

# **Resource-Parameterized Program Analysis using Observation Sequences**

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# Static analysis and concurrency

Complicated shared-state interaction

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Subtle bugs, easily missed by humans

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Complicated thread-local behavior

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Can decide under a fixed resource bound:

"No violations within 8 context switches"

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Can decide under a fixed resource bound:

"No violations within 8 context switches"

But what if violation would appear after 9?

# New proof technique

Checking safety in concurrent systems



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Prove, not just refute

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Checking safety in concurrent systems

Prove, not just refute

Practical automation despite undecidability

# Contents

- Past work: Context-bounded analysis

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$q^I \in Q$  Starting state

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Nondeterminism models acting on input

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Machine: Fixed collection of PDSes

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Shared: state set, current state

Per-PDS: stack alphabet, program

# Decidability

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✓ Shared state only

✗ Both at once

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Can we violate safety property with only 5 context switches?

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Finitely many single-PDS reachability questions

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Finitely many single-PDS reachability questions

Can only refute safety properties, not prove them

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Proof technique built on CBA

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CBA: "No safety violation within  $k$  context switches"



# Context-unbounded analysis (CUBA)

Proof technique built on CBA

CBA: "No safety violation within  $k$  context switches"

CUBA: "No  $k$  is big enough for CBA to observe safety violation"

# Observation Sequence

Definition parameterized over

$\mathcal{P}$  a CPDS (program we're investigating)

$\mathcal{D}$  a poset (space of possible observations)

$\mathcal{C}$  a property of resource-bounded CPDSes  
(what we're trying to check)

# Observation Sequence

An observation sequence for property  $\mathcal{C}$  on machine  $\mathcal{P}$  over a poset  $\mathcal{D}$  is a sequence  $(O_k)_{k=0}^{\infty}$  with the following properties

**Monotonicity:**  $\forall k \in \mathbb{N}. O_k \sqsubseteq O_{k+1}$

**Computability:** There is a computable function  $f : \mathbb{N} \rightarrow \mathcal{D}$  such that  $f(k) = O_k$

**Expressibility:** There is a computable predicate  $p$  on  $\{O_k | k \in \mathbb{N}\}$  such that  $p(O_k)$  holds iff  $\mathcal{P}$  has property  $\mathcal{C}$  when subject to resource bound  $k$

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Definition captures important properties for safety proofs

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Definition captures important properties for safety proofs

**Monotonicity:** With more resources, more results are possible

**Computability:** We can actually make these observations

**Expressibility:** What we observe informs us about what we care about

# Guaranteeing convergence

Unbounded stack size ➡ Infinite state space



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Observe only top of stack ➡ Finite observation poset

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Monotonic sequence must eventually converge

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Data flow analysis: iterate function to find least fixed point

$$f : D \rightarrow D$$

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CUBA: grow input until convergence

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CUBA: grow input until convergence

$$f : \mathbb{N} \rightarrow D$$

No fixed points!

$$f(n + 1) = f(n) \not\Rightarrow f(n + 2) = f(n)$$

# Stuttering

How do we know when to stop?

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**Recall: CPDS reachability is undecidable!**

