



NAVAL
POSTGRADUATE
SCHOOL

OS4118

Statistical and Machine Learning

Spatial Data and Maps

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- My distinction: “spatial statistics” vs. “spatial analysis”
- Spatial **statistics** studies the properties of spatial processes; spatial **analysis** studies real data
 - I claim that real data rarely comes from nicely-defined spatial processes



- If there is a spatial component to a process, the values of a process at two points will be more correlated if those two points are close together than if they're far away
- Positive correlation implies attraction, negative correlation implies repulsion



- Can be discrete (a “point process”)...
 - E.g. earthquakes, IEDs (“marked PP”)
- ...or continuous (a “random field”)
 - E.g. ozone, strength of cell-phone signal
- Without spatial dependence, these can be “completely spatially random” (**CSR**)
 - E.g. two-d homog. Poisson proc. (HPP)
 - If not homogeneous, is it correlation, varying intensity, both, or something else?

- We can evaluate whether a process is CSR by measuring F - and G -functions
 - **G -function**: CDF of distance from one event to its nearest neighbor
 - **F -function**: CDF of distance from arbitrary point to nearest event (“empty space func.”)
 - **J -function**: $(1 - G(r))/(1 - F(r))$ is 1 $\forall r$ for HPP
 - Methods for estimating these
 - Compare to values simulated under CSR



- Estimate intensity by, e.g. kernel smoothing
- Intensity is a “first-order process”
- “Second order” is correlation
 - Do the points cluster? Is there competition, pushing points away from one another?
 - ***K*-function** computes number of points within s of an arbitrary event
- Old-school approaches like the K are being augmented with newer approaches


```
library (sp); library (spatstat) # Spatial statistics libraries
##
class (japanesepines) # "ppp", i.e. "point pattern in the plane"
#
# A ppp has a matrix-like thing of coordinates and also an
# observation window (of class owin). In general the as() construct
# lets you convert one type to another supported type. E.g.:
#
pppfake  <- as.ppp (spatial.poisson(), owin (c(0 ,20), c(0, 20)))
#
# Example of envelope() command for F-function
#
envelope (pppfake, fun = Fest, nrank=3)
```

- Instead of incident-type data we have continuous measurements at locations
- **Variogram** measures correlation as a function of distance
 - $\gamma(h) = (1/2) \mathbf{E}\{[Z(s) - Z(s + h)]^2\} \dots$
 - ...Under stationarity assumption
 - Under “isotropy,” direction doesn’t matter; replace h with its length



- Geographic data carries location information
 - Longitude, latitude, maybe altitude and time
 - Alternatives: Military Grid Reference System, Universal Transverse Mercator
- The earth is round-ish, the map is flat
 - Data must be projected onto the plane
 - There are lots of projections, each producing different sorts of distortion
 - Choose one that meets our needs



Maps in R 1: Simple Maps

- The `maps` library makes it straightforward to make simple maps
- Particularly strong on US lower 48 (by county)
- Projections are preserved by default from one call to the next
- Countries appear as sets of named polygons (e.g. France, UK)
- Higher-res data in `library (mapdata)`, `rnaturalearth`, probably others



- Libraries: `map`, `mapdata`, `mapproj`
- County map of California with Monterey highlighted
- State map of California and Arizona with indications of tunnels
- Examples of projections
 - Path from (0, 90) to (0, 0) to (90, 0) to (90, 60) to (60, 0)
- These are ordinary R graphics, though you will have to project points, lines, text, etc.



- A GIS is software to hold, display and analyze geographically-referenced data
- GIS is at the intersection of cartography, statistics, and database management
- Our goal: display data in space and time
- Bigger goal: perform analyses of spatial processes
 - Visualization; inference; optimization...

