

THE RADIO SKY AT METER WAVELENGTHS: *M*-MODE ANALYSIS IMAGING WITH THE OWENS VALLEY LONG WAVELENGTH ARRAY

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ABSTRACT

I present all-sky maps of the sky from the Owens Valley Long Wavelength Array. These maps are created from the application of *m*-mode analysis.

Keywords: cosmology: observations – dark ages, reionization, first stars – radio continuum: galaxies
– radio continuum: ISM

1. INTRODUCTION

Studies of the cosmic microwave background (CMB) have given us an unprecedented understanding of the universe during the epoch of recombination (Hinshaw et al. 2013; Planck Collaboration et al. 2014, 2016b). Before arriving at the Earth, the light from the CMB propagates through the intergalactic medium (IGM), intervening galaxies and galaxy clusters, and the Milky Way’s interstellar medium (ISM). As photons from the CMB propagate through this intervening material, scattering, absorption, or additional emission can perturb or corrupt the thermal CMB spectrum. In order to measure the pristine CMB, these foreground components (eg. synchrotron emission, free-free emission, thermal dust emission) are a nuisance and careful modeling and removal of these components is essential (Planck Collaboration et al. 2016a,c).

However in many cases the study of CMB foregrounds is scientifically interesting in its own right. Measurements of dust-correlated anomalous microwave emission (Leitch et al. 1997) led to the discovery of spinning dust emission (Draine & Lazarian 1998). Thomson scattering in the IGM attenuates the CMB spectrum, but the optical depth implies a mean redshift to the Epoch of Reionization (EoR) of $z_r = 8.8^{+1.7}_{-1.4}$ (Planck Collaboration et al. 2016b). The thermal Sunyaev-Zel’dovich effect (Sunyaev & Zel’dovich 1970, 1972) has been used to discover new galaxy clusters (Vanderlinde et al. 2010) and measure the distance to galaxy clusters when combined with X-ray measurements (Bonamente et al. 2006). The kinetic Sunyaev-Zel’dovich effect has been used to constrain the duration of reionization $\Delta z_r \leq 4.4$ (Zahn et al. 2012).

At redshifts $20 \gtrsim z \gtrsim 7$ the 21 cm hyperfine structure line of neutral hydrogen is expected to produce a 10 to 100 mK perturbation in the CMB spectrum (Furlanetto et al. 2006; Pritchard & Loeb 2012). The amplitude of this perturbation on a given line-of-sight is a function of the neutral fraction of hydrogen, the baryon overdensity, the spin temperature relative to the CMB temperature at the given redshift, and the line-of-sight peculiar velocity of the gas. The spatial power spectrum of this perturbation is thought to be dominated by inhomogeneous heating of the IGM at $z \sim 20$ (Fialkov et al. 2014), and by growing ionized bubbles during the EoR at $z \sim 7$ where a detection can constrain the ionizing efficiency of early galaxies, the UV photon mean-free-path, and the minimum halo mass that can support star formation (Greig & Mesinger 2015).

Current 21 cm cosmology experiments can be broadly separated into two classes: global experiments that are aiming to detect the spectral signature of the cosmologi-

cally redshifted 21 cm transition after averaging over the entire sky, and power spectrum experiments that incorporate angular information to attempt to measure the 3D spatial power spectrum of cosmological 21 cm perturbations. Ongoing global experiments include EDGES (Bowman & Rogers 2010; Monsalve et al. 2017), LEDA (Price 2017), BIGHORNS (Sokolowski et al. 2015), SCI-HI (Voytek et al. 2014), and SARAS 2 (Singh et al. 2017). Ongoing power spectrum experiments include PAPER/HERA (Ali et al. 2015; DeBoer et al. 2016), LOFAR (Patil et al. 2017), and the MWA (Beardsley et al. 2016).

Just as for CMB experiments, foreground removal or suppression is an essential component of both classes of 21 cm cosmology experiments. The brightness temperature of the galactic synchrotron emission at high galactic latitudes is measured by Rogers & Bowman (2008) as

$$T \sim 300 \text{ K} \times \left(\frac{\nu}{150 \text{ MHz}} \right)^{-2.5}. \quad (1)$$

Therefore experiments conservatively need to achieve at least 4 orders of dynamic range against this foreground emission before the cosmological signal can be measured. Current foreground removal methods (for example, Parsons et al. 2012) rely on the assumption that the foreground emission (after convolving with the instrumental response) is spectrally smooth. However the low-frequency radio sky is composed of several components: galactic synchrotron emission, supernova remnants, radio galaxies, free-free emission and absorption from H II regions, and a confusing background of radio sources. Ideally a foreground removal strategy should be informed by the measured spatial structure and frequency spectrum of all foreground components. However this possibility is limited by the availability of suitable high-fidelity low-frequency sky maps on angular scales ranging from tens of degrees to arcminutes.

The Global Sky Model (GSM) (de Oliveira-Costa et al. 2008; Zheng et al. 2017a) is a data-driven interpolation of various maps between 10 MHz and 100 GHz. However the majority of information contained in the GSM is derived at higher frequencies where the majority of the input maps are located. Below 408 MHz, the interpolation is largely driven by the Haslam 408 MHz map (Haslam et al. 1981, 1982). At lower frequencies, free-free absorption and synchrotron self-absorption becomes increasingly important and hence spectral indices derived at higher frequencies need corrections at lower frequencies.

Recently a host of new low-frequency sky surveys have been conducted including MSSS (Heald et al. 2015), GLEAM (Wayth et al. 2015), and TGSS (Intema et al. 2017). However, the primary data product generated by

these surveys is a catalog of radio point sources. Surveys that capture the diffuse emission include at 45 MHz, where Guzmán et al. (2011) produced a map of the sky with 5° resolution, and the LWA1 Low Frequency Sky Survey (Dowell et al. 2017), which covers a range of frequencies between 35 MHz and 80 MHz with resolution between 4.5° and 2° .

In this paper we will present a series of new low-frequency maps of the sky between 36.528 MHz and 73.152 MHz, capturing the full sky visible from the Owens Valley Radio Observatory (OVRO) with angular resolution of roughly $10'$. These maps are generated using m -mode analysis imaging – a new imaging technique for transit telescopes.

2. ALL-SKY IMAGING

The goal of all imaging algorithms is to estimate the brightness of the sky $I_\nu(\hat{r})$ in the direction \hat{r} and frequency ν . A radio interferometer measures the visibilities V_ν^{ij} between pairs of antennas – here numbered i and j respectively. If the antennas are separated by the baseline \vec{b}_{ij} , and $A_\nu(\hat{r})$ describes their response to the incident radiation, then

$$V_\nu^{ij} = \int_{\text{sky}} A_\nu(\hat{r}) I_\nu(\hat{r}) \exp\left(2\pi i \hat{r} \cdot \vec{b}_{ij}/\lambda\right) d\Omega. \quad (2)$$

Constructing an image from the output of a radio interferometer therefore consists of estimating $I_\nu(\hat{r})$ given the available measurements V_ν^{ij} .

For later convenience we will define the baseline transfer function $B_\nu^{ij}(\hat{r})$ such that

$$V_\nu^{ij} = \int_{\text{sky}} B_\nu^{ij}(\hat{r}) I_\nu(\hat{r}) d\Omega. \quad (3)$$

The baseline transfer function defines the response of a single baseline to the sky, and is a function of the antenna primary beam, and baseline length and orientation.

Naively one might attempt to solve Equation 2 by discretizing, and subsequently solving the resulting matrix equation. If the interferometer is composed of N_{base} baselines, and measures N_{freq} frequency channels over N_{time} integrations, then the entire data set consists of $N_{\text{base}}N_{\text{freq}}N_{\text{time}}$ complex numbers. If the sky is discretized into N_{pix} pixels then the relevant matrix has dimensions of $(N_{\text{base}}N_{\text{freq}}N_{\text{time}}) \times (N_{\text{pix}})$. For making single-channel maps with the OVRO-LWA this becomes a 5 petabyte array (assuming each matrix element is a 64-bit complex floating point number). This matrix equation is therefore prohibitively large, and solving Equation 2 by means of discretization is usually impossible although Zheng et al. (2017b) demonstrate this technique with the MITEOR telescope.

Instead it is common to make mild assumptions that simplify Equation 2 and ease the computational burden in solving for $I_\nu(\hat{r})$. For example, when all of the baselines \vec{b}_{ij} lie in a plane and the field-of-view is small, Equation 2 can be well-approximated by a two-dimensional Fourier transform (Thompson et al. 2001). The restriction on baseline co-planarity and field-of-view can be relaxed by using W-projection (Cornwell et al. 2008). Known primary beam effects can also be accounted for during imaging by using A-projection (Bhattacharjee et al. 2013).

2.1. m -Mode Analysis

On the other hand, transit telescopes can take advantage of a symmetry in Equation 2 that greatly reduces the amount of computer time required to image the full-sky with exact incorporation of widefield imaging effects. This technique, called m -mode analysis, also obviates the need for gridding and mosaicing. Instead the entire sky is imaged in one coherent synthesis imaging step.

