



NAVAL
POSTGRADUATE
SCHOOL

OS4118

Statistical and Machine Learning

Association Rules

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- Another unsupervised technique
- Given categorical data, construct **rules**
- A rule usually has the form

If variable A has value a **and** variable B has value b, **then** variable D will have value d

- Here we have two **antecedents** (conditions) and one **consequent**
- Usually rules have antecedents joined by “and” and exactly one consequent



- Rules generally concern categorical variables (sets)
- Continuous variables must be discretized
- Binary variables should often be treated asymmetrically
- No response variable: any variable can be “predictor” or “response”
- Example: market basket
 - E.g. “If ‘hot dog buns’ are in the basket, then ‘hot dogs’ are in the basket”



Market Basket Examples

- Items are items, baskets are baskets, look for shoppers' similarities
- Items are words, baskets are documents, look for linked concepts
- Items are sentences, baskets are documents, look for plagiarism
- Items are genes, baskets are people...



- Humans have about 30,000 genes and there are six-seven billion of us
- Wal-Mart sells about 100,000 items and can store millions of baskets
- The Web has 100,000,000 words and billions of pages
- Data off-line, need few passes



Support and Confidence

- Object: find rules with high **support** (frequency, coverage) and high **confidence** (accuracy)
- **Support**: proportion of sample meeting the conditions of the antecedents
- **Confidence**: proportion of supported sample meeting the consequent



- I go to work by tunnel, by Route 68, or through the Presidio of Monterey
- Each rule carries a probability
- “If I take Rte 68, I’ll be late with probability 90%” compared to “Today I will be late with probability 20%”
- The difference between the 90% and the 20% **confidences** is one measure of the rule’s usefulness – unless I never take Rte 68 (which is measured by **support**)

Route	Rte 68	Tunnel	Presidio
Not Late	4%	20%	24%
Late	21%	21%	10%
Marginal	25%	41%	34%

The rule “If Rte 68, then Late” has **25%** support. The confidence is the usual estimate of the conditional probability

$$\begin{aligned}\Pr (L \mid 68) &= \Pr (L \ \& \ 68) / \Pr (68) = .21/.25 \\ &= \mathbf{84\%}\end{aligned}$$



Rules vs. Classification Trees

- In a tree, there is one response variable
- The “rules” are mutually exclusive and exhaustive (no overlap)
- Association rules use any variable as a response
- Many observations are covered by more than one rule (much overlap)



- The hard part is finding “frequent itemset patterns,” sets of conditions whose support exceeds a threshold s
- In one pass we can find frequent items defined by one condition
- “A and B” is frequent only if A and B are both frequent: $\Pr(A \& B) < \Pr(A)$
- In general a set is frequent only if all its subsets are themselves frequent



Finding Frequent Sets

- On pass two we can examine all pairs of frequent sets to compute their frequency
- On pass three, examine all triplets
 - The number of “sets of sets” grows quickly, so s needs to be chosen wisely
 - Number of conditions can be limited
- One more pass generates rules
 - For a set A , enumerate all possible rules like “if A , then B ”, evaluate accuracy
- Lots of rules, lots of overlap

- Evaluating “If A then B ” :
 1. **Confidence**: $\Pr (B | A)$
 2. Conf. difference: $\Pr (B|A) - \Pr (B)$
 3. **Lift**: $\Pr (B|A) / \Pr (B)$
 - Or $\Pr(A\&B)/\Pr(A)\Pr(B)$ in our package
 4. Conf. ratio: $[\Pr (B|A) / \Pr (B)] - 1$
 5. Information Difference: $\text{Gain}_A - \text{Gain}$
 6. Normalized χ^2 (Cramer’s coefficient)

These seem like the two most commonly used



- R implementation in `library(arules)`
- **Tabular** vs. **transactional** data
 - Transactional data: only the items present in the basket are passed
- Items that are rarer than the minimum support level can never appear in a rule
 - Some algorithms let you specify a different minimum support for each item
 - We need to keep very common items out of rules for rare items
 - Note: our “support” is $\Pr(A)$, but `apriori()` uses $\Pr(A \text{ and } B)$



- AdultUCI/Adult data set from arules
- Goal: Characterize relationships among descriptors of survey responders
- Code mostly taken from the help pages
- Problem of “very common” items dominating rule sets

- Database of tunnels under the U.S. border
- Goal 1: characterize tunnels by entrance, length, sophistication, etc.
- Goal 2: identify locations where tunnels are more likely to appear
- Let's do this thing!

