

# Mini-batch gradient descent

## Batch vs. mini-batch gradient descent

Vectorization allows you to efficiently compute on m examples.

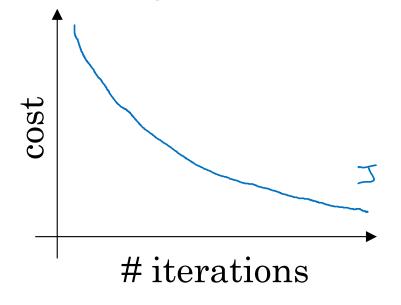
stop of grabit deat Mini-batch gradient descent (as ifmel 500) report 2 for t = 1,..., 5000 { Formal peop on X [t].  $A_{CO} = a_{CO} \left( \frac{S_{CO}}{S_{CO}} \right)$   $A_{CO} = a_{CO} \left( \frac{S_{CO}}{S_{CO}} \right)$  (1200 example) (1200 example)Compute cost  $J^{\ell\ell}_{\overline{J}} = \frac{1}{1000} \stackrel{\text{def}}{=} J(y,y) + \frac{\lambda}{2.1000} \stackrel{\text{E}}{=} ||W^{\ell\ell}_{\overline{J}}||_{F}^{2}$ . Backprop to compart gradults cort Jser (usy (xser) YEER)) W:= W(1) - 2 ddw(1), b(1) = b(1) - 2 db(1) "I epoch" poss through training set.



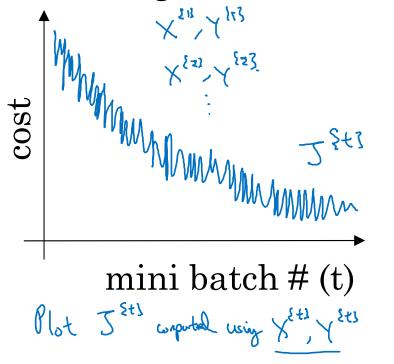
Understanding mini-batch gradient descent

### Training with mini batch gradient descent

Batch gradient descent



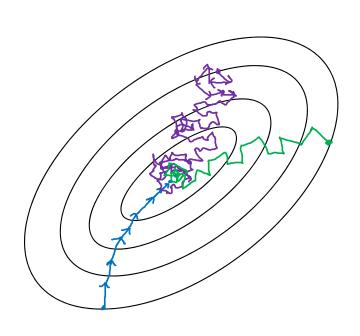
Mini-batch gradient descent



### Choosing your mini-batch size

> If mini-both size = m: Sorth godnet desch.  $(X^{SIS}, Y^{SIS}) = (X, Y)$ > If mini-both size = 1: Stochaster graphet descet. Every example is it own  $(X^{SIS}, Y^{SIS}) = (K^{(I)}, Y^{(I)}) \dots (K$ 

In practice: Socialis in-between I all m



Stochostic

gradent

begant

Lose spealup

from vontation

In-bothern

(min-hoth size

not too by/small)

Fustest learnly.

Vectorantian.

(N1000)

· Make poor without
prolessy extire truy set.

Botch
godiet desut
(min; both size = n)

Two long per iteration

### Choosing your mini-batch size

If small tray set: Use borth graher descent.

(m < 2500)

Typical mint-borth sizes:

(c) 64, 128, 256, 512

20 20 20 20 20

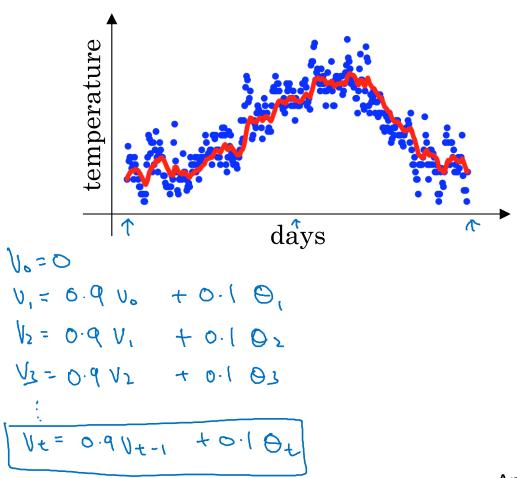
Male sue mintbook fit is CPU/GPU memony.