In this context we will define a transit telescope as any interferometer where the response pattern of the individual elements does not change with respect to time. This may be an interferometer like the OVRO-LWA where the correlation elements are fixed dipoles, but it may also be an interferometer like LOFAR or the MWA if the steerable beams are held in a fixed position (not necessarily at zenith).

We will briefly summarize m -mode analysis below, but the interested reader should consult Shaw et al. (2014, 2015) for a complete derivation.

For a transit telescope, the visibilities V_ν^{ij} are a periodic function of sidereal time.¹ Therefore it is a very natural operation to compute the Fourier transform of the visibilities with respect to sidereal time $\phi \in [0, 2\pi]$.

$$V_{m,\nu}^{ij} = \int_0^{2\pi} V_\nu^{ij}(\phi) \exp\left(-im\phi\right) d\phi \quad (4)$$

The output of this Fourier transform is the set of m -modes $V_{m,\nu}^{ij}$ where $m = 0, \pm 1, \pm 2, \dots$ is the Fourier conjugate variable to the sidereal time. The m -mode corresponding to $m = 0$ is a simple average of the visibilities over sidereal time. Similarly $m = 1$ corresponds to the component of the visibilities that varies over half-day timescales. Larger values of m correspond to components that vary on quicker timescales.

It can be shown that there is a discrete linear relationship between the measured m -modes $V_{m,\nu}^{ij}$ and

¹ This is not strictly true. Ionospheric fluctuations and non-sidereal sources (such as the sun) will violate this assumption. This paper will, however, demonstrate that the impact on the final maps is mild.

the spherical harmonic coefficients of the sky brightness $a_{lm,\nu}$.

$$V_{m,\nu}^{ij} = \sum_l B_{lm,\nu}^{ij} a_{lm,\nu}, \quad (5)$$

where the transfer coefficients $B_{lm,\nu}^{ij}$ define the interferometer's response to the sky. These transfer coefficients are computed from the spherical harmonic transform of the baseline transfer function defined by Equation 3.

Equation 5 can be recognized as a matrix equation where the transfer matrix \mathbf{B} is block-diagonal.

$$\underbrace{\begin{pmatrix} \vdots \\ m\text{-modes} \\ \vdots \end{pmatrix}}_{\mathbf{v}} = \underbrace{\begin{pmatrix} \ddots & & \\ & \text{transfer matrix} & \\ & & \ddots \end{pmatrix}}_{\mathbf{B}} \underbrace{\begin{pmatrix} \vdots \\ a_{lm} \\ \vdots \end{pmatrix}}_{\mathbf{a}} \quad (6)$$

$$\mathbf{B} = \begin{pmatrix} m=0 & & & \\ & m=\pm 1 & & \\ & & m=\pm 2 & \\ & & & \ddots \end{pmatrix} \quad (7)$$

The vector \mathbf{v} contains the list of m -modes and the vector \mathbf{a} contains the list of spherical harmonic coefficients representing the sky brightness. In order to take advantage of the block-diagonal structure in \mathbf{B} , \mathbf{v} and \mathbf{a} must be sorted by the absolute value of m . Positive and negative values of m are grouped together because the brightness of the sky is real-valued, and the spherical harmonic transform of a real-valued function has $a_{l(-m)} = (-1)^m a_{lm}^*$.

In practice we now need to pick the set of spherical harmonics we will use to represent the sky. For an interferometer like the OVRO-LWA with lots of short baselines, a sensible choice is to use all spherical harmonics with $l \leq l_{\max}$ for some l_{\max} . The parameter l_{\max} is determined by the maximum baseline length of the interferometer. For an interferometer without short spacings, a minimum value for l might also be used. This l_{\min} parameter should be determined by the minimum baseline length. When creating the maps presented in this paper, we use $l_{\min} = 0$ and $l_{\max} = 1000$.

The interferometer's sensitivity to the monopole (a_{00}) deserves special consideration. Venumadhav et al. (2016) prove – under fairly general assumptions – that a baseline with nonzero sensitivity to a_{00} must also have some amount of cross-talk or common-mode noise. In fact the sensitivity to a_{00} is proportional to a sum of these effects. For example, one way a baseline can have nonzero sensitivity to a_{00} is if the baseline is extremely

short. In this case the antennas are so close together that voltage fluctuations in one antenna can couple into the other antenna. In order to make an interferometric measurement of a_{00} , this coupling must be measured and calibrated.

The size of a typical block in the transfer matrix is $(2N_{\text{base}}N_{\text{freq}}) \times (l_{\max})$. If each element of the matrix is stored as a 64-bit complex floating point number, a single block is 500 MB for the case of single-channel imaging with the OVRO-LWA. Compare this number with the 5 PB required for the naive approach. The power of m -mode analysis is the block-diagonal structure of Equation 6. By breaking up the problem into N independent blocks, the computational complexity involved in inverting a single block is reduced by a factor of N^3 relative to a dense matrix. However we must invert N blocks, so the overall computational savings is proportional to N^2 . For the case of the OVRO-LWA the equation breaks up into $\sim 10^3$ blocks and so we save a factor of $\sim 10^6$ in processing time by using m -mode analysis.

2.2. m -Mode Analysis Imaging

Imaging in m -mode analysis essentially amounts to inverting Equation 6 to solve for the spherical harmonic coefficients \mathbf{a} . The linear-least squares solution, which minimizes $\|\mathbf{v} - \mathbf{Ba}\|^2$, is given by

$$\hat{\mathbf{a}}_{\text{LLS}} = (\mathbf{B}^* \mathbf{B})^{-1} \mathbf{B}^* \mathbf{v}, \quad (8)$$

where $*$ indicates the conjugate-transpose. However, usually one will find that \mathbf{B} is not full-rank and hence $\mathbf{B}^* \mathbf{B}$ is not an invertible matrix. For example, an interferometer located in the northern hemisphere will never see a region of the southern sky centered on the southern celestial pole. The m -modes contained in the vector \mathbf{v} must contain no information about the sky around the southern celestial pole, and therefore the act of multiplying by \mathbf{B} must destroy some information about the sky. The consequence of this fact is that \mathbf{B} must have at least one singular value that is equal to zero. It is then trivial to show that $\mathbf{B}^* \mathbf{B}$ must have at least one eigenvalue that is equal to zero, which means it is not an invertible matrix.

Another way of looking at the problem is that because the interferometer is not sensitive to part of the southern hemisphere, there are infinitely many possible solutions to Equation 6 that will fit the measured data equally well. So we need to regularize the problem and apply an additional constraint that prefers a unique solution. For example, you may prefer that in the absence of any information the sky should be set to zero or you may prefer that the sky should be set to some prior expectation.

2.2.1. Tikhonov Regularization

The process of Tikhonov regularization minimizes $\|\mathbf{v} - \mathbf{B}\mathbf{a}\|^2 + \varepsilon\|\mathbf{a}\|^2$ for some arbitrary value of $\varepsilon > 0$ chosen by the observer. The solution that minimizes this expression is given by

$$\hat{\mathbf{a}}_{\text{Tikhonov}} = (\mathbf{B}^* \mathbf{B} + \varepsilon \mathbf{I})^{-1} \mathbf{B}^* \mathbf{v}. \quad (9)$$

Tikhonov regularization adds a small value ε to the diagonal of $\mathbf{B}^* \mathbf{B}$, fixing the matrix's singularity. We can see this by using the singular value decomposition (SVD) of the matrix $\mathbf{B} = \mathbf{U} \Sigma \mathbf{V}^*$. Equation 9 becomes

$$\hat{\mathbf{a}}_{\text{Tikhonov}} = \mathbf{V} (\Sigma^2 + \varepsilon \mathbf{I})^{-1} \Sigma \mathbf{U}^* \mathbf{v}, \quad (10)$$

where

$$\Sigma = \begin{pmatrix} \sigma_1 & & \\ & \sigma_2 & \\ & & \ddots \end{pmatrix}.$$

The diagonal elements of Σ are the singular values of \mathbf{B} and so the contribution of each singular component to the Tikhonov-regularized solution is scaled by $\sigma_i / (\sigma_i^2 + \varepsilon)$, where σ_i is the singular value for the i th singular component. Tikhonov regularization therefore acts to suppress any component for which $\sigma_i \lesssim \sqrt{\varepsilon}$. If $\sigma_i = 0$, the component is set to zero.

In practice the measurement \mathbf{v} is corrupted by noise with covariance \mathbf{N} . For illustrative purposes we will assume that $\mathbf{N} = n\mathbf{I}$ for some scalar n . In this case the covariance of the Tikhonov-regularized spherical harmonic coefficients is

$$\mathbf{C} = n\mathbf{V} (\Sigma^2 + \varepsilon \mathbf{I})^{-2} \Sigma^2 \mathbf{V}^*. \quad (11)$$

Each singular component is scaled by a factor of $\sigma_i^2 / (\sigma_i^2 + \varepsilon)^2$. In the absence of Tikhonov regularization ($\varepsilon = 0$) singular components with the smallest singular values – the ones that the interferometer is the least sensitive to – actually come to dominate the covariance of the measured spherical harmonic coefficients. Tikhonov regularization improves this situation by downweighting these components.