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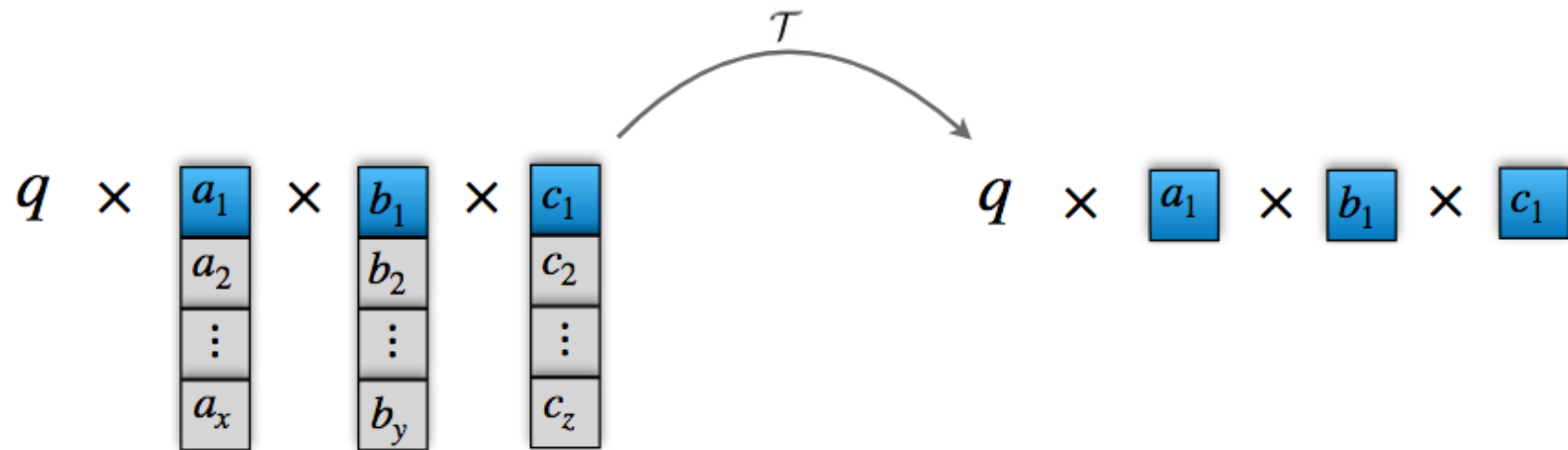
**Recall: CPDS reachability is undecidable!**

**Key automation challenge: distinguish stuttering from convergence**

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Finitize the observation sequences to guarantee convergence



# Stutter Detection is undecidable

Since convergence is guaranteed, but the problem is undecidable, stutter detection is undecidable



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Must approximate!

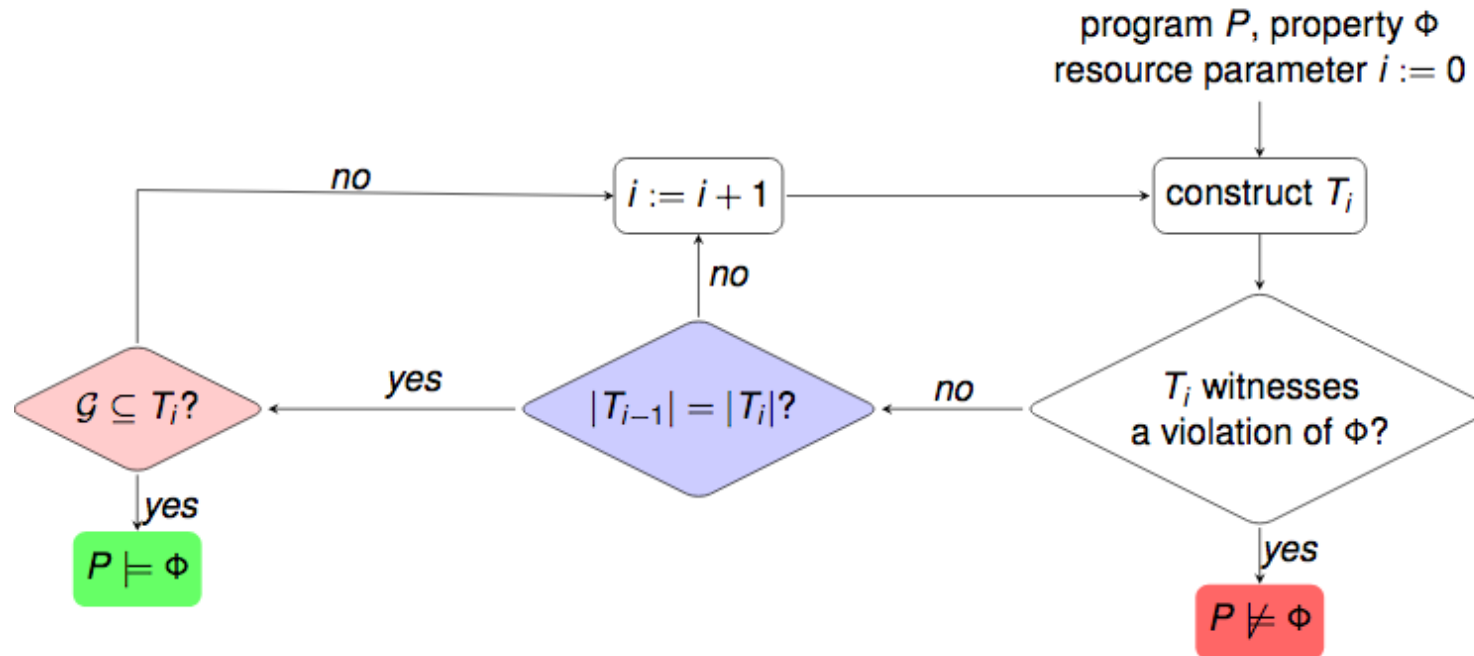
# Only certain instructions can change observation set