XXX, YXX, YXX

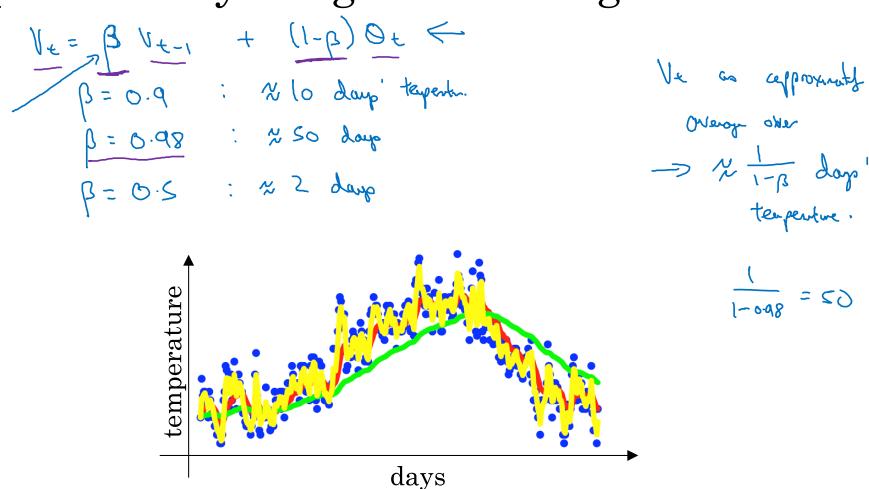


# Exponentially weighted averages

### Temperature in London



## Exponentially weighted averages





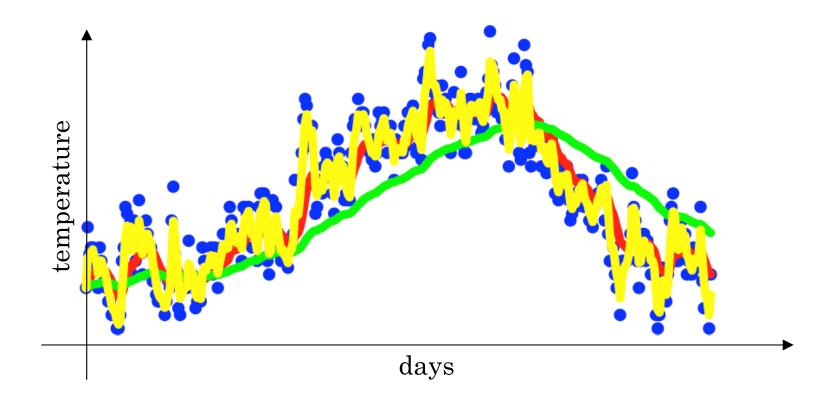
Understanding exponentially weighted averages

### Exponentially weighted averages

$$v_t = \beta v_{t-1} + (1-\beta)\theta_t$$

$$\beta = 0.9$$

$$6.99$$



### Exponentially weighted averages

Exponentially weighted averages 
$$v_t = \beta v_{t-1} + (1-\beta)\theta_t$$

$$v_{100} = 0.9v_{99} + 0.1\theta_{100}$$

$$v_{99} = 0.9v_{98} + 0.1\theta_{99}$$

$$v_{98} = 0.9v_{97} + 0.1\theta_{98}$$
...
$$v_{100} = 0.9v_{97} + 0.1\theta_{99}$$
...
$$v_{100} = 0.9v_{$$

## Implementing exponentially weighted averages

$$v_0 = 0$$
  
 $v_1 = \beta v_0 + (1 - \beta) \theta_1$   
 $v_2 = \beta v_1 + (1 - \beta) \theta_2$   
 $v_3 = \beta v_2 + (1 - \beta) \theta_3$   
...

