{(i)} + b), \text{ where } \sigma(z^{(i)}) = \frac{1}{1+e^{-z^{(i)}}} \quad z^{(i)} = w^T x^{(i)} + b$$

Given  $\{(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})\}$ , want  $\hat{y}^{(i)} \approx y^{(i)}$ .

$x^{(i)}$   
 $y^{(i)}$   
 $z^{(i)}$   $i$ -th example.

Loss (error) function:  $\mathcal{L}(\hat{y}, y) = \frac{1}{2} (\hat{y} - y)^2$



$$\mathcal{L}(\hat{y}, y) = - (y \log \hat{y} + (1-y) \log (1-\hat{y})) \leftarrow$$

If  $y=1$ :  $\mathcal{L}(\hat{y}, y) = -\log \hat{y} \leftarrow$  Want  $\log \hat{y}$  large, Want  $\hat{y}$  large.

If  $y=0$ :  $\mathcal{L}(\hat{y}, y) = -\log (1-\hat{y}) \leftarrow$  Want  $\log (1-\hat{y})$  large .... Want  $\hat{y}$  small

$$\text{Cost function: } J(w, b) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) = \frac{1}{m} \sum_{i=1}^m [y^{(i)} \log \hat{y}^{(i)} + (1-y^{(i)}) \log (1-\hat{y}^{(i)})]$$



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# Basics of Neural Network Programming

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## Gradient Descent

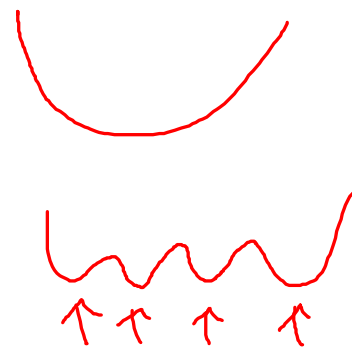
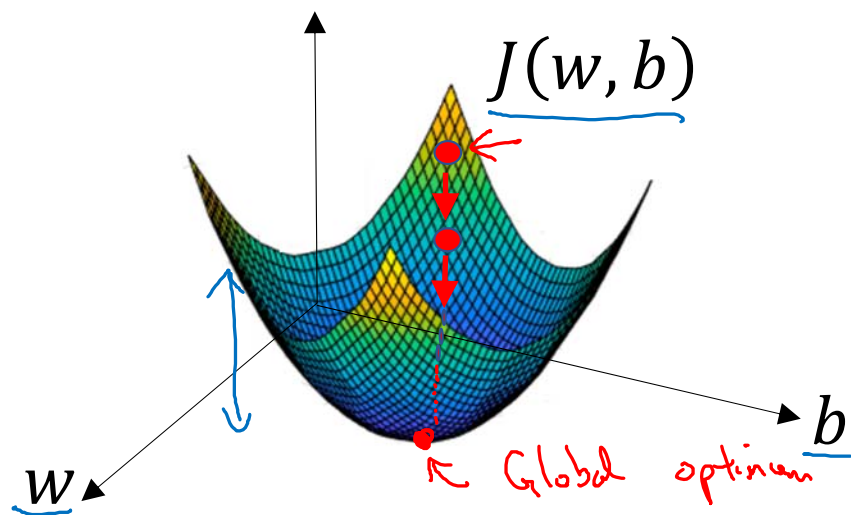


# Gradient Descent

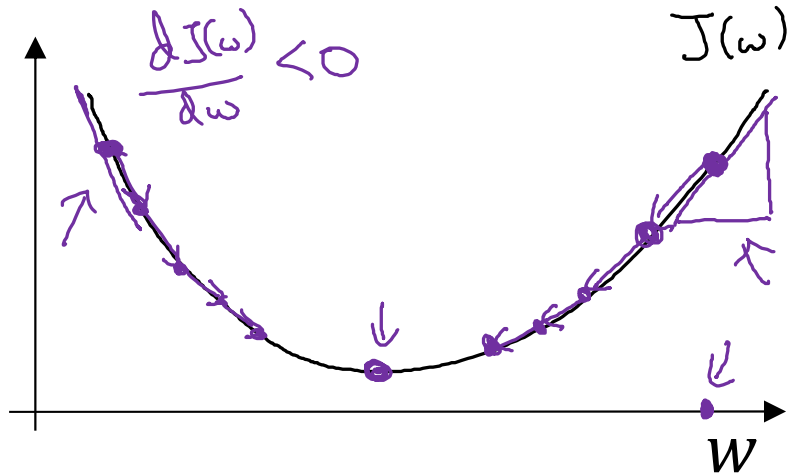
Recap:  $\hat{y} = \sigma(w^T x + b)$ ,  $\sigma(z) = \frac{1}{1+e^{-z}}$  ←

