

# Chapter 3 Concept Test

**Due** Apr 8 at 12pm**Points** 1**Questions** 6**Time Limit** None

## Instructions

Read the chapter, review the pre-class material, then take this concept test

## Attempt History

	Attempt	Time	Score
LATEST	<a href="#">Attempt 1</a>	9 minutes	1 out of 1

Score for this quiz: **1** out of 1

Submitted Apr 8 at 9:52am

This attempt took 9 minutes.

### Question 1

**0 / 0 pts**

You are fitting a simple linear regression model to predict the prices of the items for sale in a store ( $Y_i$ ) based on the weight of the item ( $X_i$ ). You have some training data with many items for sale (this data includes the weight of each item and its price). Suppose that you saw a horizontal line at  $y = 1$  when you fit the model to the data. What would this tell you about the relationship between the input variable and the output?

☐ For all input values,  $X_i$ ,  $Y_i = 1 \times X_i + \epsilon$

☐ The linear model only shows a relationship between input and output when  $y = 1$

☐ For all input values,  $X_i$ ,  $Y_i = 1 \times X_i$  (the model is a perfect fit without errors)

**Correct!**

The linear model does not reveal a relationship between the input variable and the output variable

Correct - since the model always predicts  $y=1$ , the model's prediction is unaffected by the weight of the item.

**Question 2****0 / 0 pts**

You have a dataset with  $n$  observations and  $p$  features. Assuming that each feature will be used at most once in your model (first-order terms only, no interaction terms), how many possible individual multiple linear regression models could be formed using the  $p$  features?

☐  $p^2$

☐  $p + 1$

☐  $\frac{p(p-1)}{2}$

☒  $2^p$

**Correct!**

Correct. Since you must decide whether or not to use each feature in a model, the total number of possible models is the number of possible subsets of the original set of features. In other words, the answer is the cardinality of the powerset:  $2^p$

**Question 3****0 / 0 pts**

Suppose you train a multiple linear regression to predict  $y$  on a dataset with 4 input variables. During preprocessing you normalized the data so that all inputs were

gaussian normalized with mean 0 and variance 1. You then trained the model. Your trained linear model coefficients are:  $\beta_1 = 0.5$ ,  $\beta_2 = 0.4$ ,  $\beta_3 = 0.001$  and  $\beta_4 = -0.85$ . What can you infer about the importance of inputs  $x_1$ ,  $x_2$ ,  $x_3$ , and  $x_4$ ? (select all that apply)

Correct!

- ☒  $X_4$  has a stronger relationship with  $y$  than  $X_3$

Yes, due to its magnitude, the fourth feature has a stronger relationship to  $y$  than the third feature.

- ☐ A model using  $X_4$  alone will produce  $y$  values which are 85% accurate



The hypothesis that  $X_3$  has no relationship with  $y$  can be rejected since  $0.001 < 0.05$

You Answered

- ☒ A model using only  $X_1$  and  $X_2$  will outperform a model using only  $X_4$

From the coefficients alone, it is not possible to know whether a different model would perform because the coefficients do not directly indicate the performance of the model and the coefficient's values are applicable only indicative of feature importance in the current model. In other words, the coefficients in the four-feature model do not provide information about the values of the respective coefficients in a model with fewer features.

Since the data was pre-processed and all the features used the same scale, the coefficients can be directly compared. The larger the magnitude of a coefficient, the more the effect of that input on the model. Thus, given that we build the model with all four features,  $x_4$  has a large effect on the model,  $x_1$  has the second largest,  $x_2$  has the third largest, and  $x_3$  has a negligible effect on the model. The coefficients do not directly indicate model performance or probability that the coefficient's value is due to chance.

**Question 4****0 / 0 pts**

You have a dataset with  $n > 30$  observations and  $p$  features and each observation has a real value output  $y$ . Suppose you form a hypothesis  $H_0$  that none of the  $p$  predictors (features) of a dataset has a linear relationship with the output variable  $y$ . The alternative hypothesis  $H_a$  is that at least one of the predictors (features) of the dataset has a linear relationship with the output variable  $y$ . Which of the following techniques is appropriate for evaluating that hypothesis if you would like to have inappropriately rejected the null no more often than 5% of the time?



For each predictor compute the variance inflation factor (VIF) on each coefficient. If all VIFs are below 5 then reject the null hypothesis  $H_0$ .



Compute the correlation between each pair of features in the dataset. If at least two are correlated with 0.95 or higher, then we can reject the null hypothesis  $H_0$ .



Compute the  $t$ -statistic for each predictor. Compute the probability of that value of  $t$  occurring. If the probability  $< 0.05$  for any predictor then reject the null hypothesis  $H_0$ .

Some software packages provide p values for each coefficient. These values can be used to determine whether the null hypothesis can be rejected.



Compute the Residual Sum of Squares (RSS) for a simple linear regression using each individual member of the possible features which could be used for regression. If there exists at least one with  $RSS \leq 0.05$  then reject the null hypothesis  $H_0$ .

**Correct!****Question 5****0 / 0 pts**

What was the **most interesting** concept in the material you reviewed for this pre-class assignment? Be specific - wherever possible, include page

numbers, filenames, concept names to help your instructor understand what you are referring to:

Your Answer:

The section on qualitative predictions was the most interesting.

### Question 6

1 / 1 pts

What was the **most confusing** aspect of the material you reviewed? Be specific - wherever possible, include page numbers, filenames, concept names to help your instructor understand what you are referring to:

Your Answer:

Interpreting the results of the regression, i.e. interpreting what the coefficients that come out of the model are was the most confusing part.

Quiz Score: **1** out of 1