If a stutter ends it has to be the consequence of a stack pop.

The observation sequence converges if all reachable popping states are in the observation set

We give an overapproximation of this set to stay decidable

# Algorithm Summary



$\mathcal{G} := \{\text{reachable generators}\}$

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# Empirical Evaluation

Evaluated our CUBA algorithm on 9 CPDSs converted from concurrent programs in C/Java

For comparison, evaluated most of those using JMoped, a CBA implementation

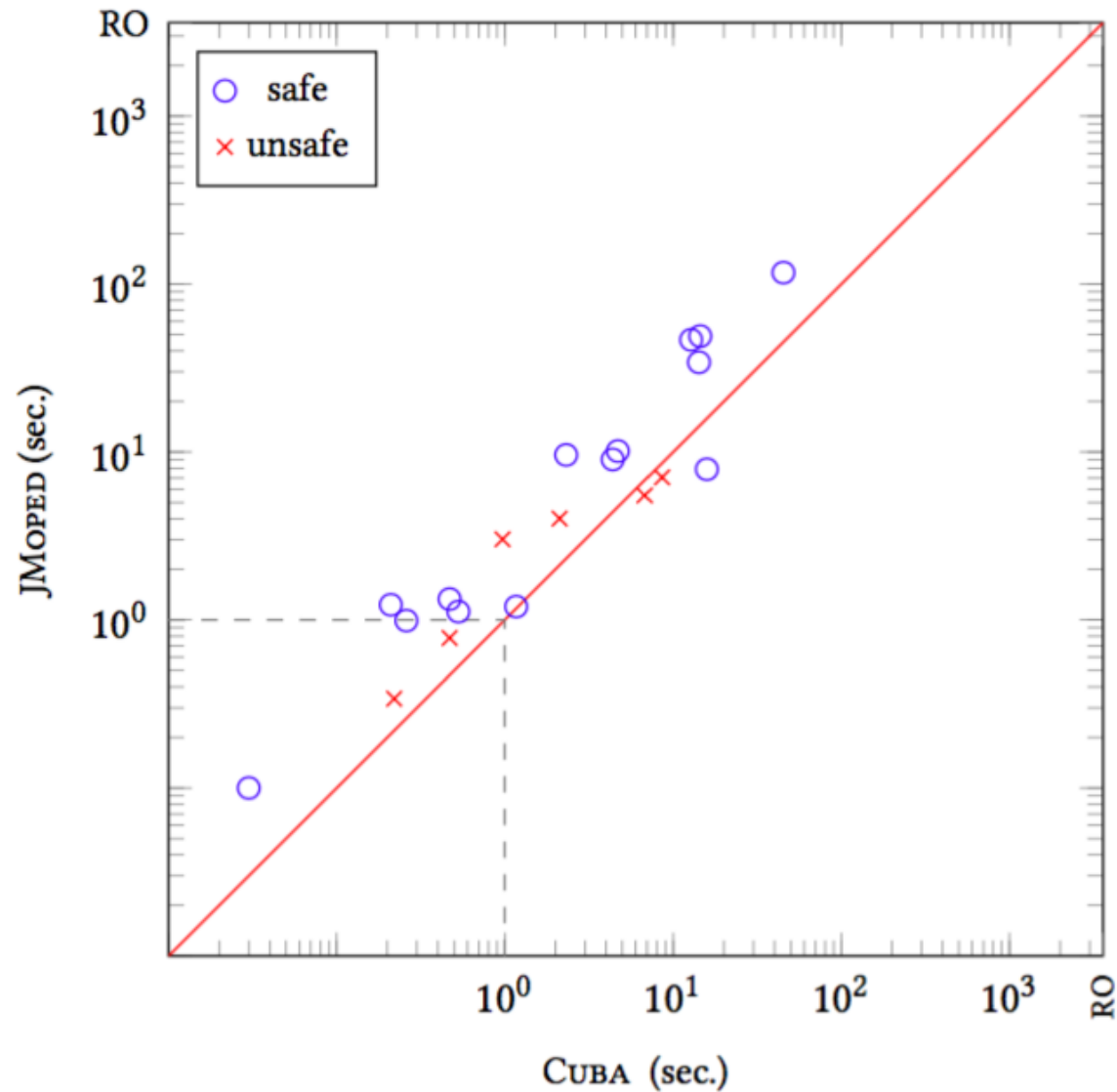
# CUBA is effective at proving and refuting safety