$$\underline{J(w, b)} = \frac{1}{m} \sum_{i=1}^m \underline{\mathcal{L}(\hat{y}^{(i)}, y^{(i)})} = -\frac{1}{m} \sum_{i=1}^m y^{(i)} \log \hat{y}^{(i)} + (1 - y^{(i)}) \log(1 - \hat{y}^{(i)})$$

Want to find  $w, b$  that minimize  $J(w, b)$



# Gradient Descent



Repeat {

$$w := w - \alpha \frac{dJ(w)}{dw}$$

}  $w := w - \alpha \underline{dw}$

$\frac{dJ(w)}{dw} = ?$

learning rate

"dw"

$J(w, b)$

$$w := w - \alpha \frac{\partial J(w, b)}{\partial w}$$

$$b := b - \alpha \frac{\partial J(w, b)}{\partial b}$$

$$\frac{\partial J(w, b)}{\partial w}$$

$$\frac{\partial J(w, b)}{\partial b}$$

"partial derivative"

$\partial$

$\partial$

$dw$

$db$



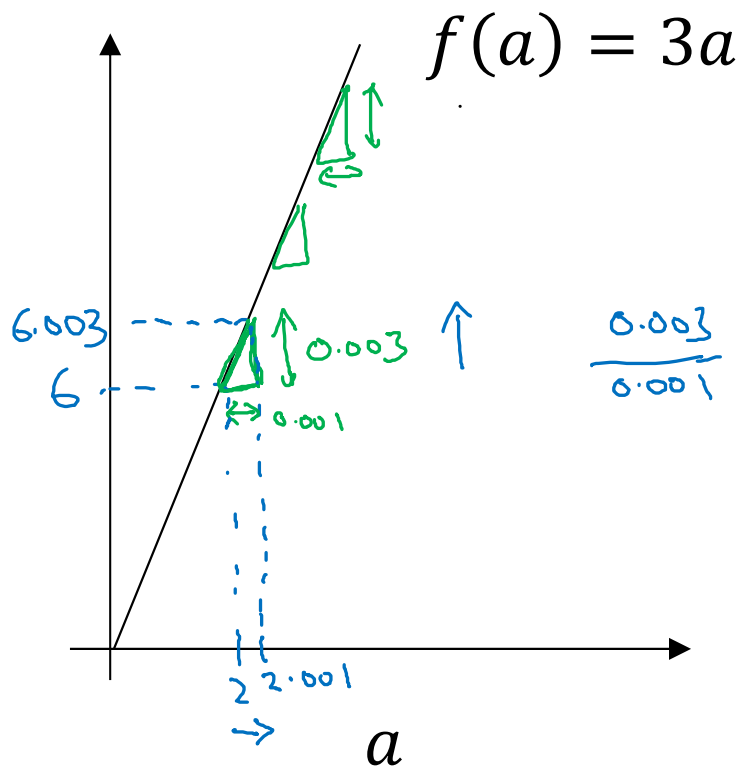
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# Basics of Neural Network Programming

