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ABSTRACT

The Cleveland Heart Disease Data found in the UCI machine learning repository consists of 14 variables measured on 303 individuals. Each person has been classified as 1 indicating presence of Heart Disease, or 0 indicating absence of it. This variable has been named as the "target".

Because of the binary classification problem found in this dataset, we aim to explore a logistic regression model capable to predict the target value based on the variables which provide statistically significance to that prediction.

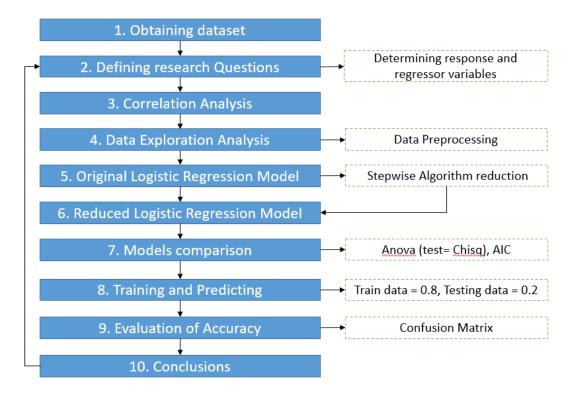
The results indicate that 8 regressor variables from the original 13 allow for a prediction accuracy of 90% based on a logistic regression model.

OBJECTIVES

- To understand the relationship between the regressor variables and the presence or absence of heart disease based on a correlation analysis and a general data exploratory analysis.
- To build a parsimonious model capable to predict the target variable by selecting the regressors that explain most of the variability in the dataset.
- To develop the best regression model that predicts the probability to either have a heart disease or not.
- To identify the most important variables that predict a heart disease.

DATA ANALYSIS FLOW

In order to obtain results and answer our objective questions, we defined the next data analysis flow:



1. DATASET

The dataset, which the main source is found in the Machine Learning Repository (https://archive.ics.uci.edu/ml/datasets/Heart+Disease), has been obtained from Kaggle following the next link: https://www.kaggle.com/ronitf/heart-disease-uci.

Specifically, we will work with the Cleveland Heart Disease Data which consists of 14 variables measured on 303 individuals.

The 14 variables included in the dataset are described in the next section.

VARIABLES DEFINITION

Variable Name	Class	Description
age	Numerical	The person's age in years
sex	Factor	The person's genre. 1 = male, 0 = female
ср	Factor	The chest pain type experienced; • 0 = typical angina • 1 = atypical angina • 2 = non-anginal pain • 3 = asymptomatic
trestbps	Numerical	The person's resting blood pressure (mm Hg on admission to the hospital)
chol	Numerical	The person's cholesterol serum measurement in mg/dl
fbs	Factor	The person's fasting blood sugar > 120 mg/dl; 1 = true, 0 = false
restecg	Factor	 Resting electrocardiographic measurement; 0 = normal 1 = having ST-T wave abnormality 2 = showing probable or definite left ventricular hypertrophy
thalach	Numerical	The person's maximum heart rate achieved
exang	Factor	Exercise induced angina; 1 = yes, 0 = no
oldpeak	Numerical	ST depression induced by exercise relative to rest ('ST' relates to positions on the EKG plot)
slope	Factor	The slope of the peak exercise ST segment; 3 levels. • 0 = upsloping • 1 = flat • 2 = downsloping
ca	Factor	The number of major vessels colored by fluoroscopy: 0-4 vessels
thal	Factor	Thallium stress test level. output 0 -1 = normal 2 = fixed defect 3 = reversable defect
target	Factor	Heart disease. 0 = no, 1 = yes

