

## Problem 1

**Answer:** A bootstrap confidence interval constructed based on a biased sample will still yield an unbiased estimate for the population parameter of interest.

## Problem 2

**Answer:**

- ▷ Version 1: Each observation in one data set is subtracted from the average of the other data set's observations.
- ▷ Version 2: The data can't be considered paired data because the days for which we have Intel data may be different from the days for which we have Southwest Airlines data.

## Problem 3

**Answer:** Sampling distribution

## Problem 4

**Answer:**

- ▷ Version 1: The study's authors are 95% confident that babies born to non-smoking mothers are on average 0.2 to 0.9 pounds heavier than babies born to smoking mothers.
- ▷ Version 2: Since 0 is apparently an unusual value for the statistic, then at the 5% significance level we would fail to reject a null hypothesis that claims that the fathers' and mothers' average IQs are equal.

## Problem 5

**Answer:**

- ▷ Version 1: Because the standard error estimate may not be accurate.
- ▷ Version 2: A confidence interval based on this sample is not accurate since the sample size is small.

## Problem 6

**Answer:** It becomes more normal looking.

## Problem 7

**Answer:** Tom has a one-sided alternative hypothesis and should do a paired t-test.

## Problem 8

**Answer:**

- ▷ Version 1: Between 0.02 and 0.05.
- ▷ Version 2:  $T < -1.71$

```
# Version 1
n <- 26
t <- 2.485
p_value <- 2 * pt(t, n - 1, lower.tail = F)
print(p_value)
```

0.0200048010978179

```
# Version 2
print_p_value <- function(t, n) {
  p_value <- pt(t, n - 1)
  cat("T =", t, "--- p-value =", p_value, "\n")
}
```

```
n <- 25
ts <- c(-1.71, -1.32, 1.32, 1.71, 1.96)
for (t in ts) {
  print_p_value(t, n)
}
```

```
T = -1.71 --- p-value = 0.05008269
T = -1.32 --- p-value = 0.09964372
T = 1.32 --- p-value = 0.9003563
T = 1.71 --- p-value = 0.9499173
T = 1.96 --- p-value = 0.969147
```

## Problem 9

**Answer:** F-test (ANOVA)

## Problem 10

**Answer:**

- ▷ Version 1: There should be at least 10 successes and 10 failures.
- ▷ Version 2: Side-by-side box plots showing roughly equally sized boxes for each group.

## Problem 11

**Answer:** 1.87

```
p <- 1 - 0.0767
df1 <- 7
df2 <- 189
f_stat <- round(qf(p, df1, df2), digits = 2)
print(f_stat)
```

1.87

## Problem 12

**Answer:**

- ▷ Version 1: At least two group means are significantly different from each other.
- ▷ Version 2:

$$H_0 : \mu_1 = \mu_2 = \mu_3 = \mu_4 = \mu_5$$

$$H_A : \text{at least one } \mu_i \text{ is different}$$

## Problem 13

### Answer:

▷ Version 1: Decrease

▷ Version 2: 1.023

```
# Version 2
n1 <- 18
s1 <- 3.4

n2 <- 18
s2 <- 2.7

sp <- sqrt(((n1 - 1) * s1^2 + (n2 - 1) * s2^2) / (n1 + n2 - 2))
std_err <- sp * sqrt(1 / n1 + 1 / n2)
signif(std_err, digits = 4)

[1] 1.023
```

## Problem 14

### Answer:

▷ Version 1:  $\alpha' = 0.005$

▷ Version 2:  $K = 10$

The adjusted significance level is given by

$$\alpha' = \frac{\alpha}{K}, \quad (1)$$

where  $K$  can be obtained from the number of groups  $k = 5$  as follows:

$$K = \frac{k(k-1)}{2} = \frac{5(5-1)}{2} = 10. \quad (2)$$

Using this result and  $\alpha = 0.05$ , we get

$$\alpha' = \frac{0.05}{10} = 0.005. \quad (3)$$