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## Derivatives

# Intuition about derivatives



$$\frac{0.003}{0.001} \quad \text{height} \\ \text{width}$$

$\rightarrow a = 2 \quad f(a) = 6$   
 $a = 2.001 \quad f(a) = 6.003$

slope (derivative) of  $f(a)$  at  $a = 2$  is 3

$\rightarrow a = 5 \quad f(a) = 15$   
 $a = 5.001 \quad f(a) = 15.003$

slope at  $a = 5$  is also 3

$$\frac{df(a)}{da} = 3 = \frac{d}{da} f(a)$$

$0.001 \leftarrow$   
 $0.000000001$   
 $0.0000000001$



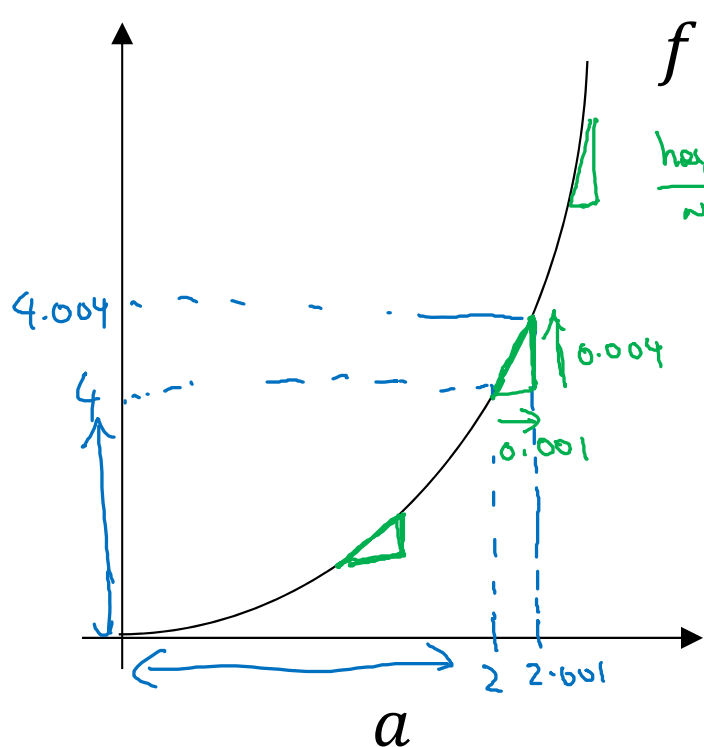
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# Basics of Neural Network Programming

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More derivatives  
examples

# Intuition about derivatives



$$f(a) = a^2$$

height  
width

$$\frac{d}{da} a^2 = 2a$$

$$0.001$$

$$(2a) \times 0.001$$

$0.001 \leftarrow$   
 $0.000000 \dots 01 \leftarrow$

$a = 2$   $f(a) = 4$   
 $a = 2.001$   $f(a) \approx 4.004$   
 $(4.004 \text{ } 004)$   
 slope (derivative) of  $f(a)$  at  
 $a = 2$  is  $4$ .