Initial Data Structure

```
303 obs. of 14 variables:
data.frame':
$ i..age : int 63 37 41 56 57 57 56 44 52 57 ...
               : Factor w/ 2 levels "0","1": 2 2 1 2 1 2 1 2 2 2 ...
: Factor w/ 4 levels "0","1","2","3": 4 3 2 2 1 1 2 2 3 3 ...
$ cp
$ trestbps: int
                       145 130 130 120 120 140 140 120 172 150 ...
                       233 250 204 236 354 192 294 263 199 168 ...
              : int
$ fbs : Factor w/ 2 levels "0","1": 2 1 1 1 1 1 1 1 2 1 ...
$ restecg : Factor w/ 3 levels "0","1","2": 1 2 1 2 2 2 1 2 2 2 ...
$ thalach : int 150 187 172 178 163 148 153 173 162 174 ...
              : Factor w/ 2 levels "0","1": 1 1 1 1 2 1 1 1 1 1 ...
$ exang
$ oldpeak : num 2.3 3.5 1.4 0.8 0.6 0.4 1.3 0 0.5 1.6 ...
              : Factor w/ 3 levels "0","1","2": 1 1 3 3 3 2 2 3 3 3 ...
: Factor w/ 5 levels "0","1","2","3",..: 1 1 1 1 1 1 1
$ slope
$ ca     : Factor w/ 5 levels "0","1","2","3",..: 1 1 1 1 1 1 1 1 1 1 1 ...
$ thal     : Factor w/ 4 levels "0","1","2","3": 2 3 3 3 2 3 4 4 3 ...
$ target     : Factor w/ 2 levels "0","1": 2 2 2 2 2 2 2 2 2 2 ...
```

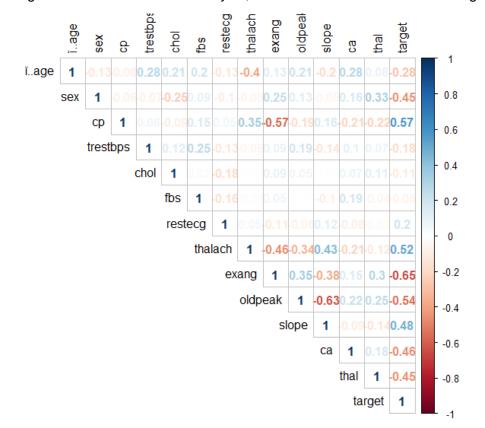
2. RESEARCH QUESTIONS

Based on the objectives mentioned before, we want to answer the next questions:

- What are the relationships between the regressors and the target variable?
- What is the best model to predict a heart disease state?

3. CORRELATION ANALYSIS

Using a heterogeneous data correlation analysis, the results are shown in the next graphic:

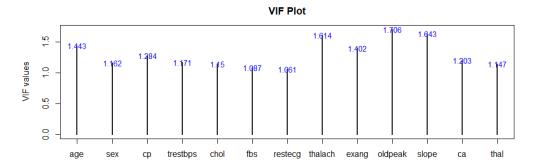


This correlation graphic highlights the correlations between regressors and between target and regressors. Positive correlations are shown in blue, and negative correlations are in red. In addition, color intensity is directly related to the grade of the correlation coefficients. Thus, we have:

- There is a negative correlation of -0.45 between the target and the variable sex.
- There is a negative correlation of -0.65 between the target and the variable exang.
- There is a negative correlation of -0.54 between the target and the variable oldpeak.
- There is a negative correlation of -0.46 and -0.45 between the target and the variables ca and thal respectively.
- There is a positive correlation of 0.57 between the target and the variable cp.
- There is a positive correlation of 0.52 between the target and the variable thalach.
- There is a positive correlation of 0.48 between the target and the variable slope.
- There is a negative correlation of -0.57 between the variables exang and cp.
- There is a negative correlation of -0.63 between the variables oldpeak and slope.

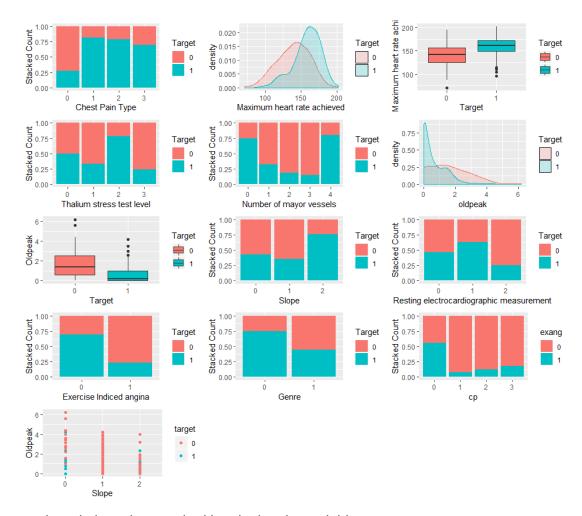
Eight variables show a moderate positive or negative correlation related to the target. These variables are sex, cp, thalach, exang, oldpeak, slope, ca, and thal. These may be the features that play a more significant role in driving the prediction of the target.