- Much of the market is held by Esri Corp.'s ArcGIS product, so much of the vocabulary comes from that product
- Many other products exist in different niches (e.g. mapping, waterways, ...)
 - Open-source GRASS; also, tools in R (!)
- We have **ArcGIS**, **Google Earth** installed
 - ArcGIS: very powerful, flexible, extensible, but very complicated and hard to learn
 - Google Earth: easy, pretty, links to Google Maps, essentially no analysis



Maps in R 2: Mapping in GIS

- GIS like Google Earth let us combine “layers” of information (photos, roads, geography, waterways, rail, etc.) in a straightforward way
- In GE some of these come automatically
- Google Earth supports only one projection; if our data comes from different sources we may need to re-project some layers, maybe in ArcGIS, to get them to match up
- Main data formats: KML, “Shape files”



- Google Earth is almost entirely for display
- Other GIS perform analyses:
 - “Which polygon contains these points?”
 - “What roads are close to these points?”
 - “Which placement of sub-stations maximizes the number of people within 2,000 m?”
 - “Can this location be seen from that tower?”
- Google Earth is very cool, but it is not a tool for analysis
- Besides ArcGIS, the open-source GRASS is widely used



Format 1: Remember XML?

- XML is a standard mechanism for storing and transporting (but not displaying) data
- It looks like HTML
 - But HTML's focus is on the display
- XML is text-based, so it's not particularly well-suited for floating-point data
- XML isn't quite a language; it's a set of tools for defining a new language

- **KML** (“Keyhole markup language”) is the implementation of XML used by Google Earth
 - KMZ: a zipped version that can be read directly
- Google Earth/Maps import and export KML
- KML includes support for
 - Time stamps and animation
 - Altitude and tours
 - Custom data and more



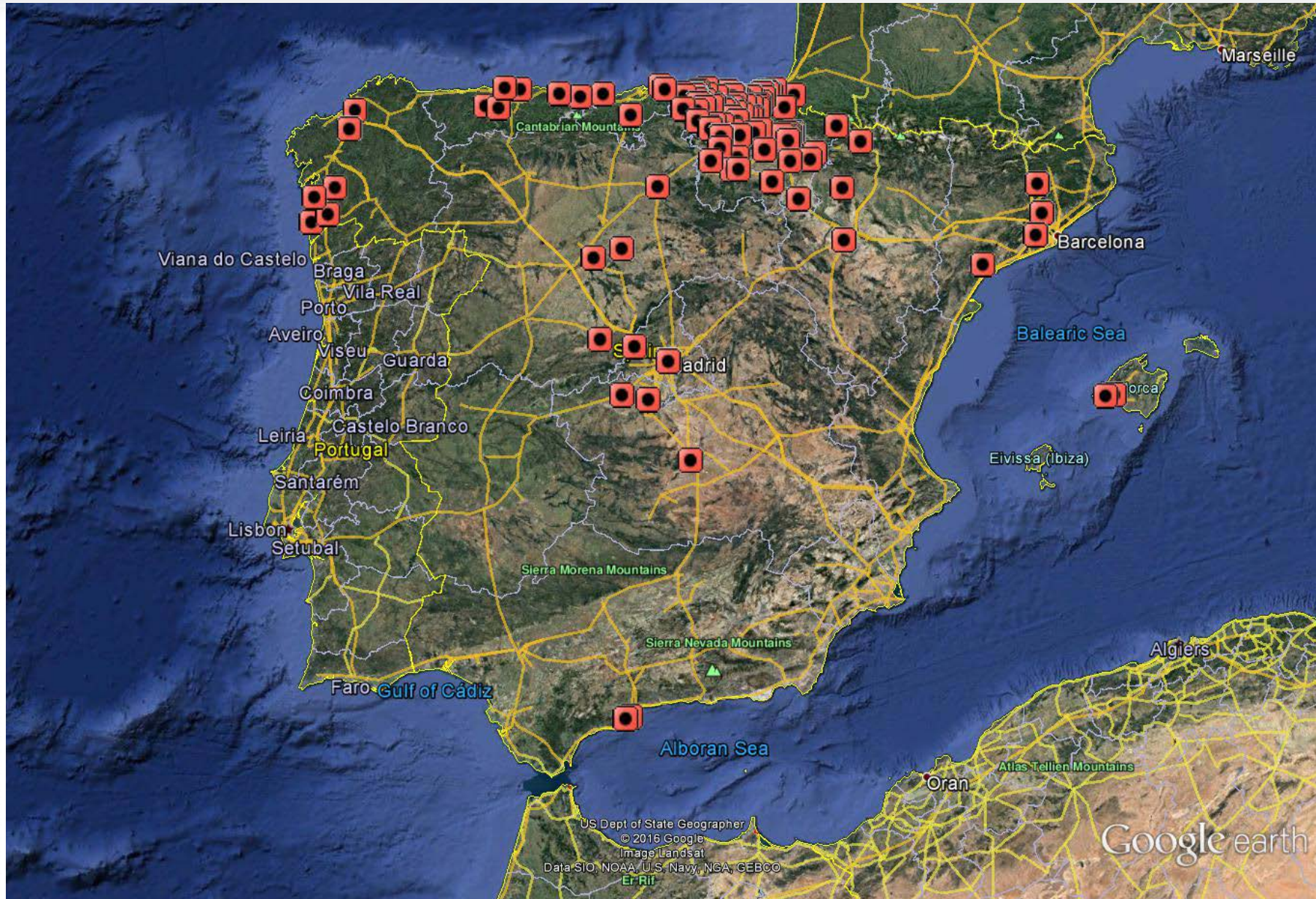
```
<?xml version="1.0" encoding="UTF-8"?>
<kml xmlns="http://www.opengis.net/kml/2.2">
<Placemark>
  <TimeStamp>
    <when>2016-09-04T11:00:00-08:00</when>
  </TimeStamp>
<description>Glasgow Hall, NPS</description>
  <Point>
    <coordinates>
      -121.877573,36.59858,0
    </coordinates>
  </Point>
</Placemark>
</kml>
```