$$\frac{d}{da} f(a) = 4 \text{ when } a = 2$$

$a = 5$   $f(a) = 25$   
 $a = 5.001$   $f(a) \approx 25.010$

$$\frac{d}{da} f(a) = 10 \text{ when } a = 5$$

$$\frac{d}{da} f(a) = \frac{d}{da} a^2 = 2a$$

# More derivative examples

$$f(a) = a^2$$

$$\frac{d}{da} f(a) = \frac{2a}{4}$$

$$a = 2$$

$$f(a) = 4$$

$$a = 2.001$$

$$f(a) \approx 4.004$$

$$f(a) = a^3$$

$$\frac{d}{da} f(a) = \frac{3a^2}{3 \times 2^2 = 12}$$

$$a = 2$$

$$f(a) = 8$$

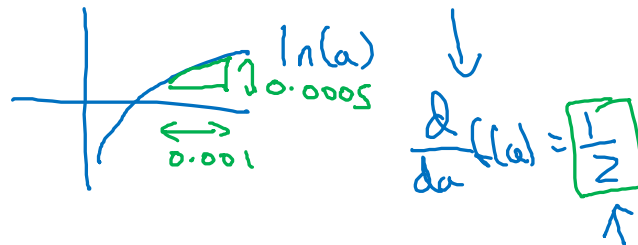
$$a = \underline{2.001}$$

$$f(a) \approx \underline{8.012}$$

$$f(a) = \log_e(a)$$

$$\ln(a)$$

$$\frac{d}{da} f(a) = \frac{1}{a}$$