While Tikhonov regularization will force unmeasured modes to zero, if a prior map of the sky already exists, it will be preferable to instead minimize $\|\mathbf{v} - \mathbf{B}\mathbf{a}\|^2 + \varepsilon\|\mathbf{a} - \mathbf{a}_{\text{prior}}\|^2$.

2.2.2. L-Curves

Tikhonov regularization requires the observer to pick the value of ε . If ε is too large then too much importance is placed on minimizing the norm of the solution and the least-squares residuals will suffer. However if ε is too

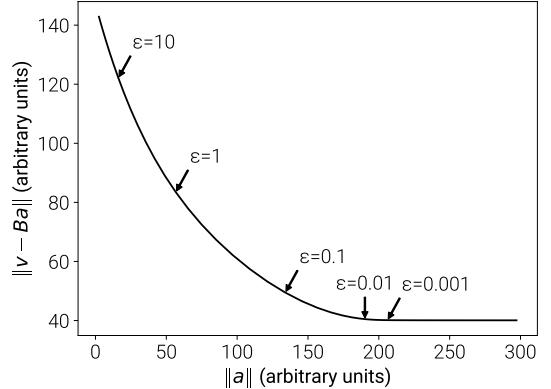


Figure 1. An example L-curve using OVRO-LWA data at 36.528 MHz. The x -axis is the norm of the solution (in this case the spherical harmonic coefficients) given in arbitrary units. The y -axis is the least-squares norm given in arbitrary units. ε is the regularization parameter. When the regularization parameter is small, the norm of the solution grows rapidly. When the regularization parameter is large, the least-squares norm grows rapidly.

small then the problem will be poorly regularized and the resulting sky map may not represent the true sky. Picking the value of ε therefore requires understanding the trade-off between the two norms.

This trade-off can be analyzed quantitatively by trialing several values of ε and computing $\|\mathbf{v} - \mathbf{B}\mathbf{a}\|^2$ and $\|\mathbf{a}\|^2$ for each trial. An example is shown in Figure 1. The shape of this curve has a characteristic L-shape, and as a result this type of plot is called an L-curve. The ideal value of ε lies near the turning point of the plot. At this point a small decrease in ε will lead to an undesired rapid increase in $\|\mathbf{a}\|^2$, and a small increase in ε will lead to an undesired rapid increase in $\|\mathbf{v} - \mathbf{B}\mathbf{a}\|^2$.

In practice, the L-curve should be used as a guide to estimate a reasonable value of ε . However better results can often be obtained by tuning the value of ε . For instance increasing the value of ε can improve the noise properties of the map by down-weighting noisy modes. Decreasing the value of ε can improve the resolution in the map by up-weighting the contribution of longer baselines, which are likely fewer in number. In this respect choosing the value of ε is analogous to picking the weighting scheme in traditional imaging where robust weighting schemes can be tuned to similar effect (Briggs 1995).

2.2.3. The Moore-Penrose Pseudoinverse

The Moore-Penrose pseudoinverse (denoted in this paper with a superscript \dagger), is commonly applied to find the minimum-norm linear-least squares solution to a set of linear equations. This can be used in place of

Tikhonov regularization as

$$\hat{\mathbf{a}}_{\text{Moore-Penrose}} = \mathbf{B}^\dagger \mathbf{v}. \quad (12)$$

Much like Tikhonov regularization, the Moore-Penrose pseudoinverse sets components with small singular values (below some user-defined threshold) to zero. Components with large singular values (above the user-defined threshold) are included in the calculation at their full amplitude with no down-weighting of modes near the threshold. The essential difference between using the Moore-Penrose pseudoinverse and Tikhonov regularization is that the pseudoinverse defines a hard transition from on to off. Modes are either set to zero or included in the map at their full amplitude. On the other hand Tikhonov regularization smoothly interpolates between these behaviors. Because of this, Tikhonov regularization tends to produce better results in practical applications.

2.3. CLEAN

In traditional radio astronomy imaging, the CLEAN algorithm (Högbom 1974) is used to interpolate the measured visibilities onto the uv -plane. In the absence of this interpolation, gaps in the interferometer's uv -coverage are assumed to be zero, and in the image plane sources are convolved with a point spread function (PSF) that is characteristic of the uv -coverage. Fundamentally, the interferometer's PSF in the dirty images is determined by which modes were assumed to be zero in the initial imaging process.

In m -mode analysis imaging, we assumed modes were zero in two separate ways:

1. We selected a set of spherical harmonic coefficients a_{lm} to describe the sky brightness distribution. All modes with $l > l_{\max}$ are neglected and assumed to be zero.
2. Tikhonov regularization forces linear combinations of spherical harmonic coefficients with $\sigma_i \lesssim \sqrt{\varepsilon}$ towards zero.

As a consequence the final map of the sky is not assembled from a complete set of spherical harmonics. Therefore just as in traditional imaging, m -mode analysis imaging produces dirty maps where sources are convolved with a PSF. This PSF can be improved by increasing the number and variety of baselines, which increases the number of modes where $\sigma_i \gg \sqrt{\varepsilon}$. Alternatively by collecting more data, the signal-noise ratio of the measured m -modes increases, which allows the observer to lower the value of ε without increasing the noise in the maps. Finally, the CLEAN algorithm can be

applied to interpolate some of the missing information that was assumed to be zero.

The PSF of a dirty m -mode analysis map may be computed with

$$\mathbf{a}_{\text{PSF}}(\theta, \phi) = (\mathbf{B}^* \mathbf{B} + \varepsilon \mathbf{I})^{-1} \mathbf{B}^* \mathbf{B} \mathbf{a}_{\text{PS}}(\theta, \phi), \quad (13)$$

where $\mathbf{a}_{\text{PSF}}(\theta, \phi)$ is the vector of spherical harmonic coefficients representing the PSF at the spherical coordinates (θ, ϕ) , and $\mathbf{a}_{\text{PS}}(\theta, \phi)$ is the vector of spherical harmonic coefficients for a point source at (θ, ϕ) given by

$$\mathbf{a}_{\text{PS}}(\theta, \phi) = \begin{pmatrix} \vdots \\ Y_{lm}^*(\theta, \phi) \\ \vdots \end{pmatrix} = \begin{pmatrix} \vdots \\ Y_{lm}^*(\theta, 0) \times e^{im\phi} \\ \vdots \end{pmatrix}. \quad (14)$$

In general the PSF can be a function of the right ascension and declination. However point sources at the same declination take the same track through the sky and therefore (barring any ionospheric effects) will have the same PSF. The PSF is therefore only a function of the declination. For example, sources at low elevations will tend to have an extended PSF along the north-south axis due to baseline foreshortening. An example computed PSF is shown in Figure 2. Adapting CLEAN for m -mode analysis requires either pre-computing Equation 13 at a grid of declinations, or a method for rapidly evaluating Equation 13 on the fly.

TODO: cite lincoln's paper on cleaning with a changing psf

For an interferometer with more baselines than spherical harmonics used in the maps (eg. the OVRO-LWA), $\mathbf{B}^* \mathbf{B}$ can be a much smaller matrix than the full transfer matrix \mathbf{B} . Therefore pre-computing $\mathbf{B}^* \mathbf{B}$ can allow the entire matrix to fit into memory on a single machine. This greatly reduces the amount of disk I/O necessary for solving Equation 13.

Additionally we can pre-compute the Cholesky decomposition of $\mathbf{B}^* \mathbf{B} + \varepsilon \mathbf{I} = \mathbf{U}^* \mathbf{U}$, where \mathbf{U} is an upper-triangular matrix. Inverting an upper triangular matrix is an $\mathcal{O}(N^2)$ operation (instead of $\mathcal{O}(N^3)$ for a general matrix inverse).² Equation 13 can then be rapidly evaluated from right to left as:

$$\mathbf{a}_{\text{PSF}} = \mathbf{U}^{-1} (\mathbf{U}^*)^{-1} (\mathbf{B}^* \mathbf{B}) \mathbf{a}_{\text{PS}}. \quad (15)$$

Furthermore, Equation 15 does not need to be separately evaluated for each CLEAN component. Instead

² Inverting a matrix is numerically unstable and should be avoided. Instead of computing \mathbf{A}^{-1} , the linear equation $\mathbf{Ax} = \mathbf{b}$ is solved each time the matrix inverse is needed.

we can identify N CLEAN components, accumulate \mathbf{a}_{PS} for each component, and evaluate Equation 15 on the accumulation. This can greatly reduce the number of times this equation needs to be evaluated, but care must be taken to ensure that the N components are not so close together that sidelobes from one may interact with another.