- `Sp`, `rgdal`, `plotKML`, and some other R packages have some KML facility
- My function will work for now: let's convert the Global Terrorism Database incidents in Spain into KML
- Visualize in Google Earth



Terrorist Incidents in Spain





- Google Earth's servers maintain layers of things like roads and photos, so we get them automatically
- Available in browser or as standalone
- There are servers in the secret labs, too
- Cool examples: Three-d buildings, tours, flight simulator, some underwater mapping...



- Bing Maps / Open Street Map provide nice static maps, **geocoding**
 - Without giving out your credit card number, as Google now requires
 - For “real” products we will need to pay somebody...
 - ...By some as-yet undetermined mechanism



Format 2: Shape Files

- This mostly open format started with ArcGIS, now widely used
- A “shapefile” is actually a set of three or more disk files
- Lots available on the web – projection information necessary
- As with Google Earth, a map will be made up of “layers” of different sorts, each with its own display parameters (opacity, point size, line colors, etc.)

1. Feature Classes

- Points, lines or polygons with georeferences

2. Attributes

These two are “vector” data

- Data that describe features: road class, county names, hospital/school/police dept....

3. Image data

- “Raster data,” data in grid/pixel form
- Can also include non-pictorial continuous data like elevation or other attributes



- Vector shapefile support from:
 - Libraries `sp`, `shapefiles`, `rgdal`
 - “Geospatial data abstraction library”
- Library `raster` for imagery, gridded data
- `rgeos` library for computations like areas, boundaries, centroids, convex hulls...
 - “Geometry engine, open source”
- Three important operations:
 - Reprojection: `spTransform()`
 - Intersection: `over()`
 - Build a buffer: `buffer()`



Spatial Analysis Examples

- “Which polygon contains these points?”
- “What roads are close to these points?”
- “Which placement of sub-stations maximizes ‘# of people within 2,000 m’ ?”
- “Can this location be seen from that tower?”
- Ex. 1: “Which roads in Monterey County are > 30 miles from a health care facility?”
- Ex. 2: “What proportion of Malians live within 50 km of a railroad?”



Monterey County Example

- Read (CA health) and (county) shape files
- **Reproject** health to match county
- **Intersect** health with Monterey County
 - Producing health care facilities in county
- **Reproject** health to UTM projection
- **Buffer** facilities to 48,300 m
- Read Monterey roads shapefile
- **Intersect** roads with buffer – find roads that do **not** overlap

Pretty Pictures