$$a = 2$$

$$f(a) \approx 0.69315$$

$$a = \underline{2.001}$$

$$\underline{f(a) \approx 0.69365}$$

$$0.0005 \leftarrow \underline{0.0005}$$

Andrew Ng



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## Computation Graph

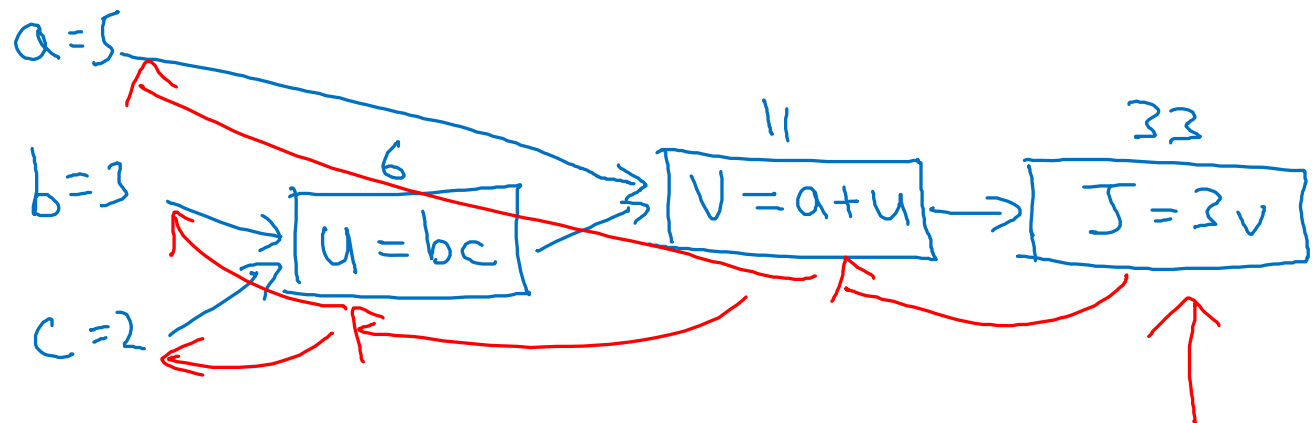


# Computation Graph

$$J(a, b, c) = 3(a + \underbrace{bc}_u) = 3(5 + \underbrace{3 \times 2}_v) = 33$$

$\underbrace{\hspace{1.5cm}}_J$

$$\begin{aligned} u &= bc \\ V &= a + u \\ J &= 3V \end{aligned}$$





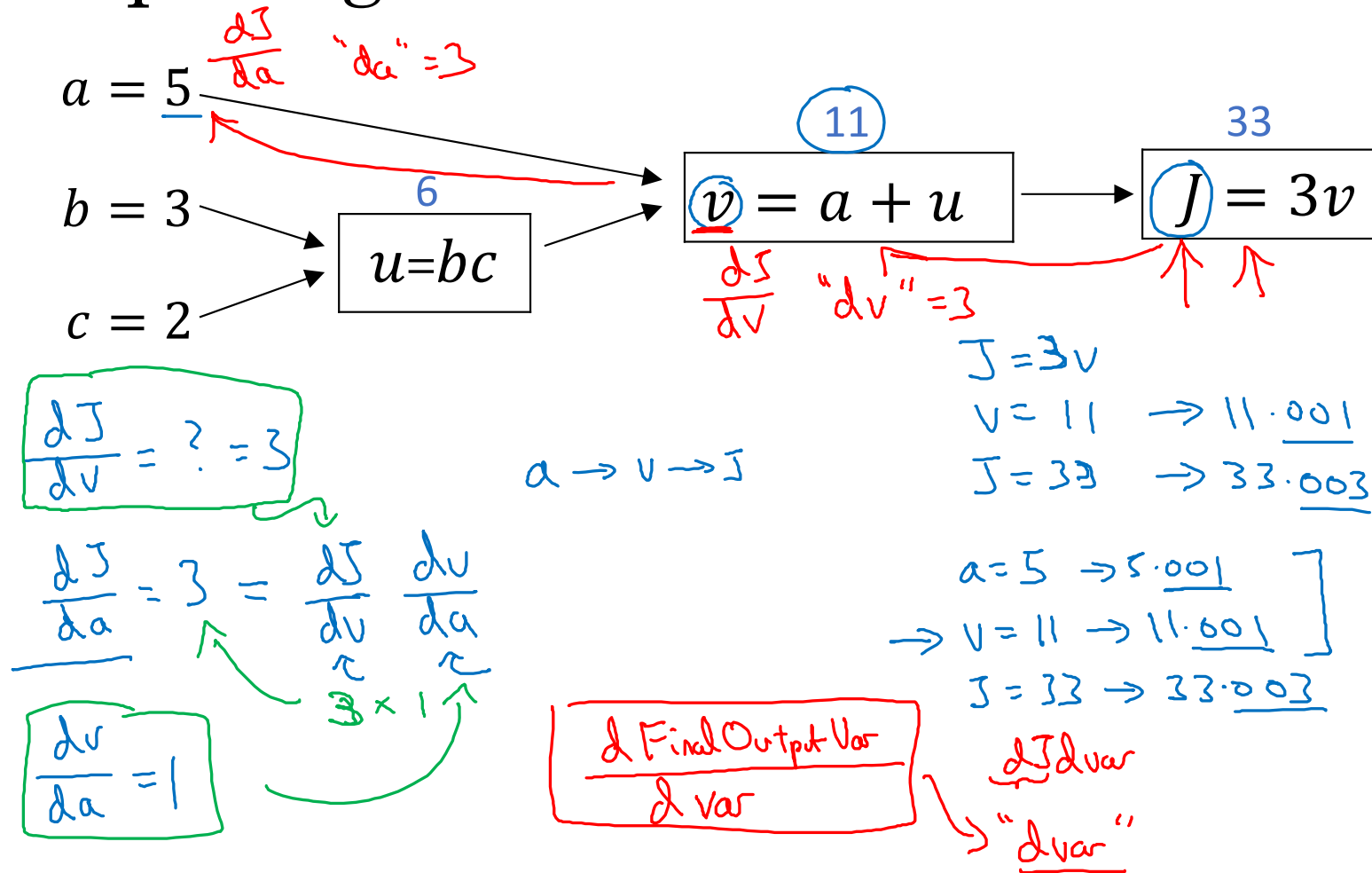
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# Basics of Neural Network Programming