TODO: describe blurring to avoid cleaning the diffuse emission

Altogether the adaptation of CLEAN applied to the maps presented in this paper is summarized below.

Precondition: \mathbf{a} is the solution to Equation 9

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1: function CLEAN( $\mathbf{a}$ )
2:    $\mathbf{M} \leftarrow \mathbf{B}^* \mathbf{B}^*$ 
3:    $\mathbf{U} \leftarrow \text{chol}(\mathbf{B})$             $\triangleright$  Cholesky decomposition
4:   while noise in map > threshold do
5:     find  $N$  pixels with the largest residual flux
6:      $\mathbf{x} \leftarrow \sum_{i=1}^N (\text{pixel flux}) \times \mathbf{a}_{\text{PS}}(\theta_i, \phi_i)$ 
7:      $\mathbf{y} \leftarrow \mathbf{U}^{-1}(\mathbf{U}^*)^{-1} \mathbf{M} \mathbf{x}$ 
8:      $\mathbf{a} \leftarrow \mathbf{a} - (\text{loop gain}) \times \mathbf{y}$ 
9:     record subtracted components
10:     $\mathbf{a} \leftarrow \mathbf{a} + (\text{restored components})$ 
11:   return  $\mathbf{a}$ 
```

3. OBSERVATIONS

3.1. The Owens Valley Long Wavelength Array

The Owens Valley Long Wavelength Array (OVRO-LWA) is a 288-element interferometer located at the Owens Valley Radio Observatory near Big Pine, California (Hallinan 2017). The OVRO-LWA is a low-frequency instrument with instantaneous bandwidth covering 27.384 MHz to 84.912 MHz with 24 kHz channelization. Each antenna stand hosts two perpendicular broadband dipoles so that there are 288×2 signal paths in total. These signal paths feed into the 512-input LEDA correlator (Kocz et al. 2015), which allows the OVRO-LWA to capture the entire visible hemisphere in a single snapshot image. In the current configuration 32 antennas (64 signal paths) are unused.

The 288 antennas are arranged in a pseudo-random configuration optimized to minimize sidelobes in snapshot imaging. 251 of the antennas are contained within a 200 m diameter core. 32 antennas are placed outside of the core in order to extend the maximum baseline length to ~ 1.5 km. The final 5 antennas are equipped with noise-switched front ends for calibrated total power measurements of the global sky brightness. These antennas are used as part of the LEDA experiment (Price 2017) to measure the global signal of 21 cm absorption from the cosmic dawn. The left panel of Figure 2 is a diagram of the antenna configuration.

3.2. The Rainy Day Dataset

The dataset used in this paper spans 28 consecutive hours beginning at 2017-02-17 12:00:00 UTC time. This time was chosen based on the fact that it was raining at OVRO and rain tends to improve the low-frequency RFI environment considerably. During this time the OVRO-LWA operated as a zenith-pointing drift scanning interferometer. The correlator dump time was selected to be 13 seconds such that the correlator output evenly divides a sidereal day.

The geomagnetic conditions during this time were mild. The Disturbance storm time (Dst) index was > -30 nT during the entirety of the observing period.³ Following the classification scheme of Kintner et al. (2008), a weak geomagnetic storm has Dst < -30 nT. Therefore there were no geomagnetic storms during the time of these observations.

3.3. Gain Calibration

Antenna gain calibration is accomplished using an iterative method independently developed by Mitchell et al. (2008) and Salvini & Wijnholds (2014). The calibration routine is written in the Julia programming language (Bezanson et al. 2017), and is publicly available online⁴ under an open source license (GPLv3+).

Cyg A and Cas A are – by an order of magnitude – the brightest point-like radio sources in the northern hemisphere. Therefore the optimal time to solve for the interferometer’s gain calibration is when these sources are at high elevations. The antenna complex gains are measured from a 22 minute track of data from when Cyg A and Cas are at high elevations. The gains measured in this way are then used to calibrate the entire 28 hour dataset. The calibration sky model consists only of Cyg A and Cas A. The model flux of Cyg A is set to the Baars et al. (1977) spectrum while the flux of Cas A is measured from the data itself (using a preliminary calibration).

Temperature fluctuations within the electronics shelter generate 0.1 dB sawtooth oscillations in the analog gain. These oscillations occur with a variable 15 to 17 minute period. The amplitude of these gain fluctuations is calibrated by smoothing the autocorrelation amplitudes on 45 minute timescales. The ratio of the measured auto-correlation power to the smoothed auto-correlation power defines a per-antenna amplitude correction that is then applied to the cross-correlations.

³ The Dst index was obtained from the World Data Center for Geomagnetism, Kyoto University (<http://swdcwww.kugi.kyoto-u.ac.jp/>).

⁴ <https://github.com/mwestwood/TTCal.jl>

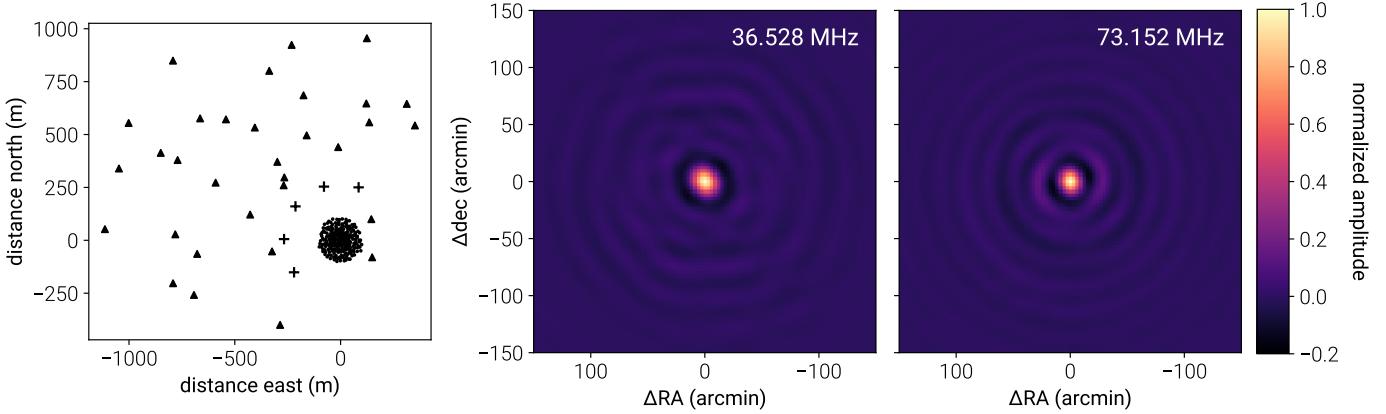


Figure 2. (left panel) This figure shows the antenna layout for the OVRO-LWA. Black dots correspond to antennas within the 200 m diameter core of the array. The 32 open circles are the expansion antennas built in early 2016 in order to increase the longest baseline to 1.5 km. The 5 crosses are antennas equipped with noise-switched front ends. (middle panel) The computed m -mode analysis imaging PSF for the OVRO-LWA for a point source at a declination of $+45^\circ$ and frequency of 36.528 MHz. (right panel) The computed m -mode analysis imaging PSF for the OVRO-LWA for a point source at a declination of $+45^\circ$ and frequency of 73.152 MHz.

3.4. Primary Beam Measurements