ID/Program	Prog. Features			$(R_k)_{k=0}^{\infty}$		$(\mathcal{T}(R_k))_{k=0}^{\infty}$	
	Thread	FCR?	Safe?	$k_{max}$	$k_{max}$	Time	Mem
1/BLUETOOTH-1	1 + 1	●	✗	$\geq 7$	6 (4)	0.26	18.14
	1 + 2	●	✗	$\geq 7$	6 (3)	2.32	136.26
	2 + 1	●	✗	$\geq 8$	7 (4)	12.76	347.74
2/BLUETOOTH-2	1 + 1	●	✗	$\geq 7$	6 (4)	0.53	23.43
	1 + 2	●	✗	$\geq 7$	6 (3)	4.39	196.73
	2 + 1	●	✗	$\geq 8$	7 (4)	14.21	387.23
3/BLUETOOTH-3	1 + 1	●	✓	$\geq 7$	6	0.47	22.15
	1 + 2	●	✓	$\geq 7$	6	4.71	180.11
	2 + 1	●	✓	$\geq 8$	7	14.46	375.42

ID/Program	Prog. Features			$(R_k)_{k=0}^{\infty}$		$(\mathcal{T}(R_k))_{k=0}^{\infty}$	
	Thread	FCR?	Safe?	$k_{max}$	$k_{max}$	Time	Mem
4/BST-INSERT	1 + 1	●	✓	2	2	1.17	24.53
	2 + 1	●	✓	3	3	15.84	140.93
	2 + 2	●	✓	$\geq 5$	4	45.21	355.74
5/FILECRAWLER	1* + 2	●	✓	6	6	0.03	5.35
6/K-INDUCTION	1 + 1	○	✓	$\geq 4$	3	0.23	3.78
7/PROC-2	2 + 2*	○	✓	$\geq 4$	3	0.52	18.04
8/STEFAN-1	2	○	✓	$\geq 3$	2	1.01	2.81
	4	○	✓	$\geq 5$	4	16.36	1185.62
	8	○	–	$\geq 8$	$\geq 8$	–	OOM
9/DEKKER	2*	●	✓	6	6	0.21	13.42

