

# Convergence for Individualizing Treatment Using Statistical approaches (CITRUS)

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TI PhD Seminar



- 1 Introduction
- 2 Data Generation: Considered Scenarios
- 3 Estimation: Considered Methods

*CITRUS =  
Convergence for Individualizing Treatment Using  
Statistical approaches*

- Project of the Econometric Institute and Erasmus Medical Center;
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**Evidence-based medicine:** the “*conscientious, explicit and judicious use of current best evidence in making decisions about the care of individual patients*” (Sackett et al., 1996).

- Identify *heterogeneous treatment effects* (HTE)!
- Methods from modern causal inference?
- CITRUS: Which methods are most eligible for medical data?
- Simulate common characteristics of medical data.

# Introduction

In a **perfect** world, we'd have...

- *Many* observations:  $n \rightarrow \infty$ ;
- Perfect information on relevant covariates (unconfoundedness);
- I.I.D. data from randomized experiment;
- Continuous data.

BUT: The world is **not** perfect (especially in medicine...)





**Frank Harrell**

@f2harrell



Note to [#Statistics](#) paper authors: If you have the word "asymptotic" in your title or abstract, the probability that I'll read the paper is reduced by a factor of 4. I'm only interested in real-world performance of analytical methods. [@vandy\\_biostat](#)

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# Introduction

In medical data, we typically have...

- Very finite sample sizes ( $n \geq 500$  is rare);
- Noisy to incomplete representation of relevant covariates;
- Non-identically distributed samples;
- Improper randomization (sometimes...);
- Non-continuous data (e.g. categorical).

**CITRUS research question:**

- To what extent does this affect the performance of each HTE estimation method?



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Let there be  $n$  independent observations  $(\mathbf{X}_i, Y_i, W_i)$ .

- $\mathbf{X}_i$  is  $p$ -dimensional covariate vector;
- $Y_i$  is outcome variable. Binary mortality indicator here:  $Y_i = 1$  if  $i$  dies.
- $W_i$  is binary treatment assignment variable:  $W_i = 1$  if  $i$  is in treatment group.

The DGP for **potential** outcomes can w.l.o.g. be viewed as

$$Y_i(W_i) = g_i \left( \theta(\mathbf{X}_i) W_i + \nu(\mathbf{X}_i) + \varepsilon_i \right).$$

- $g_i : \mathbb{R} \rightarrow \{0, 1\}$  maps to binary outcome space;
- $\theta(\mathbf{X}_i)$  is the HTE function: causal effect of  $W_i$  on  $Y_i$ ;
- $\nu(\mathbf{X}_i)$  is the nuisance function: raw effect of  $\mathbf{X}_i$  on  $Y_i$ ;
- $\varepsilon_i$  is zero-mean noise term.

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## Bias In Medicine: Last Week Tonight with John Oliver (HBO)

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# References

- Sackett, D. L., Rosenberg, W. M., Gray, J. M., Haynes, R. B., and Richardson, W. S. (1996). Evidence-Based Medicine: What it is and What it isn't. *The British Medical Journal*, 312(7023):71–72.

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