In order to generate wide-field images of the sky, the response of the antenna to the sky must be known. Drift-scanning interferometers like the OVRO-LWA can empirically measure their primary beam under a mild set of symmetry assumptions (Pober et al. 2012). In this work we assume that the primary beam is invariant under north-south and east-west flips, and additionally that the x - and y -dipoles have the same response to the sky after rotating one by 90° . These symmetries are apparent in the antenna design, but real-world defects and coupling with nearby antennas will contribute towards breaking these symmetries at some level. However some amount of symmetry must be assumed in order to break the degeneracy between source flux and beam amplitude when the flux of a source is unknown.

We measure the flux of several bright sources (Cyg A, Cas A, Tau A, Vir A, Her A, Hya A, Per B, and 3C 353) as they pass through the sky and then fit a beam model composed of Zernike polynomials to those flux measurements. We select the basis functions to have the desired symmetry ($Z_0^0, Z_2^0, Z_4^0, Z_4^4, Z_6^0, Z_6^4, Z_8^0, Z_8^4, Z_8^8$) and the beam amplitude at zenith is constrained to be unity. See Figure 3 for an illustration of a fitted beam model at 36.528 MHz. This process is repeated for each frequency channel.

3.5. Source Removal

3.5.1. Cygnus A and Cassiopeia A

Without removing bright sources from the data, sidelobes from bright sources will dominate the variance in the image. At 74 MHz Cyg A is a 15,000 Jy source (Baars et al. 1977). A conservative estimate for the con-

fusion limit at 74 MHz with a 10 arcminute beam is 500 mJy (Lane et al. 2012). Therefore we require that Cyg A's sidelobes be at least -45 dB down from its peak flux to prevent Cyg A's sidelobes from dominating the variance in the image.

At low frequencies, propagation effects through the ionosphere must be accounted for in order to achieve high dynamic range images. This necessitates the use of direction-dependent calibration and peeling (Mitchell et al. 2008; Smirnov & Tasse 2015). In the dataset used in this paper, scintillation and diffraction events on the timescale of a single integration (13 seconds) are observed. Therefore the direction dependent calibration changes on these timescales and the we must solve for one set of complex gains per source per integration.

The largest angular scale of Cas A is ~ 8 arcminutes, and the largest angular scale of Cyg A is ~ 2 arcminutes. With a ~ 10 arcminute resolution, the OVRO-LWA marginally resolves both sources. A resolved source model is needed for both sources. We fit a self-consistent resolved source model to each source. This is performed by minimizing the variance within an aperture located on each source after peeling. By phasing up a large number of integrations before imaging (at least 1 hour) it is possible to smear out the contribution of the rest of the sky. We then use NLOpt's Sbplx routine (Johnson 2008; Rowan 1990) to vary the parameters in a source model until the variance within the aperture is minimized.

Armed with resolved source models for both Cyg A and Cas A, these two sources can be peeled from the dataset to the required dynamic range.

TODO: slice through Cyg A and Cas A to illustrate the removal process

TODO: Give a plot with the updated source models

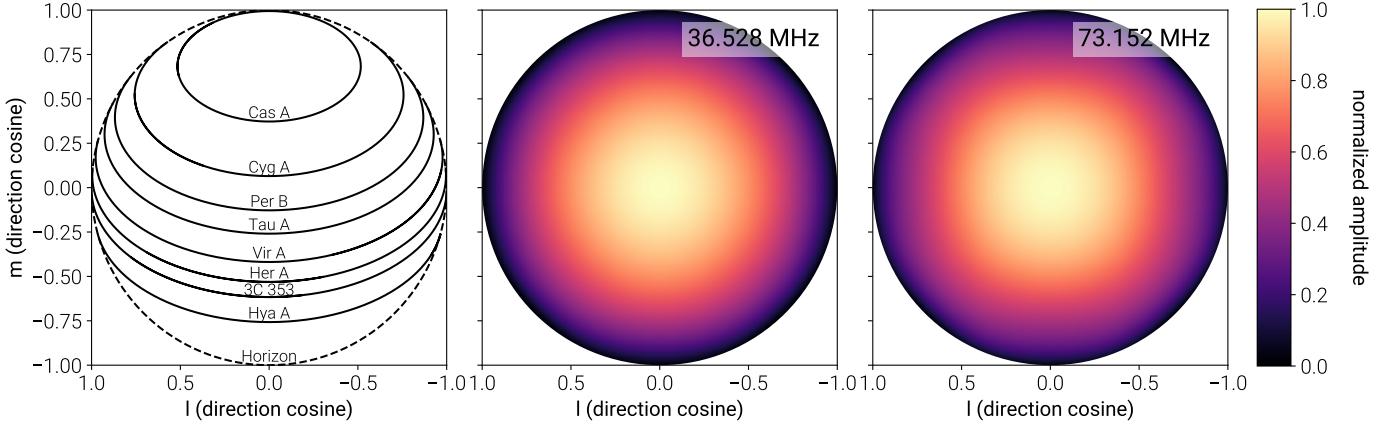


Figure 3. (left panel) The tracks traced through the sky by the 8 brightest point sources visible to the OVRO-LWA. (middle panel) The amplitude of the OVRO-LWA beam at 36.528 MHz as a result of the beam model fit using Zernike polynomials and the symmetry assumptions outlined in the text. (right panel) The amplitude of the OVRO-LWA beam at 73.152 MHz as a result of the beam model fit using Zernike polynomials and the symmetry assumptions outlined in the text.

3.5.2. Other Bright Sources

Other bright sources including Vir A, Tau A, Her A, Hya A, Per B, and 3C 353 are also removed from the visibilities prior to imaging. Because these sources are much fainter than Cyg A and Cas A, we do not need resolved source models to be able to remove these sources from the visibilities without residual sidelobes contaminating the image.

However, the ionosphere will cause these sources to scintillate and refract. So the position and flux of each source is measured separately in each channel and integration. The sources are then subtracted from the visibilities using the updated position and flux of the source. The brightest of these sources (Vir A and Tau A) will be peeled using a direction dependent calibration when they are at high elevations.

3.5.3. The Sun

The sun can be trivially removed from any map of the sky by constructing the map using only data taken at night. A map of the entire sky can be obtained by using observations spaced 6 months apart. However the dataset used in this paper consists of 28 consecutive hours. Therefore we attempt to suppress the contribution of the sun to the maps with the goal of suppressing its sidelobes. The sun is well-resolved by the OVRO-LWA and hence a detailed source model is needed. In fact the optical depth $\tau = 1$ surface of the sun changes with frequency and as a consequence a new model is needed for each of the 8 channel maps produced in this paper. While we could fit a limited number of Gaussian components to Cyg A and Cas A, this is insufficient for the Sun. Additionally while most astronomical sources at these frequencies have negative spectral indices, the Sun has a positive spectral index. Therefore more care

will need to be taken in subtracting the Sun at higher frequencies than at lower frequencies.