$$V_{0} := 0$$
 $V_{0} := \beta v + (1-\beta) O_{1}$ 
 $V_{0} := \beta v + (1-\beta) O_{2}$ 
 $V_{0} := \beta v + (1-\beta) O_{2}$ 

No=0

Kapeart 
$$\xi$$

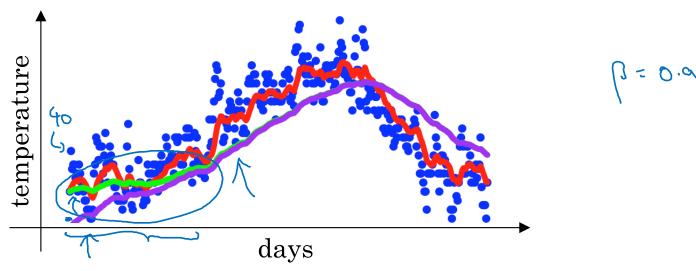
Cert rest  $O_{\xi}$ 
 $V_{\phi} := \beta V_{\phi} + (1-\beta)O_{\xi}$ 

Andrew Ng



Bias correction in exponentially weighted average

#### Bias correction



$$v_{t} = \beta v_{t-1} + (1 - \beta)\theta_{t}$$

$$V_{0} = 0$$

$$V_{1} = 0.98 V_{0} + 0.02 \Theta_{1}$$

$$V_{2} = 0.98 V_{1} + 0.02 \Theta_{2}$$

$$= 0.98 \times 0.02 \times \Theta_{1} + 0.02 \Theta_{2}$$

$$= 0.0196 \Theta_{1} + 0.02 \Theta_{2}$$

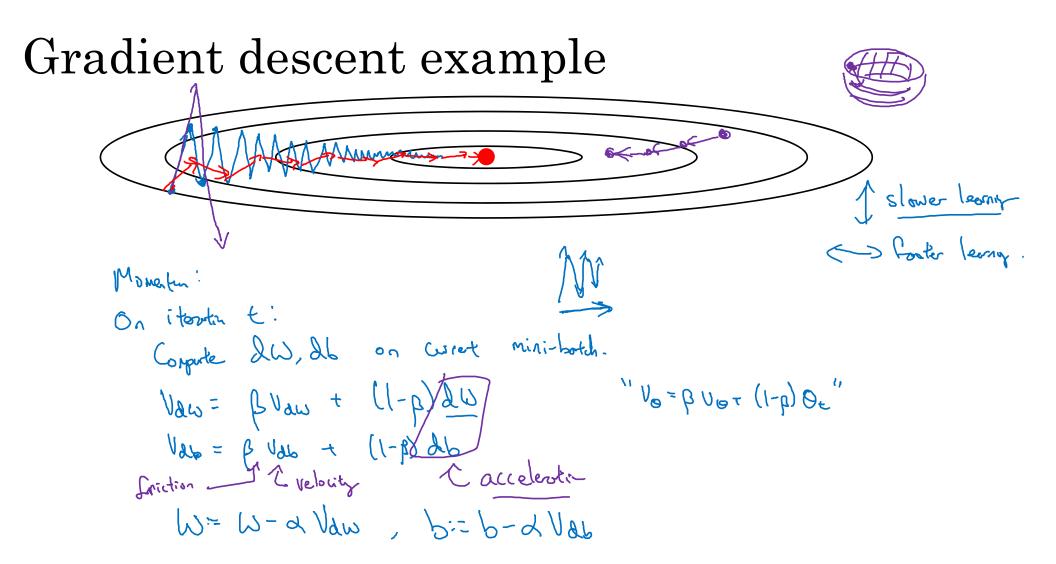
$$\frac{1-\beta^{t}}{1-\beta^{t}}$$

$$t=2: 1-\beta^{t} = 1-(0.98)^{2} = 0.0396$$

$$\frac{1-\beta^{t}}{0.0396} = 0.0396$$



# Gradient descent with momentum



### Implementation details

#### On iteration *t*:

Compute dW, db on the current mini-batch

$$\rightarrow v_{dW} = \beta v_{dW} + M \beta dW$$

$$> v_{db} = \beta v_{db} + (1 - \beta) db$$

$$W = W - \alpha v_{dW}, \ b = b - \alpha v_{db}$$

Hyperparameters: 
$$\alpha, \beta$$

$$\beta = 0.9$$
Overloge on lost 100 graduits



## RMSprop

## RMSprop W., Wz, W2 On iteration t: Compute DW, db on count mini-both Saw = B2 Saw + (1-P2) dw? = small $\Rightarrow$ Sab = $\beta_2$ Sab + $(1-\beta_2)$ $db^2$ < large W:= W- & dw < b:= b-2 db < JSab+E < Z=10-8