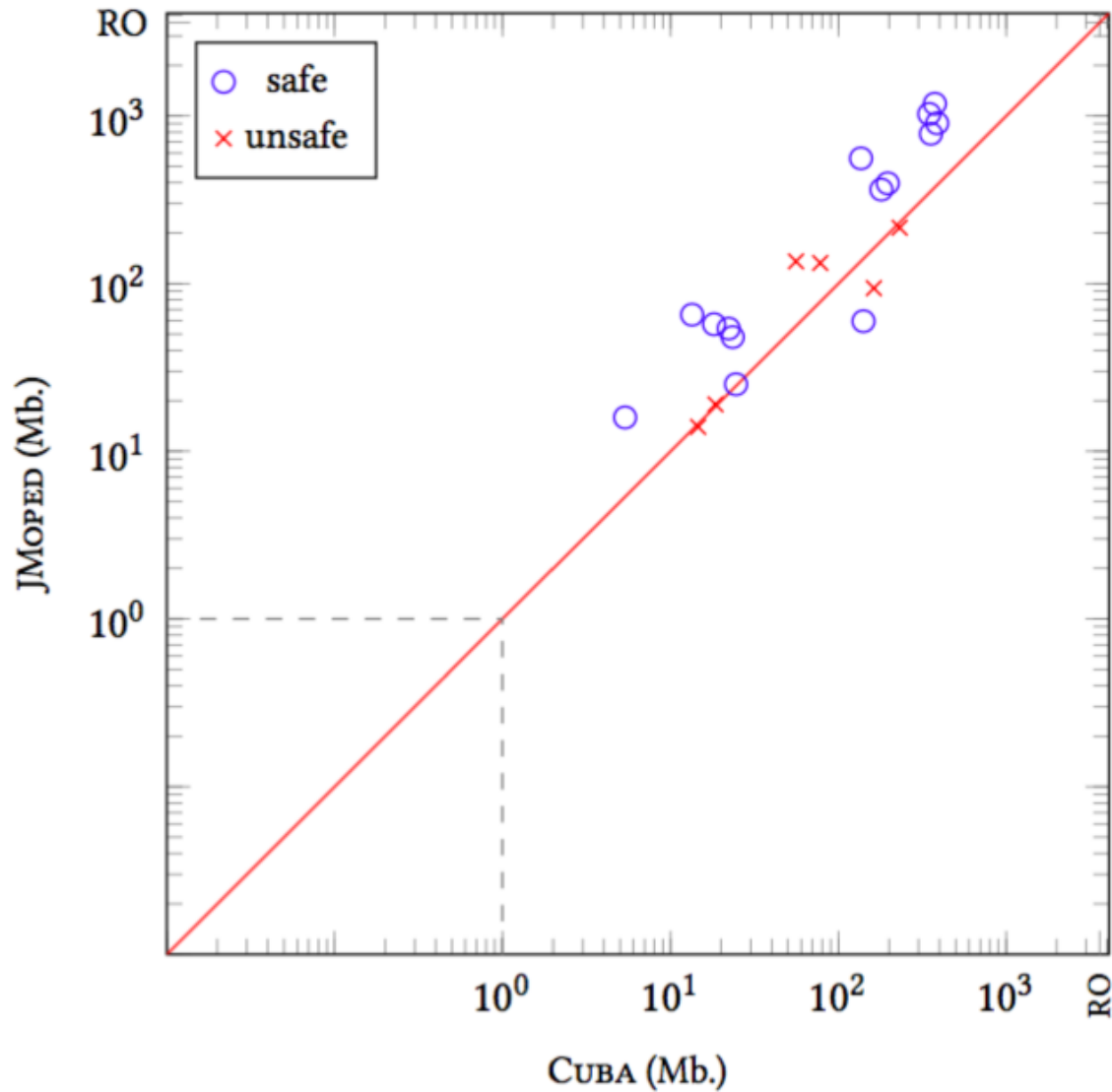
# CUBA has competitive performance with CBA

Runtime



# CUBA has competitive performance with CBA

## Memory Usage





# More in the paper!

- Systematic theory of observation sequences
- How we represent observation sequences efficiently?
- How to compute generator sets

# Conclusions

- Context UnBounded Analysis can automatically find bugs and prove safety of concurrent programs
- Observation sequences provide unifying perspective for understanding resource constrained analyses
- As efficient as previous, weaker analyses