

TIONAL INSTITUTE OF PUBLIC ADMINISTRATION

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PROGRAM: BUSINESS ADMINISTRATION

COURSE: MACRO ECONOMICS

COURSE CODE: DIBA 1070

MODE OF STUDY: FULL TIME

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DATA

TAX RATE $t = 20\%$

LUMP SUM TAX $T = 1,000$

CONSUMPTION FUNCTION:

$$C = 4000 + 0.9Y_d$$

SOLUTIONS

$$Y_d = Y$$

With tax rate (20%)

$$Y_d = (1 - 0.2) Y = 0.8Y$$

With lump sum ($T = 1000$)

$$Y_d = Y - 1000$$

With both (20% + 1000)

$$Y_d = 0.8Y - 1000$$

$$Y = 5000$$

1) $C = 4000 + 0.9Y_d$

No tax:

$$C = 4000 + 0.9(5000) = 4000 + 4500 = 8500$$

With t :

$$C = 4000 + 0.9(4000) = 4000 + 3600 = 7600$$

With T :

$$C = 4000 + 0.9(4000) = 4000 + 3600 = 7600$$

With $t + T$:

$$C = 4000 + 0.9(3000) = 4000 + 2700 = 6700$$

$$Y = 6000$$

No tax:

2) $C = 4000 + 0.9(6000) = 4000 + 5400 = 9400$

With t :

$$C = 4000 + 0.9(4800) = 4000 + 4320 = 8320$$

With T :

$$C = 4000 + 0.9(5000) = 4000 + 4500 = 8500$$

With $t + T$

$$C = 4000 + 0.9(3800) = 4000 + 3420 = 7420$$

$$Y = 7000$$

No tax:

$$3) C = 4000 + 0.9 (7000) = 4000 + 6300 = 10,300$$

With t:

$$C = 4000 + 0.9 (5600) = 4000 + 5040 = 9040$$

With T:

$$C = 4000 + 0.9 (6000) = 4000 + 5400 = 9400$$

With t + T

$$C = 4000 + 0.9 (4600) = 4000 + 4140 = 8140$$

Final Table

Y(Income)	C (No tax)	C (With t)	C (With T)	C (With t & T)
5000	8500	7600	7600	6700
6000	9400	8320	8500	7420
7000	10300	9040	9400	8140

2) Each tax affects the consumption function

No tax: $C = 4000 + 0.9Y$. Marginal propensity to consume (MPC) = 0.9 and autonomous consumption = 4000.

Proportional tax ($t = 0.2$): disposable income $Y_d = 0.8Y$. Consumption becomes $C = 4000 + 0.9(0.8Y) = 4000 + 0.72Y$.

The MPC Falls from 0.9 to 0.72 (slope decreases); autonomous consumption 4000 stays the same

Lump sum tax ($T = 1,000$): $Y_d = Y - 1000$. Consumption becomes

$$C = 4000 + 0.9 (Y - 1000) = 3100 + 0.9Y.$$

The MPC remains 0.9 (Slope unchanged) but the function shifts down by 900 since $0.9 * 1000 = 900$). This is a constant reduction in consumption for all income levels.

Both taxes: $Y_d = 0.8Y - 1000$. Consumption becomes

$C = 4000 + 0.9 (0.8Y - 1000) = 3100 + 0.72Y$, so consumption is both shifted down and has a lower slope.

Interpretation of the numbers in the table

For each income level, the proportional tax causes a larger absolute consumption drop as income rises (because the reduction equals $0.8Y$).

The lump-sum tax reduces consumption by the same absolute amount (900) at every income level – therefore its relative burden is heavier on lower incomes.

With both taxes the consumption level is lowest because the individual loses from both a lower MPC and a constant downwards shift.

iii) Proportional taxes reduce consumption more for high incomes (absolute term) and lower the economy's overall MPC. Lump-sum taxes cut consumption by the same absolute amount for everyone, hurting low-income individuals relatively more. Policy makers should weigh equity (lump-sum is regressive) against efficiency and revenue needs when choosing tax instruments