# Adam optimization algorithm

### Adam optimization algorithm

### Hyperparameters choice:

$$\rightarrow$$
 d: needs to be tune  
 $\rightarrow$   $\beta_i$ : 0.9  $\longrightarrow$  (dw)  
 $\rightarrow$   $\beta_2$ : 0.999  $\longrightarrow$  (dw²)  
 $\rightarrow$   $\Sigma$ : 10-8

Adam: Adaptiv moment estimation

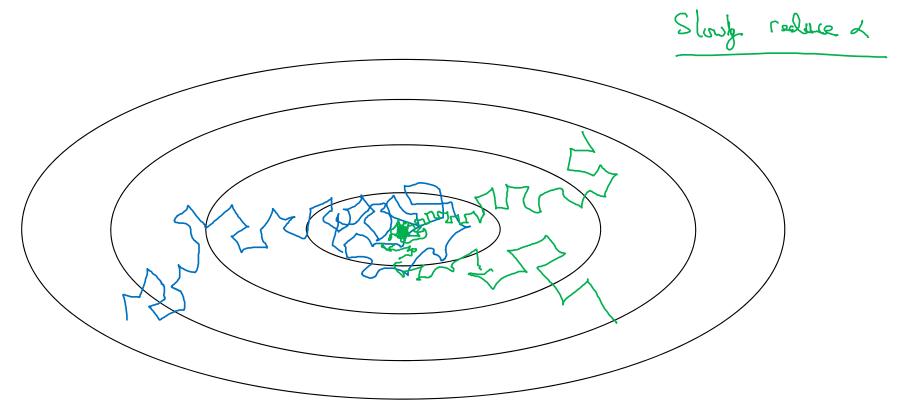


**Adam Coates** 



# Learning rate decay

## Learning rate decay



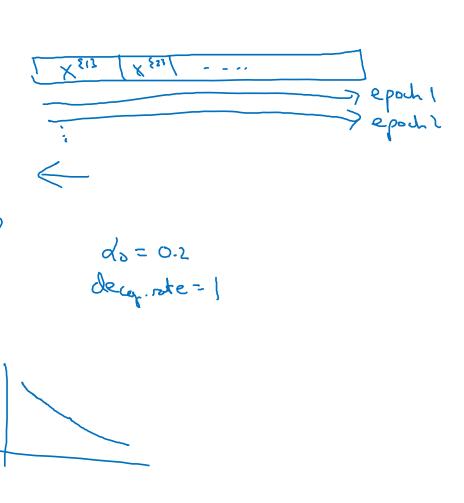
## Learning rate decay

2 poch = 1 pass throgh dort.