The strategy used for removing the Sun below 55 MHz involves fitting a shapelet (Refregier 2003) model to the Sun and subtracting without the use of direction dependent gains. The shapelet fitting is performed in the visibility space. Above 55 MHz a model is fit to the Sun by minimizing the residuals after peeling (in the same way that models are obtained for Cyg A and Cas A). The Sun is then peeled from each integration using direction dependent gains.

3.6. Flux Scale

The flux scale of the data was tied to the Baars et al. (1977) spectrum of Cyg A during gain calibration. However gain calibration is also a function of the beam model and the spectrum used for Cas A. Recent work by Scaife & Heald (2012) using archival data from the literature and Perley & Butler (2017) using the VLA has expanded the number of low-frequency radio sources with calibrated flux measurements from one (just Cyg A) to eleven in total. While the Scaife & Heald (2012) flux scale is valid between 30 MHz and 300 MHz, the Perley & Butler (2017) flux scale is somewhat more limited because the lowest frequency observations come from the VLA 4-band system. As a consequence the Perley & Butler (2017) flux scale is not valid below 50 MHz.

Figure 4 shows a comparison between flux measurements made using the all-sky maps from this work, and spectra from the aforementioned flux scales. Generally the OVRO-LWA flux measurements agree to better than 10% with the Scaife & Heald (2012) spectra. Below 50 MHz there can be substantial departures with respect to the Perley & Butler (2017) spectra (for eg. 3C 286, 3C 295, and 3C 380), but it is usually the case that we

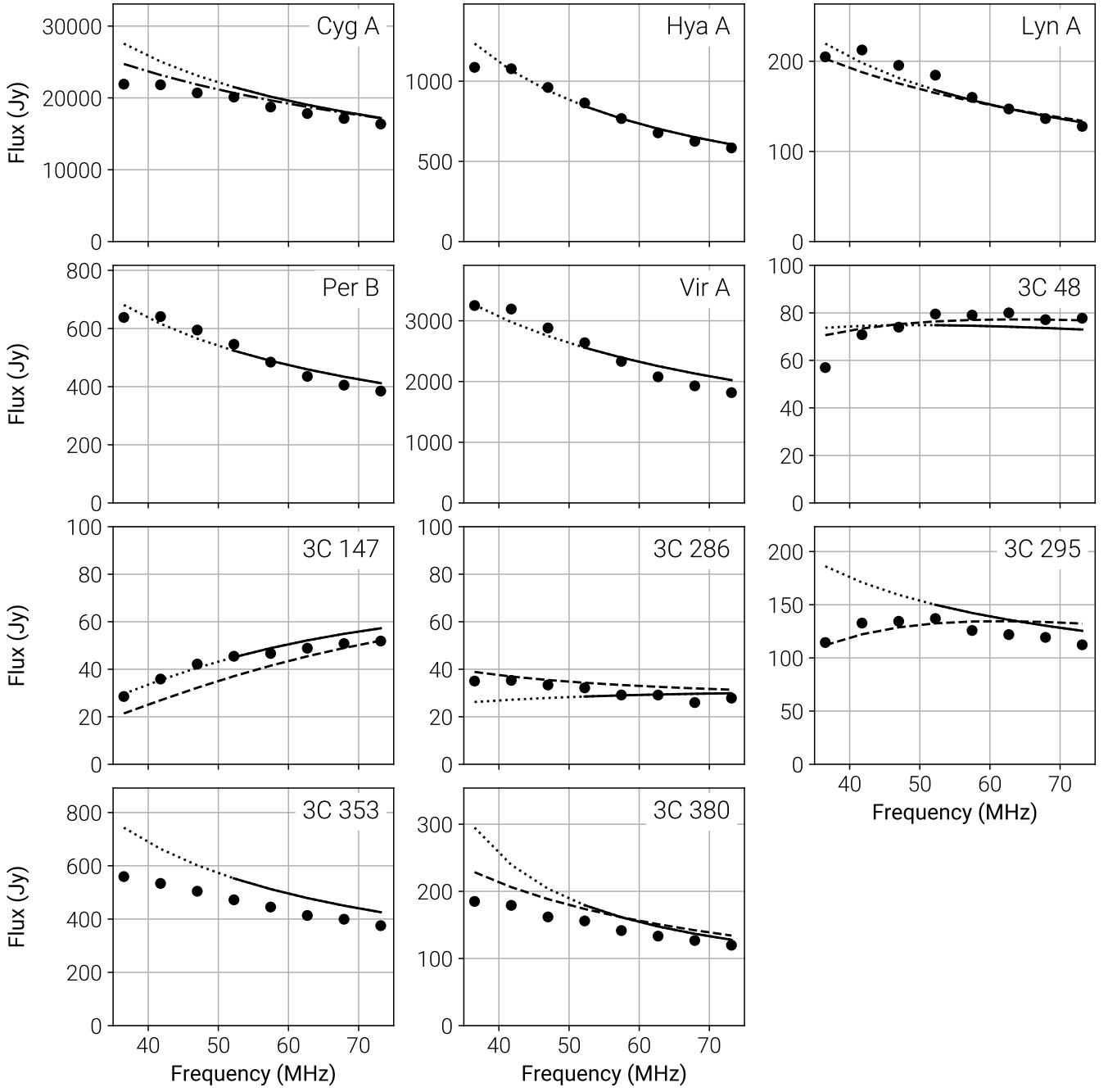


Figure 4. This figure shows the measured fluxes (black points) of 11 sources plotted against the published spectra from Perley & Butler (2017) (solid line above 50 MHz, dotted line below 50 MHz), Scaife & Heald (2012) (dashed line), and Baars et al. (1977) (dot-dash line).

have much better agreement with the Scaife & Heald (2012) spectra. This indicates that the Perley & Butler (2017) spectra can diverge from the truth rapidly below 50 MHz.

4. RESULTS

Eight sky maps are presented in Figure 5. Their properties are briefly summarized in Table 1. In this section

we will describe the new imaging technique used to generate these maps.

TODO: text

5. ERROR ANALYSIS

5.1. Jackknife Resampling

TODO: text

#	Frequency	Bandwidth	FWHM	Thermal Noise		Spherical Harmonics		Singular Values
	MHz	MHz	arcmin	K	Jy	$l = 0$	$m = 0$	fraction $> \sqrt{\varepsilon}$
1	36.528	0.024	16.2	372.8		no	yes	
2	41.760	0.024	14.7	321.2		no	yes	
3	46.992	0.024	14.2	247.0		no	no	
4	52.224	0.024	13.6	205.7		no	no	
5	57.456	0.024	13.5	167.7		no	no	
6	62.688	0.024	13.5	137.6		no	no	
7	67.920	0.024	13.5	114.9		no	no	
8	73.152	0.024	13.7	93.4		no	no	

Table 1. Summary of the generated all-sky maps

5.2. Terrestrial Interference and Pickup

When writing down Equation 2, it is implicitly assumed that the correlated voltage fluctuations measured between pairs of antennas are exclusively generated by astronomical sources of radio emission. In practice this implicit assumption can be violated. For instance a low-frequency interferometer located in the vicinity of an arcing power line will see an additional contribution from the radio-frequency interference (RFI) generated by the arcing process. Similarly common-mode pickup along the analog signal path of the interferometer may generate an additional spurious contribution to the measured visibilities. While the amplitude and phase of these contaminating signals may fluctuate with time, they do not sweep across the sky at the sidereal rate characteristic of astronomical sources.

The Owens Valley is an important source of water and power for the city of Los Angeles. Unfortunately this means that high voltage power lines run along the valley to the west of the OVRO-LWA. Some of these power line poles have faulty insulators that arc and produce pulsed, broadband RFI. Because these poles exist in the near-field of the array, we have been able to localize some of them by using the curvature of the incoming wavefront to infer a distance. Efforts are currently underway to work with the utility pole owners to have these insulators replaced.

In the meantime it is possible to suppress their contamination in the dataset. The contribution of these RFI sources to the visibilities can be plainly seen by averaging > 24 hours of data with the phase center set to zenith. In this way, true sky components are smeared along tracks of constant declination while terrestrial sources (ie. the arcing power lines or any common-mode pickup) are not smeared. Obtaining a model for the RFI is complicated by the fact that the contaminating sources are at extremely low elevations where

the antenna response is essentially unknown (and inhomogeneous due to antenna shadowing effects). Therefore it is not enough to know the physical location of the faulty insulator generating the RFI. In addition you must also know the response of each antenna (amplitude and phase) in the appropriate direction. This motivates the use of peeling (Mitchell et al. 2008; Smirnov & Tasse 2015), which allows the antenna response to be a free parameter. Therefore model visibilities for the RFI can be obtained by peeling the sources after smearing the visibilities over > 24 hours. See Figure 7 for an illustration of this process.