The next VIF plot indicates that there is not a problem of multicollinearity, and so we don't delete any variable based on this.



4. DATA EXPLORATION ANALYSIS

According to the correlation results, we identified the variables to perform the data exploration analysis to understand how they are related, by visualizing their relationships and reviewing the available literature. The next figure shows the relationships.



Next are the relations that resulted by plotting the variables:

Chest pain and target:

the cp type 1 = "Atypical angina" has the biggest incidence of heart disease compared to the others. However, the graph indicates that cp type 2 and 3 have an important relationship to heart disease.

Angina is a type of chest pain caused by reduced blood flow to the heart. is often described as squeezing, pressure, heaviness, tightness or pain in the chest. During stable angina, episodes of chest discomfort are usually predictable. They can occur during exertion (such as running) or during mental or emotional stress. Normally, the chest discomfort is relieved with rest, use of nitroglycerin, or both. In unstable angina, chest pain can occur at any time—often while a person is resting. The discomfort may be more severe and last longer than in typical angina. The most common cause is reduced blood flow to the heart muscle because the coronary arteries are narrowed by fatty buildups.

There is an atypical case of angina known as Prinzmetal angina. While in general the outlook of patients with Prinzmental angina is quite good, this condition can cause serious problems. It can trigger dangerous and potentially fatal cardiac arrhythmias, especially ventricular fibrillation. And while heart attacks are uncommon with Prinzmetal angina, they indeed can occur, producing permanent damage to the heart muscle.

Prinzmetal angina occurs when an area within one of the major coronary arteries suddenly goes into spasm, temporarily shutting off blood flow to the heart muscle supplied by that artery. During these episodes, the electrocardiogram (ECG) shows dramatic elevations of the "ST segment" — the same ECG changes commonly seen with heart attacks.

We can see that the type of angina is directly related to the fact to present a heart disease.

• Thalach and target:

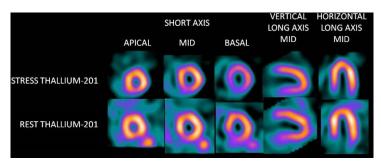
the heart disease count is present when the thalach is over 150. The median of this variable is 153

A normal heart rate is usually stated as 60 to 100 beats per minute. Slower than 60 is bradycardia ("slow heart"); faster than 100 is tachycardia ("fast heart").

Thal and target:

The stress level of 2 (fixed defect) indicates the mayor incidence to have heart disease.

A thallium stress test is a nuclear imaging test that shows how well blood flows into the heart while the patient is exercising or at rest (as in the next figure). This test is also called a cardiac or nuclear stress test. Abnormal results may indicate: Reduced blood flow to part of the heart caused by narrowing or blockage of one or more arteries that supply your heart muscle; Scarring of the heart muscle due to a previous heart attack; heart disease; a too-large heart, indicating other heart complications.



ca and target:

0 and 4 vessels indicate a mayor incidence to have heart disease

Five great vessels enter and leave the heart: the superior and inferior vena cava, the pulmonary artery, the pulmonary vein, and the aorta. Doctors use angiography to diagnose and treat blood vessel diseases and conditions. Angiography exams produce pictures of major blood vessels throughout the body. In some cases, contrast material is used.

• Oldpeak and target:

Lower Oldpeak (or depression) indicates heart disease

Slope and target:

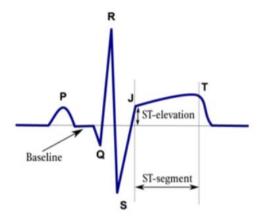
slope of Level 2 = downsloping indicates heart disease.

Slope and oldpeak:

there is more incidence of heart disease for patients with a slope of 2 and low oldpeak

An electrocardiogram — abbreviated as EKG or ECG — is a test that measures the electrical activity of the heartbeat. With each beat, an electrical impulse (or "wave") travels through the heart. This wave causes the muscle to squeeze and pump blood from the heart. A normal heartbeat on ECG will show the timing of the top and lower chambers.

For a better understanding of variables describing the EKG results, we can see in the next figure that a normal ST segment has a slight upward concavity. Flat, downsloping or depressed ST segments may indicate coronary ischemia. ST elevation may indicate transmural myocardial infarction.