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## Derivatives with a Computation Graph

# Computing derivatives



$$f(a) = 3a$$

$$\frac{df(a)}{da} = \frac{df}{da} = 3$$

$$J = 3v$$

$$\frac{dJ}{dv} = 3$$

$$J = 3v$$

$$v = 11 \rightarrow 11.001$$

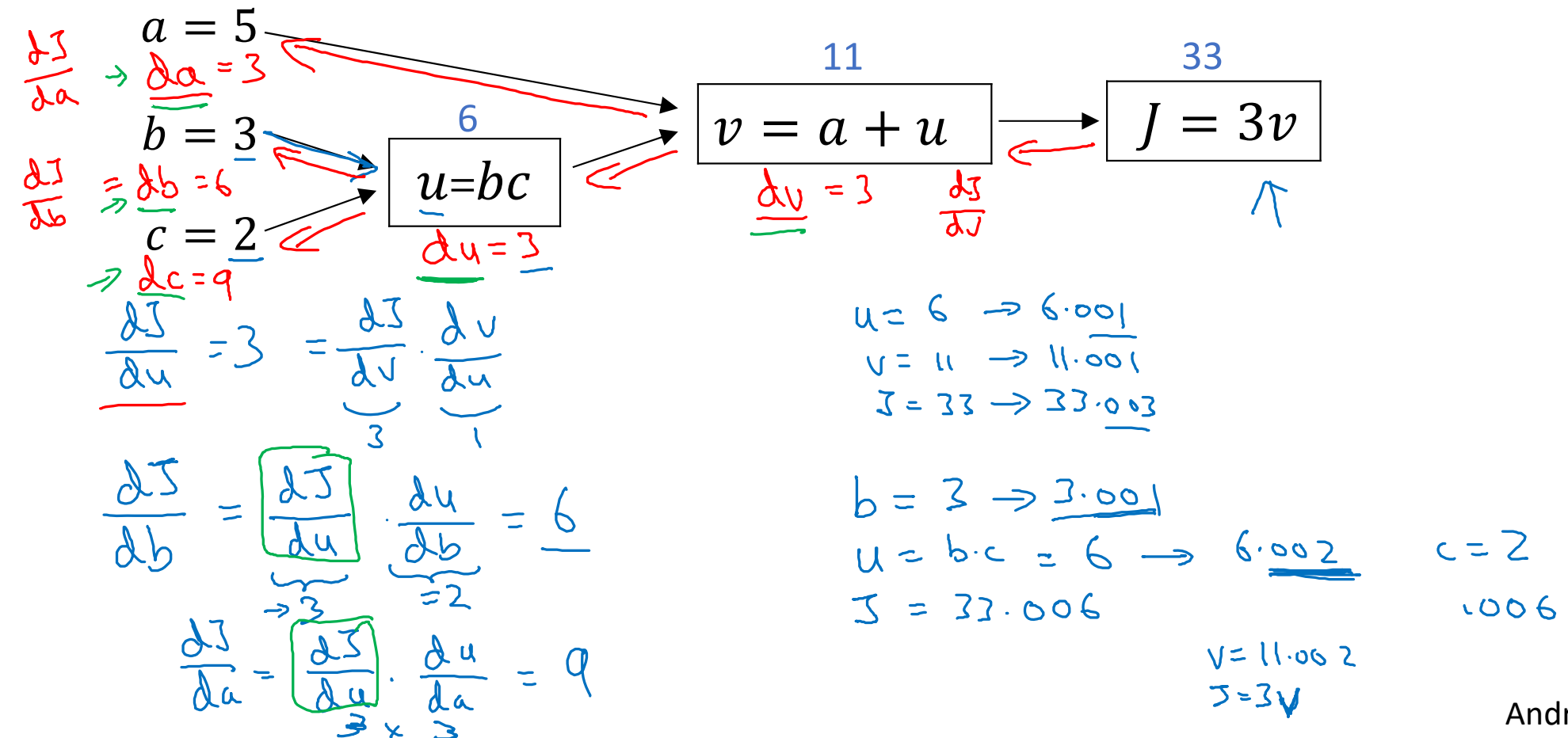
$$J = 33 \rightarrow 33.003$$

$$a = 5 \rightarrow 5.001$$

$$\rightarrow v = 11 \rightarrow 11.001$$

$$J = 33 \rightarrow 33.003$$

# Computing derivatives





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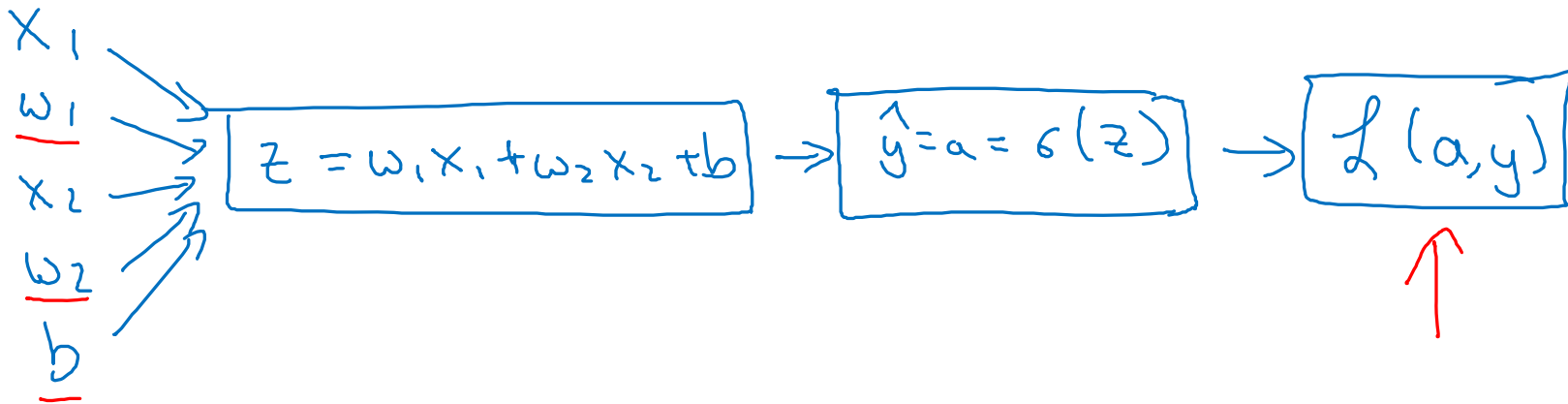
# Basics of Neural Network Programming