However while attempting to peel RFI sources from the averaged visibilities, it was discovered that frequently peeling would prefer to remove components from the visibilities that are not obviously associated with any source on the horizon or elsewhere in the sky (see panel (d) in Figure 7). In many cases the amplitude of these unassociated components exhibit the same sawtooth oscillations indicative of gain fluctuations in the analog electronics even after these gain fluctuations have been calibrated. This seems to imply that these unassociated components originate as common-mode pickup in the analog signal chain. That is, if the pickup occurs somewhere in the middle of the analog signal chain, it will not see the same gain as the astronomical signal. Therefore correcting the temperature dependence of the gains for the astronomical signal does not correct the temperature dependence of the pick-up and hence it will have a sawtooth pattern with respect to time.

The first step in Equation 9 is to compute $\mathbf{B}^* \mathbf{v}$. In this step we compute the projection of the measurement \mathbf{v} onto the space spanned by the columns of \mathbf{B} . Each column of \mathbf{B} describes the interferometer's response to a corresponding spherical harmonic coefficient of the sky brightness distribution. Therefore the act of computing $\mathbf{B}^* \mathbf{v}$ is to project the measured m -modes onto the space

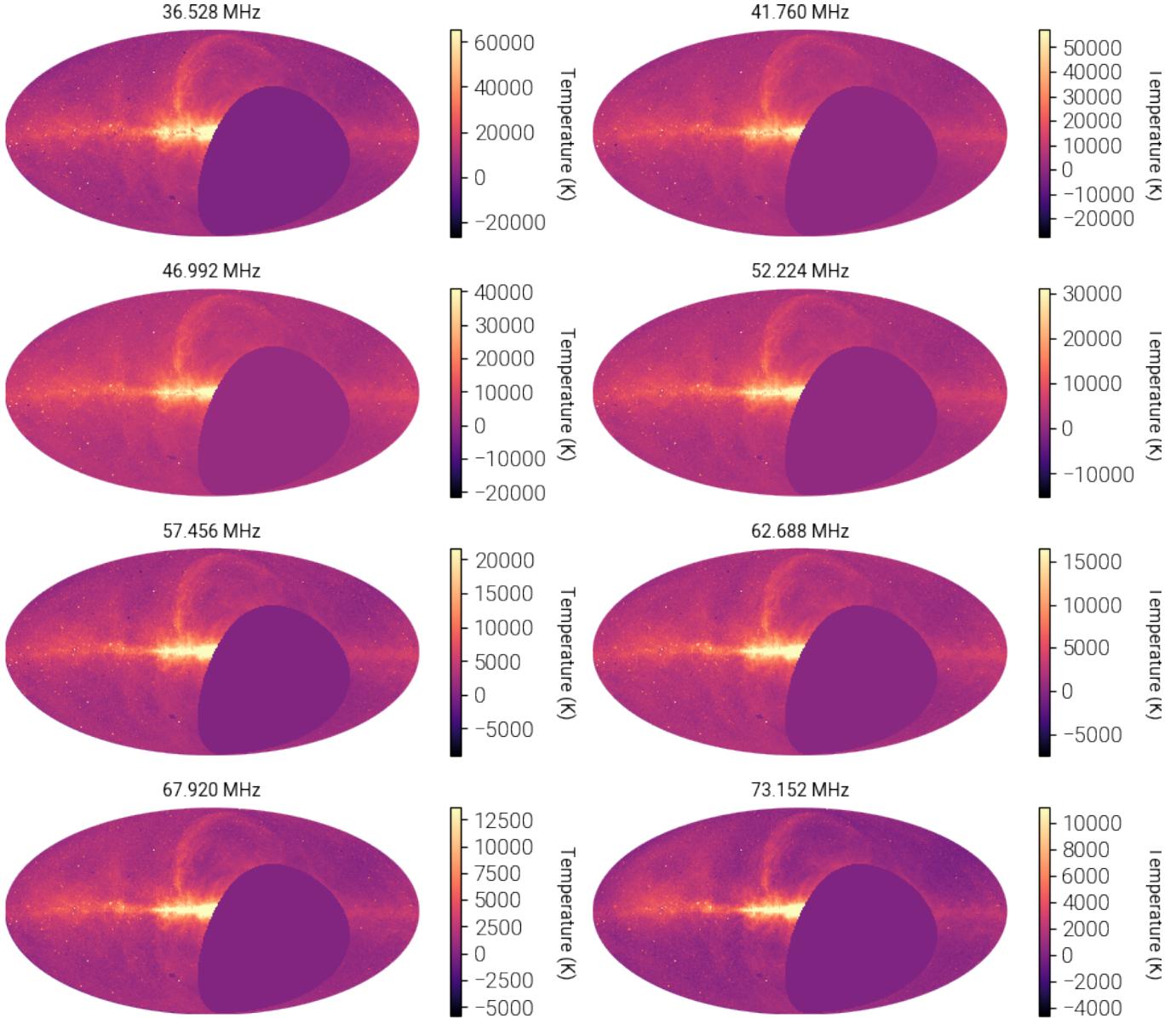


Figure 5. Mollweide-projected maps of the VHF sky north of -30° generated using the OVRO-LWA and m -mode analysis imaging. The properties of each map are summarized in Table 1. The color scale is logarithmic and has units of Kelvin. As described in the text, 8 bright sources have been subtracted. The small blank region near the bottom of each map corresponds to the region of sky within 2 degrees of the Sun at the time of the observations.

of m -modes which could be generated by astronomical sources. The degree to which a source of terrestrial interferer will contaminate a map generated using m -mode analysis imaging is determined by its amplitude after projection.

For instance, a bright interfering source might contribute $\mathbf{v}_{\text{terrestrial}}$ to the measured m -modes. However, if $\mathbf{v}_{\text{terrestrial}}$ is actually perpendicular to all of the columns of \mathbf{B} , there will be no contamination in the map because $\mathbf{B}^* \mathbf{v}_{\text{terrestrial}} = \mathbf{0}$. In practice this is unlikely. In general the contamination is proportional to the overall amplitude of the interference ($\|\mathbf{v}_{\text{terrestrial}}\|$) and the de-

gree to which the interference mimics an astronomical signal ($\|\mathbf{B}^* \mathbf{v}_{\text{terrestrial}}\| / \|\mathbf{v}_{\text{terrestrial}}\|$).

TODO: compute $\mathbf{B}^* \mathbf{v}$ for panels (c) and (d) to show that the pick-up is pretty bad. my expectation is that it is actually worse than the RFI, but I don't actually know for sure

These terrestrial sources do not rotate with the sky and hence their contamination tends to be restricted to modes with small m . In this dataset the contamination is largely restricted to $m \lesssim 3$. As a result if the contamination is not suppressed, it will manifest itself as

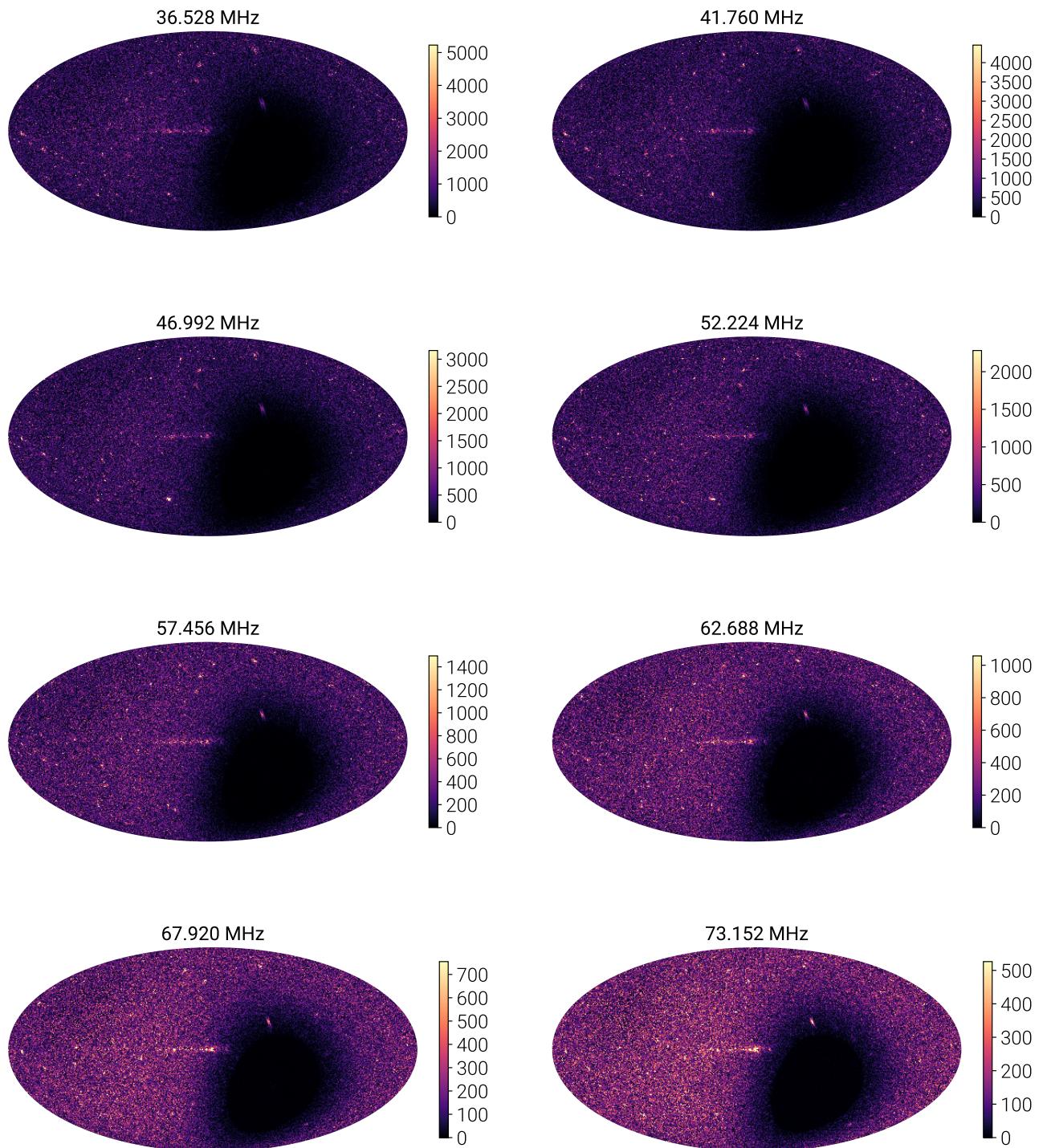


Figure 6. The jackknife estimated standard deviation corresponding to the maps presented in Figure 5. The color scale is logarithmic and has units of Kelvin.

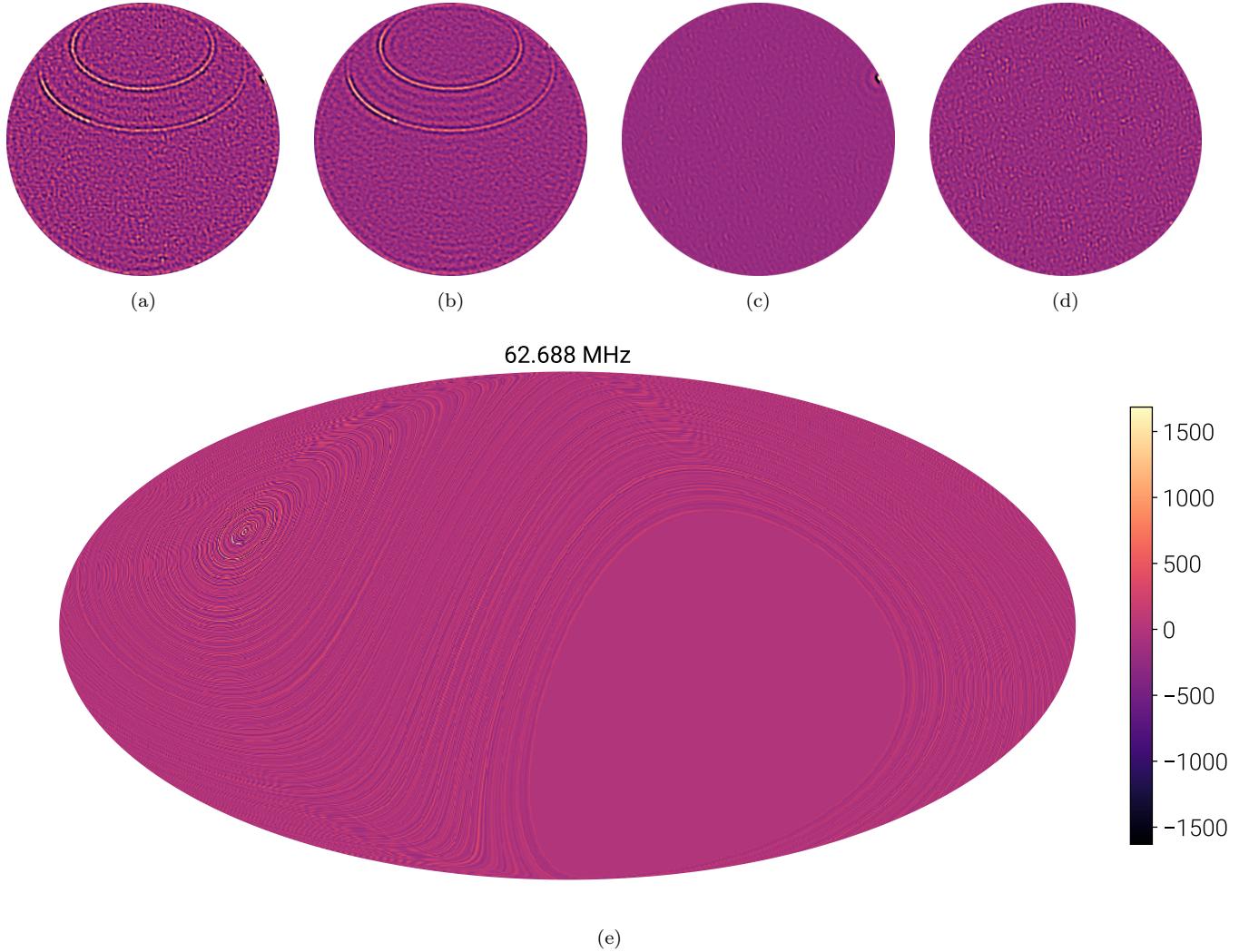


Figure 7. This figure illustrates the process of fitting for terrestrial sources of correlated noise. Each image is of the entire visible hemisphere above the OVRO-LWA but the data has been averaged over the entire 28 hour observing period. Because of this Cas A and Cyg A are smeared along tracks of constant declination. These images are generated using WSCLEAN (Offringa et al. 2014), uniform weighting, and baselines shorter than 15 wavelengths are flagged. (a) This image shows the initial data before any sources have been removed. (b) This image shows the final state after 3 terrestrial sources of correlated noise have been removed. (c) This image illustrates the contribution of an RFI source towards the north-west that was removed by peeling. (d) This removed component is not associated with a dot on the horizon. Instead it is likely associated with common-mode pickup in the analog signal chain. (e) The resulting contamination in the full-sky maps from the horizon RFI and common-mode pickup. Note that because these contaminating components are not moving sidereally, they tend to generate stripes along lines of constant declination. The color scale is in units of Kelvin.

rings along stripes of constant declination. This effect is plainly visible in Figure 7.

However because these rings are so distinctive in the final maps, it is possible to construct a Wiener filter that removes them at the cost of losing a small amount of information about astronomical sources.

TODO: describe how the Wiener filter works

5.3. Beam Errors

A good model of the antenna beam is essential for widefield imaging. Because m -mode analysis imaging operates on a full sidereal day of data, images are constructed after watching each point in the sky move through large slices through the beam (excepting the celestial poles). The beam model therefore serves two purposes:

1. setting the flux scale as a function of declination
2. reconciling observations from two separate sidereal times

In the first case, all sources at a given declination take the same path through the antenna primary beam. If the antenna response is overestimated along this track then all sources at this declination will have their flux underestimated. Similarly if the antenna response is underestimated then all the sources will have their flux overestimated.