The right and left atria or upper chambers make the first wave called a "P wave" — following a flat line when the electrical impulse goes to the bottom chambers. The right and left bottom chambers or ventricles make the next wave called a "QRS complex." The final wave or "T wave" represents electrical recovery or return to a resting state for the ventricles.

The variables that describe ECG: Restecg, Oldpeak, and Slope.

Restecg and target:

Restecg of 1 indicates having ST-T wave abnormality. The majority of observations with a heart disease had this measure. Interestingly, some of the patients with a normal level of 0 had a heart disease event.

Exang and target:

The level 0=no exercise angina (exang) indicate a count with patients with heart disease compared to level 1 = yes

• Exang and cp:

For a typical angina there is more incidence to have an exercise induced angina.

Gender and target:

women had more incidence of heart disease compared to men (in proportion to each genre).

It is known that gender plays a role in the symptoms, treatments and outcomes of coronary artery disease (CAD). According to the Texas Heart Institute, cardiovascular diseases affect more women than men and are responsible for more than 40% of all deaths in American women.

A simple linear regression model indicates that the features that had a moderate correlation with the target variable also have significant p-values. This points towards a possible reduction in the needed number of variables when shaping an optimal model for prediction. This could result in an improvement of the R-squared value which is 0.5175 considering all the regressors in the model.

```
lm(formula = target ~ ., data = heart2)
Residuals:
Min 1Q Median 3Q Max
-0.94748 -0.21270 0.06608 0.25022 0.93509
              Estimate Std. Error t value Pr(>|t|)
                         0.2929344
(Intercept) 0.8288987
                                      2.830 0.004987
                                    -0.304 0.761129
             -0.0008204
                         0.0026962
age
                         0.0471429
                                     -4.157 4.24e-05 ***
                                      5.036 8.40e-07 ***
             0.1127034
                         0.0223816
trestbps
             -0.0019910
                         0.0012573
                                    -1.583 0.114407
cho1
             -0.0003535
                         0.0004217
                                     -0.838 0.402545
fbs
             0.0173736
                         0.0596669
                                      0.291 0.771125
restecq
             0.0498480
                         0.0399228
                                      1.249 0.212819
thalach
                         0.0011304
                                      2.671 0.007988
exang
                         0.0513689
                                     -2.804 0.005387 **
oldpeak
             -0.0587887
                         0.0229269
                                     -2.564 0.010847
             0.0789788
slope
                         0.0423896
                                     1.863 0.063453
                         0.0218565
                                     -4.603 6.25e-06
thal
             -0.1190392
                         0.0356550 -3.339 0.000952 ***
signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 0.3542 on 289 degrees of freedom
Multiple R-squared: 0.5175, Adjusted R-squared: 0.49
F-statistic: 23.85 on 13 and 289 DF, p-value: < 2.2e-16
```

LOGISTIC REGRESSION MODEL

5. ORIGINAL LOGISTIC REGRESSION MODEL

In this model all the variables are included in the regression equation resulting in an AIC of 225.63

Applying a Stepwise Algorithm in direction backward, the lowest AIC of 219.79 is achieved by dropping the variables age, fbs, chol, restecg, and thalach from the original dataset. Most of these variables were suggested by the imndiag() function as non-significant when testing fo multicollinearity.

```
VTF
                   TOI
                            Wi
                                    Fi Leamer
                                                 CVIF Klein IND1
                                                                     IND2
        1.4435 0.6928 10.7173 11.7319 0.8323 -2.2366
                                                          0 0.0287 1.4009
ï..age
         1.1619 0.8607
                        3,9118 4,2821 0,9277 -1,8002
                                                          0 0.0356 0.6353
sex
                                7.5251 0.8823 -1.9902
         1.2845 0.7785
                        6.8743
                                                          0 0.0322 1.0098
cp
trestbps 1.1706 0.8543
                        4.1226
                                4.5129 0.9243 -1.8137
                                                          0 0.0353 0.6645
         1.1502 0.8694
                        3.6292
                                3.9728 0.9324 -1.7821
                                                          0 0.0360 0.5954
cho1
fbs
         1.0874 0.9196
                        2.1117
                                2.3116 0.9590 -1.6848
                                                          0 0.0381 0.3664
                                1.6137 0.9708 -1.6439
                                                          0 0.0390 0.2621
resteca 1.0610 0.9425
                        1.4741
thalach 1.6137 0.6197 14.8317 16.2359 0.7872
                                              -2.5003
                                                          0 0.0256 1.7342
                        9.7150 10.6348 0.8446
                                                          0 0.0295 1.3074
exang
         1.4020 0.7133
                                              -2.1723
oldpeak
         1.7059 0.5862 17.0582 18.6731 0.7656 -2.6431
                                                          0 0.0243 1.8868
slope
         1.6426 0.6088 15.5294 16.9995 0.7803 -2.5451
                                                          0 0.0252 1.7838
         1,2026 0,8316
                        4.8954
                                5.3589 0.9119 -1.8633
                                                          0 0.0344 0.7681
ca
thal
         1.1473 0.8716 3.5592 3.8962 0.9336 -1.7776
                                                          0 0.0361 0.5853
1 --> COLLINEARITY is detected by the test
0 --> COLLINEARITY is not detected by the test
ï..age , trestbps , chol , fbs , restecg , slope , coefficient(s) are non-significant may be due to multicollinearity
R-square of y on all x: 0.5175
```