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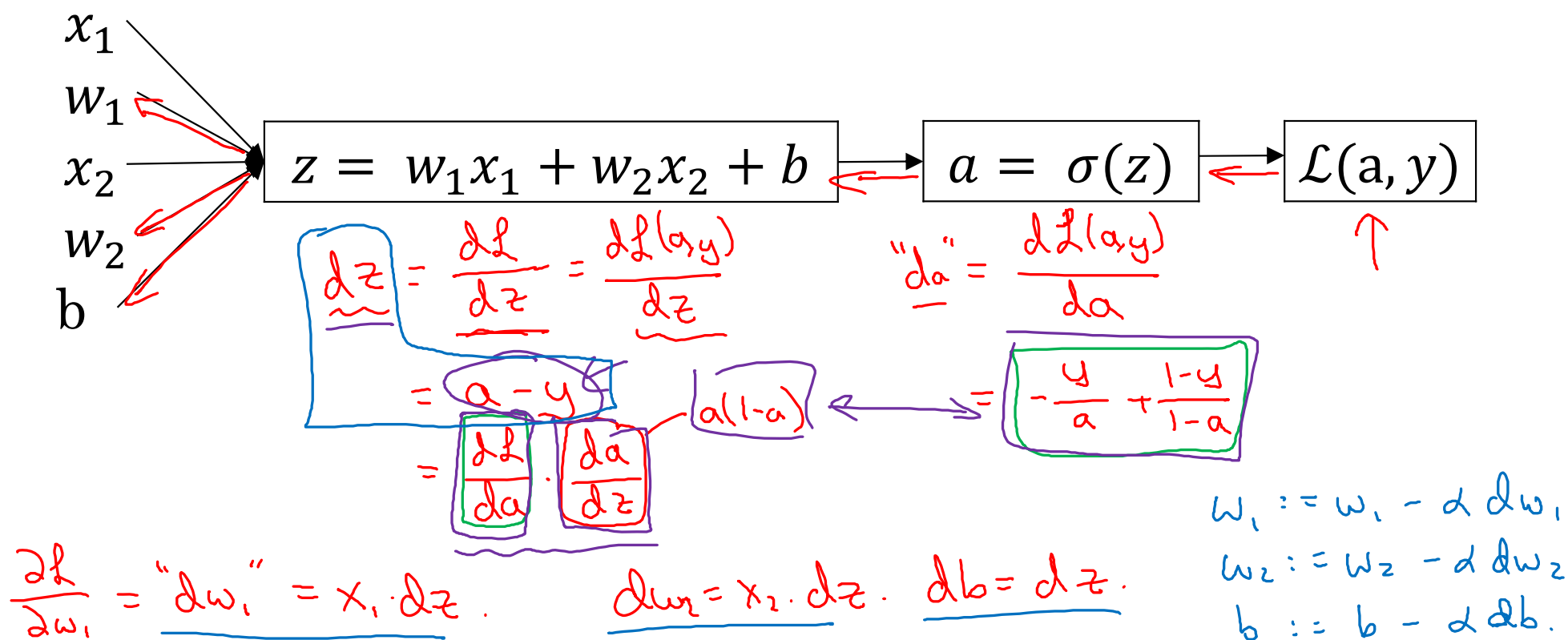
## Logistic Regression Gradient descent

# Logistic regression recap

- $z = w^T x + b$
- $\hat{y} = a = \sigma(\underline{z})$
- $\mathcal{L}(a, y) = -(y \log(a) + (1 - y) \log(1 - a))$



# Logistic regression derivatives





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# Basics of Neural Network Programming

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Gradient descent  
on  $m$  examples



# Logistic regression on $m$ examples

$$J=0; \quad \underline{dw_1}=0; \quad \underline{dw_2}=0; \quad \underline{db}=0$$

→ For  $i=1$  to  $m$

$$z^{(i)} = w^T x^{(i)} + b$$

$$a^{(i)} = \sigma(z^{(i)})$$

$$J += -[y^{(i)} \log a^{(i)} + (1-y^{(i)}) \log(1-a^{(i)})]$$

$$\underline{dz^{(i)}} = a^{(i)} - y^{(i)}$$

$$\begin{array}{l} \uparrow \\ dw_1 += x_1^{(i)} dz^{(i)} \\ dw_2 += x_2^{(i)} dz^{(i)} \\ db += dz^{(i)} \\ \downarrow \end{array} \quad \begin{array}{l} \uparrow \\ n=2 \\ \downarrow \end{array}$$

$$J /= m \leftarrow$$

$$\begin{array}{ccc} dw_1 /= m & ; & dw_2 /= m; db /= m. \leftarrow \\ \uparrow & & \uparrow \end{array}$$

$$dw_1 = \frac{\partial J}{\partial w_1}$$

$$w_1 := w_1 - \alpha \underline{dw_1}$$

$$w_2 := w_2 - \alpha \underline{dw_2}$$

$$b := b - \alpha \underline{db}$$

Vectorization