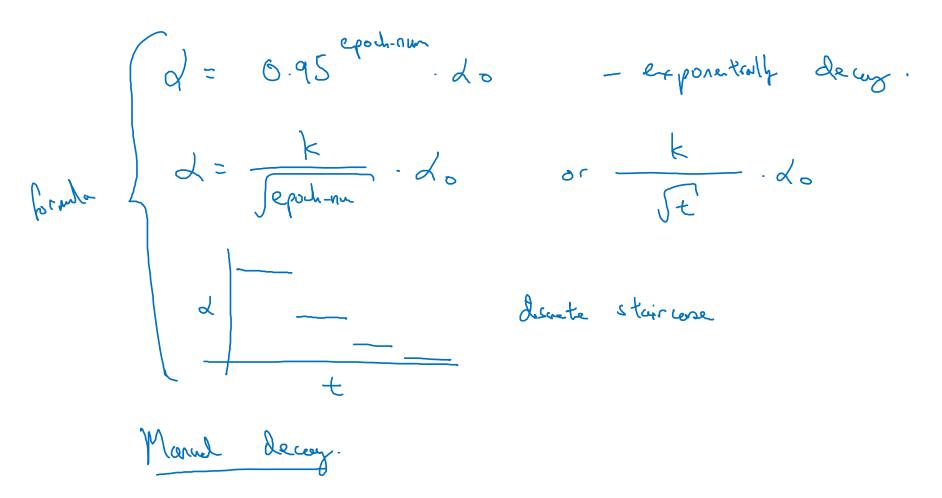
d = 1

1 t decay-rate \* epoch-num

Epoch	1
	0.1
2	0.67
3	6.5
4	6.4
	-



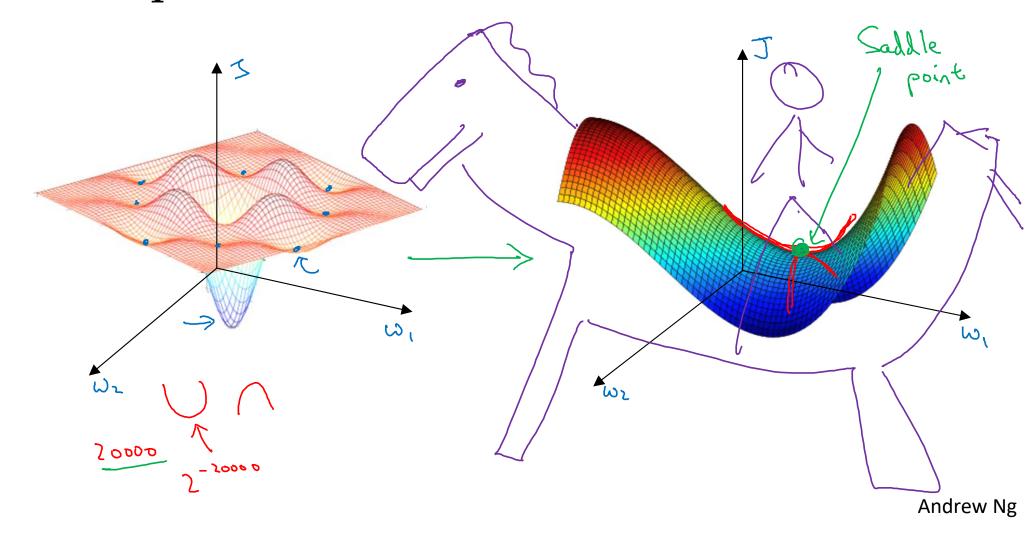
### Other learning rate decay methods



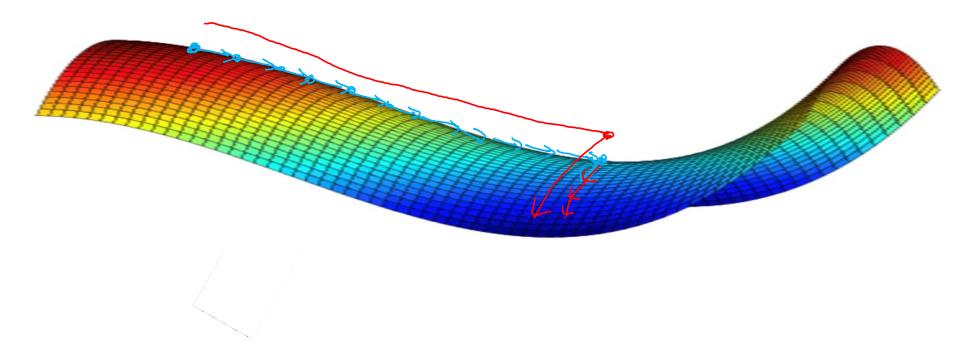


# The problem of local optima

## Local optima in neural networks



### Problem of plateaus



- Unlikely to get stuck in a bad local optima
- Plateaus can make learning slow