6. REDUCED LOGISTIC REGRESSION MODEL

According to the variable reduction procedure, we generated a dataset modified which contains 8 variables: exang, trestbps (resting blood pressure), oldpeak, thal, sex, slope, cp, ca.

The result from the reduced logistical regression model results on an AIC of **219.79**, lower than I the original model.

7. MODELS COMPARISON

Both the original model and reduced model are shown in the next figure.

Original model (AIC = 225.63)

Reduced model (AIC = 219.79)

```
glm(formula = target ~ ., family = "binomial", data = heart)
Deviance Residuals:
Min 1Q
-2.9459 -0.2738
                   Median
                            3Q
0.4515
                                                                   call:
                   0.1012
                                                                   glm(formula = target ~ ., family = "binomial", data = new_heart)
Coefficients:
                                                                   Deviance Residuals:
             Estimate Std. Error z value Pr(>|z|)
                                                                   Min 1Q
-3.0264 -0.3305
                                                                                       Median
                                                                                                3Q
0.4577
             0.179045
0.027819
                        3.705420
0.025428
(Intercept)
                                    0.048 0.961461
                                                                                       0.1082
                                                                                                           2.9873
                                    1.094 0.273938
ï..age
                        0.570844
0.578000
sex1
             -1.862297
                                   -3.262 0.001105
                                                                   Coefficients:
             0.864708
cp1
                                    1.496 0.134645
                                                                                Estimate Std. Error z value Pr(>|z|)
             2.003186
2.417107
                                    3.784 0.000154 ***
cp2
                        0.529356
                                                                   (Intercept) 3.30454
                                                                                             4.33809
                        0.719242
                                                                                                        0.762 0.446210
                                    3.361 0.000778
ср3
                                                                                 -0.85234
                                                                                             0.43663
                                                                                                       -1.952 0.050925
                                                                   exang1
trestbps
chol
             -0.026162
                        0.011943
                                   -2.191 0.028481
             -0.004291
                                                                   slope1
                                                                                -0.90675
                                                                                             0.82751
                                                                                                       -1.096 0.273189
                        0.004245
                                   -1.011 0.312053
                                                                   slope2
                                                                                 0.70078
                                                                                             0.89682
                                                                                                        0.781 0.434570
fbs1
             0.445666
                        0.587977
                                    0.758 0.448472
             0.460582
                        0.399615
                                                                   trestbps
                                                                                 -0.02211
                                                                                             0.01093
                                                                                                       -2.023 0.043051
restecg1
restecq2
             -0.714204
                        2.768873
                                   -0.258 0.796453
                                                                   o1dpeak
                                                                                -0.47970
                                                                                             0.23137
                                                                                                       -2.073 0.038142
thalach
             0.020055
                        0.011859
                                                                   tha 1
                                                                                 2.62410
                                                                                             4.07723
                                                                                                        0.644 0.519836
                                                                                 2.36301
exang1
             -0.779111
                        0.451839
                                   -1.724 0.084652
                                                                   thal2
                                                                                             4.01217
                                                                                                        0.589 0.555888
            -0.397174
-0.775084
oldpeak
                        0.242346
                                   -1.639 0.101239
                                                                                 0.91673
                                                                                             4.01441
                                                                                                        0.228 0.819366
                                                                   thal3
                                   -0.880 0.378707
                                                                                -1.63154
                                                                                                       -3.095 0.001967
slope1
                        0.880495
                                                                   sex1
                                                                                             0.52712
s1ope2
             0.689965
                        0.947657
                                    0.728 0.466568
                                                                   cp1
                                                                                 1.03058
                                                                                             0.56475
                                                                                                        1.825 0.068023
                        0.527416
                                   -4.441 8.95e-06
             -2.342301
                                                                                             0.51711
ca1
                                                                                 2.22015
                                                                   cp2
                                                                                                        4.293 1.76e-05
ca2
            -3.483178
                        0.811640
                                   -4.292 1.77e-05 ***
                                                                                                        3.644 0.000268 ***
                                                                   ср3
                                                                                 2 55944
                                                                                             0 70231
ca3
             -2.247144
                        0.937629
                                   -2.397 0.016547
                                                                                 -2.35513
                                                                                             0.49869
                                                                                                       -4.723 2.33e-06
                                                                   ca1
                        1.720014
2.684285
ca4
             1.267961
                                    0.737 0.461013
                                                                   ca2
                                                                                -3.10939
                                                                                             0.75361
0.90067
                                                                                                       -4.126 3.69e-05 ***
                                    0.983 0.325808
             2.637558
                                                                   ca3
                                                                                -2.26756
                                                                                                       -2.518 0.011815
thal2
             2.367747
                        2.596159
                                    0.912 0.361759
                                                                                 1.23217
                                                                                             1.62177
                                                                                                        0.760 0.447393
             0.915115
                        2.600380
                                                                   Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
                                                                   (Dispersion parameter for binomial family taken to be 1)
(Dispersion parameter for binomial family taken to be 1)
                                                                       Null deviance: 417.64 on 302
                                                                                                         degrees of freedom
    Null deviance: 417.64 on 302 degrees of freedom
Residual deviance: 179.63 on 280 degrees of freedom
                                                                   Residual deviance: 185.79 on 286
                                                                                                         degrees of freedom
AIC: 225.63
                                                                   AIC: 219.79
Number of Fisher Scoring iterations: 6
                                                                   Number of Fisher Scoring iterations: 6
```