TODO: discuss the possibility of declination dependent flux-scale errors in these maps

The second case is more subtle. Sources are observed at a wide range of locations in the primary beam of the antenna. The imaging process must reconcile all of these observations together. The beam model essentially provides the instructions on how to do this. For example if at a time t_1 the antenna gain towards a source is g and at a later time t_2 the antenna gain towards that same source (which has now moved) is $g/2$, then in order to correctly estimate the flux of the source the observations from time t_1 need to be multiplied by $1/g$ but the observations from time t_2 need to be multiplied by $2/g$. A mistake in the beam model here will lead to a mistake in the estimated flux. However in general the amplitude and phase of the antenna response needs to be known and so beam model errors can lead to observations being combined with incorrect phase as well. This will lead to a degraded PSF in the final map.

TODO: quick simulation of this?

5.4. The Ionosphere

One of the key assumptions made by m -mode analysis is that the sky is completely static. We assume

that the only time-dependent behavior is the rotation of the Earth, which slowly rotates the sky through the fringe patterns of the interferometer. At low frequencies the ionosphere violates this assumption. In particular, ionospheric scintillation will cause even static sources to exhibit significant variability.

The correlation observed on a given baseline for a single point source is

$$V_\nu(t_{\text{sidereal}}) = I_\nu B_\nu(t_{\text{sidereal}}), \quad (16)$$

where I_ν is the flux of the source at the frequency ν , and B_ν is the baseline transfer function. The transfer function is a function of the direction to the source, which is in turn a function of the sidereal time t_{sidereal} . If the source is varying, from intrinsic variability or due to scintillation, than the source flux is also a function of the time coordinate t such that

$$V_\nu(t_{\text{sidereal}}) = I_\nu(t) B_\nu(t_{\text{sidereal}}), \quad (17)$$

where $t_{\text{sidereal}} = (t \bmod 23.9345 \text{ hours})$.

Now assume we have observed with our interferometer for a single sidereal day. In order to compute the m -modes we must Fourier transform with respect to sidereal time. In a real measurement this is a discrete Fourier transform of the observed correlation with respect to time (where the sum over time is restricted to a sidereal day).

$$V_{\nu,m} = \sum_t V_\nu(t) e^{-imt} \quad (18)$$

Define $V_{\nu,m}^{\text{static}}$ to be the observed m -modes if the source was actually static ($I_\nu(t) \equiv I_{\nu,0}$). Then as a consequence of the Fourier convolution theorem

$$V_{\nu,m} \propto \sum_{m'} V_{m'}^{\text{static}} I_{\nu,m-m'}. \quad (19)$$

This will tend to scatter power between m -modes (Shaw 2016).

TODO: Simulate images of point sources with this
TODO: I think the conclusion is sort of exactly what you would expect: refraction broadens the PSF while scintillation effects the flux scale, but honestly not by much because we have such large averages that unless the scintillation is Cauchy distributed it is not that bad..

6. COMPARISONS WITH OTHER SKY MAPS

6.1. Haslam 408 MHz Map

The Haslam 408 MHz map (Haslam et al. 1981, 1982) was reprocessed by Remazeilles et al. (2015) to remove artifacts associated with $1/f$ noise and bright sources.

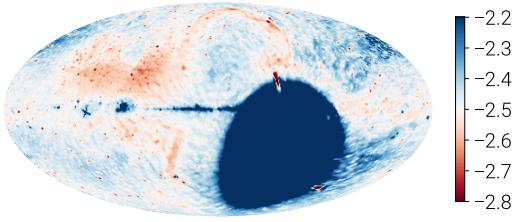


Figure 8. The spectral index between the reprocessed Haslam 408 MHz map and the OVRO-LWA maps (degraded to 56 arcmin resolution). The larger blue patch around the south celestial pole corresponds to where the OVRO-LWA map has a blank region.

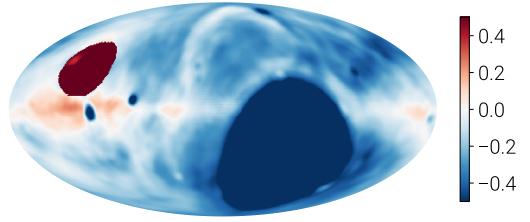


Figure 9. This Mollweide projection map compares the fractional difference between the Guzmán 45 MHz map, and the OVRO-LWA map at 46.992 MHz (degraded to 5° resolution). A positive value indicates regions where the OVRO-LWA map has more emission than the Guzmán map, and a negative value indicates regions where the Guzmán map has more emission than the OVRO-LWA map. The red patch around the north celestial pole corresponds to where the Guzmán map has a blank region. The larger blue patch around the south celestial pole corresponds to where the OVRO-LWA map has a blank region. Note also that the OVRO-LWA map has several bright point sources subtracted that are not subtracted from the Guzmán map.

In order to compare the OVRO-LWA maps with the lower resolution Haslam map, the OVRO-LWA maps were degraded to 56 arcmin resolution. A spectral index map computed between the OVRO-LWA maps and the Haslam map is shown in Figure 8.

6.2. Guzmán 45 MHz Map

A direct comparison between the OVRO-LWA at 46.992 MHz and the Guzmán 45 MHz map (Guzmán et al. 2011) can be seen in Figure 9. In order to make this comparison the OVRO-LWA map was degraded to a 5° resolution by convolving with a Gaussian kernel. This figure shows that the majority of the galactic synchrotron emission is consistent between the two maps to better than 5% however there are patches (particularly near the north celestial pole) where there is a discrepancy on the order of 20%. Off of the galactic plane, the OVRO-LWA map underestimates the flux compared to the Guzmán map by a factor of 20%. This can be attributed to the absence of zero-spacing data.

7. CONCLUSION

TODO: text

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