The test for significance has been applied by performing ANOVA test. The p-values are calculated using the chi-squared distribution, but like the parametric alternative they indicate whether each of the predictors has a significant effect on the probability of achieving an indicator value of 1.

The next figure shows the anova test for both the original and reduced models.

In the original model we see that the variables chol, fbs, and restecg are not significant for the model, whereas for the reduced model all the variables are significant at different levels of significance.

Original model

Reduced model

```
lr.anova <- anova(heart_mod1, test="Chisq")
lr.anova
                                                                       1r.anova_red
Analysis of Deviance Table
Model: binomial. link: logit
Response: target
                                                                     Response: target
Terms added sequentially (first to last)
         Df Deviance Resid. Df Resid. Dev Pr(>Chi)
                                     417.64
401.86 7.128e-05 ***
NULL
                             302
                             301
ï..age
                                     370.57 2.225e-08 ***
sex
               31.287
                            300
                                                                     NULL
ср
                                             0.026464 *
trestbps
               4.925
                                                                     exang
                            296
                                     287.99
cho1
                            295
294
                                             0.123181
                2.376
                                     285.62
                                                                     slope
                0.024
                                     285.59
                                                                     trestbps
restecg
thalach
                3.212
                            292
                                     282.38 0.200670
                                                                     oldpeak
              19.406
                                     262.98 1.057e-05 ***
257.36 0.017841 *
                            291
                                                                     thal
exang
oldpeak
                5.612
                            290
                            289
                                     240.17 3.371e-05 ***
               5.440
                            287
                                     slope
                                                                                3
                                                                     ср
ca '
thal
               41.394
                            283
                                                                                4
                                                                     ca
                                     179.63 0.003339 **
              13.703
                            280
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

```
lr.anova_red <- anova(heart_mod2, test="Chisq")</pre>
Analysis of Deviance Table
Model: binomial, link: logit
Terms added sequentially (first to last)
         Df Deviance Resid. Df Resid. Dev Pr(>Chi)
                                   417.64
                           302
              59.735
                                    357.90 1.085e-14 ***
                           301
                                    328.78 4.747e-07 ***
              29.121
                           299
               4.346
                           298
                                    324.44
                                            0.03710 *
              20.581
                           297
                                    303.85 5.716e-06 ***
              37.759
                           294
                                    266.10 3.179e-08 ***
               5.892
                           293
                                    260.20 0.01521 *
              29.857
                           290
                                   230.35 1.479e-06 ***
              44.562
                                   185.79 4.903e-09 ***
                           286
signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Now, performing an ANOVA test comparing both the original and reduced models, the P-value based on chi-squared distribution indicates that we fail in reject the null Hypothesis which estates that the two models are equal. What this means is that the reduced model is better that the original containing all the regressor variables.

From the reduced model, we can see that for example if all regressors are held at a fixed value, the odds of getting heart disease for males (sex=1) over the odds of getting heart disease for females is exp(-1.63154) = 0.1956 i.e. the odds are lower than the odds of the women getting heart disease. This was known already from the data exploratory analysis.

8. TRAINING AND PREDICTING BASED ON LOGISTIC REGRESSION MODEL

The distribution of the target attribute is 138 patients with positive diagnostic and 165 healthy people, indicating that there is not a problem of class imbalance, therefore, we can proceed to create a predictive model.

Prediction was performed based on both the original dataset and the reduced dataset.

For each model, a random subset of the datasets of 80% represents the training datasets, and 20% the testing datasets. For each one, there is not a problem of class imbalance.

In the reduced dataset, the logistic regression model results in the probability for an observation to be classified as 1 or 0. As an example, next is a subset of those probabilities:

```
0 1
2 0.06652322 0.93347678
4 0.04068366 0.95931634
7 0.10056956 0.89943044
11 0.24336317 0.75663683
19 0.33146211 0.66853789
21 0.91022795 0.08977205
```

9. ACCURACY EVALUATION

Original Prediction model

Reduced Prediction model

```
Confusion Matrix and Statistics
                                           Confusion Matrix and Statistics
         Reference
                                                     Reference
Prediction 0 1
                                           Prediction 0 1
0 22 1
        0 20 1
        1 7 32
                                                    1 5 32
              Accuracy: 0.8667
                                                          Accuracy: 0.9
                95% CI : (0.7541, 0.9406)
                                                            95% ci : (0.7949, 0.9624)
   No Information Rate : 0.55
                                               No Information Rate: 0.55
   P-Value [Acc > NIR] : 1.653e-07
                                               P-Value [Acc > NIR] : 4.558e-09
                 карра : 0.7251
                                                             карра : 0.7952
Mcnemar's Test P-Value: 0.0771
                                            Mcnemar's Test P-Value: 0.2207
            Sensitivity: 0.7407
                                                       Sensitivity: 0.8148
           Specificity: 0.9697
                                                       Specificity: 0.9697
        Pos Pred Value: 0.9524
                                                   Pos Pred Value : 0.9565
        Neg Pred Value : 0.8205
                                                   Neg Pred Value : 0.8649
            Prevalence: 0.4500
                                                        Prevalence: 0.4500
        Detection Rate: 0.3333
                                                   Detection Rate: 0.3667
  Detection Prevalence : 0.3500
                                              Detection Prevalence: 0.3833
     Balanced Accuracy : 0.8552
                                                 Balanced Accuracy : 0.8923
       'Positive' Class: 0
                                                  'Positive' Class: 0
```

For the original dataset, Logistic Regression Modeling resulted in 86% of accuracy prediction. Whereas for the reduced dataset the prediction accuracy was 90%.

Both models are more specific than sensitive, which means that they predict better false negative cases.

Because we are analyzing a human disease, a False Negative (ignoring the probability of disease there in reality there is one) is more dangerous than a False Positive indicating the case when the prediction results in 1 when in reality is 0. We see that in both models, the false negative resulted in just 1 observation.

Both models performed well based on the Area Under the Curve defined by the levels of Specificity and sensitivity. For both models the AUC= 0.945

10. CONCLUSIONS

- The variables slope, exang, trestbps, oldpeak, thal, sex, cp, and ca are the features that play a significant role in driving the prediction of the heart disease condition.
- These variables allowed for a prediction accuracy of 90% based on a logistic regression model, resulting in both a parsimonious and specific model. This is the best model built under this approach, however, further analysis by training and testing different models could be necessary to compare to the logistic regression model.

REFERENCES

https://www.texasheart.org/heart-health/heart-information-center/topics/women-and-heart-disease/

https://www.mayoclinic.org/diseases-conditions/angina/symptoms-causes/syc-20369373